

StereoVision

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Summary

- Camera models and Camera calibration
- Stereo Vision
 - Frontal parallel arrangement
 - Epipolar geometry
 - Essential and Fundamental Matrix
 - Image rectification
 - Stereo Correspondences

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Introduction

What is stereo?

Where is it coming from?

Where can you see it or use it?

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Human Visual System

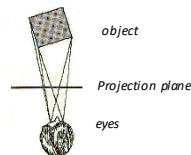
- Many of the perceptual cues we use to visualize 3D structure are available in 2D projections
- Such cues include:
 - occlusion (one object partially covering another)
 - perspective (point of view)
 - familiar size (we know the real-world sizes of many objects)
 - atmospheric haze (objects further away look more washed out)
- Four cues are missing from single 2D views:
 - stereo parallax—seeing a different image with each eye
 - movement parallax—seeing different images when we move the head
 - accommodation—the eyes' lenses focus on the object of interest
 - convergence—both eyes converge on the object of interest

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Stereopsis

Stereo = "solid" or "three-dimensional"
opsis = appearance or sight

Also: "binocular vision",
"binocular depth perception"
"stereoscopic depth perception"



- Stereopsis is the impression of depth that is perceived when a scene is viewed with both eyes by someone with normal binocular vision
- Binocular disparity is due to the different position of our two eyes

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Stereopsis

- Depth perception in stereo is based on stereopsis:
 - when the brain registers and fuses two images
 - Image parallax means that the two eyes register different images (horizontal shift)
 - The amount of shift depends on the "inter-pupillary distance" (IPD) (varies for each person in the range of 53-73 mm)
 - Works in the near field (to a few meters from the eye)

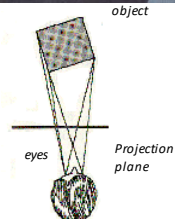
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Stereopsis



(Hearn and Baker, 2002)

Right eye image Left eye image



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Stereopsis: implications for Graphic devices

- Need to present two images of the same scene
- The two images can be presented:
 - at the same time on two displays (HMD)
 - time-sequenced on one display (active glasses)
 - spatially-sequenced on one display (auto-stereoscopic displays)



Left eye, right eye images
(Burdea and Coffet., 2003)



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Common ways to produce 3D sensation

- Anaglyphs: two colored images and color coded glasses (red/cyan/green)



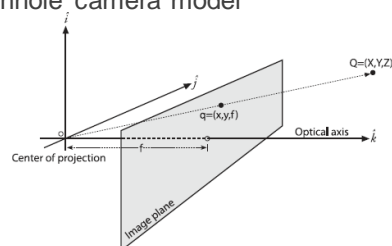
- Two images with different light polarization and polarizing glasses
 - Linear and circular
- Double frame-rate displays combined with LCD shutter glasses
- Autostereoscopic displays
 - Parallax barrier and lenticular lens
- Head Mounted Displays (HMDs)
- and "exotic displays"



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Camera model

- pinhole camera model



- We get

$$x = f \frac{X}{Z} \quad y = f \frac{Y}{Z}$$

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OpenCV Camera model

- OpenCV Camera model:
 - 4 intrinsic parameters:
 - Focal distance: f_x, f_y
 - Optical centre: c_x, c_y
 - 5 distortion parameters
 - Lens distortion: k_1, k_2, k_3, p_1, p_2
 - 6 extrinsic parameters:
 - Rotation: r_x, r_y, r_z
 - Translation: t_x, t_y, t_z

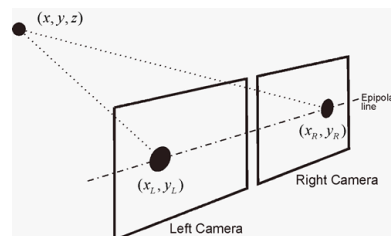
Total: 15 parameters

- Other models: Tsai, Heikkila, Zhang

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StereoVision

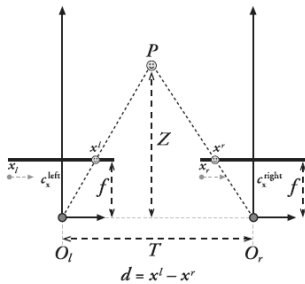
- Capability to define depth from 2 images
- Possible by computing correspondences between two images



