

1 Julia Output 2021-01-04

To check the covariance matrix generator function, I printed out the "Latexified" symbolic matrix generated in Julia using $N = 2, T = 3$.

LEFT HALF OF COVARIANCE MATRIX

$$\begin{bmatrix} \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} & \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \\ \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} & \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \\ \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} \\ \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} \\ \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \\ \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \end{bmatrix} \quad (1)$$

RIGHT HALF OF COVARIANCE MATRIX

$$\begin{bmatrix} \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} \\ \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} & \sigma_u^2 \left(\frac{1}{2}\rho^2 + \frac{\rho^4}{2-2\rho} \right) + \frac{\sigma_a^2 \rho^2}{1-\rho^2} \\ \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \\ \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) \\ \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} & \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} \\ \frac{\sigma_a^2 \rho}{1-\rho^2} + \sigma_u^2 \left(\frac{1}{2}\rho + \frac{\rho^3}{2-2\rho} \right) & \frac{\sigma_a^2}{1-\rho^2} + \frac{\sigma_u^2 \rho^2}{2-2\rho} & \sigma_u^2 \left(1.0 + \frac{\rho^2}{2-2\rho} \right) + \frac{\sigma_a^2}{1-\rho^2} \end{bmatrix} \quad (2)$$

Upon inspection with the 2021-12 note, this output matches the form of the covariance matrix given for the $N = 2, T = 3$ example.