

```
In [1]: using Pkg  
Pkg.activate("..")  
Pkg.instantiate()  
Pkg.update()  
  
Activating project at `~/logic-and-machine-learning`  
Updating registry at `~/.julia/registries/General.toml`  
Updating git-repo `https://github.com/aclai-lab/ManyExpertDecisionTree  
s.jl`  
Updating git-repo `https://github.com/aclai-lab/SoleReasoners.jl#embed  
ding`  
No Changes to `~/logic-and-machine-learning/Project.toml`  
No Changes to `~/logic-and-machine-learning/Manifest.toml`
```

```
In [2]: using Random  
  
Random.seed!(1235)
```

```
Out[2]: TaskLocalRNG()
```

Identifying academically vulnerable learners in first-year science programmes

Identifying academically vulnerable learners in first-year science programmes at a South African higher-education institution

```
In [3]: using ARFFFiles  
using DataFrames  
  
data = ARFFFiles.load(  
    DataFrame,  
    joinpath(.., "datasets", "academically-vulnerable-learners.arff")  
)  
  
describe(data)
```

Out[3]: 45×7 DataFrame

20 rows omitted

Row	variable	mean	min	median	max	nmissing
	Symbol	Union... Any	Union... Any	Int64		
1	Risk Status		Medium Risk		High Risk	0
2	YearStarted	2012.62	2008.0	2012.59	2018.0	0
3	PlanCode		SB000DFLT		SPROGSOC90	0
4	PlanDescription		SB000 Default		Science Occ Studies (UG)	0
5	Majors		MATH		PALP	0
6	APS Code		STATNSC		AIN11	0
7	APS Value	39.6162	0.0	41.4386	68.0	94
8	Streamline		Unknown Streamline		Earth Science Degree	0
9	Homeprovince		GA		KZ	0
10	Homecountry		ZAF		ZMB	0
11	AgeatFirstYear	24.722	17.0	24.8654	40.0	0
12	SchoolQuintile		Q2		NaN	0
13	isRuralorUrban		RURAL		NaN	0
:	:	:	:	:	:	:
34	Civil	90.0	90.0	90.0	90.0	799
35	BusinessEconomics	59.8053	0.0	73.0	88.0	755
36	ReligiousStudies	37.2	0.0	0.0	100.0	795
37	PhysicsChem	56.3617	0.0	65.5511	100.0	119
38	InternationalRelations	63.5714	0.0	66.0	90.0	793
39	Geography	64.2156	0.0	72.0	98.0	613
40	Hospitality	78.0	78.0	78.0	78.0	799
41	History	63.1071	0.0	79.0	91.0	772
42	Politics	NaN				800
43	LifeSciences	57.4927	0.0	71.865	97.0	218

Row	variable	mean	min	median	max	nmissing
	Symbol	Union...	Any	Union...	Any	Int64
44	ForiegnSubject	NaN				800
45	SportScience	70.0	70.0	70.0	70.0	799

Oh no! Some attributes have many missing values!!!

```
In [4]: attributes_with_missings = Vector{Tuple{String, Int}}()

for attribute_name in names(data)
    n_missings = count(x -> ismissing(x), data[:, attribute_name])

    if n_missings > 0
        push!(attributes_with_missings, (attribute_name, n_missings))
    end
end

attxmiss = sort!(attributes_with_missings, by = x -> x[2], rev = false)
```

```
Out[4]: 33-element Vector{Tuple{String, Int64}}:
("APS Value", 94)
("MathematicsMatricMajor", 98)
("PhysicsChem", 119)
("AdditionalLanguage", 137)
("LifeOrientation", 213)
("LifeSciences", 218)
("NBTAL", 443)
("NBTQL", 448)
("NBTMA", 450)
("EnglishFirstLang", 472)
("EnglishFirstAdditional", 607)
("Geography", 613)
("AdditionalMathematics", 668)
:
("InternationalRelations", 793)
("ReligiousStudies", 795)
("Music", 797)
("MathematicsMatricLit", 798)
("Mechanical", 798)
("Civil", 799)
("Hospitality", 799)
("SportScience", 799)
("Statistics", 800)
("OverallAggregate", 800)
("Politics", 800)
("ForiegnSubject", 800)
```

We have some preprocessing to do!

Let's start by dropping the columns with more missing values.

```
In [5]: # we want to drop these features
colstodrop = [feature for (feature, nmisses) in attxmiss[11:end]]
```

```
Out[5]: 23-element Vector{String}:
"EnglishFirstAdditional"
"Geography"
"AdditionalMathematics"
"Accounting"
"ComputerStudies"
"BusinessEconomics"
"History"
"Agriculture"
"Electrical"
"ArtDesign"
"CraftSpeechDrama"
"InternationalRelations"
"ReligiousStudies"
"Music"
"MathematicsMatricLit"
"Mechanical"
"Civil"
"Hospitality"
"SportScience"
"Statistics"
"OverallAggregate"
"Politics"
"ForeignSubject"
```

```
In [6]: [select!(data, Not(Symbol(col))) for col in colstodrop];      # remember this
describe(data)
```

Out[6]: 22×7 DataFrame

Row	variable	mean	min	median	max	nmissi
	Symbol	Union... Any	Union... Any			Int64
1	Risk Status		Medium Risk		High Risk	
2	YearStarted	2012.62	2008.0	2012.59	2018.0	
3	PlanCode		SB000DFLT		SPROGSOC90	
4	PlanDescription		SB000 Default		Science Occ Studies (UG)	
5	Majors		MATH		PALP	
6	APS Code		STATNSC		AIN11	
7	APS Value	39.6162	0.0	41.4386	68.0	
8	Streamline		Unknown Streamline		Earth Science Degree	
9	Homeprovince		GA		KZ	
10	Homecountry		ZAF		ZMB	
11	AgeatFirstYear	24.722	17.0	24.8654	40.0	
12	SchoolQuintile		Q2		NaN	
13	isRuralorUrban		RURAL		NaN	
14	LifeOrientation	64.0089	0.0	79.0245	100.0	2
15	MathematicsMatricMajor	58.0737	0.0	69.0	100.0	
16	EnglishFirstLang	64.6558	0.0	71.0	95.4928	2
17	NBTAL	61.6059	31.0	63.2377	87.0	2
18	NBTMA	50.7234	25.0	49.0	94.0	2
19	NBTQL	55.0162	24.5085	54.0442	94.0	2
20	AdditionalLanguage	64.1048	0.0	71.3761	98.0	1
21	PhysicsChem	56.3617	0.0	65.5511	100.0	1
22	LifeSciences	57.4927	0.0	71.865	97.0	2

We still have some missings!

Let's remove rows with missing values.

```
In [7]: using Impute  
data_nomissing = Impute.filter(data; dims=:rows)
```

Out[7]: 118×22 DataFrame

93 rows omitted

Row	Risk Status	YearStarted	PlanCode	PlanDescription	Majors	APS Code	AP Va
	Cat...	Float64	Cat...	Cat...	Cat...	Cat...	Flc
1	No Risk	2011.0	SMAJADES10	Advanced Earth Sciences	GEOG	STATNSC	
2	Medium Risk	2017.0	SMAJGEN00	General	COMS	AIN12	
3	Low Risk	2009.77	SMAJASTR10	Astronomy Astrophysics	COMS	STATNSC	40
4	Low Risk	2013.0	SMAJEEC10	Ecology, Environment and Conservation	APES	AIN12	
5	No Risk	2012.83	SMAJAEBI10	Applied & Experimental Physiology	PHSL	STATNSC	44
6	No Risk	2016.0	SMAJACSI10	Actuarial Science	MATH	AIN12	
7	Low Risk	2015.0	SMAJAPES10	Animal, Plant and Environmental Sciences	APES	AIN12	
8	No Risk	2012.01	SMAJBIO10	Biochemistry and Cell Biology	MCBG	STATNSC	40
9	Medium Risk	2013.0	SMAJCOMM10	Computer Science	MATH	AIN12	
10	No Risk	2010.0	SMAJAEBI10	Applied & Experimental Physiology	MCBG	STATNSC	
11	Medium Risk	2011.0	SB000DFLT	SB000 Default	ECON	STATNSC	
12	Low Risk	2011.0	SMAJHPHS10	Human Physiology	PHSL	STATNSC	
13	High Risk	2013.0	SMAJGENE10	Genetics & Development Biology	MCBG	AIN12	
:	:	:	:	:	:	:	:
107	No Risk	2016.0	SMAJGEN00	General	CHEM	AIN12	

Row	Risk Status	YearStarted	PlanCode	PlanDescription	Majors	APS Code	AP Va
	Cat...	Float64	Cat...	Cat...	Cat...	Cat...	Flo
108	Medium Risk	2010.0	SB000DFLT	SB000 Default	BIOL	STATNSC	
109	Low Risk	2010.43	SMAJASTR10	Astronomy Astrophysics	MATH	AIN12	53
110	No Risk	2014.03	SMAJAEBI10	Applied & Experimental Physiology	PHSL	AIN12	40
111	Low Risk	2012.0	SMAJBIO10	Biochemistry and Cell Biology	MCBG	STATNSC	
112	High Risk	2014.99	SMAJBIOL10	Biological Sciences	MATH	AIN12	41
113	No Risk	2012.0	SMAJGENE10	Genetics & Development Biology	MCBG	STATNSC	
114	Medium Risk	2009.0	SB000DFLT	SB000 Default	MATH	STATNSC	
115	Medium Risk	2018.0	SMAGEN00	General	MATH	AIN12	
116	Low Risk	2010.0	SMAJCAMS10	Computational and Applied Mathematics	MATH	STATNSC	
117	No Risk	2016.0	SMAJECOS10	Economic Science	MATH	AIN12	
118	No Risk	2016.0	SMAJGENE10	Genetics & Development Biology	MCBG	AIN12	

