

Will leggy

Quiz 2

1) dist between pt $(0, 1, 6)$ and plane $x + y + 2z = 1$

$$d = \frac{|\vec{PR} \cdot \vec{n}|}{|\vec{n}|} \quad \begin{array}{l} \vec{n} = \langle 1, 1, 2 \rangle \\ \vec{R} = \langle 0, 0, 0 \rangle \end{array}$$

$$\vec{PR} = \langle 0-0, 0-1, 0-6 \rangle = \langle 0, -1, -6 \rangle$$

$$d = \frac{|\langle 0, -1, -6 \rangle \cdot \langle 1, 1, 2 \rangle|}{\sqrt{1^2 + 1^2 + 2^2}} = \frac{|1(0) + 1(-1) + 2(-6)|}{\sqrt{6}}$$

$$d = \frac{13}{\sqrt{6}} = 5.307$$

2) find angle between $\vec{r}_1(t) = \langle t+1, 2t+3, -3t-1 \rangle$ & $\vec{r}_2(s) = \langle -4s, 1, 2s+2 \rangle$ - acute/rads

$$\theta = \cos^{-1} \left(\frac{\vec{A} \cdot \vec{B}}{|\vec{A}| |\vec{B}|} \right) \quad \begin{array}{l} \vec{v}(\vec{r}(t)) = \langle 1, 2, -3 \rangle \\ \vec{v}(\vec{r}(s)) = \langle -4, 0, 2 \rangle \end{array}$$

$$= \cos^{-1} \left(\frac{-4(1) + (2)(0) + (-3)(2)}{\sqrt{1^2 + 2^2 + (-3)^2} \cdot \sqrt{(-4)^2 + 0^2 + 2^2}} \right) = \cos^{-1} \left(\frac{-10}{\sqrt{14} \cdot \sqrt{20}} \right)$$

$$\cos^{-1} \left(\frac{-10}{\sqrt{14} \cdot \sqrt{20}} \right) = |2.211 - \pi| = 0.930$$