

1) Linear system of first ODEs

A: Apparently falls exponentially and independently of k_2 , hence the approach:

$$A' = -k_1 A$$

B: Starts converging towards 1 for a low k_2 , then falls and falls even faster for higher k_2 :

$$B' = A k_1 - B k_2$$

C: See A-argumentation

$$C' = k_2 C$$

with $A(0) = 1$, $B(0) = C(0) = 0$

2) Implementation of Euler and Heun

I implemented Euler and Heun as functions that take a function with parameters as arguments to iterate over every k_2 and pass a lambda function as argument

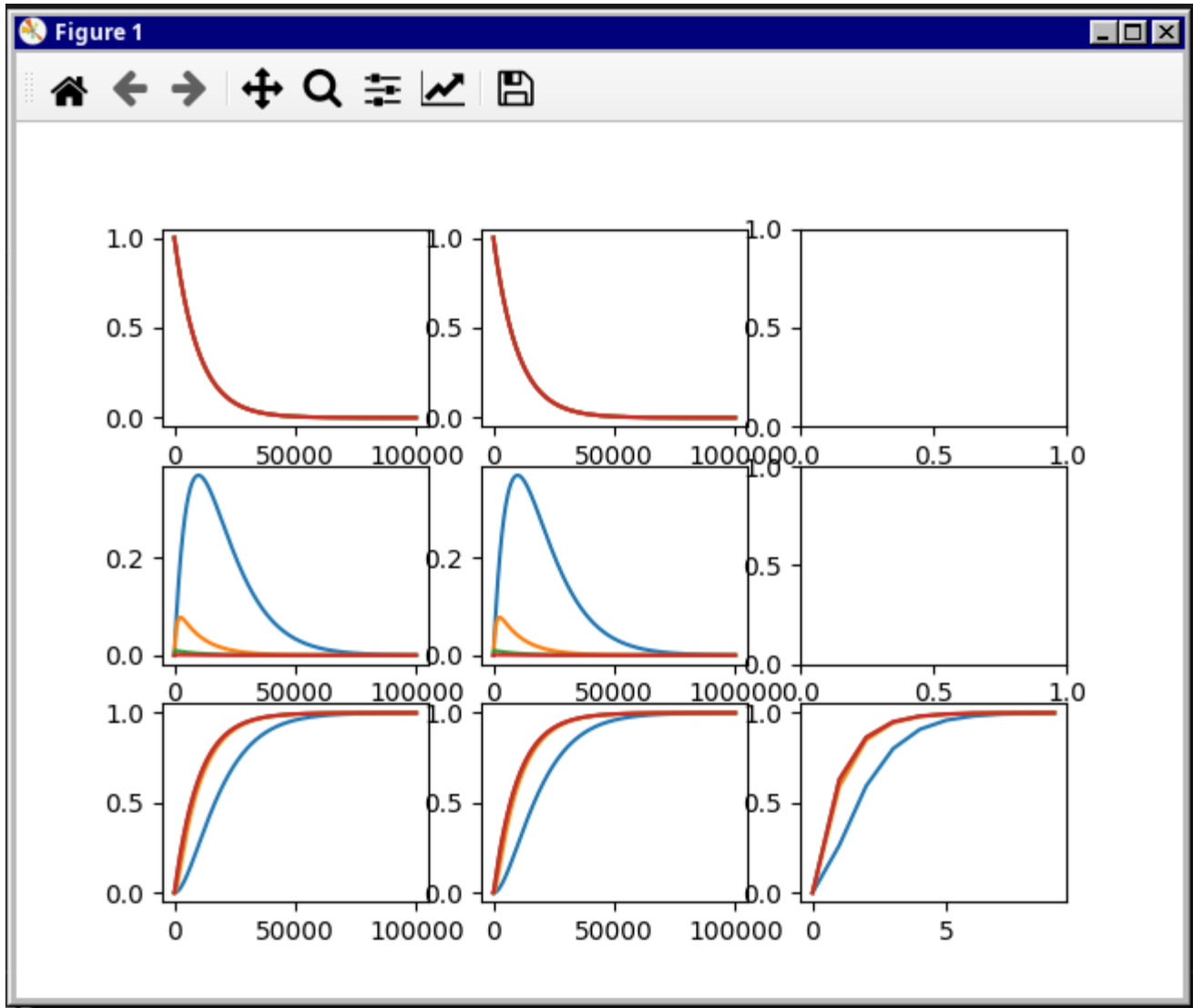
```
def euler(func, k2, startingValue, oldValues = range(iterations)):
    values = []
    values.append(startingValue)
    for n in np.arange(1, iterations):
        f = values[n-1] + h*func(values[n-1], oldValues[n-1], k2)
        values.append(f)
    return values

def Heun(func, k2, startingValue, oldValues=range(iterations)):
    values = []
    values.append(startingValue)
    for n in np.arange(1, iterations):
        ystrich = values[n-1] + h*func(values[n-1], oldValues[n-1], k2)
        f = values[n-1] + h/2*(func(values[n-1], oldValues[n-1], k2) + func(ystrich, oldValues[n], k2))
        values.append(f)
    return values
```

Note that every lambda function has 3 arguments in order to make this work, but only B actually takes 3 as an input

```
k2s = [1, 10, 100, 1000];
Aprime = lambda A, y, z: -k1*A
Bprime = lambda B, A, k2: k1*A - k2*B;
Cprime = lambda C, B, k2: k2*B;
```

3) Visualization and Comparisation



The first column contains the Euler method, the second column the Heun method. In the third column in the last row, the analytical form of C is shown. Each color is a k_2 .

I didn't notice any great differences in runtime between Euler and Heun, but I have reason to believe that Heun would have to be a bit more accurate and might be a bit slower for large iterations because you have to calculate more terms.