In [8]: `using MLJ`

```
schema(data_nomissing)
```

Out[8]:

names	scitypes	types
Risk Status	Multiclass{4}	CategoricalValue{String, UInt32}
YearStarted	Continuous	Float64
PlanCode	Multiclass{60}	CategoricalValue{String, UInt32}
PlanDescription	Multiclass{49}	CategoricalValue{String, UInt32}
Majors	Multiclass{29}	CategoricalValue{String, UInt32}
APS Code	Multiclass{8}	CategoricalValue{String, UInt32}
APS Value	Continuous	Float64
Streamline	Multiclass{5}	CategoricalValue{String, UInt32}
Homeprovince	Multiclass{14}	CategoricalValue{String, UInt32}
Homecountry	Multiclass{25}	CategoricalValue{String, UInt32}
AgeatFirstYear	Continuous	Float64
SchoolQuintile	Multiclass{6}	CategoricalValue{String, UInt32}
isRuralorUrban	Multiclass{3}	CategoricalValue{String, UInt32}
LifeOrientation	Continuous	Float64
MathematicsMatricMajor	Continuous	Float64
EnglishFirstLang	Continuous	Float64
NBTAL	Continuous	Float64
NBTMA	Continuous	Float64
NBTQL	Continuous	Float64
AdditionalLanguage	Continuous	Float64
PhysicsChem	Continuous	Float64
LifeSciences	Continuous	Float64

Let's see which kind of models we could use...

In [9]:

```
y, X = unpack(data_nomissing, ==(Symbol("Risk Status")))

models(matching(X,y))
```

```
Out[9]: 7-element Vector{NamedTuple{(:name, :package_name, :is_supervised, :abst
ract_type, :constructor, :deep_properties, :docstring, :fit_data_scitype
, :human_name, :hyperparameter_ranges, :hyperparameter_types, :hyperpara
meters, :implemented_methods, :inverse_transform_scitype, :is_pure_julia
, :is_wrapper, :iteration_parameter, :load_path, :package_license, :pack
age_url, :package_uuid, :predict_scitype, :prediction_type, :reporting_o
perations, :reports_feature_importances, :supports_class_weights, :suppo
rts_online, :supports_training_losses, :supports_weights, :target_in_fit
, :transform_scitype, :input_scitype, :target_scitype, :output_scityp
e)}}:
(name = CatBoostClassifier, package_name = CatBoost, ... )
(name = ConstantClassifier, package_name = MLJModels, ... )
(name = DecisionTreeClassifier, package_name = BetaML, ... )
(name = DeterministicConstantClassifier, package_name = MLJModels, ... )
)
(name = EvoTreeClassifier, package_name = EvoTrees, ... )
(name = NeuralNetworkClassifier, package_name = MLJFlux, ... )
(name = RandomForestClassifier, package_name = BetaML, ... )
```

Too bad! Most models don't work with categorical values out of the box...

This includes the `DecisionTreeClassifier` from `DecisionTree.jl`!

Hence, we first need to encode these values as numerical values.

One possibility is to convert the type of the associated features from `Multiclass` to `Continuous` or `OrderedFactor`.

```
In [10]: data_preprocessed = coerce(data_nomissing, "Risk Status"=>OrderedFactor)
data_preprocessed = coerce(data_preprocessed, Multiclass=>Continuous)

schema(data_preprocessed)
```

Out[10]:

names	scitypes	types
...		
Risk Status Int32} ...	OrderedFactor{4}	CategoricalValue{String, U
YearStarted	Continuous	Float64
...		
PlanCode	Continuous	Float64
...		
PlanDescription	Continuous	Float64
...		
Majors	Continuous	Float64
...		
APS Code	Continuous	Float64
...		
APS Value	Continuous	Float64
...		
Streamline	Continuous	Float64
...		
Homeprovince	Continuous	Float64
...		
Homecountry	Continuous	Float64
...		
AgeatFirstYear	Continuous	Float64
...		
SchoolQuintile	Continuous	Float64
...		
isRuralorUrban	Continuous	Float64
...		
LifeOrientation	Continuous	Float64
...		
MathematicsMatricMajor	Continuous	Float64
...		
EnglishFirstLang	Continuous	Float64
...		
NBTAL	Continuous	Float64
...		
NBTMA	Continuous	Float64
...		
NBTQL	Continuous	Float64
...		
AdditionalLanguage	Continuous	Float64
...		
PhysicsChem	Continuous	Float64
...		
LifeSciences	Continuous	Float64
...		

Let's have a look at the data...

In [11]: `y, X = unpack(data_preprocessed, ==(Symbol("Risk_Status")))`

```

Out[11]: (CategoricalArrays.CategoricalValue{String, UInt32}["No Risk", "Medium Risk", "Low Risk", "Low Risk", "No Risk", "No Risk", "Low Risk", "No Risk", "Medium Risk", "No Risk", ... "Low Risk", "No Risk", "Low Risk", "High Risk", "No Risk", "Medium Risk", "Medium Risk", "Low Risk", "No Risk", "No Risk"], 118×21 DataFrame
  Row | YearStarted  PlanCode  PlanDescription  Majors  APS Code  APS Va
  lue  S ...          | Float64      Float64      Float64      Float64  Float64  Float64
  4    F ...
  |-----|-----|-----|-----|-----|-----|-----|
  1 | 2011.0      18.0       17.0       9.0      1.0     46.0
  ... 
  2 | 2017.0      10.0       10.0       11.0      2.0     40.0
  3 | 2009.77     2.0        2.0        11.0      1.0     40.8
  845
  4 | 2013.0      7.0        7.0        6.0      2.0     39.0
  5 | 2012.83     3.0        3.0        3.0      1.0     44.0
  344
  6 | 2016.0      15.0       14.0       1.0      2.0     50.0
  7 | 2015.0      33.0       29.0       6.0      2.0     42.0
  8 | 2012.01     5.0        5.0        4.0      1.0     40.5
  945
  9 | 2013.0      27.0       18.0       1.0      2.0     39.0
  ... 
  10 | 2010.0      3.0        3.0        4.0      1.0     49.0
  11 | 2011.0      1.0        1.0        15.0      1.0     36.0
  ...
  . .
  109 | 2010.43     2.0        2.0        1.0      2.0     53.4
  871
  110 | 2014.03     3.0        3.0        3.0      2.0     40.7
  176
  111 | 2012.0      5.0        5.0        4.0      1.0     40.0
  112 | 2014.99     4.0        4.0        1.0      2.0     41.3
  076
  113 | 2012.0      17.0       16.0       4.0      1.0     39.0
  114 | 2009.0      1.0        1.0        1.0      1.0     42.0
  ...
  115 | 2018.0      13.0       10.0       1.0      2.0     48.0
  116 | 2010.0      22.0       20.0       1.0      1.0     46.0
  117 | 2016.0      9.0        9.0        1.0      2.0     43.0
  118 | 2016.0      17.0       16.0       4.0      2.0     43.0
  ...
  ...
  15 columns and 97 rows
  omitted)

```

Great! We can now use a `DecisionTreeClassifier` like in our example!

```

Out[12]: 54-element Vector{NamedTuple{(:name, :package_name, :is_supervised, :abstract_type, :constructor, :deep_properties, :docstring, :fit_data_scitype, :human_name, :hyperparameter_ranges, :hyperparameter_types, :hyperparameters, :implemented_methods, :inverse_transform_scitype, :is_pure_julia, :is_wrapper, :iteration_parameter, :load_path, :package_license, :package_url, :package_uuid, :predict_scitype, :prediction_type, :reporting_operations, :reports_feature_importances, :supports_class_weights, :supports_online, :supports_training_losses, :supports_weights, :target_in_fit, :transform_scitype, :input_scitype, :target_scitype, :output_scitype)}}:
    (name = AdaBoostClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = AdaBoostStumpClassifier, package_name = DecisionTree, ... )
    (name = BaggingClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = BayesianLDA, package_name = MLJScikitLearnInterface, ... )
    (name = BayesianLDA, package_name = MultivariateStats, ... )
    (name = BayesianQDA, package_name = MLJScikitLearnInterface, ... )
    (name = BayesianSubspaceLDA, package_name = MultivariateStats, ... )
    (name = CatBoostClassifier, package_name = CatBoost, ... )
    (name = ConstantClassifier, package_name = MLJModels, ... )
    (name = DecisionTreeClassifier, package_name = BetaML, ... )
    (name = DecisionTreeClassifier, package_name = DecisionTree, ... )
    (name = DeterministicConstantClassifier, package_name = MLJModels, ... )
    (name = DummyClassifier, package_name = MLJScikitLearnInterface, ... )
    :
    (name = RandomForestClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = RidgeCVClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = RidgeClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = SGDClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = SVC, package_name = LIBSVM, ... )
    (name = SVMClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = SVMLinearClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = SVMNuClassifier, package_name = MLJScikitLearnInterface, ... )
    (name = StableForestClassifier, package_name = SIRUS, ... )
    (name = StableRulesClassifier, package_name = SIRUS, ... )
    (name = SubspaceLDA, package_name = MultivariateStats, ... )
    (name = XGBoostClassifier, package_name = XGBoost, ... )

```

Let's first choose a random sample from our dataset: we will use it later to evaluate our model.

```

In [13]: y, X = unpack(data_preprocessed, ==(Symbol("Risk Status")))

(X_train, X_test), (y_train, y_test) = partition(
    (X, y),
    0.8,
    rng=13,
    shuffle=true,
    multi=true
);

```

Let's try to work following the pipeline we learned this week!

```
In [14]: try
    DecisionTreeClassifier = @load DecisionTreeClassifier pkg=DecisionTree
catch
    println("The DecisionTreeClassifier symbol has already been imported.
end
```

