

PRECAUTIONARY SAVINGS, LIQUIDITY CONSTRAINTS, AND SELF-CONTROL

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THREE IMPORTANT IDEAS

- Precautionary Saving
- Liquidity Constraints
- Self-Control Problems

CERTAINTY EQUIVALENCE

- Suppose for simplicity $\beta(1 + r) = 1$
- Consumption Euler equation:

$$U'(C_t) = E_t U'(C_{t+1})$$

- With quadratic utility:

$$C_t = E_t C_{t+1}$$

- This implies certainty equivalence:
 - C_t depends only on $E_t C_{t+1}$ not $\text{var}_t(C_{t+1})$ (or any higher moments)

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 - C_t depends only on $E_t C_{t+1}$ not $\text{var}_t(C_{t+1})$ (or any higher moments)
- Very extreme model:
 - Savings behavior unaffected by uncertainty!!
 - Consumption smoothing and intertemporal substitution only forces affecting savings
(same thing for linearized or log-linearized models)

QUADRATIC UTILITY AND RISK

- With quadratic utility, utility cost of given variance of consumption independent of the level of consumption
 - Amount of curvature of utility independent of level
 - Jensen's inequality term independent of the level
- But marginal utility falls with level of consumption
- Thus, with quadratic utility, consumers are willing to pay more to avoid a given amount of uncertainty (particular dollar coin toss) the richer they are
- Quadratic utility implies increasing absolute risk aversion

COMMON UTILITY FUNCTIONS

- Constant Relative Risk Aversion (CRRA):

$$U(C) = \begin{cases} \frac{C^{1-\gamma}-1}{1-\gamma} & \text{if } \gamma \neq 1 \\ \log C & \text{if } \gamma = 1 \end{cases}$$

$$\text{Relative Risk Aversion} = -\frac{U''(C)C}{U'(C)} = \gamma$$

- Constant Absolute Risk Aversion (CARA):

$$U(C) = -\frac{\exp(AC)}{A}$$

$$\text{Absolute Risk Aversion} = -\frac{U''(C)}{U'(C)} = A$$

RISK AVERSION IN REALITY

- Increasing absolute risk aversion completely unrealistic
- Implications for portfolio allocation:
 - CRRA: Constant share in risky assets
 - CARA: Constant dollar amount in risky assets
 - IARA: Decreasing dollar amount in risky assets
as wealth increases
- In reality, richer people allocate **larger share** of wealth to risky assets
- Suggests decreasing relative risk aversion (DRRA)
(CRRA not such a bad approximation)

See Gollier (2001, ch 2.) for more detailed discussion of various forms of risk aversion.

PRECAUTIONARY SAVINGS

- Curvature of utility almost surely falls as consumption rises:

$$U'''(C_t) > 0$$

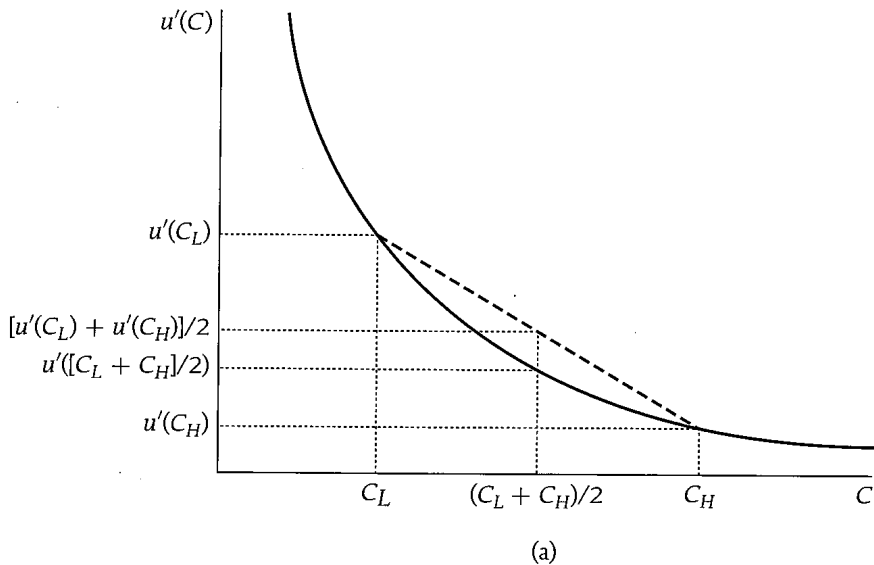
- What does this imply about savings?

