

Willlegg - Quiz 4

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$$\nabla f = \langle 2x, 1 \rangle$$

$$\nabla g = \langle 2x-6, 1 \rangle$$

$$\nabla f = \lambda \nabla g$$

$$\langle 2x, 1 \rangle = \lambda \langle 2x-6, 0 \rangle$$

$$2x = \lambda(2x-6)$$

$$x \neq 0 \rightarrow 1 = \lambda$$

$$1 = \lambda(1)$$

$$y = -5 \quad x = -5, 1$$

$$y = x^2 - 6x$$

$$(-5, -5) \quad (1, -5)$$

$$\text{if } x=0 \quad y=0 \rightarrow (0,0)$$

$$\lambda = 5/8$$

$$x=5 \rightarrow \lambda = 5/8$$

$$x=1 \rightarrow \lambda = -1/2$$

$$(-5, -5) \quad (1, -5)$$

$$\lambda = -1/2$$

$$(1, -5) \quad (0,0)$$

$$f(-5, -5) = (-5)^2 + (-5) = 20 \leftarrow \text{local max}$$

$$f(1, -5) = (1)^2 + (-5) = -4 \leftarrow \text{local min}$$

$$f(0,0) = (0)^2 + (0) = 0$$