[Info: For silent loading, specify `verbosity=0`.
import MLJDecisionTreeInterface ✓

```
Out[14]: MLJDecisionTreeInterface.DecisionTreeClassifier
```

```
In [15]: model = MLJDecisionTreeInterface.DecisionTreeClassifier()
```

```
Out[15]: DecisionTreeClassifier(
    max_depth = -1,
    min_samples_leaf = 1,
    min_samples_split = 2,
    min_purity_increase = 0.0,
    n_subfeatures = 0,
    post_prune = false,
    merge_purity_threshold = 1.0,
    display_depth = 5,
    feature_importance = :impurity,
    rng = TaskLocalRNG())
```

```
In [16]: mach = machine(model, X_train, y_train)
```

```
Out[16]: untrained Machine; caches model-specific representations of data
         model: DecisionTreeClassifier(max_depth = -1, ...)
         args:
           1: Source @399 ↴ Table{AbstractVector{Continuous}}
           2: Source @546 ↴ AbstractVector{OrderedFactor{4}}}
```

```
In [17]: fit!(mach)
```

[Info: Training machine(DecisionTreeClassifier(max_depth = -1, ...), ...).

```
Out[17]: trained Machine; caches model-specific representations of data
         model: DecisionTreeClassifier(max_depth = -1, ...)
         args:
           1: Source @399 ↴ Table{AbstractVector{Continuous}}
           2: Source @546 ↴ AbstractVector{OrderedFactor{4}}}
```

```
In [18]: 🌱 = fitted_params(mach).tree # \:seedling:
```

```
Out[18]: YearStarted < 2016.0
    └─ Majors < 1.5
        └─ APS Value < 42.05
            └─ LifeOrientation < 87.76
                └─ Medium Risk (8/8)
                └─ High Risk (1/1)
            └─ AdditionalLanguage < 74.95
                └─ High Risk (5/5)
                └─ AgeatFirstYear < 27.6
                    └─ Low Risk (7/7)
                    └─ Medium Risk (1/1)
    └─ Majors < 5.0
        └─ PlanCode < 6.5
            └─ Homeprovince < 1.5
                └─ YearStarted < 2010.0
                    :
                └─ AgeatFirstYear < 22.5
                    :
    └─ YearStarted < 2013.0
        └─ Homeprovince < 1.5
            :
        └─ LifeOrientation < 23.71
            :
    └─ PhysicsChem < 75.0
        └─ Majors < 7.5
            └─ Low Risk (5/5)
            └─ PlanDescription < 14.0
                :
    └─ MathematicsMatricMajor < 87.5
        └─ MathematicsMatricMajor < 85.0
            :
        └─ Low Risk (5/5)
    └─ Medium Risk (17/17)
```

Let's evaluate performance!

```
In [19]: y_predict_probabilities = predict(mach, X_test)
y_predict = mode.(y_predict_probabilities)
cm = confusion_matrix(y_predict, y_test)
```

Out[19]:

Predicted	Ground Truth			
	Medium R...	Low Risk	No Risk	High Risk
Medium R...	12	0	0	2
Low Risk	0	4	2	0
No Risk	0	0	4	0
High Risk	0	0	0	0

```
In [20]: accuracy(cm)
```

```
Out[20]: 0.8333333333333334
```

Let's extract logical rules!

```
In [21]: using SoleModels
```

```
tree = solemodel(leaf) # \:evergreen_tree:
```

WARNING: using SoleModels.models in module Main conflicts with an existing identifier.

```
Out[21]: ┌─ ([YearStarted] < 2016.5)
  ├─ ([Majors] < 1.5)
    ├─ ([APS Value] < 42.0546825)
      ├─ ([LifeOrientation] < 87.761518)
        ├─ Medium Risk
        └─ High Risk
      └─ ([AdditionalLanguage] < 74.950632)
        ├─ High Risk
        └─ ([AgeatFirstYear] < 27.5967815)
          ├─ Low Risk
          └─ Medium Risk
    └─ ([Majors] < 5.0)
      ├─ ([PlanCode] < 6.5)
        ├─ ([Homeprovince] < 1.5)
          ├─ ([YearStarted] < 2009.5)
            ├─ Low Risk
            └─ No Risk
          └─ ([AgeatFirstYear] < 22.5)
            ├─ Medium Risk
            └─ ([AdditionalLanguage] < 34.0)
              ├─ No Risk
              └─ Low Risk
        └─ ([YearStarted] < 2013.2996785)
          ├─ ([Homeprovince] < 1.5)
            ├─ Low Risk
            └─ ([YearStarted] < 2012.5)
              ├─ No Risk
              └─ High Risk
            └─ ([LifeOrientation] < 23.71375)
              ├─ Low Risk
              └─ No Risk
      └─ ([PhysicsChem] < 75.0)
        ├─ ([Majors] < 7.5)
          ├─ Low Risk
          └─ ([PlanDescription] < 14.0)
            ├─ Medium Risk
            └─ Low Risk
          └─ ([MathematicsMatricMajor] < 87.5)
            ├─ ([MathematicsMatricMajor] < 85.0)
              ├─ No Risk
              └─ Medium Risk
            └─ Low Risk
        └─ Medium Risk
```

```
In [22]: listrules(tree)
```

Out[22]: 22-element Vector{ClassificationRule{String}}:

- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] < 1.5]) \wedge ([[APS \text{ Value}] < 42.0546825]) \wedge ([[LifeOrientation}] < 87.761518)) \Rightarrow \text{Medium Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] < 1.5]) \wedge ([[APS \text{ Value}] < 42.0546825]) \wedge ([[LifeOrientation}] \geq 87.761518)) \Rightarrow \text{High Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] < 1.5]) \wedge ([[APS \text{ Value}] \geq 42.0546825]) \wedge ([[AdditionalLanguage}] < 74.950632)) \Rightarrow \text{High Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] < 1.5]) \wedge ([[APS \text{ Value}] \geq 42.0546825]) \wedge ([[AdditionalLanguage}] \geq 74.950632) \wedge ([[AgeatFirstYear}] < 27.5967815)) \Rightarrow \text{Low Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] < 1.5]) \wedge ([[APS \text{ Value}] \geq 42.0546825]) \wedge ([[AdditionalLanguage}] \geq 74.950632) \wedge ([[AgeatFirstYear}] \geq 27.5967815)) \Rightarrow \text{Medium Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] < 6.5) \wedge ([[Homeprovince}] < 1.5) \wedge ([[YearStarted}] < 2009.5)) \Rightarrow \text{Low Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] < 6.5) \wedge ([[Homeprovince}] < 1.5) \wedge ([[YearStarted}] \geq 2009.5)) \Rightarrow \text{No Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] < 6.5) \wedge ([[Homeprovince}] \geq 1.5) \wedge ([[AgeatFirstYear}] < 22.5)) \Rightarrow \text{Medium Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] < 6.5) \wedge ([[Homeprovince}] \geq 1.5) \wedge ([[AgeatFirstYear}] \geq 22.5) \wedge ([[AdditionalLanguage}] < 34.0)) \Rightarrow \text{No Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] < 6.5) \wedge ([[Homeprovince}] \geq 1.5) \wedge ([[AgeatFirstYear}] \geq 22.5) \wedge ([[AdditionalLanguage}] \geq 34.0)) \Rightarrow \text{Low Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] \geq 6.5) \wedge ([[YearStarted}] < 2013.2996785) \wedge ([[Homeprovince}] < 1.5)) \Rightarrow \text{Low Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] \geq 6.5) \wedge ([[YearStarted}] < 2013.2996785) \wedge ([[Homeprovince}] \geq 1.5) \wedge ([[YearStarted}] < 2012.5)) \Rightarrow \text{No Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] \geq 6.5) \wedge ([[YearStarted}] < 2013.2996785) \wedge ([[Homeprovince}] \geq 1.5) \wedge ([[YearStarted}] \geq 2012.5)) \Rightarrow \text{High Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] \geq 6.5) \wedge ([[YearStarted}] \geq 2013.2996785) \wedge ([[LifeOrientation}] < 23.71375)) \Rightarrow \text{Low Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] < 5.0]) \wedge ([[PlanCode}] \geq 6.5) \wedge ([[YearStarted}] \geq 2013.2996785) \wedge ([[LifeOrientation}] \geq 23.71375)) \Rightarrow \text{No Risk}$
- $([[\text{YearStarted}] < 2016.5]) \wedge ([[\text{Majors}] \geq 1.5]) \wedge ([[Majors] \geq 5.0]) \wedge ([[PhysicsChem}] < 75.0) \wedge ([[Majors] < 7.5])) \Rightarrow \text{Low Risk}$

- $(([\text{YearStarted}] < 2016.5)) \wedge (([\text{Majors}] \geq 1.5)) \wedge (([\text{Majors}] \geq 5.0)) \wedge (([\text{PhysicsChem}] < 75.0)) \wedge (([\text{Majors}] \geq 7.5)) \wedge (([\text{PlanDescription}] < 14.0)) \rightarrow \text{Medium Risk}$
- $(([\text{YearStarted}] < 2016.5)) \wedge (([\text{Majors}] \geq 1.5)) \wedge (([\text{Majors}] \geq 5.0)) \wedge (([\text{PhysicsChem}] < 75.0)) \wedge (([\text{Majors}] \geq 7.5)) \wedge (([\text{PlanDescription}] \geq 14.0)) \rightarrow \text{Low Risk}$
- $(([\text{YearStarted}] < 2016.5)) \wedge (([\text{Majors}] \geq 1.5)) \wedge (([\text{Majors}] \geq 5.0)) \wedge (([\text{PhysicsChem}] \geq 75.0)) \wedge (([\text{MathematicsMaticMajor}] < 87.5)) \wedge (([\text{MathematicsMaticMajor}] < 85.0)) \rightarrow \text{No Risk}$
- $(([\text{YearStarted}] < 2016.5)) \wedge (([\text{Majors}] \geq 1.5)) \wedge (([\text{Majors}] \geq 5.0)) \wedge (([\text{PhysicsChem}] \geq 75.0)) \wedge (([\text{MathematicsMaticMajor}] < 87.5)) \wedge (([\text{MathematicsMaticMajor}] \geq 85.0)) \rightarrow \text{Medium Risk}$
- $(([\text{YearStarted}] < 2016.5)) \wedge (([\text{Majors}] \geq 1.5)) \wedge (([\text{Majors}] \geq 5.0)) \wedge (([\text{PhysicsChem}] \geq 75.0)) \wedge (([\text{MathematicsMaticMajor}] \geq 87.5)) \rightarrow \text{Low Risk}$
- $([\text{YearStarted}] \geq 2016.5) \rightarrow \text{Medium Risk}$

