

Modal Symbolic Learning: Day 2

NATOPS: Interpretable gesture recognition

```
In [ ]: using Pkg
Pkg.activate(".")
Pkg.instantiate()
Pkg.update()
Pkg.status()
```

```
Activating project at `~/Desktop/modal-symbolic-learning-course`
Updating registry at `~/.julia/registries/General`
Updating git-repo `https://github.com/JuliaRegistries/General.git`
Installed BenchmarkTools — v1.4.0
Installed LoweredCodeUtils — v2.3.2
Installed ModalDecisionTrees — v0.3.3
Installed SoleLogics — v0.6.11
Installed SoleModels — v0.5.3
Updating `~/Desktop/modal-symbolic-learning-course/Project.toml`
[e54bda2e] ↑ ModalDecisionTrees v0.3.2 ⇒ v0.3.3
[b002da8f] ↑ SoleLogics v0.6.10 ⇒ v0.6.11
[4249d9c7] ↑ SoleModels v0.5.2 ⇒ v0.5.3
Updating `~/Desktop/modal-symbolic-learning-course/Manifest.toml`
[6e4b80f9] ↑ BenchmarkTools v1.3.2 ⇒ v1.4.0
[6f1432cf] ↑ LoweredCodeUtils v2.3.1 ⇒ v2.3.2
[e54bda2e] ↑ ModalDecisionTrees v0.3.2 ⇒ v0.3.3
[b002da8f] ↑ SoleLogics v0.6.10 ⇒ v0.6.11
[4249d9c7] ↑ SoleModels v0.5.2 ⇒ v0.5.3
Precompiling project...
✓ BenchmarkTools
✓ LoweredCodeUtils
✓ Revise
✓ SoleLogics
✓ SoleModels
```

```
In [8]: # Import libraries for statistics & Machine Learning
using Random
using DataFrames
using Plots
using StatsBase

using MLJ
using Sole
```

```
In [13]: using JLD2
using DataFrames # (Maybe need version v1.6.1?)
JLD2.@load "COVID-dataset.jld2"
(X1_df, X2_df, y) = dataset;
```

```
In [9]: countmap(y)
```

```
Out[9]: Dict{String, Int64} with 2 entries:  
  "POSITIVE" => 91  
  "NEGATIVE" => 106
```

```
In [21]: using SoleData
```

```
X_multimodal = MultiModalDataset([X1_df, X2_df])
```

```
Out[21]: ● MultiModalDataset{DataFrame}
  └─ dimensionalities: (1, 1)
- Modality 1 / 2
  └─ dimensionality: 1
```

197×30 SubDataFrame

Row	cough_F1	cough_F2
c ...	SubArray...	SubArray...
S ...		
1	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0658202, 0.0389503, 0.505408,...
2	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[1.62005, 0.648436, 0.248455, 0...
3	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[2.95991, 1.13398, 0.151934, 0.1...
4	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[3.66094, 0.709991, 0.342895, 0...
5	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[1.26265, 0.966647, 0.281845, 0...
6	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[4.12442, 2.09424, 0.267123, 0.1...
7	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[3.42468, 1.26102, 0.164075, 0.0...
8	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[10.8754, 0.646552, 0.395368, 0...
9	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[18.1984, 2.61893, 1.77536, 1.02...
10	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[3.37013, 1.19436, 0.97079, 0.60...
11	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[2.34154, 0.925767, 0.378433, 0...
⋮	⋮	⋮
188	[0.0726378, 0.00766837, 0.016578...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
189	[0.35084, 0.093121, 0.0471824, 0...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
190	[0.00220116, 0.0199147, 0.166516...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
191	[0.0770436, 0.00820453, 0.001445...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
192	[0.0453022, 0.00469916, 0.001939...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
193	[3.23477e-5, 0.000132317, 0.0001...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
194	[0.127782, 0.101379, 0.0369538, ...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
195	[0.00149723, 0.000397901, 0.0010...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
196	[0.00252365, 0.0540424, 0.065236...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
197	[0.115361, 0.0464483, 0.0123202,...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...