PRECAUTIONARY SAVINGS

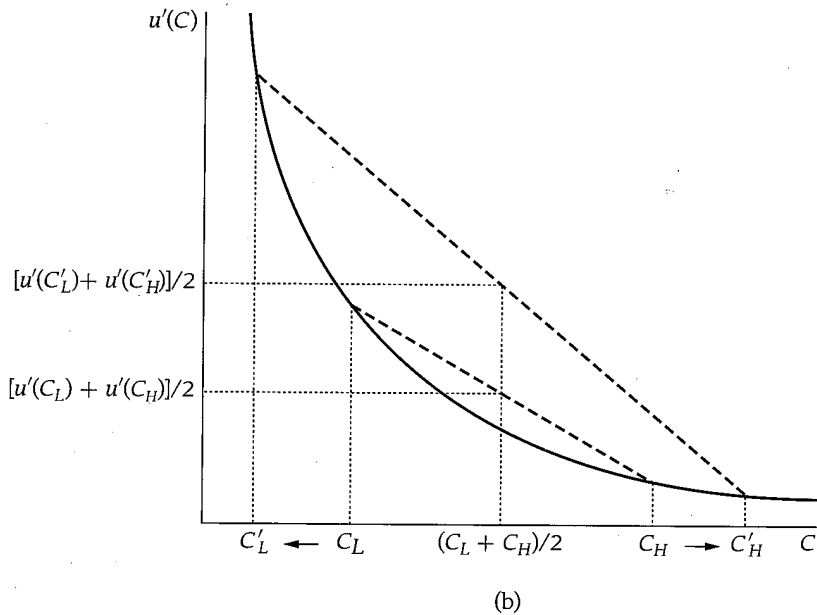
- Curvature of utility almost surely falls as consumption rises:

$$U'''(C_t) > 0$$

- What does this imply about savings?
- With $U'''(C_t) > 0$, $U'(C_t)$ is convex
- If $C_t = E_t C_{t+1}$, then
 - $U'(C_t) < E_t U'(C_{t+1})$ (since $U'(C_t) = U'(E_t C_{t+1}) < E_t U'(C_{t+1})$)
 - Marginal reduction in C_t (increase in saving) increases utility
- This extra saving relative to certainty equivalent case is called **precautionary saving**



Source: Romer (2019). 50-50 chance of C_H and C_L .



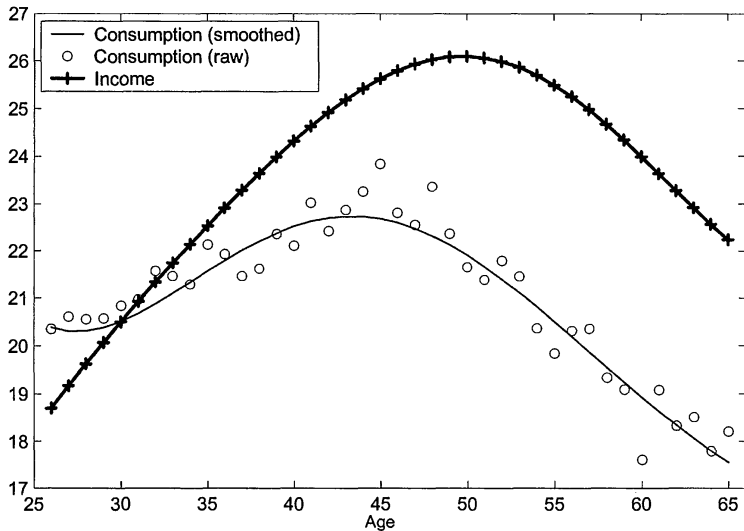
Source: Romer (2019)

Definition: (Kimball, 1990) An agent is **prudent** if adding an uninsurable zero-mean risk to his/her future wealth raises his/her optimal savings

Proposition: (Leland, 1968) An agent is prudent if and only if the marginal utility of future consumption is convex.

LIQUIDITY CONSTRAINTS

Thousands of 1987 dollars



- Consumption smoothing over the life-cycle likely involves substantial borrowing early in life
- Simple PIH/LCH model assumes people can borrow (unsecured) at same rate as they can save
- Highly unrealistic:
 - Most household borrowing is secured (e.g., mortgages, car loans)
 - Interest rates on car loans and even mortgages substantially higher than on savings accounts
 - Interest rates on unsecured consumer lending (i.e., credit cards) extremely high ($\sim 20\%$)
 - Limits on unsecured borrowing beyond which can't go at any rate

Two effects of liquidity constraints:

1. Less borrowing when they bind
2. Less borrowing even when they don't bind because they may bind in the future
 - Bad shock tomorrow may cause low consumption due to binding liquidity constraint at that point
 - Consumer saves today to “self-insure” against this future bad shock

- Liquidity constraints and prudence cause households facing uninsurable income risk to engage in **buffer stock saving** (i.e., self-insurance)
- Other sources of saving:
 - **Life-cycle saving** to smooth consumption over the life-cycle relative to life-cycle profile of income
 - Saving due to **patience/impatience**. If $1/\beta \neq (1 + r)$ household will tilt consumption profile (down if impatient, up if patient)

HOW MUCH BUFFER STOCK SAVING?