Let's evaluate each formula (or logical rule) separately.

```
In [23]: apply!(, X_test, y_test);
metricstable(
    ;
    normalize = true,
    metrics_kwarg = ();
    additional_metrics = ();
    height = r->SoleLogics.height(antecedent(r))
)
)
```

Antecedent	Consequent	ninstances	ncovered	coverage	confidence
lift	natoms	height			
$([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS\ Value] < 42.0546825) \wedge ([LifeOrientation] < 87.761518)$	Medium Risk	24	9	0.375	0.77777
8 1.55556 4 3					
$([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS\ Value] < 42.0546825) \wedge ([LifeOrientation] \geq 87.761518)$	High Risk	24	0	0.0	NaN
N NaN 4 3					
$([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS\ Value] \geq 42.0546825) \wedge ([AdditionalLanguage] < 74.950632)$	High Risk	24	0	0.0	NaN
NaN 4 3					
$([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS\ Value] \geq 42.0546825) \wedge ([AdditionalLanguage] \geq 74.950632) \wedge ([AgeatFirstYear] < 27.5967815)$	Low Risk	24	2	0.0833333	0.0
0.0 5 4					
$([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS\ Value] \geq 42.0546825) \wedge ([AdditionalLanguage] \geq 74.950632) \wedge ([AgeatFirstYear] \geq 27.5967815)$	Medium Risk	24	0	0.0	NaN
NaN 5 4					
$([YearStarted] < 2009.5) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] < 6.5) \wedge ([Homeprovince] < 1.5)$	Low Risk	24	0	0.0	NaN
NaN 4 3					
$([YearStarted] \in [2009.5, 2016.5]) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] < 6.5) \wedge ([Homeprovince] < 1.5)$	No Risk	24	4	0.166667	1.0
4.0 4 3					
$([YearStarted] < 2016.5) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] < 6.5) \wedge ([Homeprovince] \geq 1.5) \wedge ([AgeatFirstYear] < 22.5)$	Medium Risk	24	0	0.0	NaN
NaN 5 4					
$([YearStarted] < 2016.5) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] < 6.5) \wedge ([Homeprovince] \geq 1.5) \wedge ([AgeatFirstYear] \geq 22.5) \wedge ([AdditionalLanguage] < 34.0)$	No Risk	24	0	0.0	NaN
NaN 6 5					
$([YearStarted] < 2016.5) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] < 6.5) \wedge ([Homeprovince] \geq 1.5) \wedge ([AgeatFirstYear] \geq 22.5) \wedge ([AdditionalLanguage] \geq 34.0)$	Low Risk	24	0	0.0	NaN
NaN 6 5					
$([YearStarted] < 2013.2996785) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] \geq 6.5) \wedge ([Homeprovince] < 1.5)$	Low Risk	24	1	0.0416667	1.0
6.0 4 3					
$([YearStarted] < 2012.5) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] \geq 6.5) \wedge ([Homeprovince] \geq 1.5)$	No Risk	24	0	0.0	NaN
NaN 4 3					
$([YearStarted] \in [2012.5, 2013.2996785]) \wedge ([Majors] \in [1.5, 5.0]) \wedge ([PlanCode] \geq 6.5) \wedge ([Homeprovince] \geq 1.5)$	No Risk	24	0	0.0	NaN
NaN 4 3					

Let's summarize our model joining rules associated with the same class!

```
In [24]: metricstable(joinrules(); min_ncovered = 1, normalize = true))
```

Antecedent	Consequent	ninstances	ncovered	coverage	confidence
lift	natoms				
(([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS Value] < 42.0546825) \wedge ([LifeOrientation] < 87.761518)) \vee ([YearStarted] \geq 2016.5) Medium Risk 48 14 0.291667 0.857143 1.71429 5					
(([YearStarted] < 2016.5) \wedge ([Majors] < 1.5) \wedge ([APS Value] \geq 42.0546825) \wedge ([AdditionalLanguage] \geq 74.950632) \wedge ([AgeatFirstYear] < 27.5967815)) \vee ([YearStarted] < 2013.2996785) \wedge ([Majors] \in [1.5,5.0)) \wedge ([PlanCode] \geq 6.5) \wedge ([Homeprovince] < 1.5)) \vee ([YearStarted] < 2016.5) \wedge ([Majors] \in [5.0,7.5)) \wedge ([PhysicsChem] < 75.0)) \vee ([YearStarted] < 2016.5) \wedge ([Majors] \geq 7.5) \wedge ([PhysicsChem] < 75.0) \wedge ([PlanDescription] \geq 14.0)) Low Risk 96 6 0.0625 0.666667 4.0 16					
[YearStarted] \in [2009.5,2016.5) \wedge [Majors] \in [1.5,5.0) \wedge [PlanCode] < 6.5 \wedge [Homeprovince] < 1.5 No Risk 24 4 0.166667 1.0 4.0 4					

Let's now try to learn a random forest.

```
In [25]: try
    RandomForestClassifier = @load RandomForestClassifier pkg=DecisionTree
catch
    println("The RandomForestClassifier symbol has already been imported.
end
```

[Info: For silent loading, specify `verbosity=0`.
import MLJDecisionTreeInterface ✓

Out[25]: MLJDecisionTreeInterface.RandomForestClassifier

```
In [26]: forest = MLJDecisionTreeInterface.RandomForestClassifier(n_trees=10)
```

```
Out[26]: RandomForestClassifier(  
    max_depth = -1,  
    min_samples_leaf = 1,  
    min_samples_split = 2,  
    min_purity_increase = 0.0,  
    n_subfeatures = -1,  
    n_trees = 10,  
    sampling_fraction = 0.7,  
    feature_importance = :impurity,  
    rng = TaskLocalRNG())
```

```
In [27]: forestmach = machine(forest, X_train, y_train)
```

```
Out[27]: untrained Machine; caches model-specific representations of data  
model: RandomForestClassifier(max_depth = -1, ...)  
args:  
1: Source @568 ↴ Table{AbstractVector{Continuous}}  
2: Source @586 ↴ AbstractVector{OrderedFactor{4}}
```

```
In [28]: MLJ.fit!(forestmach, verbosity=0)
```

```
Out[28]: trained Machine; caches model-specific representations of data  
model: RandomForestClassifier(max_depth = -1, ...)  
args:  
1: Source @568 ↴ Table{AbstractVector{Continuous}}  
2: Source @586 ↴ AbstractVector{OrderedFactor{4}}
```

```
In [29]: 🌱 = fitted_params(forestmach).forest # \seedling:
```

```
Out[29]: Ensemble of Decision Trees  
Trees: 10  
Avg Leaves: 17.3  
Avg Depth: 7.4
```

Let's evaluate its performance.

```
In [30]: y_predict_probabilities = MLJ.predict(forestmach, X_test)  
y_predict = mode.(y_predict_probabilities)  
cm = confusion_matrix(y_predict, y_test)
```

```
Out[30]:
```

Predicted	Ground Truth			
	Medium R...	Low Risk	No Risk	High Risk
Medium R...	11	0	2	0
Low Risk	1	4	0	0
No Risk	0	0	4	0
High Risk	0	0	0	2

```
In [31]: accuracy(cm)
```

```
Out[31]: 0.875
```

