

Controlador Integral $\rightarrow \frac{k_I}{s} = \frac{1}{T_I s}$

Sistema $\rightarrow \frac{40}{4s+1}$

$$\boxed{\frac{k_I}{s}} \rightarrow \boxed{\frac{40}{4s+1}}$$

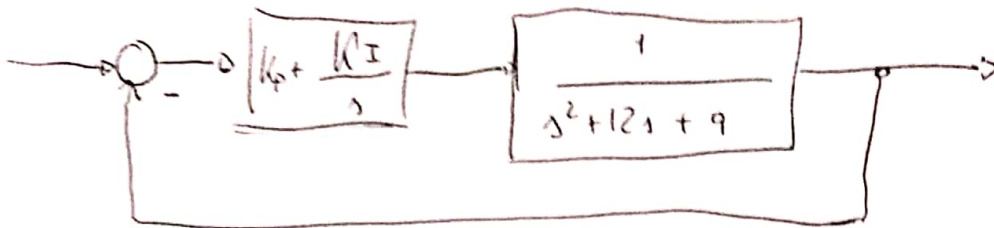
$$\rightarrow \frac{40k_I}{s(4s+1)} = \frac{4(10k_I)}{4s(s+0,25)}$$

$$\Rightarrow \frac{10k_I}{s(s+0,25)}$$

$$FTCF = \frac{G}{1+GH} = \frac{\frac{10k_I}{s^2+0,25s}}{1 + \frac{10k_I}{s^2+0,25s}}$$

$$= \frac{10k_I}{s^2 + \frac{1}{4}s + 10k_I}$$

$$\left. \begin{array}{l} \omega_0^2 = 10k_I \\ 2\xi\omega_0 = \frac{1}{4} \end{array} \right\} \Rightarrow \left. \begin{array}{l} k_I = \frac{\omega_0^2}{10} \\ \omega_0 = \frac{0,25}{2\xi} \end{array} \right\} \Rightarrow \left. \begin{array}{l} k_I = \frac{\left(\frac{0,25}{2\xi}\right)^2}{10} \\ \text{Para } \xi = \frac{\sqrt{2}}{2} \rightarrow k_I = \frac{1}{320} \end{array} \right\}$$



$$K_P + \frac{K_I}{s} = \frac{K_P s + K_I}{s} = \frac{K_I \left(\frac{K_P s}{K_I} + 1 \right)}{s}$$

$$s^2 + 12s + 9 = 0 \Rightarrow s = -11,20 \quad \vee \quad s = -0,80$$

$$\frac{1}{s^2 + 12s + 9} = \frac{1}{(s + 11,20)(s + 0,8)} = \frac{1}{(11,2 \times 0,8) (1,25s + 1) (0,09s + 1)}$$

$$\frac{\cancel{K_I} \left(\frac{K_P s}{\cancel{K_I}} + 1 \right)}{s} = \frac{1}{8,96 (1,25s + 1) (0,09s + 1)}$$

$$= \frac{K_I}{s} \cdot \frac{1}{8,96 (0,09s + 1)} = \frac{K_I}{s} \cdot \frac{0,112}{(0,09s + 1)} = \frac{0,112 K_I}{s(0,09s + 1)}$$

$$\frac{K_I}{K_P} = 1,25$$

FTCF

$$L \rightarrow \frac{0,112 K_I}{s(0,09s + 1)}$$

$$= \frac{0,112 K_I}{0,09s^2 + s + 0,112 K_I} = \frac{1,24 K_I}{s^2 + 11,1s + 1,24 K_I}$$

$$1 + \frac{0,112 K_I}{s(0,09s + 1)} = \frac{s^2 + 12s + 9 + 0,112 K_I}{s(0,09s + 1)}$$

$$\left. \begin{array}{l} K_I = \frac{W_0^2}{1,24} \\ 2\xi W_0 = 11,1 \end{array} \right\} \Rightarrow \left. \begin{array}{l} K_I = 7,14 \\ W_0 = 11,1 \end{array} \right\}$$

$\zeta = \frac{W_0}{2}$	$\zeta = 0,1$	$\zeta = 4$
$W_0 = 7,85$	$W_0 = 55,5$	$W_0 = 1,375$
$K_I = 49,68$	$K_I = 2484,07$	$K_I = 1,52$
$K_P = 39,744$	$K_P = 1987,26$	$K_P = 1,216$