

Will Legg

Week 3 Review

2) Where does helix $r(t) = \langle \sin t, \cos t, 3t \rangle$ intersect the sphere $x^2 + y^2 + z^2 = 10$

plug helix into sphere $\sin^2 t + \cos^2 t + (3t)^2 = 10$

$$t = \pm 1$$

$$\begin{aligned} r(1) &= (\sin(1), \cos(1), 3(1)) \\ &\& r(-1) = (\sin(-1), \cos(-1), -3) \end{aligned}$$

5) find curve of intersection of cylinder $x^2 + y^2 = 16$ and plane $x + z = 5$

use trig sub w/ cylinder $\rightarrow \begin{cases} x = 4\cos t \\ y = 4\sin t \end{cases}$

$$\hookrightarrow z = 5 - (4\cos t)$$

$$r(t) = \langle 4\cos t, 4\sin t, 5 - 4\cos t \rangle$$

Week 3 Review

4) Determine arc length of $r(t) = \langle 2t, \frac{2}{3}(t-5)^{3/2}, -t \rangle$
between $9 \leq t \leq 16$

$$\begin{aligned} \text{a) } \int_9^{16} |r'(t)| &= \int_9^{16} \sqrt{(2)^2 + ((t-5)^{1/2})^2 + (-1)^2} \\ &= \int_9^{16} \sqrt{4 + t - 5 + 1} = \int_9^{16} \sqrt{t} \\ &= \int_9^{16} \sqrt{t} = \left. \frac{2}{3} t^{3/2} \right|_9^{16} = \boxed{\frac{74}{3}} \end{aligned}$$

$$\text{b) } L(t) = \int_9^t \sqrt{t} = \left. \frac{2}{3} t^{3/2} - 18 \right| = 16$$

↳ solve for t
 $t \approx 19.5, -9 \Rightarrow \boxed{4 \text{ sec}}$

11) false cylinder

$$\begin{aligned} x &= \rho \sin \phi \cos \theta \\ y &= \rho \sin \phi \sin \theta \\ z &= \rho \end{aligned}$$