Let's extract logical rules!

```
In [32]:  = solemodel() # \:evergreen_tree:
```

```

Out[32]: └─ Ensemble{UInt32} of 10 models of type Branch{UInt32}
  ├ [1/10] └─ (V1 < 2015.015294)
    └─ ↘ (V2 < 1.5)
      └─ ↘ 1 : (ninstances = 5, ncovered = 5, confidence = 1.0, lift =
        1.0)
        └─ ↖ (V19 < 45.665659500000004)
          └─ ↘ 3 : (ninstances = 5, ncovered = 5, confidence = 1.0, lift
            = 1.0)
            └─ ↖ (V19 < 71.94951499999999)
              └─ ↘ (V20 < 79.614036)
                └─ ↘ (V2 < 7.0)
                  └─ ↘ (V3 < 5.5)
                    └─ ↘ 3 : (ninstances = 1, ncovered = 1, confidence = 1.
                      0, lift = 1.0)
                    └─ ↖ 4 : (ninstances = 5, ncovered = 5, confidence = 1.
                      0, lift = 1.0)
                      └─ ↖ (V7 < 3.5)
                        └─ ↘ 1 : (ninstances = 2, ncovered = 2, confidence = 1.
                          0, lift = 1.0)
                        └─ ↖ (V15 < 68.5)
                          └─ ↘ 2 : (ninstances = 2, ncovered = 2, confidence =
                            1.0, lift = 1.0)
                          └─ ↖ 3 : (ninstances = 1, ncovered = 1, confidence =
                            1.0, lift = 1.0)
                          └─ ↖ 2 : (ninstances = 5, ncovered = 5, confidence = 1.0,
                            lift = 1.0)
                            └─ ↖ (V5 < 1.5)
                              └─ ↘ (V4 < 6.0)
                                └─ ↘ (V13 < 74.0)
                                  └─ ↘ 3 : (ninstances = 4, ncovered = 4, confidence =
                                    1.0, lift = 1.0)
                                  └─ ↖ (V19 < 83.5)
                                    └─ ↘ 2 : (ninstances = 2, ncovered = 2, confidence =
                                      1.0, lift = 1.0)
                                    └─ ↖ 3 : (ninstances = 2, ncovered = 2, confidence =
                                      1.0, lift = 1.0)
                                      └─ ↖ 1 : (ninstances = 1, ncovered = 1, confidence =
                                        1.0, lift = 1.0)
                                      └─ ↖ 2 : (ninstances = 8, ncovered = 8, confidence = 1.0,
                                        lift = 1.0)
                                        └─ ↖ (V14 < 76.5)
                                          └─ ↘ (V1 < 2017.0)
                                            └─ ↘ (V4 < 2.0)
                                              └─ ↘ 1 : (ninstances = 1, ncovered = 1, confidence =
                                                1.0, lift = 1.0)
                                              └─ ↖ 3 : (ninstances = 14, ncovered = 14, confidence = 1.0,
                                                lift = 1.0)
                                                └─ ↖ 1 : (ninstances = 2, ncovered = 2, confidence = 1.0,
                                                  lift = 1.0)
                                                  └─ ↖ 1 : (ninstances = 5, ncovered = 5, confidence = 1.0, lift =
                                                    1.0)
  ├ [2/10] └─ (V19 < 37.026329000000004)
    └─ ↘ 3 : (ninstances = 7, ncovered = 7, confidence = 1.0, lift =
      1.0)
      └─ ↖ (V1 < 2015.5)
        └─ ↘ (V7 < 3.5)
          └─ ↘ (V11 < 3.5)
            └─ ↘ (V15 < 71.2623505)
              └─ ↘ (V4 < 4.0)
                └─ ↘ (V5 < 1.5)

```



```

= 1.0) |   ✓ 2 : (ninstances = 4, ncov = 4, confidence = 1.0, lift
|       ↳ 4 : (ninstances = 3, ncov = 3, confidence = 1.0, lift
= 1.0)
|           ↳ (V14 < 90.0)
|               ✓ (V19 < 71.318906)
|                   ✓ (V7 < 2.0)
|                       ✓ 3 : (ninstances = 4, ncov = 4, confidence = 1.0, lif
t = 1.0)
|                           ↳ (V13 < 77.5)
|                               ✓ 2 : (ninstances = 2, ncov = 2, confidence = 1.0, l
ift = 1.0)
|                                   ↳ 3 : (ninstances = 2, ncov = 2, confidence = 1.0, l
ift = 1.0)
|                                       ↳ (V21 < 82.5)
|                                           ✓ 1 : (ninstances = 14, ncov = 14, confidence = 1.0, l
ift = 1.0)
|                                               ↳ (V3 < 25.0)
|                                                   ✓ 1 : (ninstances = 7, ncov = 7, confidence = 1.0, l
ift = 1.0)
|                                                       ↳ (V2 < 46.0)
|                                                           ✓ 2 : (ninstances = 2, ncov = 2, confidence = 1.0, lif
lift = 1.0)
|                                                               ↳ 3 : (ninstances = 1, ncov = 1, confidence = 1.0, lif
lift = 1.0)
|                                                                   ↳ 2 : (ninstances = 6, ncov = 6, confidence = 1.0, lift =
1.0)
|[5/10] ↳ (V10 < 20.5)
|    ✓ 1 : (ninstances = 11, ncov = 11, confidence = 1.0, lift =
1.0)
|        ↳ (V1 < 2011.0241065)
|            ✓ (V20 < 62.9324955)
|                ✓ 1 : (ninstances = 5, ncov = 5, confidence = 1.0, lift
= 1.0)
|                    ↳ (V21 < 81.5)
|                        ✓ 2 : (ninstances = 5, ncov = 5, confidence = 1.0, lif
t = 1.0)
|                            ↳ (V15 < 75.29259400000001)
|                                ✓ 2 : (ninstances = 1, ncov = 1, confidence = 1.0, l
ift = 1.0)
|                                    ↳ (V13 < 82.5)
|                                        ✓ 3 : (ninstances = 4, ncov = 4, confidence = 1.0,
lift = 1.0)
|                                            ↳ 1 : (ninstances = 2, ncov = 2, confidence = 1.0, lif
lift = 1.0)
|                                                ↳ (V4 < 9.0)
|                                                    ✓ (V7 < 2.5)
|                                                        ✓ 3 : (ninstances = 15, ncov = 15, confidence = 1.0, l
ift = 1.0)
|                                                            ↳ (V2 < 7.0)
|                                                                ✓ (V4 < 2.0)
|                                                                    ✓ 4 : (ninstances = 2, ncov = 2, confidence = 1.0, lif
lift = 1.0)
|                                                                        ↳ 3 : (ninstances = 7, ncov = 7, confidence = 1.0, lif
lift = 1.0)
|                                                                            ↳ (V10 < 24.578322)
|                                                                                ✓ (V16 < 78.0)
|                                                                                    ✓ 3 : (ninstances = 5, ncov = 5, confidence = 1.0, lif
0, lift = 1.0)
|                                                                                        ↳ 2 : (ninstances = 2, ncov = 2, confidence = 1.

```

```

0, lift = 1.0)
|   |   ↳ (V3 < 12.0)
|   |   |   ✓ 2 : (ninstances = 1, ncovred = 1, confidence = 1.
0, lift = 1.0)
|   |   ↳ 4 : (ninstances = 1, ncovred = 1, confidence = 1.
0, lift = 1.0)
|   |   ↳ (V15 < 76.5)
|   |   |   ✓ 2 : (ninstances = 3, ncovred = 3, confidence = 1.0, lif
t = 1.0)
|   |   |   ↳ 1 : (ninstances = 1, ncovred = 1, confidence = 1.0, lif
t = 1.0)
|[6/10] (V10 < 20.5)
|   |   ✓ 1 : (ninstances = 18, ncovred = 18, confidence = 1.0, lift =
1.0)
|   |   ↳ (V4 < 2.0)
|   |   |   ✓ (V6 < 41.0546825)
|   |   |   |   ✓ 1 : (ninstances = 5, ncovred = 5, confidence = 1.0, lift
= 1.0)
|   |   |   |   ↳ (V7 < 2.5)
|   |   |   |   |   ✓ 2 : (ninstances = 4, ncovred = 4, confidence = 1.0, lif
t = 1.0)
|   |   |   |   |   ↳ 4 : (ninstances = 5, ncovred = 5, confidence = 1.0, lif
t = 1.0)
|   |   |   |   ↳ (V1 < 2015.4700990000001)
|   |   |   |   |   ✓ (V2 < 6.0)
|   |   |   |   |   |   ✓ (V20 < 3.678195)
|   |   |   |   |   |   |   ✓ (V6 < 43.0)
|   |   |   |   |   |   |   |   ✓ 1 : (ninstances = 1, ncovred = 1, confidence = 1.0,
lift = 1.0)
|   |   |   |   |   |   |   |   |   ↳ 2 : (ninstances = 1, ncovred = 1, confidence = 1.0,
lift = 1.0)
|   |   |   |   |   |   |   |   |   |   ↳ 3 : (ninstances = 5, ncovred = 5, confidence = 1.0, l
ift = 1.0)
|   |   |   |   |   |   |   |   |   |   ↳ (V19 < 71.0)
|   |   |   |   |   |   |   |   |   |   |   ✓ (V11 < 2.0)
|   |   |   |   |   |   |   |   |   |   |   |   ✓ 3 : (ninstances = 1, ncovred = 1, confidence = 1.0,
lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   ↳ (V10 < 25.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   ✓ 2 : (ninstances = 3, ncovred = 3, confidence = 1.
0, lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   ↳ 3 : (ninstances = 1, ncovred = 1, confidence = 1.
0, lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   ↳ (V17 < 39.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   |   ✓ (V21 < 41.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   ✓ 4 : (ninstances = 1, ncovred = 1, confidence = 1.
0, lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   ↳ 2 : (ninstances = 1, ncovred = 1, confidence = 1.
0, lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   ↳ 2 : (ninstances = 11, ncovred = 11, confidence = 1.
0, lift = 1.0)
|   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   |   ↳ 3 : (ninstances = 8, ncovred = 8, confidence = 1.0, lift
= 1.0)
|[7/10] (V1 < 2016.5)
|   |   |   ✓ (V6 < 39.3047615)
|   |   |   |   ✓ (V17 < 26.0)
|   |   |   |   |   ✓ 3 : (ninstances = 1, ncovred = 1, confidence = 1.0, lift
= 1.0)
|   |   |   |   |   |   ↳ (V19 < 77.0)
|   |   |   |   |   |   |   ✓ (V16 < 70.5)
|   |   |   |   |   |   |   |   ✓ (V17 < 30.5)