28 columns and 176 rows om

itted

- Modality 2 / 2
└ dimensionality: 1

197×30 SubDataFrame

Row	breath_F1	breath_F2
b ...	Array...	Array...
A ...		
1	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0275974, 0.123487, 0.954918, ...
[...		
2	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.00551542, 0.738461, 1.23345, ...
[
3	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0171132, 0.0128541, 0.175568,...
[
4	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0713483, 0.191903, 0.0599709,...
[
5	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0346951, 0.026089, 6.83611, 2...
[...		
6	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0372815, 1.61098, 7.59596, 1...
[
7	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0179035, 0.0158171, 6.72805, ...
[
8	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.038656, 0.202587, 0.0588298, ...
[
9	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.177666, 0.296219, 0.00581333,...
[...		
10	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.407654, 0.4168, 0.0640127, 0...
[
11	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...	[0.0442603, 0.0363921, 1.94756, ...
[
:	:	:
...		
188	[0.000519218, 0.000857345, 0.000...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
189	[0.0134826, 0.495593, 0.0, 0.0, ...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[...		
190	[0.000243355, 0.000393873, 0.000...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
191	[0.000504018, 0.00280926, 0.0030...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
192	[0.00447856, 0.0114002, 0.004106...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
193	[0.00081567, 0.00117782, 0.00106...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[...		
194	[0.101095, 0.472197, 0.0360748, ...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
195	[0.00159912, 0.00231749, 0.00020...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
196	[0.0280692, 0.0461481, 0.218395,...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[
197	[0.251001, 0.0259159, 0.0174663,...	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0...
[...		

28 columns and 176 rows om

itted

```
In [23]: modality(X_multimodal, 1) # Cough modality
```

Out[23]: 197×30 SubDataFrame

172 rows omitted

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
1	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0658202,	[0.0130705,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00454093,	[
		0.0389503,	0.00773471,		0.00181044,	0
		0.505408,	0.100364,		0.00463918,	0
		0.659653,	0.130993,		0.00812784,	0
		0.479911,	0.0953002,		0.0114677,	1
		0.198311,	0.0393805,		0.00279443,	0
		0.038341,	0.00761372,		0.00452539,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
2	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1.62005,	[0.321709,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0714415,	[
		0.648436,	0.128766,		0.0461039,	4
		0.248455,	0.0493379,		0.0216893,	2
		0.272204,	0.0540539,		0.0326628,	3
		0.115829,	0.0230012,		0.019149,	1
		0.701655,	0.139334,		0.0363546,	3
		0.730142,	0.144991,		0.0479683,	4
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
3	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[2.95991,	[0.587777,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.287868,	[
		1.13398,	0.225185,		0.100246,	9
		0.151934,	0.0301709,		0.00532329,	0
		0.122773,	0.0243801,		0.00555218,	0
		0.0847807,	0.0168357,		0.00194837,	0
		0.0358195,	0.00711301,		0.00139787,	0
		0.023554,	0.00467733,		0.0025744,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
4	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[3.66094,	[0.726986,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.596604,	[
		0.709991,	0.140989,		0.143737,	1
		0.342895,	0.0680918,		0.0243013,	2
		0.265306,	0.0526841,		0.017446,	1
		0.0468018,	0.00929385,		0.00756199,	0
		0.0975574,	0.0193729,		0.00591798,	0
		0.0396136,	0.00786644,		0.000982618,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
		0.0, 0.0, 0.0,	0.0, 0.0, 0.0,		0.0, 0.0, 0.0,	0
5	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1.26265,	[0.250736,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.128993,	[
		0.966647,	0.191956,		0.0764966,	7
		0.281845,	0.0559685,		0.0233883,	2
		0.14006,	0.027813,		0.0117256,	1
		0.0330181,	0.00655671,		0.00282783,	0
		0.0189545,	0.00376397,		0.00201767,	0