Depends crucially on $\beta(1 + r)$

- If $\beta(1 + r) = 1$:
 - Households will eventually save themselves out of constraint
 - I.e., save enough that they will eventually never hit constraint
 - At that point, full consumption smoothing
- If $\beta(1 + r) < 1$
 - Households sufficiently impatient that they don't eventually save themselves out of the constraint
 - Finite amount of buffer stock savings
 - Lack of full consumption smoothing even in the long run
- If $\beta(1 + r) > 1$: Asset holdings explode in the long run

ZELDES-DEATON-CARROLL MODEL

- Households maximize

$$\mathbb{E}_0 \sum_{t=0}^{\infty} \beta^t \frac{C_t^{1-\gamma}}{1-\gamma},$$

- subject to

$$W_{t+1} = R(W_t + Y_t - C_t)$$

$$Y_t = P_t V_t$$

$$P_t = P_{t-1} N_t$$

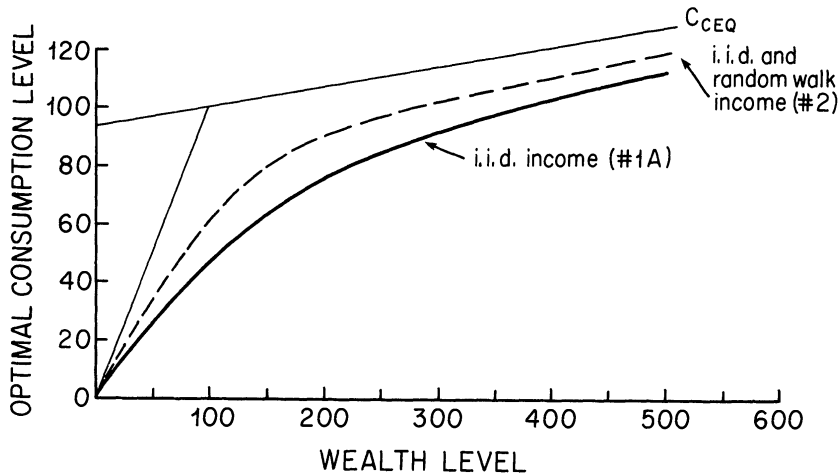
where V_t and N_t are i.i.d. log-normal random variables.

- R is given exogenously (partial equilibrium)
- Household income shocks are uninsurable

See Zeldes (1989), Deaton (1991), Carroll (1992, 1997)

ZELDES-DEATON-CARROLL MODEL

- Problem Sets 8 and 9 ask you to solve two versions of this model
- Zeldes-Deaton-Carroll argue that model helps explain:
 - High MPC out of transitory windfalls
 - That consumption tracks income over the life-cycle
(need impatient households for this)
- Sometimes called the “buffer stock model”
- General equilibrium version called Bewely-Aiyagari-Hugget model
(i.e., interest rate is endogenous)



$T=15$

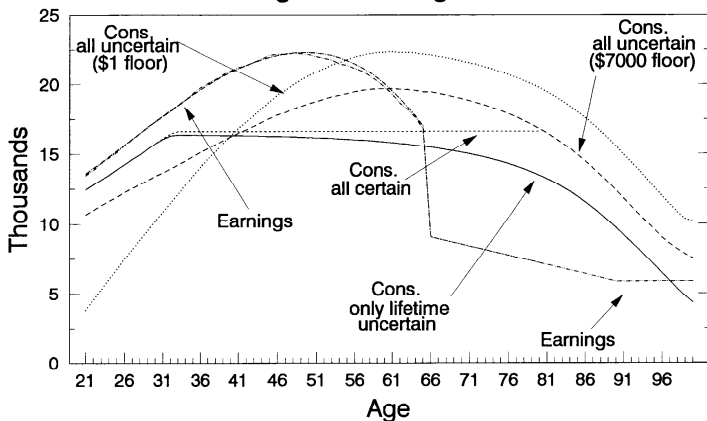
Income Processes: # 1A, # 2

$$U = \frac{C^{1-A}}{1-A} \quad A=3 \quad \text{Expected future income equals 100 per period}$$

Source: Zeldes (1989)

- Basic Zeldes-Deaton-Carroll model very stylized
- Is buffer stock saving important quantitatively?
- Add:
 - Realistic life-cycle income process with retirement
 - Longevity risk
 - Health expenses
 - Taxes and government transfer programs

Figure 3a
Average Consumption and Earnings by Age
No High School Degree

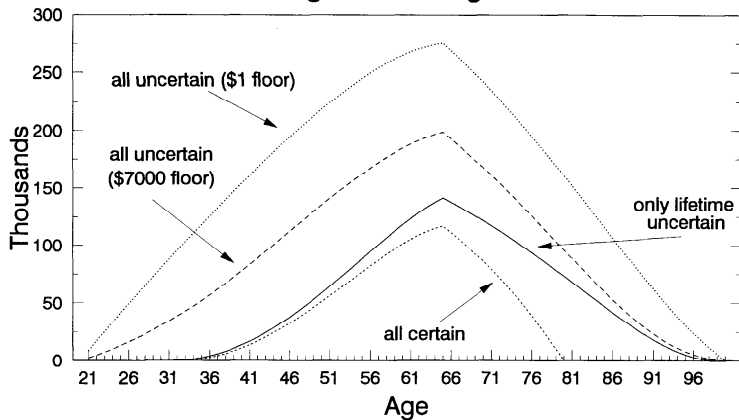


$\gamma=3, \delta=.03$

Source: Hubbard-Skinner-Zeldes (1994)

Consumption does not equal earning for young in certainty case because of medical expenses.