```



```
lift = 1.0) |   Lx 3 : (ninstances = 1, ncov... = 1.0, li
             |   Lx (V2 < 1.5)
             |   |   ✓ 1 : (ninstances = 2, ncov...
ft = 1.0)   |   |   Lx (V10 < 24.706846)
             |   |   |   ✓ (V18 < 48.0)
             |   |   |   |   ✓ 3 : (ninstances = 1, ncov...
, lift = 1.0) |   |   |   Lx 2 : (ninstances = 13, ncov...
             .0, lift = 1.0) |   |   |   Lx (V16 < 79.4806935)
             |   |   |   |   ✓ (V13 < 40.0)
             |   |   |   |   |   ✓ 2 : (ninstances = 4, ncov...
             .0, lift = 1.0) |   |   |   |   Lx 3 : (ninstances = 2, ncov...
             |   |   |   .0, lift = 1.0) |   |   |   Lx 3 : (ninstances = 3, ncov...
             |   |   |   , lift = 1.0) |   |   |   Lx (V16 < 76.0)
             |   |   |   |   ✓ (V16 < 70.5)
             |   |   |   |   |   ✓ (V14 < 69.5)
             |   |   |   |   |   |   ✓ 1 : (ninstances = 3, ncov...
lift = 1.0) |   |   |   |   Lx 3 : (ninstances = 1, ncov...
lift = 1.0) |   |   |   Lx 3 : (ninstances = 2, ncov...
ft = 1.0)   |   |   Lx 1 : (ninstances = 3, ncov...
= 1.0)
```

In [33]: `listrules(🌲🌲🌲)`

```

OutOfMemoryError()

Stacktrace:
 [1] GenericMemory
   @ ./boot.jl:516 [inlined]
 [2] new_as_memoryref
   @ ./boot.jl:535 [inlined]
 [3] Array
   @ ./boot.jl:588 [inlined]
 [4] Array
   @ ./boot.jl:594 [inlined]
 [5] similar
   @ ./abstractarray.jl:868 [inlined]
 [6] similar
   @ ./abstractarray.jl:867 [inlined]
 [7] _array_for
   @ ./array.jl:676 [inlined]
 [8] collect(itr::Base.Generator{Base.Iterators.Zip{Tuple{Base.Iterator
s.ProductIterator{NTuple{10, Vector{Rule{UInt32}}}}}}, IterTools.var"#3#
4"{SoleModels.var"#191#194"{Bool, DecisionEnsemble{UInt32, Branch{UInt32},
SoleModels.var"#81#91"{SoleModels.var"#81#82#92"{DecisionTreeExt.var"#1#
3"}}, Nothing}}}})
   @ Base ./array.jl:796
 [9] listrules(m::DecisionEnsemble{UInt32, Branch{UInt32}}, SoleModels.va
r"#81#91"{SoleModels.var"#81#82#92"{DecisionTreeExt.var"#1#3"}}, Nothing);
compute_metrics::Bool, metrics_kwarg::@NamedTuple{}, use_shortforms::Bo
ol, use_leftmostlinearform::Nothing, normalize::Bool, normalize_kwarg::@Na
medTuple{allow_atom_flipping::Bool, rotate_commutatives::Bool}, scalar_sim
plification::Bool, force_syntaxtree::Bool, min_coverage::Nothing, min_ncov
ered::Nothing, min_ninstances::Nothing, min_confidence::Nothing, min_lif
t::Nothing, metric_filter_callback::Nothing, kwarg::@Kwarg{()})
   @ SoleModels ~/.julia/packages/SoleModels/bbNUZ/src/rule-extraction.j
l:223
 [10] listrules(m::DecisionEnsemble{UInt32, Branch{UInt32}}, SoleModels.va
r"#81#91"{SoleModels.var"#81#82#92"{DecisionTreeExt.var"#1#3"}}, Nothing)
   @ SoleModels ~/.julia/packages/SoleModels/bbNUZ/src/rule-extraction.j
l:166
 [11] top-level scope
   @ In[33]:1

```

This probably caused an `OutOfMemoryError()` (on my machine, it sure did!)

To appreciate this last part, let's play with a smaller model.

```

In [34]: forest = MLJDecisionTreeInterface.RandomForestClassifier(max_depth=3, n_t
Out[34]: RandomForestClassifier(
    max_depth = 3,
    min_samples_leaf = 1,
    min_samples_split = 2,
    min_purity_increase = 0.0,
    n_subfeatures = -1,
    n_trees = 3,
    sampling_fraction = 0.7,
    feature_importance = :impurity,
    rng = TaskLocalRNG())

```

```

In [35]: forestmach = machine(forest, X_train, y_train)

```

```
Out[35]: untrained Machine; caches model-specific representations of data
         model: RandomForestClassifier(max_depth = 3, ...)
         args:
           1: Source @650 ↗ Table{AbstractVector{Continuous}}
           2: Source @281 ↗ AbstractVector{OrderedFactor{4}}
```

```
In [36]: MLJ.fit!(forestmach, verbosity=0)
```

```
Out[36]: trained Machine; caches model-specific representations of data
         model: RandomForestClassifier(max_depth = 3, ...)
         args:
           1: Source @650 ↗ Table{AbstractVector{Continuous}}
           2: Source @281 ↗ AbstractVector{OrderedFactor{4}}
```

```
In [37]: 🌱 = fitted_params(forestmach).forest # \:seedling:
```

```
Out[37]: Ensemble of Decision Trees
         Trees:      3
         Avg Leaves: 6.333333333333333
         Avg Depth:  3.0
```

Let's evaluate its performance.

```
In [38]: y_predict_probabilities = MLJ.predict(forestmach, X_test)
         y_predict = mode.(y_predict_probabilities)
         cm = confusion_matrix(y_predict, y_test)
```

```
Out[38]:
```

		Ground Truth			
Predicted	Medium R...	Low Risk	No Risk	High Risk	
Medium R...	11	0	1	2	
Low Risk	1	2	2	0	
No Risk	0	2	3	0	
High Risk	0	0	0	0	

```
In [39]: accuracy(cm)
```

```
Out[39]: 0.6666666666666666
```

Let's extract logical rules!

```
In [40]: 🌲 = solemodel(🌱) # \:evergreen_tree:
```

```

Out[40]: └─ Ensemble{UInt32} of 3 models of type Branch{UInt32}
  ├─ [1/3] └─ (V10 < 20.5)
    |   └─ ✓ 1 : (ninstances = 10, ncovred = 10, confidence = 1.0, lift = 1.0)
    |       └─ ✘ (V21 < 75.411651)
    |           └─ ✓ 1 : (ninstances = 14, ncovred = 14, confidence = 0.57, lift = 1.0)
    |               └─ ✘ 3 : (ninstances = 20, ncovred = 20, confidence = 0.5, lift = 1.0)
    |                   └─ ✘ (V3 < 24.5)
    |                       └─ ✓ 2 : (ninstances = 16, ncovred = 16, confidence = 0.62, lift = 1.0)
    |                           └─ ✘ 3 : (ninstances = 5, ncovred = 5, confidence = 1.0, lift = 1.0)
  ├─ [2/3] └─ (V13 < 78.0)
    |   └─ ✓ (V13 < 42.151293)
    |       └─ ✓ (V13 < 10.947654)
    |           └─ ✓ 3 : (ninstances = 16, ncovred = 16, confidence = 0.38, lift = 1.0)
    |               └─ ✘ 4 : (ninstances = 6, ncovred = 6, confidence = 0.67, lift = 1.0)
    |                   └─ ✘ (V18 < 57.7403355)
    |                       └─ ✓ 3 : (ninstances = 3, ncovred = 3, confidence = 0.67, lift = 1.0)
    |                           └─ ✘ 3 : (ninstances = 6, ncovred = 6, confidence = 1.0, lift = 1.0)
    |                               └─ ✘ (V1 < 2016.5)
    |                                   └─ ✓ (V14 < 72.5)
    |                                       └─ ✓ 3 : (ninstances = 10, ncovred = 10, confidence = 0.4, lift = 1.0)
    |                                           └─ ✘ 2 : (ninstances = 17, ncovred = 17, confidence = 0.88, lift = 1.0)
    |                                               └─ ✘ 1 : (ninstances = 7, ncovred = 7, confidence = 1.0, lift = 1.0)
  └─ [3/3] └─ (V17 < 39.690162)
    |   └─ ✓ (V4 < 2.0)
    |       └─ ✓ 1 : (ninstances = 4, ncovred = 4, confidence = 1.0, lift = 1.0)
    |           └─ ✘ (V1 < 2011.0)
    |               └─ ✓ 1 : (ninstances = 2, ncovred = 2, confidence = 1.0, lift = 1.0)
    |                   └─ ✘ 3 : (ninstances = 8, ncovred = 8, confidence = 1.0, lift = 1.0)
    |                       └─ ✘ (V4 < 1.5)
    |                           └─ ✓ (V21 < 75.83743150000001)
    |                               └─ ✓ 4 : (ninstances = 7, ncovred = 7, confidence = 0.71, lift = 1.0)
    |                                   └─ ✘ 2 : (ninstances = 10, ncovred = 10, confidence = 0.9, lift = 1.0)
    |                                       └─ ✘ (V1 < 2016.5)
    |                                           └─ ✓ 2 : (ninstances = 24, ncovred = 24, confidence = 0.54, lift = 1.0)
    |                                               └─ ✘ 1 : (ninstances = 10, ncovred = 10, confidence = 1.0, lift = 1.0)

```

In [41]: `listrules(🎄🎄)`

```

Out[41]: 5×7×7 Array{Rule{UInt32}, 3}:
[:, :, 1] =
    □ ((V10 < 20.5)) ∧ ((V13 < 78.0)) ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.94
7654)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1
        ... □ ((V10 < 20.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
< 2.0)) ↳ 1
        □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
< 2.0)) ↳ 3
        □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
< 2.0)) ↳ 2
        □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
< 2.0)) ↳ 3
        □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 < 2.0)) ↳ 1

[:, :, 2] =
    □ ((V10 < 20.5)) ∧ ((V13 < 78.0)) ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.94
7654)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 2011.0)) ↳ 1
        ... □ ((V10 < 20.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 20
11.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 < 2011.0)) ↳ 1
        □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 20
11.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 < 2011.0)) ↳ 3
        □ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 20
11.0)) ↳ 1

    □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 < 2011.0)) ↳ 2
        □ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 20
11.0)) ↳ 1