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
		0.0202496, 0.00427777, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.00402115, 0.000849476, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]		0.00842082, 0.00644938, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0 0 0 0 0
6	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[4.12442, 2.09424, 0.267123, 0.100803, 0.104586, 0.0637793, 0.0165705, 0.0220245, 0.0118193, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.819024, 0.415873, 0.053045, 0.0200174, 0.0207686, 0.0126652, 0.00329055, 0.0043736, 0.00234707, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.164946, 0.138568, 0.0176139, 0.00586853, 0.00260732, 0.00219175, 0.00100813, 0.00768144, 0.00797681, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1 1 0 0 0 0 0 0 0 0 0 0
7	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[3.42468, 1.26102, 0.164075, 0.0827096, 0.0727358, 0.0332375, 0.00864315, 0.0294517, 0.0301729, 0.0451799, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.680069, 0.250411, 0.0325819, 0.0164244, 0.0144438, 0.00660026, 0.00171635, 0.00584848, 0.00599171, 0.00897178, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.201791, 0.102281, 0.0150567, 0.00414152, 0.00349754, 0.00190844, 0.000577779, 0.000441292, 0.00100831, 0.00227998, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[9 1 0 0 0 0 0 0 0 0 0 0
8	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[10.8754, 0.646552, 0.395368, 0.306463, 0.0464313, 0.0182149, 0.0898324, 0.11998, 0.025443, 0.011258, 0.0263648, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[2.15962, 0.128392, 0.0785118, 0.0608572, 0.00922028, 0.00361709, 0.0178388, 0.0238254, 0.00505245, 0.00223559, 0.00523549, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.531624, 0.0291421, 0.0249703, 0.0202988, 0.00218111, 0.00111567, 0.00265106, 0.00404789, 0.00576916, 0.00679558, 0.00494477, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[2 2 1 0 0 0 0 0 0 0 0 0
9	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[18.1984, 2.61893, 1.77536, 1.02094, 0.197965, 0.506792, 0.250556, 0.112402,	[3.61381, 0.520065, 0.35255, 0.202737, 0.0393117, 0.100638, 0.0497552, 0.0223206,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1.0694, 0.227274, 0.472316, 0.224377, 0.0118801, 0.0112027, 0.0299956, 0.0321187,	[2 4 2 1 1 2 2 3

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
		0.234197, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.0465066, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]		0.027308, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	2 0 0 0
10	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[3.37013, 1.19436, 0.97079, 0.600305, 0.176715, 0.0773258, 0.0182055, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.669236, 0.237175, 0.192778, 0.119208, 0.0350919, 0.0153553, 0.00361524, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.446583, 0.20182, 0.068445, 0.0334676, 0.0137318, 0.00983118, 0.00542909, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1 1 6 3 1 0 0 0 0 0 0
11	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[2.34154, 0.925767, 0.378433, 0.123683, 0.0554886, 0.0348641, 0.0349075, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.464981, 0.183838, 0.0751489, 0.0245608, 0.0110189, 0.00692327, 0.0069319, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.388725, 0.139274, 0.0471144, 0.0156152, 0.0121435, 0.0237099, 0.0155309, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1 4 1 1 2 1 0 0 0 0 0
12	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[3.07298, 2.57072, 0.687283, 0.322323, 0.214695, 0.0641531, 0.0246654, 0.0356907, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.61023, 0.510491, 0.13648, 0.0640066, 0.0426338, 0.0127395, 0.00489802, 0.00708743, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.204552, 0.231794, 0.051393, 0.0287529, 0.0233669, 0.00844628, 0.00442164, 0.00340762, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[2 5 2 2 0 0 0 0 0 0 0 0
13	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1.77748, 0.796787, 0.0738923, 0.0442614, 0.0555183, 0.0385192, 0.0508226, 0.101736, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.352971, 0.158225, 0.0146735, 0.00878938, 0.0110248, 0.0076491, 0.0100923, 0.0202027, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.203237, 0.0634473, 0.00590952, 0.00739434, 0.0543729, 0.0397721, 0.0168973, 0.0131004, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[6 0 0 5 3 1 1 0 0 0 0