Figure 2a
Average Assets by Age
No High School Degree



$\gamma=3$, $\delta=.03$

Source: Hubbard-Skinner-Zeldes (1994)

Precautionary savings and liquidity constraints:

- Yield life-cycle consumption profile the tracks income substantially
- Can contribute substantially to asset accumulation

- Go one step further than Hubbard-Skinner-Zeldes 94
- Estimate the preference parameters

Thousands of 1987 dollars

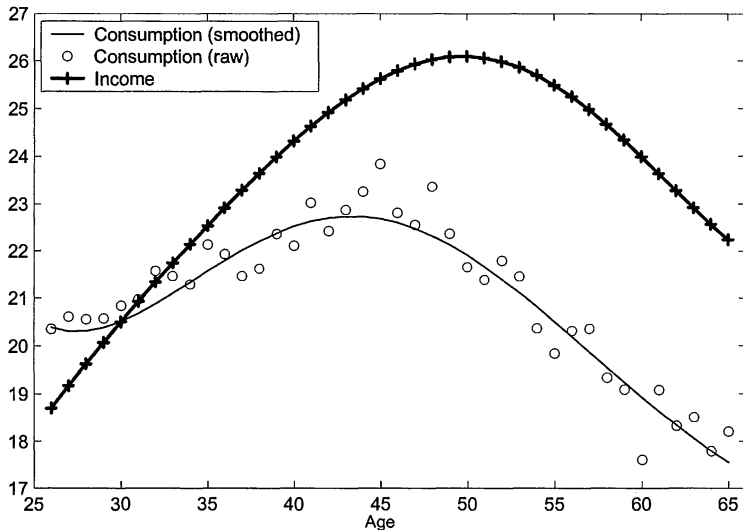


FIGURE 2.—Household consumption and income over the life cycle.

Source: Gourinchas-Parker (2002)

TABLE III
STRUCTURAL ESTIMATION RESULTS

MSM Estimation	Robust Weighting	Optimal Weighting
Discount Factor (β)	0.9598	0.9569
S.E.(A)	(0.0101)	
S.E.(B)	(0.0179)	(0.0150)
Discount Rate ($\beta^{-1} - 1$)(%)	4.188	4.507
S.E.(A)	(1.098)	
S.E.(B)	(1.949)	(1.641)
Risk Aversion (ρ)	0.5140	1.3969
S.E.(A)	(0.1690)	
S.E.(B)	(0.1707)	(0.1137)
Retirement Rule:		
γ_0	0.0015	$5.68 \cdot 10^{-6}$
S.E.(A)	(3.84)	
S.E.(B)	(3.85)	(16.49)
γ_1	0.0710	0.0613
S.E.(A)	(0.1215)	
S.E.(B)	(0.1244)	(0.0511)
χ^2 (A)	175.25	
χ^2 (B)	174.10	185.67

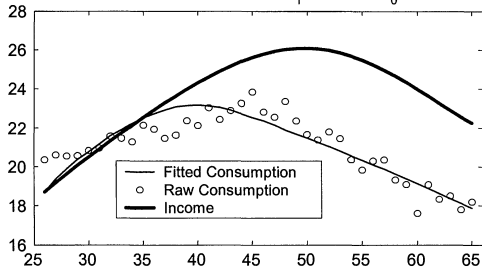
Note: MSM estimation for entire group. Standard errors calculated without (A) and with (B) correction for first stage estimation. Cell size is 36,691 households. The last row reports a test of the overidentifying restrictions distributed as a Chi-squared with 36 degrees of freedom. The critical value at 5% is 50.71. Efficient estimates are calculated with a weighting matrix $\hat{\Omega}$ computed from the robust estimates.

Source: Gourinchas-Parker (2002)

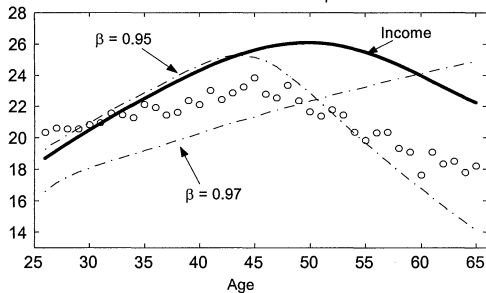
- Reasonable discount rate of 4%
(Carroll-Samwick 97 had suggested larger rates were needed)
- Reasonable IES of about 2 (sensitive to weighting matrix)
- Reasonable MPC in retirement of 7% per year