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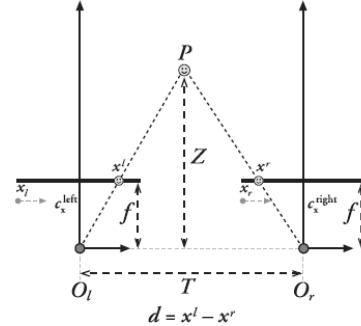
Frontal parallel arrangement

- Two perfectly aligned, coplanar cameras with same focal distance:



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Frontal parallel arrangement



- $Z = ?$

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Frontal parallel arrangement

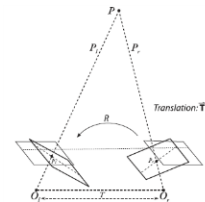
- $\frac{T}{Z} = \frac{T - (x^l - x^r)}{(Z - f)}$ then $Z = \frac{T(Z - f)}{T - (x^l - x^r)}$,
- $TZ - Z(x^l - x^r) = TZ - fT$
- So : $Z = \frac{fT}{d}$

=> Stereo system have good depth resolution for close objects since depth is inversely proportional to disparity.

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Frontal parallel arrangement

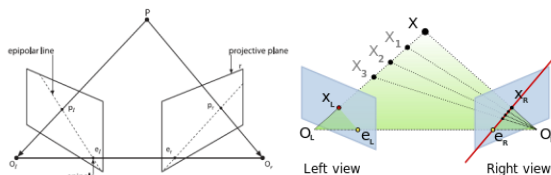
- Easy to relate correspondence to depth in frontal parallel arrangement
- Problem: how to Map real configuration to frontal parallel arrangement.



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Epipolar geometry

- An epipole is a projection of the optical centre of a camera on the other image plane



- <http://www.ai.sri.com/~luong/research/Meta3DViewer/EpipolarGeo.h.html>

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Epipolar geometry

- What is it useful for?:
 - Given a point in an image, its corresponding point in the other image lie on the corresponding epipolar line
 - Order is preserved (given 2 points A e B in a given order in one images, order will be the same in the other image)

=>Epipolar geometry transform a 2D search (in image) into a 1D search (along epipolar lines) saving resources and avoiding errors.

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Essential and Fundamental Matrices



- Epipolar Geometry is defined by:
 - Information about relative position between the cameras (rotation and translation) [extrinsic] – Essential Matrix(E)
 - Intrinsic parameters of the cameras (focal length, lens distortion, optical centre, etc...) – Fundamental Matrix(F)

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Essential matrix



- Matrix that maps a 3D point in one image with its corresponding 3D point on the other image considering translation and rotation between cameras:
- $p_l^T E p_r = 0$
- p_l and p_r are in camera 3D coordinate system

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Fundamental matrices



- Matrix that maps a pixel in one image with its corresponding pixel on the other image considering rotation, translation and intrinsic parameters of the cameras:
- $u_l^T F u_r = 0$
- u_l e u_r are in image 2D coordinate system

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Fundamental and essential matrices



- Fundamental and Essential matrices represent the transformation between the stereo pair images. Fundamental matrix operates in image coordinates (pixels) and Essential matrix operates in physical coordinates.
- Possible to evaluate with 8 point correspondences (eight point algorithm: <http://www.cs.unc.edu/~marc/tutorial/node54.html>)

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Image rectification



- Given the fundamental matrix, it is possible to rectify an image by aligning epipolar lines in rows on the two rectified images getting a frontal parallel arrangement.