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
	:	:	:	:	:	:
186	[0.0174438, 0.00310092, 0.00849625, 0.026699, 0.0209502, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0132189, 0.00241784, 0.0035302, 0.00828464, 0.00804756, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00534833, 0.000978251, 0.00142831, 0.00335194, 0.00325602, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0]
187	[0.0291811, 0.0169011, 0.0162059, 0.0177519, 0.121101, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0]	[0.0421715, 0.00966519, 0.00904388, 0.0169365, 0.0497429, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0170625, 0.00391051, 0.00365913, 0.00685247, 0.0201259, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0]
188	[0.0726378, 0.00766837, 0.016578, 0.0160573, 0.0146287, 0.011821, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0858145, 0.00341952, 0.00950763, 0.0234871, 0.0317684, 0.0292289, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0347203, 0.00138353, 0.00384676, 0.00950284, 0.0128534, 0.011826, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0 0]
189	[0.35084, 0.093121, 0.0471824, 0.766623, 6.82305, 1.83248, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.204067, 0.0762902, 0.0502624, 0.666629, 5.60448, 1.80846, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.082565, 0.0308668, 0.020336, 0.269717, 2.26756, 0.731699, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 8 4 0 0 0 0]
190	[0.00220116, 0.0199147, 0.166516, 0.0951876, 0.128625, 0.459631, 0.263766, 0.0405767,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00105089, 0.0269954, 0.201371, 0.124756, 0.0703357, 0.288238, 0.229707, 0.0601887,	[0.000425188, 0.0109223, 0.0814741, 0.0504759, 0.0284576, 0.11662, 0.0929391, 0.0243522,	[0 0 0 0 0 1 1 0]

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
	2.5724, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]			3.26771, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	1.32211, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	5 0 0 0
191	[0.0770436, 0.00820453, 0.00144554, 0.0066907, 0.143037, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.115118, 0.00808703, 0.00118068, 0.0132742, 0.0605214, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0465763, 0.00327199, 0.000477701, 0.00537071, 0.0244868, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0
192	[0.0453022, 0.00469916, 0.00193911, 0.00619609, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0162656, 0.00264962, 0.000846998, 0.00225862, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00658101, 0.00107203, 0.000342693, 0.000913833, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0
193	[3.23477e-5, 0.000132317, 0.000143602, 0.000385296, 0.0215862, 0.0367591, 0.00904464, 0.0214649, 0.0223188, 0.0445251, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[1.90018e-5, 7.08086e-5, 6.93151e-5, 0.000174685, 0.00977338, 0.0182157, 0.00556471, 0.0112506, 0.00797403, 0.0179365, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[7.68809e-6, 2.8649e-5, 2.80447e-5, 7.06772e-5, 0.00395429, 0.00737002, 0.00225147, 0.00455199, 0.00322627, 0.00725706, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[5 5 0 0 0 0 0 0 0 0 0 0 0
194	[0.127782, 0.101379, 0.0369538, 0.019505, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.136504, 0.0900751, 0.0530071, 0.0228197, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.055229, 0.0364442, 0.0214465, 0.00923281, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0 0
195	[0.00149723, 0.000397901, 0.0010245,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0,	[0.000619492, 0.000181285, 0.000723292,	[0.000250645, 7.33474e-5, 0.000292642,	[0 0 0

Row	cough_F1	cough_F2	cough_F3	cough_F4	cough_F5	c
	SubArray...	SubArray...	SubArray...	SubArray...	SubArray...	S
	0.17157, 0.276365, 0.0568549, 0.0536703, 0.439603, 0.599519, 0.126497, 0.00765833, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.162552, 0.357302, 0.139281, 0.0253212, 0.291274, 0.288937, 0.064765, 0.00581977, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0.0657682, 0.144563, 0.0563528, 0.0102449, 0.117849, 0.116903, 0.0262038, 0.00235467, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	0 0 0 0 0 0 0 0 0 0
196	[0.00252365, 0.0540424, 0.0652368, 0.019338, 0.0124232, 0.00385076, 0.00511448, 0.00346474, 0.00342869, 0.0238765, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00247622, 0.117222, 0.19843, 0.0274702, 0.0143665, 0.00181369, 0.00400859, 0.00402005, 0.00280431, 0.0134033, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.00100187, 0.0474279, 0.0802844, 0.0111144, 0.00581265, 0.000733817, 0.00162187, 0.0016265, 0.00113462, 0.00542295, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0 0 0 0
197	[0.115361, 0.0464483, 0.0123202, 0.0632743, 0.11675, 0.0424258, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0, 0.0]	[0.206398, 0.0766185, 0.0210895, 0.0674126, 0.107959, 0.0308161, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0.0835083, 0.0309996, 0.00853277, 0.027275, 0.0436798, 0.0124681, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0, 0.0]	[0 0 0 0 0 0 0 0 0 0

