

Sheet 1

①

a) Dynamic Range:- the unique values

Contrast:- the difference between highest and lowest

• Contrast =  $48 - 0 = 48$

→ Dynamic Range: 0, 1, 2, 3, 4, 5, 6, 7, 8  
9, 10, 11, 12, 13, 14, 15

Dynamic Range: 16

b) Over exposure

i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
$h(i)$	0	0	0	5	15	20	18	16	15	5	8	25	25	30	20	48
$i'$	0	1	2	3	4	6	7	8	9	10	11	12	13	14	15	
$h'(i')$	0	0	0	5	15	18	16	15	5	8	25	25	30	20	48	

Contrast =  $48 - 0 = 48$

Dynamic Range: 0, 1, 2, 3, 4, 6, 7, 8, 9, 10, 11  
12, 13, 14, 15

Dynamic Range = 15

↑  
changed

$$\underline{d)} f_{eq} \left[ H(a) \frac{K-1}{MN} \right] \quad K-1=15$$

$$MN = \text{Total Pixels} = 250$$

i	0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15
H(a)	0	0	0	5	20	40	58	74	89	94	102	127	152	182	202	250
f <sub>eq</sub>	0	0	0	0	1	2	3	4	5	5	6	7	9	10	12	15
h <sub>eq</sub>	0	0	0	0	15	20	18	16	15	5	8	25	25	30	20	48

② a) edge detection of a 45 degree

$$\underline{b)} \text{ Maximum } \begin{bmatrix} 0 & -3 & -1 \\ 3 & 0 & -3 \\ 1 & 3 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 255 & 0 & 0 \\ 255 & 255 & 0 \end{bmatrix} \Rightarrow 255$$

$$\text{Minimum } \begin{bmatrix} \quad & \quad & \quad \\ \quad & \quad & \quad \\ \quad & \quad & \quad \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \Rightarrow 0$$

$$\underline{c)} \text{ impulse } \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} \begin{bmatrix} 0 & -3 & -1 \\ 3 & 0 & -3 \\ 1 & 3 & 0 \end{bmatrix} = 3+1+3-3-1-3 = 0$$

d) Yes, because, it's an asymmetric filter

$$\textcircled{3} \begin{bmatrix} 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix} \quad \text{Shift image on pixel left and shift it on pixel up}$$

↖ shift

No.

Date

- ④ Compute the gradient vector, gradient magnitude and orientation at (3,3).

Use the filter  $s_x = [-1, 0, 1]$  to compute gradients

$$\nabla f = \left[ \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \right] \quad \theta = \tan^{-1} \left( \frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$$

gradient direction

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

	1	2	3	4	5
1	100	111	97	100	105
2	107	111	107	105	115
3	117	100	117	110	128
4	111	105	111	120	122
5	100	110	100	110	100

	1	2	3
1	-3	-11	8
2	0	-6	8
3	0	16	11
4	0	15	11
5	0	0	0

	1	2	3	4	5
1	17	-11	20	10	23
2	4	-6	4	15	7
3	-17	10	-17	0	-28

$$\nabla f_{(3,3)} = [11, -17], \quad \theta = \tan^{-1} \left( \frac{-17}{11} \right) = -57.1^\circ$$

$$\|\nabla f\| = \sqrt{410} = 20.25$$

orientation  $\Rightarrow$

Ledge

DAOM

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