Thousands
of 1987 dollars

Panel A: Baseline Estimation
 $\beta = 0.960$, $\rho = 0.514$, $\gamma_1 = 0.071$, $\gamma_0 = 0.001$



Panel B: Various β



Source: Gourinchas-Parker (2002)

TARGET CASH ON HAND

- Level of cash on hand at age t that is expected to remain unchanged:

$$\bar{x}_t = E_t[x_{t+1} | x_t = \bar{x}_t]$$

- If $x_t > \bar{x}_t$ households dissave on average
- If $x_t < \bar{x}_t$ households build up assets on average

Target cash-on-hand
(normalized)

Parameters:

$$\beta = 0.960, \rho = 0.514, \gamma_1 = 0.0071, \gamma_0 = 0.001$$

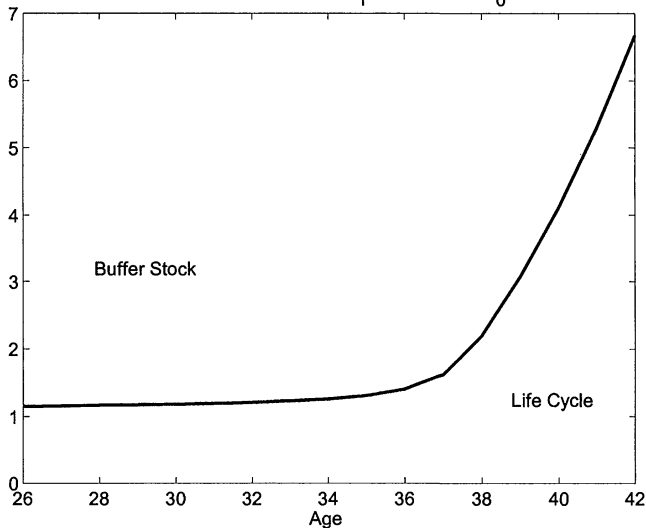


FIGURE 6.—Normalized target cash-on-hand by age.

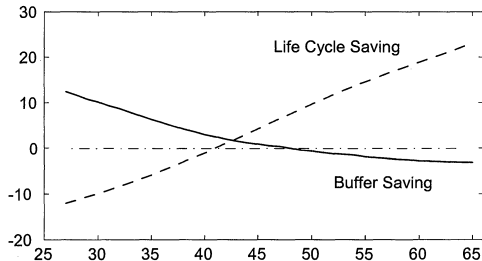
Source: Gourinchas-Parker (2002). Cash-on-hand normalized by permanent income.

LIFE-CYCLE CONSUMPTION SAVINGS

- Define life-cycle consumption as consumption under complete insurance markets
- Use this concept to construct:
 - Life-cycle savings / wealth
 - Buffer-stock savings / wealth

Thousands
of 1987 dollars

Panel A: Life Cycle and Buffer Saving



Panel B: Life Cycle and Buffer Wealth

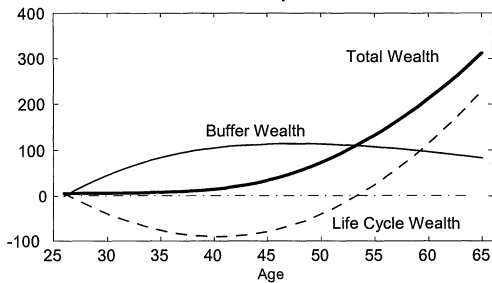


FIGURE 7.—The role of risk in saving and wealth accumulation.

Source: Gourinchas-Parker (2002)

GOURINCHAS-PARKER 02: SUMMARY

- Can uninsurable income risk explain comovement of consumption and income over the life-cycle?

GOURINCHAS-PARKER 02: SUMMARY

- Can uninsurable income risk explain comovement of consumption and income over the life-cycle?
- Yes!
- Households are impatient
(want downward sloping consumption profiles)
- Consumption constrained by income early in life
- Households save for retirement later in life

- Standard incomplete markets models can't match large estimated spending responses of consumption to tax rebates
- Argue that incorporating illiquid wealth into model is key:
 - Liquid assets (-1.5% real return)
 - Illiquid asset (2.3% real return)
 - Unsecured debt (6% real interest rate)
- Two types of hand-to-mouth agents:
 - Poor hand-to-mouth (no illiquid wealth, no liquid wealth)
 - Wealthy hand-to-mouth (have illiquid wealth, no liquid wealth)
- This model generates much higher rebate responses

- Common for people to display dissatisfaction with their choices
 - I am not saving enough for retirement
 - I eat too much and exercise too little
 - I spend too much time surfing the internet and work too little
- One reaction:
 - This is stupid. What you do are you actual preferences
 - What you say are some imagined idealized preferences
 - Everyone says they want to be fit and work really hard
 - But the costs of achieving these goals actually outweigh the benefits for many people

- An alternative reaction:
 - Consumer regret is due to **self-control problems**
 - Arises due to present biased preferences that give rise to preference reversals