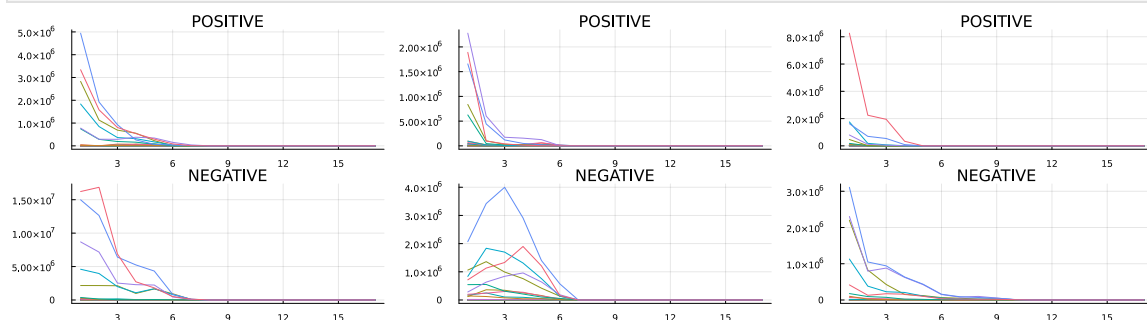
In [26]: `names(X1_df)`

Out[26]: 30-element Vector{String}:

```
"cough_F1"  
"cough_F2"  
"cough_F3"  
"cough_F4"  
"cough_F5"  
"cough_F6"  
"cough_F7"  
"cough_F8"  
"cough_F9"  
"cough_F10"  
"cough_F11"  
"cough_F12"  
"cough_F13"  
⋮  
"cough_F19"  
"cough_F20"  
"cough_F21"  
"cough_F22"  
"cough_F23"  
"cough_F24"  
"cough_F25"  
"cough_F26"  
"cough_F27"  
"cough_F28"  
"cough_F29"  
"cough_F30"
```

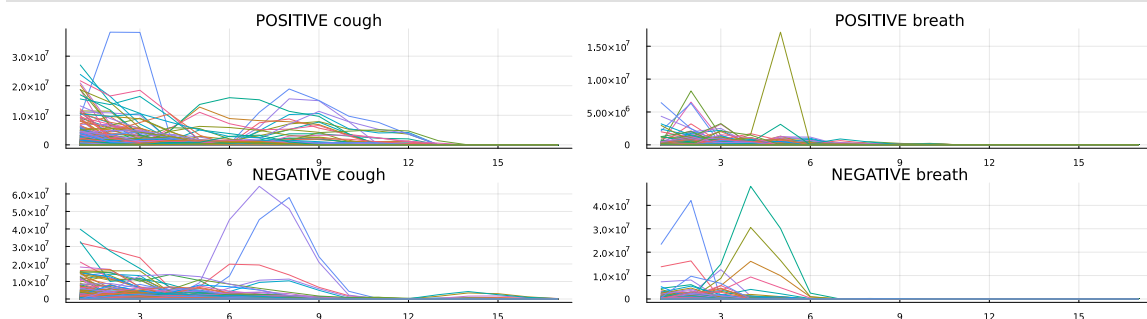
```
In [39]: # Let's inspect some instances  
plot(map(i->plot(collect(X1_df[i,:]), labels=nothing, title=y[i]), 1:35:(35*6
```

Out[39]:



```
In [41]: # All instances, grouped by class  
plot(map((((X_mod, mod_name), _y),)->plot(collect.(eachrow(X_mod[findall(_y
```

