

K-means Clustering:-

① 3 clusters, Center A_1, A_4, A_7

$$D(A_1, A_1) = 0$$

$$D(A_1, A_4) = \sqrt{13} \approx 3.61$$

$$D(A_1, A_7) = \sqrt{65} \approx 8.06$$

$$D(A_2, A_1) = 5$$

$$D(A_2, A_4) = 4.24$$

$$D(A_2, A_7) = 3.16$$

$$D(A_3, A_1) = 6$$

$$D(A_3, A_4) = 5$$

$$D(A_3, A_7) = 7.28$$

$$D(A_5, A_1) = 7.07$$

$$D(A_5, A_4) = 3.61$$

$$D(A_5, A_7) = 6.708$$

$$D(A_6, A_1) = 7.211$$

$$D(A_6, A_4) = 4.123$$

$$D(A_6, A_7) = 5.385$$

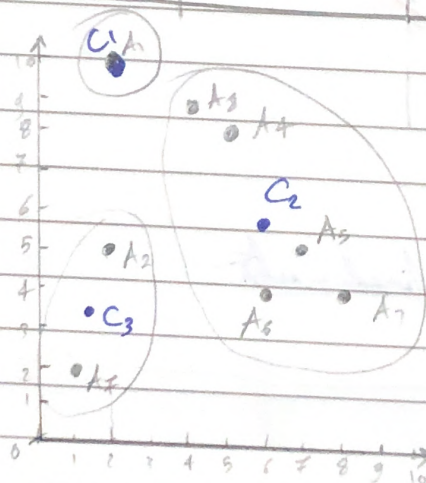
$$D(A_8, A_1) = 2.24$$

$$D(A_8, A_4) = 1.41$$

$$D(A_8, A_7) = 7.615$$

Clusters

A_1	A_4	A_7
A_1	A_3	A_2
	A_4	A_7
	A_5	
	A_6	
	A_8	