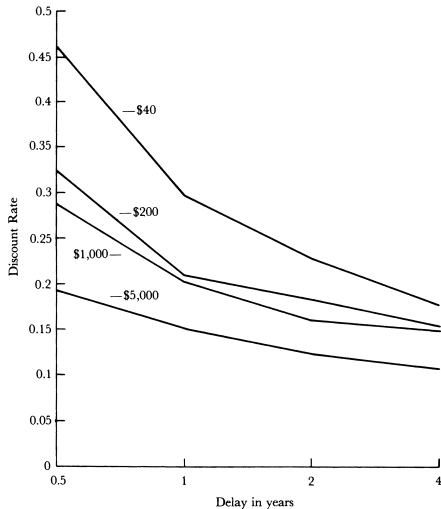
- An alternative reaction:
 - Consumer regret is due to **self-control problems**
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- Consider the following choice for a worker:
 1. 15 minute break today
 2. 20 minute break tomorrow

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- Consider the following choice for a worker:
 1. 15 minute break today
 2. 20 minute break tomorrow
- Now consider this choice:
 1. 15 minute break in 100 days
 2. 20 minute break in 101 days

- An alternative reaction:
 - Consumer regret is due to **self-control problems**
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- Consider the following choice for a worker:
 1. 15 minute break today
 2. 20 minute break tomorrow
- Now consider this choice:
 1. 15 minute break in 100 days
 2. 20 minute break in 101 days
- Choosing option 1 from the first set but option 2 from the second set indicates time-discounting that is not independent of horizon

Figure 1

Discounting as a Function of Time Delay and Money Amount.



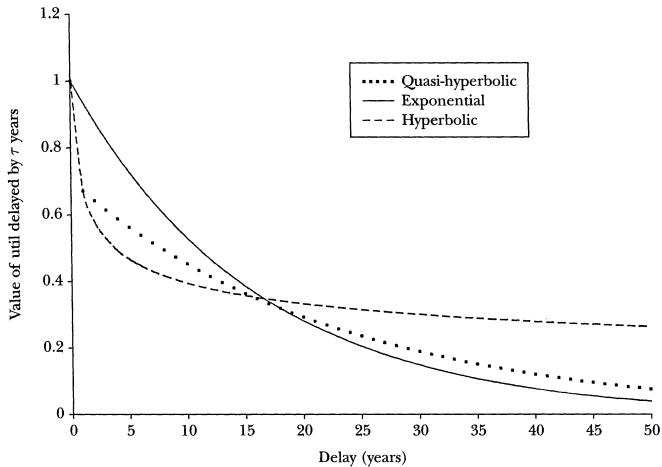
Source: Ben Zion et al. (1989).

Source: Loewenstein and Thaler (1989). Based on experiments where subjects are asked how much they need to be compensated to delay receiving a reward.

HYPERBOLIC DISCOUNTING

- Exponential discounting:
 - Discount function: β^t : 1, β , β^2 , β^3 , etc.
 - Discount rate independent of horizon
 - Degree of patience independent of horizon
- Hyperbolic discounting:
 - Discount function: $1/t$ or $1/(1 + \alpha t)$ or $1/(1 + \alpha t)^{-\gamma/\alpha}$
 - Quasi-hyperbolic discount function: $\beta\delta^t$: 1, $\beta\delta$, $\beta\delta^2$, $\beta\delta^3$, etc.
 - Non-constant rate of discounting
 - More impatient about short run than long run

Figure 1
Discount Functions



Exponential: δ^τ , with $\delta = 0.944$; hyperbolic: $(1 + \alpha\tau)^{-\gamma/\alpha}$, with $\alpha = 4$ and $\gamma = 1$; and quasi-hyperbolic: $[1, \beta\delta, \beta\delta^2, \beta\delta^3, \dots]$, with $\beta = 0.7$ and $\delta = 0.957$.

Source: Angeletos et al. (2001)

TIME-CONSISTENT PREFERENCES

- Suppose an agent makes a state-contingent plan at time 0 about optimal current and future actions
- But when the future arrives, the agent can reoptimize
- Will they want to change their plan?

TIME-CONSISTENT PREFERENCES

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- But when the future arrives, the agent can reoptimize
- Will they want to change their plan?

- If the agent discounts future utility exponentially, then they will not change their choices even if able to reoptimize
- Their preferences are **time consistent**
(aka dynamically consistent)

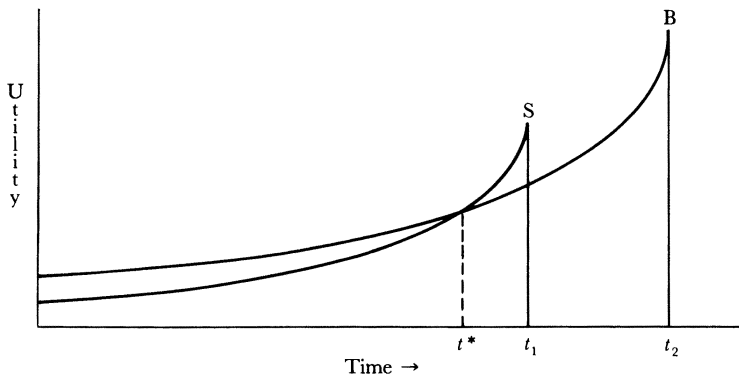
TIME-INCONSISTENT PREFERENCES

- If an agent's discount function is not exponential, then they will want to change their plan when allowed to reoptimize at a later date
- Their preferences are **time inconsistent**
(aka dynamically inconsistent)
- Hyperbolic and quasi-hyperbolic preferences are time inconsistent