Out[41]:



```
In [72]: using ModalDecisionTrees
```

```
Out[72]: untrained Machine; caches model-specific representations of data
         model: ModalDecisionTree(max_depth = nothing, ...)
         args:
           1: Source @567 ↪ Table{AbstractVector{AbstractVector{Continuous}}}
           2: Source @759 ↪ AbstractVector{Textual}
```

```
In [ ]: # Train in cross-validation!
        e = evaluate!(machine(ModalDecisionTree(; relations = :RCC8), X_multimodal,
        resampling=StratifiedCV(shuffle=true, nfolds = 3),
        measures=[accuracy],
        verbosity=0,
        check_measure=false
        )
```

```
[ Info: Precomputing logiset...
```

```
In [ ]: # Accuracies per fold
        e.per_fold
```

```
In [71]: e.report_per_fold[2].solemodel
```

```

Out[71]: ■ {1}((G)(min[V31] ≥ 0.001853897887096119))
|✓ {1}((G)((min[V31] ≥ 0.001853897887096119) ∧ (A0)(min[V27] < 76685.177202
24746)))
| |✓ {1}((G)((min[V31] ≥ 0.001853897887096119) ∧ (A0)((min[V27] < 76685.1772
0224746) ∧ (min[V28] < 44762.952262639636))))
| | |✓ {1}((G)((min[V31] ≥ 0.001853897887096119) ∧ (A0)((min[V27] < 76685.177
20224746) ∧ (min[V28] < 44762.952262639636) ∧ (DBE)(min[V50] ≥ 1885.5712367
271199))))
| | | |✓ {1}((G)((min[V31] ≥ 0.001853897887096119) ∧ (A0)((min[V27] < 76685.17
720224746) ∧ (min[V28] < 44762.952262639636) ∧ (DBE)((min[V50] ≥ 1885.57123
67271199) ∧ (min[V13] ≥ 1.400957923736261))))
| | | |✓ NEGATIVE
| | | |✗ POSITIVE
| | | |✗ NEGATIVE
| | | |✗ POSITIVE
| | | |✗ NEGATIVE
| | | |✗ {1}((G)(min[V27] ≥ 2.170219509362793e6))
| | | |✓ {1}((G)((min[V27] ≥ 2.170219509362793e6) ∧ (G)(min[V46] ≥ 5838.39077545
7752)))
| | | |✓ POSITIVE
| | | |✗ {1}((G)((min[V27] ≥ 2.170219509362793e6) ∧ (min[V19] ≥ 30000.489072536
28)))
| | | |✓ NEGATIVE
| | | |✗ {1}((G)((min[V27] ≥ 2.170219509362793e6) ∧ (min[V21] < 20414.77442768
6534)))
| | | |✓ NEGATIVE
| | | |✗ POSITIVE
| | | |✗ {1}((G)(min[V28] ≥ 553537.8712413169))
| | | |✓ POSITIVE
| | | |✗ {1}((G)(min[V2] ≥ 0.17083754207872534))
| | | |✓ {1}((G)((min[V2] ≥ 0.17083754207872534) ∧ (min[V11] ≥ 1108.1113127342
035)))
| | | |✓ NEGATIVE
| | | |✗ POSITIVE
| | | |✗ NEGATIVE

```

```
In [46]: report(mach).solemodel
```

```

Out[46]: ■ {1}((G)(min[V37] ≥ 0.0013205573259328035))
| ✓ {1}((G)((min[V37] ≥ 0.0013205573259328035) ∧ (L̄)(min[V27] ≥ 226321.99121
13276)))
| | ✓ NEGATIVE
| | ✗ {1}((G)((min[V37] ≥ 0.0013205573259328035) ∧ (min[V48] ≥ 1242.190476996
1468)))
| | | ✓ {1}((G)((min[V37] ≥ 0.0013205573259328035) ∧ (min[V48] ≥ 1242.19047699
61468) ∧ (A0)(min[V40] ≥ 3.51978641624239)))
| | | | ✓ {1}((G)((min[V37] ≥ 0.0013205573259328035) ∧ (min[V48] ≥ 1242.1904769
961468) ∧ (A0)((min[V40] ≥ 3.51978641624239) ∧ (A0)(min[V31] ≥ 1.6207745800
042226e-5))))
| | | | | ✓ POSITIVE
| | | | | ✗ NEGATIVE
| | | | | ✗ POSITIVE
| | | | | ✗ NEGATIVE
| | ✗ {1}((G)(min[V27] ≥ 2.170219509362793e6))
| | | ✓ {1}((G)((min[V27] ≥ 2.170219509362793e6) ∧ (G)(min[V46] ≥ 5838.39077545
7752)))
| | | | ✓ POSITIVE
| | | | | ✗ {1}((G)((min[V27] ≥ 2.170219509362793e6) ∧ (min[V30] < 1.6492884918659
376e6)))
| | | | | | ✓ POSITIVE
| | | | | | ✗ NEGATIVE
| | | | | ✗ {1}((G)(min[V28] ≥ 672777.1743629333))
| | | | | | ✓ POSITIVE
| | | | | | ✗ {1}((G)(min[V30] ≥ 1.0114283593133552e6))
| | | | | | | ✓ NEGATIVE
| | | | | | | ✗ POSITIVE