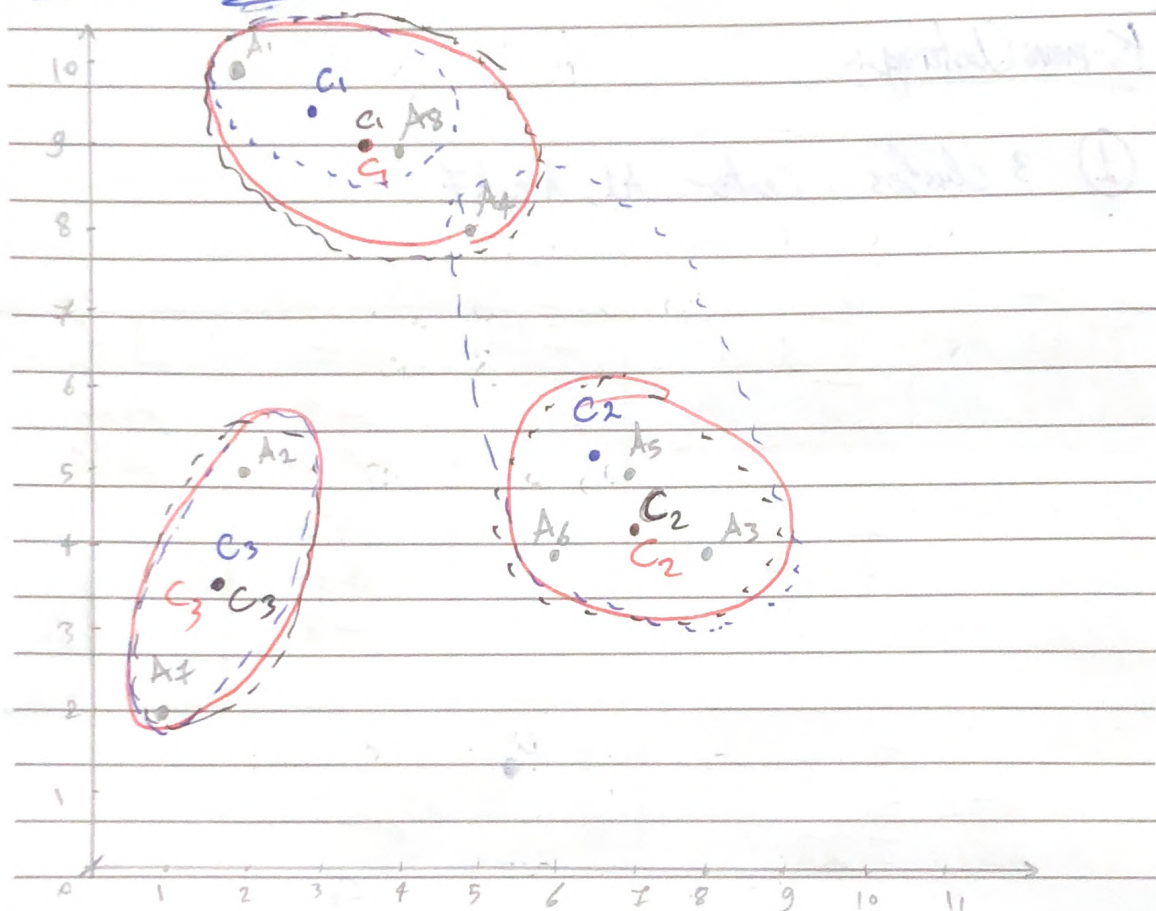
$$C_1 = (2, 10)$$

$$C_2 = (6, 6)$$

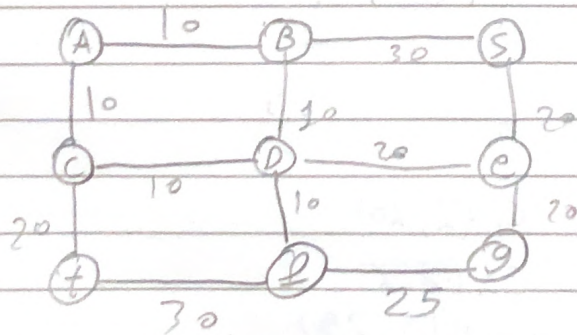
$$C_3 = (1.5, 3.3)$$

2nd Epoch & 3rd Epoch last one
4th epoch

NOTES.



Normalized Cut:



	A	B	S	C	D	e	t	f	g
A	20	0	0	0	0	0	0	0	0
B	0	50	0	0	0	0	0	0	0
S	0	0	50	0	0	0	0	0	0
C	0	0	0	40	0	0	0	0	0
D	0	0	0	0	50	0	0	0	0
e	0	0	0	0	0	60	0	0	0
t	0	0	0	0	0	0	50	0	0
f	0	0	0	0	0	0	0	65	0
g	0	0	0	0	0	0	0	0	45



NOTES

	A	B	S	C	D	e	t	f	g
A	0	10	0	10	0	0	0	0	0
B	10	0	30	0	10	0	0	0	0
S	0	30	0	0	0	20	0	0	0
C	10	0	0	0	10	0	20	0	0
D	0	10	0	10	0	20	0	10	0
e	0	0	20	0	20	0	0	0	20
t	0	0	0	20	0	0	0	30	0
f	0	0	0	0	10	0	30	0	25
g	0	0	0	0	0	20	0	25	0