```

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 < 2011.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 < 20
11.0)) ↳ 1

[:, :, 3] =

■ ((V10 < 20.5)) ∧ ((V13 < 78.0)) ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.94
7654)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 2011.0)) ↳ 3
... ■ ((V10 < 20.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 20
11.0)) ↳ 1

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 ≥ 2011.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 20
11.0)) ↳ 1

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 ≥ 2011.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 20
11.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 ≥ 2011.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 20
11.0)) ↳ 2

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 < 39.690162)) ∧ ((V4
≥ 2.0)) ∧ ((V1 ≥ 2011.0)) ↳ 3

■ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 < 39.690162)) ∧ ((V4 ≥ 2.0)) ∧ ((V1 ≥ 20
11.0)) ↳ 3

[:, :, 4] =

■ ((V10 < 20.5)) ∧ ((V13 < 78.0)) ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.94
7654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 75.83743150000000
1)) ↳ 4

... ■ ((V10 < 20.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 7
5.83743150000001)) ↳ 1

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4
< 1.5)) ∧ ((V21 < 75.83743150000001)) ↳ 4

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 7
5.83743150000001)) ↳ 1

■ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 < 78.0))

$\wedge ((V13 < 42.151293)) \wedge ((V13 < 10.947654)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 < 75.83743150000001)) \Rightarrow 3$

□ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 ≥ 2.0)) ∧ ((V13 ≥ 78.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 75.83743150000001)) → 4

■ $((V10 \geq 20.5)) \wedge ((V21 \geq 75.411651)) \wedge ((V3 < 24.5)) \wedge ((V13 < 78.0))$
 $\wedge ((V13 < 42.151293)) \wedge ((V13 < 10.947654)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 < 75.83743150000001)) \Rightarrow 4$

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 ≥ 78.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 75.83743150000001)) ⇒ 4

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 < 78.0))
 ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4
 ≤ 1.5)) ∧ ((V21 < 75.83743150000001)) ⇒ 3

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 78.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 < 75.83743150000001)) → 4

[:, :, 5] =

□ ((V10 < 20.5)) ∧ ((V13 < 78.0)) ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 ≥ 75.83743150000001)) ⇒ ?

... $\square ((V10 < 20.5)) \wedge ((V13 \geq 7.8)) \wedge ((V1 \geq 2016.5)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 \geq 75.83743150000001))$... 1

□ ((V10 ≥ 20.5)) ∧ ((V21 < 75.411651)) ∧ ((V4 < 2.0)) ∧ ((V13 < 78.0))
∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4
< 1.5)) ∧ ((V21 > 75.82742150000001)) ... 2

$\square ((V10 \geq 20.5)) \wedge ((V21 < 75.411651)) \wedge ((V4 < 2.0)) \wedge ((V13 \geq 7.8.0)) \wedge ((V1 \geq 2016.5)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 \geq 7.5.8274215000001))$

■ $((V10 \geq 20.5)) \wedge ((V21 < 75.411651)) \wedge ((V4 \geq 2.0)) \wedge ((V13 < 78.0))$
 $\wedge ((V13 < 42.151293)) \wedge ((V13 < 10.947654)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 < 75.8274215000001))$

$\square ((V10 \geq 20.5)) \wedge ((V21 < 75.411651)) \wedge ((V4 \geq 2.0)) \wedge ((V13 \geq 7.8.0)) \wedge ((V1 \geq 2016.5)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 < 1.5)) \wedge ((V21 \geq 7.5.83743150000001)) \rightarrow 2$

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 < 78.0))
 ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4
 < 1.5)) ∧ ((V21 ≥ 75.83743150000001)) ⇒ 2

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 < 24.5)) ∧ ((V13 ≥ 7
8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 ≥ 7
5.83743150000001)) ⇒ 2

■ $((V10 \geq 20.5)) \wedge ((V21 \geq 75.411651)) \wedge ((V3 \geq 24.5)) \wedge ((V13 < 78.0))$
 $\wedge ((V13 < 42.151293)) \wedge ((V13 < 10.947654)) \wedge ((V17 \geq 39.690162)) \wedge ((V4 \leq 1.5)) \wedge ((V21 \geq 75.83743150000001)) \Rightarrow 3$

□ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 78.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 < 1.5)) ∧ ((V21 ≥ 75.83743150000001)) ⇒ ?

[:, :, 6] =

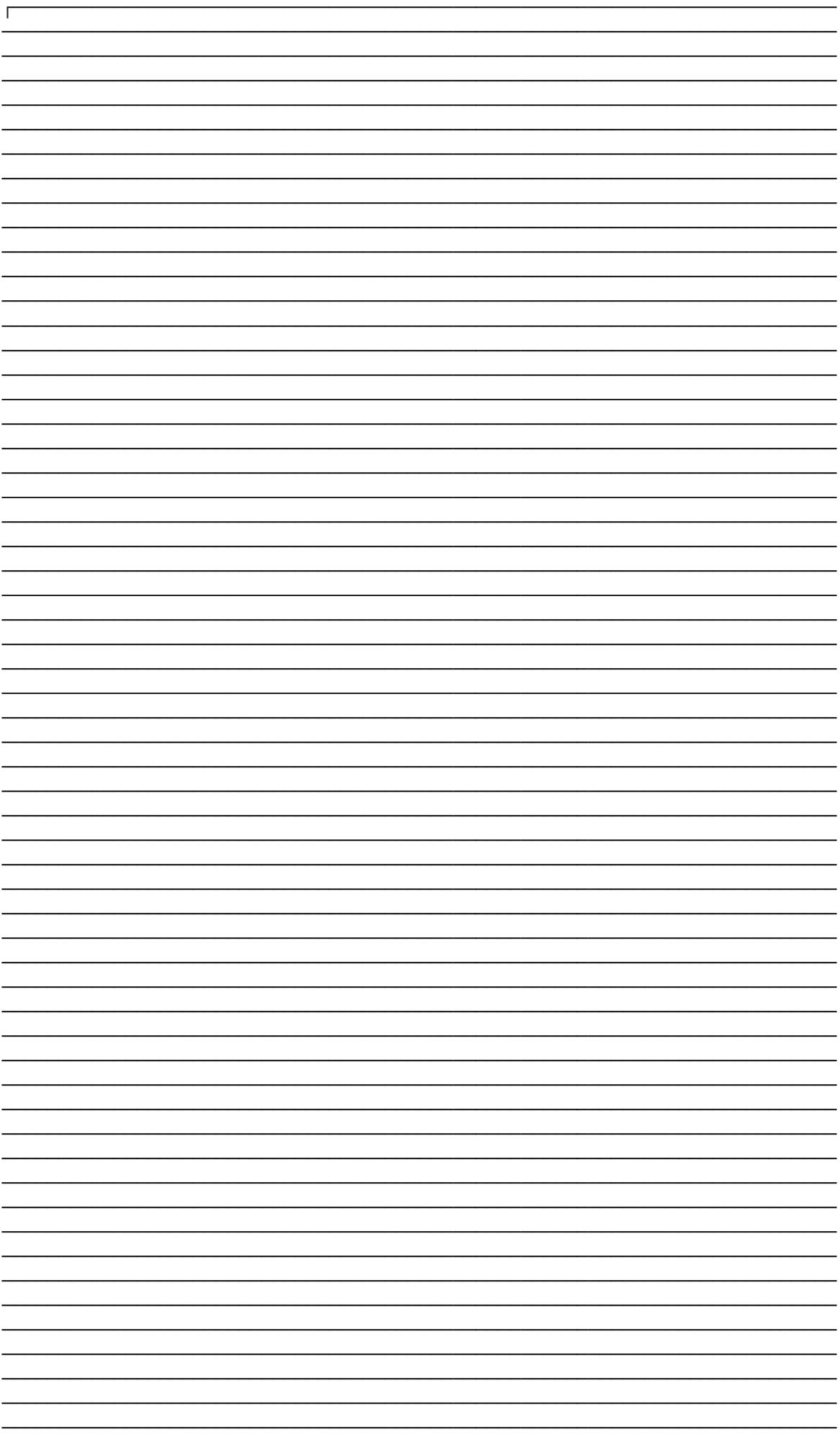
((V10 < 20.5)) \wedge ((V13 < 78.0)) \wedge ((V13 < 42.151293)) \wedge ((V13 < 10.94