PREFERENCE REVERSALS

- Consider following choice:
 - Small reward S at time t_1
 - Bigger reward B at a later time t_2
- Suppose agent has hyperbolic preferences
- Plot present utility from each option as a function of time

Figure 2
Non-Exponential Discounting.



Source: Ainslie (1975).

Source: Loewenstein and Thaler (1989).

- Hyperbolic discounting can explain the following type of behavior:
 - On Monday: “I’ll work hard tomorrow.”
 - On Tuesday: “I’ll work hard tomorrow.”
 - Etc.
- People with hyperbolic preferences want instant gratification today but simultaneously want to make patient investments tomorrow

INTRAPERSONAL STRATEGIC CONFLICT

- Useful to think of a person as having different selves, one for each point in time.
- Earlier selves wish to force later selves to act patiently
- Later selves maximize their own preferences (which are different)
- Household problem becomes a game between different selves

TWO TYPES OF HYPERBOLICS

- Sophisticates: Understand that future selves will want to act differently
 - Want to constrain actions of future selves
 - Want access to commitment devices
- Naifs: Act under false belief that future selves will carry out current plan
 - Helps explain procrastination among other things
(Akerlof, 1991; O'Donoghue and Rabin, 1999)

HYPERBOLIC DISCOUNTING AND CONSUMPTION

- Key references:
 - Angeletos et al. (2001), Laibson, Repetto, Tobacman (2003),
Laibson, Maxted, Repetto, Tobacman (2015, but originally ca. 2001)
- Build sophisticated life-cycle consumption savings model
- Compare model with exponential and hyperbolic discounting
- Ask whether hyperbolic discounting helps explain the data

HYPERBOLIC DISCOUNTING AND CONSUMPTION

- Model very similar to Kaplan-Violante (2014)
(liquid assets, illiquid assets, credit card borrowing)
- Conclusions radically different
- Laibson et al. (2015) estimate:
 - Exponential discounting: $\beta = 0.63$ (annual)
 - Hyperbolic discounting: $\beta = 0.35$ and $\delta = 0.97$
- Kaplan-Violante (2014) calibrate $\beta = 0.941$

KAPLAN-VIOLANTE VS. LAIBSON ET AL.

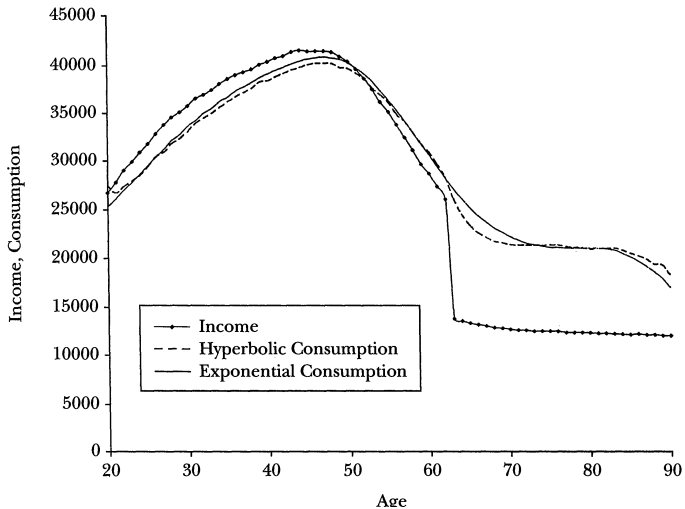
- Main difference seems to lie in moments used
- Kaplan-Violante:
 - Target a fraction of credit card borrowers of 26%
 - Compromise between fraction with negative net liquid wealth and fraction actually borrowing on credit cards
 - Many people simultaneously have liquid assets and credit card debt
- Laibson et al.
 - Target fraction of credit card borrowers of 75%

HYPERBOLIC DISCOUNTING AND CONSUMPTION

- Hyperbolic discounting helpful in explaining simultaneous:
 - High borrowing on credit cards at high interest rates
 - Large saving for retirement
- Agents with hyperbolic discounting can simultaneously display highly patient and impatient behavior