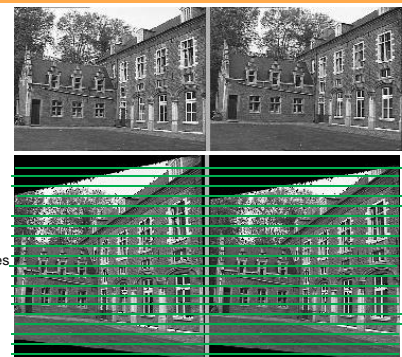
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Image rectification



Original images

Rectified images

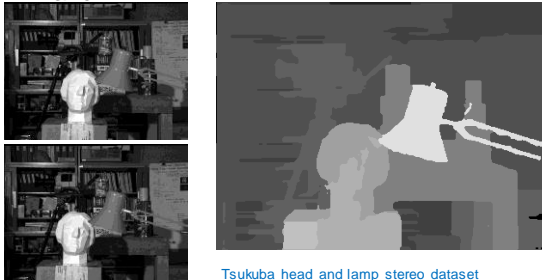


From Visual 3D Modeling from Images (<http://www.cs.unc.edu/~marc/tutorial/>)

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Disparity map

- In rectified images, disparity is simply difference between pixel coordinates x_l and x_r .



Tsukuba head and lamp stereo dataset

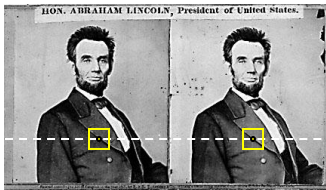
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Stereo Matching algorithm

- Match Pixels in Conjugate Epipolar Lines
 - This is a tough problem
 - Numerous approaches
 - A good survey and evaluation: <http://vision.middlebury.edu/stereo/>

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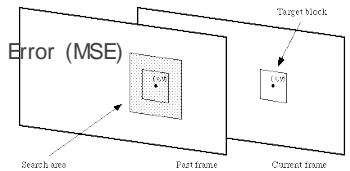
Basic stereo algorithm



- For each epipolar line
- For each pixel in the left image
- compare with every pixel on same epipolar line in right image
 - pick pixel with minimum match cost

Block Matching algorithm

- Block Matching:
 - Divides an image into macroblocks and compare each with a corresponding block and its neighbours in another image
- Several Metrics
 - Mean difference or Mean Absolute Difference (MAD)
 - Mean Squared Error (MSE)
 - ...



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Window size



$W = 3$

$W = 20$

Effect of window size

- Smaller window
 - +
 -
- Larger window
 - +
 -

Better results with adaptive window

- T. Kanade and M. Okutomi, *A Stereo Matching Algorithm with an Adaptive Window: Theory and Experiment*, Proc. International Conference on Robotics and Automation, 1991.
- D. Scharstein and R. Szeliski, *Stereo matching with cross-scale diffusion*, International Journal of Computer Vision, 28(2):155-174, July 1998

Stereo results

- Data from University of Tsukuba
- Similar results on other images without ground truth



Scene



Ground truth

Stereo Vision - Steps



- Calibrate cameras
- Rectify images
- Compute disparity
- Estimate depth

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Stereo Vision – Errors



- Camera calibration errors
- Poor image resolution
- Occlusions
- Violations of brightness constancy (specular reflections)
- Large motions
- Low-contrast image regions

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Stereo Vision in OpenCV



- [cvFindChessboardCorners](#): detect chessboard corner in stereo images
- [cvStereoCalibrate](#): calibrates stereo rig
- [cvStereoRectify](#): computes rotations that make both camera planes the same.
- [cvInitUndistortRectifyMap](#) and [cvRemap](#): use to compute undistortion map and rectified images
- Stereo correspondence (ex: [cvFindStereoCorrespondenceBM](#)): computes the disparity map.
- [cvReprojectImageTo3D](#): disparity map to 3D with calibrated cameras

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OPENCV STEREO VISION DEMO

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Some references



- Gary Bradski and Adrian Kaehler. *Learning OpenCV: Computer Vision with the OpenCV Library*. O'Reilly, Cambridge, MA, 2008.
- Olivier Faugeras Three-dimensional computer vision: a geometric viewpoint. MIT Press Cambridge, MA, USA ©1993
- Szeliski, R. (2010).. Computer Vision: Algorithms and Applications, Springer
- Quang-Tuan Luong. "[Learning Epipolar Geometry](#)". Retrieved 2007-03-04.

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