

Part D

$$x^* = \frac{x}{L_x}$$

$$y^* = \frac{y}{L_y}$$

$$T^* = \frac{T - T_0}{T_0}$$

$$T_0 = 20^\circ\text{C}$$

$$t = \frac{L_x L_y}{K} t^*$$

$$x = x^* L_x \quad y = L_y y^*$$

$$T = T_0 + T^* T_0$$

$$\frac{[\text{m}^2]}{[\frac{\text{m}^2}{\text{s}}]} = \text{s}$$

Dimensionless form

$$\frac{T_0}{\left(\frac{L_x L_y}{K}\right)} \frac{\partial T^*}{\partial t^*} = -v_x \left(\frac{T_0}{L_x}\right) \frac{\partial T^*}{\partial x} - v_y \left(\frac{T_0}{L_y}\right) \frac{\partial T^*}{\partial y} + k \left(\frac{T_0}{(L_x)^2} \frac{\partial^2 T^*}{\partial x^2} + \frac{T_0}{(L_y)^2} \frac{\partial^2 T^*}{\partial y^2} \right)$$

$$\frac{\partial T^*}{\partial t^*} = -v_x \left(\frac{L_y}{K}\right) \frac{\partial T^*}{\partial x} - v_y \left(\frac{L_x}{K}\right) \frac{\partial T^*}{\partial y} + \underbrace{\frac{L_y}{L_x} \frac{\partial^2 T^*}{\partial x^2}}_{\text{dimensionless group}} + \underbrace{\frac{L_x}{L_y} \frac{\partial^2 T^*}{\partial y^2}}_{\text{dimensionless group}}$$

$$\frac{\text{m}}{\text{s}} \times \frac{\text{m}}{\text{m}^2/\text{s}} = 1 \Rightarrow \text{dimensionless group}$$

for calculating a Peclet number we can use

$$\frac{\text{magnitude of velocity} \times L_y}{K} = \frac{\text{advective transport}}{\text{diffusive transport}}$$

Reynolds number

$$\frac{\text{magnitude of velocity} \times L_y}{\nu} = \frac{\text{inertia}}{\text{viscous}}$$