Figure 2

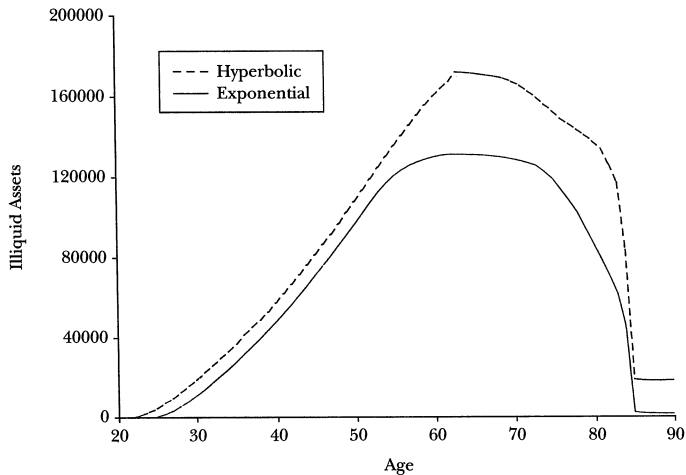
Simulated Mean Income and Consumption



Source: Angeletos et al. (2001).

Figure 4

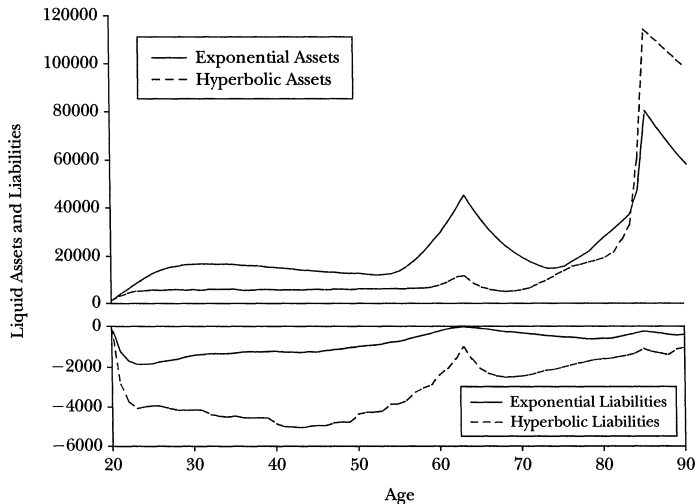
Mean Illiquid Assets of Households with Exponential and Hyperbolic Discount Functions



Source: Angeletos et al. (2001).

Figure 5

Mean Liquid Assets and Liabilities



Source: Angeletos et al. (2001).

KAPLAN-VIOLANTE VS. LAIBSON ET AL.

- Kaplan-Violante: Agents hold illiquid wealth because of high return
- Laibson et al.: Agents hold illiquid wealth for two reasons:
 - High return
 - Commitment device: Constrains impatient future selves

Table 1

Percentage of Households with Liquid Assets Greater than One Month of Income

<i>Age Group</i>	<i>Simulated Data</i>		<i>Survey of Consumer Finances</i>		
	<i>Exponential</i>	<i>Hyperbolic</i>	<i>Definition 1</i>	<i>Definition 2</i>	<i>Definition 3</i>
ALL AGES	0.73	0.40	0.37	0.43	0.52
20–29	0.52	0.34	0.18	0.19	0.26
30–39	0.72	0.39	0.21	0.24	0.36
40–49	0.72	0.38	0.26	0.31	0.42
50–59	0.76	0.43	0.35	0.41	0.50
60–69	0.91	0.42	0.58	0.68	0.76
70+	0.77	0.46	0.62	0.71	0.78

Sources: Authors' simulations and 1995 SCF.

Notes: The table reports the fraction of households who hold more than a month's income in liquid wealth. Definition 1 includes cash, checking and savings accounts. Definition 2 includes definition 1 plus money market accounts. Definition 3 includes definition 2 plus call accounts, CDs, bonds, stocks and mutual funds.

Source: Angeletos et al. (2001).

Table 2
Share of Assets in Liquid Form

<i>Age Group</i>	<i>Simulated Data</i>		<i>Survey of Consumer Finances</i>		
	<i>Exponential</i>	<i>Hyperbolic</i>	<i>Definition 1</i>	<i>Definition 2</i>	<i>Definition 3</i>
ALL AGES	0.51	0.41	0.08	0.10	0.16
20–29	0.97	0.86	0.13	0.14	0.18
30–39	0.65	0.46	0.09	0.10	0.14
40–49	0.35	0.24	0.06	0.07	0.10
50–59	0.20	0.13	0.04	0.05	0.09
60–69	0.27	0.12	0.09	0.10	0.20
70+	0.57	0.56	0.09	0.12	0.24

Sources: 1995 SCF and authors' simulations.

Notes: Asset share is liquid assets divided by total assets—liquid assets plus illiquid assets. The three different definitions used for liquid assets are the same as in Table 1. Three complementary definitions are used for illiquid assets. Illiquid assets include money market accounts, call accounts, CDs, bonds, stocks, and mutual funds if these assets were not included in the relevant liquid asset definition. In addition, illiquid assets include IRAs, defined contribution plans, life insurance, trusts, annuities, vehicles, home equity (net of mortgage), real estate, business equity, jewelry, furniture, antiques, and home durables.

Source: Angeletos et al. (2001).