```

```

In [ ]: X = scalarlogiset(X_df)
println(X)

```

```

In [ ]:

```

```

In [ ]: # Accessibles on multirelation frames
# Get the structure ("frame") of the first instance. It is a "dimensional" f
fr = SoleLogics.frame(X, 1)

```

```

In [ ]: # Enumerate all worlds
collect(allworlds(fr))

```

```

In [ ]: using SoleLogics: Interval
# Enumerate the intervals that are "Later" than [1,10]
accessibles(fr, Interval(1,10), IA_L) |> collect

```

```

In [ ]: # Remember that features are computed on each world
# Let's compute the minimum of the first variable on an arbitrary interval,
feature = UnivariateMin(1)
Sole.featvalue(feature, X, 1, Interval(10,30))

```

```

In [ ]: # Remember that atoms are *scalar conditions on features*
# Let's check one on an interval of the first instance

```

```
p = Atom(ScalarCondition(feature, >, -0.5))
check(p, X, 1, Interval(10,30))
```

```
In [ ]: # I can check any formula
p = Atom(ScalarCondition(UnivariateMin(1), >, -0.5))
q = Atom(ScalarCondition(UnivariateMin(2), <=, 10))
φ = p v q
check(φ, X, 1, Interval(10,30))
```

```
In [ ]: # Generate a random HS formula with scalar conditions on features, and check
features = [UnivariateMin(i_variable) for i_variable in 1:ncol(X_df)]
alpha = [Atom(ScalarCondition(feats, >, thresh)) for feat in features for thr

HS_connectives = SoleLogics.diamondsandboxes(SoleLogics.IARelations)
propo_connectives = SoleLogics.BASE_PROPOSITIONAL_CONNECTIVES

println("Propositional connectives: $(join(syntaxstring.(propo_connectives),
println("HS connectives: $(join(syntaxstring.(HS_connectives), ", "))")

propo_weights = fill(1/length(propo_connectives), length(propo_connectives))
HS_weights = fill(1/length(HS_connectives), length(HS_connectives))

connectives = vcat(propo_connectives, IA_connectives)

opweights = vcat(propo_weights, HS_weights)

treeheight = 3
φ2 = randformula(Random.MersenneTwister(30), treeheight, alpha, connectives;
println()
println("Random formula:")
println(syntaxstring(φ2))

check(φ2, X, 1, Interval(10,30))
```

```
In [ ]: # Let's check a formula on all the instances
check_mask = check(φ2, X, Interval(10,30))
```

```
In [ ]: # It holds on part of the instances
sum(check_mask)
```

```
In [ ]: # Let's ask whether the formula holds *all* intervals, instead of checking i
println("Applying the universal global operator: ", SoleLogics.globalbox)
println()

universal_φ = globalbox(φ2)
println("Formula: ", syntaxstring(universal_φ))
check_mask = check(universal_φ, X)

# It holds on no instance... Too restrictive!
sum(check_mask)
```

```
In [ ]: # Let's ask whether there exists any interval where the formula holds
println("Applying the existential global operator: ", SoleLogics.globaldiamc
println()
```



```

existential_φ = globaldiamond(φ2)
println("Formula: ", syntaxstring(existential_φ))
check_mask = check(existential_φ, X)

# It holds on more instances
sum(check_mask)

```

```
In [ ]: # Question: does it lead to a good rule?
```

```

println(syntaxstring(existential_φ))

println()
println(SoleLogics.experimentals.formula2natlang(existential_φ))