A

	A	B	S	C	D	e	t	f	g
A	20	-10	0	-10	0	0	0	0	0
B	-10	50	-30	0	-10	0	0	0	0
S	0	-30	50	0	0	-20	0	0	0
C	-10	0	0	40	-10	0	-20	0	0
D	0	-10	0	-10	50	-20	0	-10	0
e	0	0	-20	0	-20	60	0	0	-20
t	0	0	0	-20	0	0	50	-30	0
f	0	0	0	0	-10	0	-30	65	-25
g	0	0	0	0	0	-20	0	-25	45

$$L = \Delta - A$$

$$C_1 \Rightarrow \textcircled{A} \{B, S\}$$

$$\textcircled{B} \{A, C, D, E, T, F, G\}$$

$$C_1^T \Delta C_1 = [0, 1, 1, 0, 0, 0, 0, 0, 0]^T$$

$$C_2 [1, 0, 0, 1, 1, 1, 1, 1, 1]^T$$

$$= [0.50, 50, 0, 0, 0, 0, 0, 0, 0] C_1$$

$$= 100 = \text{Vol}(A)$$

$$C_2^T \Delta C_2 = 330 = \text{Vol}(B)$$

$$\underline{\underline{\text{CUT}(A, B) = 40}}$$

$$\text{NCUT}(A, B) = 40 \left(\frac{1}{100} + \frac{1}{330} \right)$$

$$= \frac{86}{165} \approx 0.521$$

$$C_2 \Rightarrow \textcircled{A} \{A, B, S, D, E\}$$

$$\textcircled{B} \{C, T, F, G\}$$

$$\text{CUT}(A, B) = 50$$

$$C_1 = [0, 1, 1, 1, 0, 1, 1, 0, 0, 0]$$

$$C_2 = [0, 0, 0, 1, 0, 0, 1, 1, 1, 1]$$

$$C_1^T \Delta C_1 = 230$$

$$C_2^T \Delta C_2 = 200$$

$$\text{NCUT} = 50 \left(\frac{1}{230} + \frac{1}{200} \right)$$

$$= 0.47$$

C₁ is better a graph cut but worse as a NCVT

C₂ is better a NCVT but worse as a graph cut

③ a)

~~A = Distance Matrix~~

~~Similarity Matrix = $k(C(x,y)) = \Delta$~~

A = Similarity

Δ = Distance Matrix

④

1. Conditional Entropy $H(T|C_i) = -\sum_{j=1}^K \left(\frac{n_{ij}}{n_i}\right) \log\left(\frac{n_{ij}}{n_i}\right)$

2. Purity_i = $\frac{1}{n_i} \max_k n_{ik}$, Purity = $\sum_{i=1}^K \frac{n_i}{n} \text{Purity}_i$

3. Pairwise measures (Jaccard and Rand Index)

4. Max matching when # of clusters = 3, $\text{aymax} \left\{ \frac{w(M)}{n} \right\} = \frac{w(M)}{\sum_{e \in E} w(e)}$

5. F-Measure $\text{Prec}_i = \text{Purity}_i$

$$\text{Rec}_i = \frac{n_{ii}}{|T_{ii}|}$$

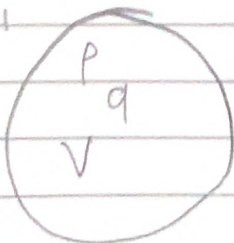
$$F_i = \frac{2 * \text{Prec}_i * \text{Rec}_i}{\text{Prec}_i + \text{Rec}_i}$$

$$F = \frac{1}{r} \sum_{i=1}^r F_i$$

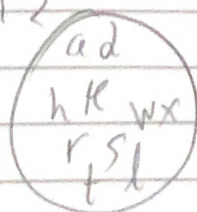
$$\text{Jaccard Index} = \frac{TP}{TP + FN + FP}$$

$$\text{Define Rand Index} = \frac{TP + TN}{TP + TN + FN + FP}$$

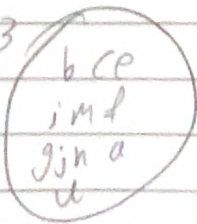
T₁



T₂



T₃



$$ii) \text{ Beta CV} = \frac{W_{in}}{N_{in}} / \frac{W_{out}}{N_{out}}$$

NOTES.

$$NC = \sum_{i=1}^K \frac{1}{\frac{W(C_i, C_i)}{W(C_i, C_i)} + 1}$$

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