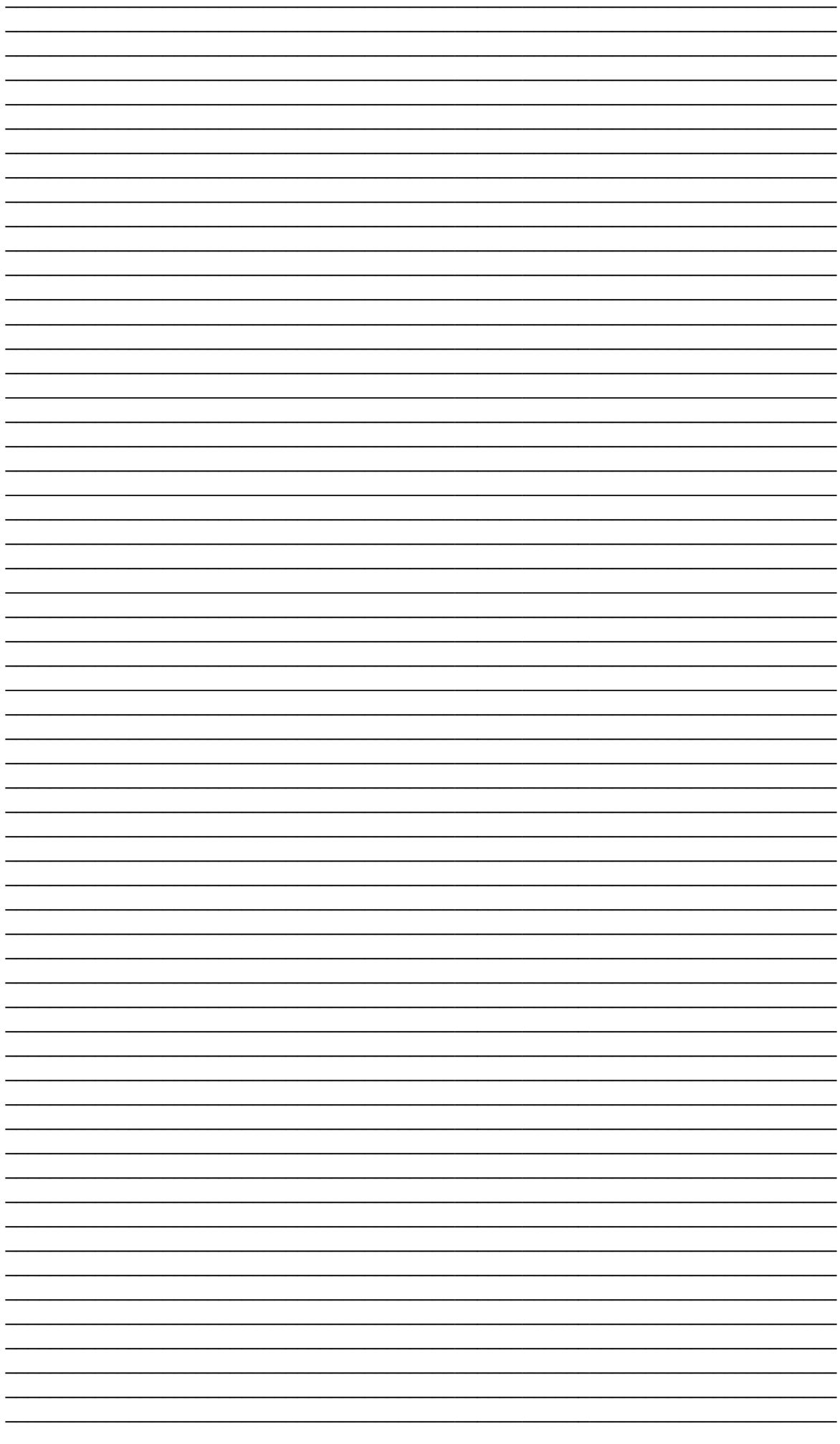

```
16.5)) => 1
```

```
  └─ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 < 78.0))
    ∧ ((V13 < 42.151293)) ∧ ((V13 < 10.947654)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4
    ≥ 1.5)) ∧ ((V1 ≥ 2016.5)) => 3
      └─ ((V10 ≥ 20.5)) ∧ ((V21 ≥ 75.411651)) ∧ ((V3 ≥ 24.5)) ∧ ((V13 ≥ 7
      8.0)) ∧ ((V1 ≥ 2016.5)) ∧ ((V17 ≥ 39.690162)) ∧ ((V4 ≥ 1.5)) ∧ ((V1 ≥ 20
      16.5)) => 1
```

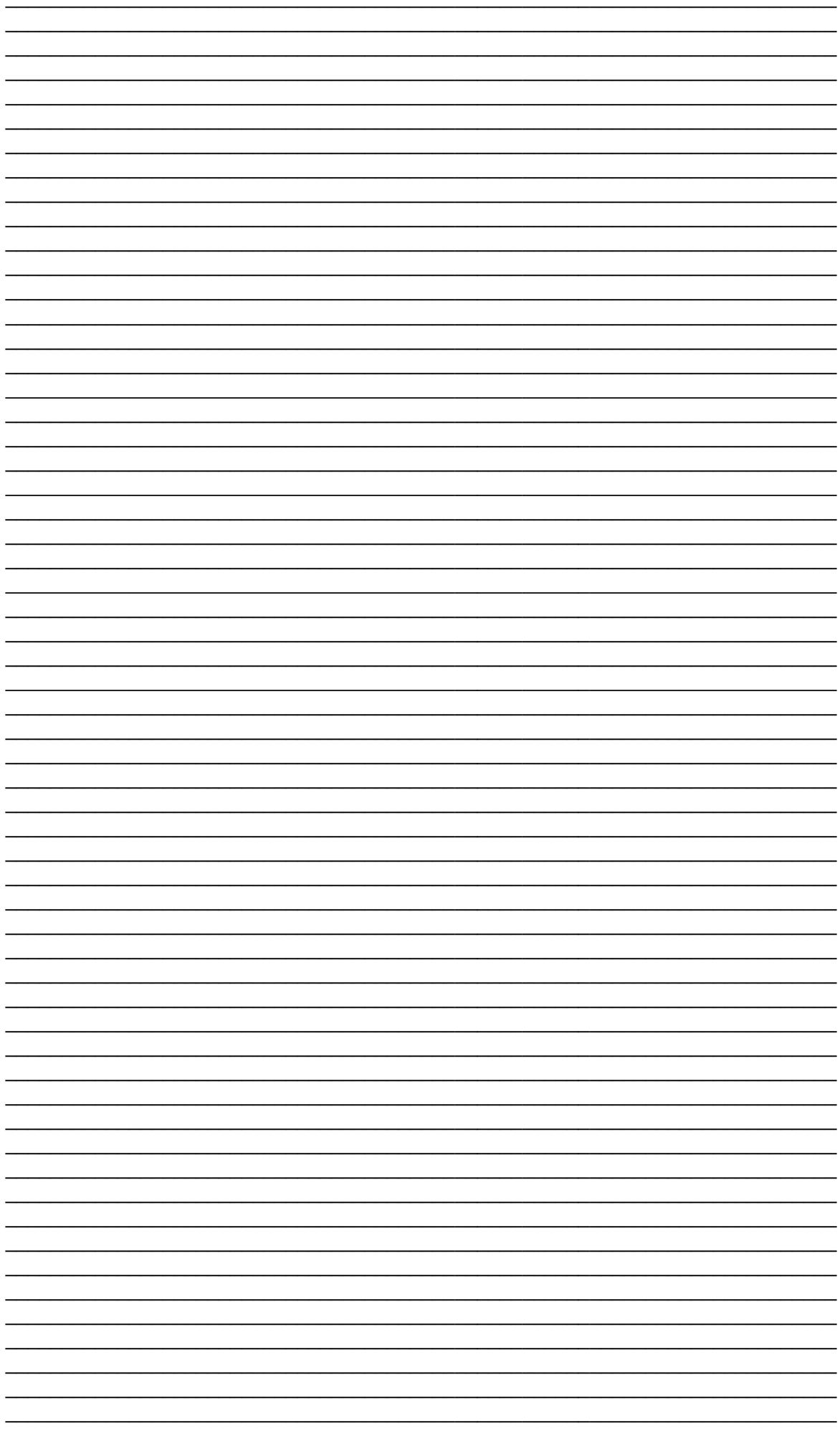
Let's summarize our model joining rules associated with the same class!

```
In [42]: metricstable(joinrules(; min_ncovered = 1, normalize = true))
```





Antecedent	Consequent	ninstances	ncovered	coverage	confidence
lift	natoms				



$((V10 < 20.5) \wedge (V13 < 10.947654) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0) \wedge (V13 < 10.947654) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 < 20.5) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 < 20.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 < 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 < 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 < 20.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 \geq 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 \geq 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 < 20.5) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 < 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 < 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 < 20.5) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 \geq 7.25) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651)$

$((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 < 10.947654) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 < 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 \geq 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 < 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 \geq 2.0) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 \geq 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 \geq 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 \geq 24.5) \wedge (V13 \geq 78.0) \wedge (V1 < 2016.5) \wedge (V14 \geq 72.5) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 < 10.947654) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge (V1 < 2011.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 < 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge (V1 < 2011.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 \geq 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge (V1 < 2011.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 \geq 24.5) \wedge (V13 \in [42.151293, 78.0)) \wedge (V18 \geq 57.7403355) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge (V1 < 2011.0))$

$((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 \geq 2.0) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 \geq 24.5) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 < 2.0)) \vee ((V10 \geq 20.5) \wedge (V21 < 75.411651) \wedge (V4 < 2.0)) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge (V1 < 2011.0)) \vee ((V10 \geq 20.5) \wedge (V21 \geq 75.411651) \wedge (V3 < 24.5) \wedge (V13 \in [10.947654, 42.151293)) \wedge (V17 < 39.690162) \wedge (V4 \geq 2.0) \wedge$

000001)) v ((V10 < 20.5) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 < 2016.5)) v ((V10 ≥ 20.5) ∧ (V21 < 75.411651) ∧ (V4 < 2.0) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 < 2016.5)) v ((V10 ≥ 20.5) ∧ (V21 < 75.411651) ∧ (V4 ≥ 2.0) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 < 2016.5)) v ((V10 ≥ 20.5) ∧ (V21 ≥ 75.411651) ∧ (V3 ≥ 24.5) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 < 2016.5)) v ((V10 ≥ 20.5) ∧ (V21 < 75.411651) ∧ (V4 ≥ 2.0) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 ≥ 2016.5)) v ((V10 ≥ 20.5) ∧ (V21 ≥ 75.411651) ∧ (V3 < 24.5) ∧ (V13 ∈ [10.947654, 42.151293]) ∧ (V17 ≥ 39.690162) ∧ (V4 ≥ 1.5) ∧ (V1 ≥ 2016.5)) | 4 | 2860 | 376 | 0.131469 | 0.744681 | 9.68085 | 310 |