```

```
In [ ]: neg_existential_φ = normalize(¬ existential_φ;
    profile = :readability,
    remove_implications = true,
    allow_atom_flipping = true
)
```

```
syntaxstring(neg_existential_φ; remove_redundant_parentheses = false)
```

```
In [ ]: (SoleLogics.precedence(Λ), SoleLogics.precedence(∨))
```

```
In [ ]: countmap(y)
```

```
In [ ]: println(existential_φ)
countmap(y[check_mask])
```

```
In [ ]: println(neg_existential_φ)
countmap(y[(!).(check_mask)])
```

```
In [ ]: branch = Branch(neg_existential_φ, "I have command", "Spread wings")
```

```
In [ ]: y_preds = SoleModels.apply(branch, X)
println("Accuracy of this branch: $(sum(y .== y_preds)/length(y))")
println("Random chance: $(60/length(y))")
```

```
In [ ]:
```

```
In [ ]: println(X)
```

```
In [ ]: # Randomly split the data: 20% training, 80% testing
N = nrow(X_df)
perm = randperm(Random.MersenneTwister(1), N)
train_idx, test_idx = perm[1:round(Int, N*.2)], perm[round(Int, N*.2)+1:end]
println("Using $(length(train_idx)) instances for training")
println("Using $(length(test_idx)) instances for testing")
```

```
In [ ]: using ModalDecisionTrees
```

```

# Bind a machine learning algorithm to logiset & labels
mach = machine(ModalDecisionTree(; relations = :IA7, features = [minimum]),

# Train!
@time fit!(mach; rows=train_idxxs);

# Compute accuracy
yhat = predict_mode(mach; rows=test_idxxs)
MLJ.accuracy(yhat, y[test_idxxs])

```

```

In [ ]: # Show the restricted MDT learnt
printmodel(report(mach).rawmodel_full; hidemodality = true)

```

```

In [ ]: # Show its *pure* version
printmodel(report(mach).solemodel_full; show_metrics = true, hidemodality =

```

```

In [ ]: simplified_restricted_tree = ModalDecisionTrees.prune(report(mach).rawmodel_
printmodel(simplified_restricted_tree)

println()
println("# Leaves: ", nleaves(simplified_restricted_tree))

```

```

In [ ]: solemodel = ModalDecisionTrees.translate(simplified_restricted_tree)

```

```

In [ ]: # Print leaf rules + their training performances
ruleset = listrules(solemodel)
printmodel.(ruleset; show_metrics = true, threshold_digits = 2, variable_nam

```

```

In [ ]: last_rule = ruleset[end]
last_antd = antecedent(last_rule)

println("First formula, translated:")
println(SoleLogics.experimentals.formula2natlang(last_antd; threshold_digits

for (i_rule, rule) in enumerate(ruleset)
    println()
    println("[$i_rule]")
    antd = antecedent(rule)
    println(SoleLogics.experimentals.formula2natlang(antd; threshold_digits
end

```

```

In [ ]: # Print rules + their *test* performances

# Sprinkle the model with the test instances!
predictions, tree_test = report(mach).sprinkle(X_df[test_idxxs,:], y[test_idx

# Extract ruleset and print its metrics
ruleset_test = listrules(tree_test);

# printmodel.(ruleset_test; show_metrics = true, threshold_digits = 2, varia
printmodel.(ruleset_test; show_metrics = true, threshold_digits = 2, parenth

```

```
In [ ]: println("IF\n\t", SoleLogics.experimentals.formula2natlang(antecedent(ruleset_test[4])))
println("THEN\n\t", consequent(ruleset_test[4]))

In [ ]: # Obtain class rules & show their *test* metrics
condensed_ruleset_test = joinrules(ruleset_test)
printmodel.(condensed_ruleset_test; show_metrics = true, threshold_digits =
```

Exercise

`ModalDecisionTrees.jl` can also handle images! In which case, they use a 2D logic of rectangles instead of a 1D logic of intervals.

Apply `ModalDecisionTrees` to [Indian Pines](#), a benchmark dataset for Land Cover Classification with 16 classes. The dataset consists of a hyperspectral image (i.e., 200 color channels instead of the typical 3 RGB channels) where many pixels have been labelled as belonging to one of the classes.

Sketch of the idea:

- Load the image and the ground truths. The package [MAT.jl](#) can be helpful;
- From the 145×145 image provided, sample a (small) number m of 3×3 patches for each class, and label each patch with the class label for the central pixel;
- Gather the ground truths into a vector of strings `y`, and the samples into a Julia `DataFrame` `X` with 200 columns, $16m$ rows and 3×3 *matrices* in the cells;
- Use MLJ to train a `ModalDecisionTree` on `X` and `y`, similarly to the above case.

Suggestion: since the formulas are desirably rotation-invariant, ask the algorithm to use *topological* relations instead of *directional* relations. Refer to the [doc](#) to know more.