

Abdel Rahman Al  
17012296

## Sheet 6

①

$\rho_w = 1 \text{ millimeter}$

$$u^L = [-3, -10, -29]$$

$$d = u^L - u^R = [33, 20, 25]$$

$$u^R = [30, 10, -3]$$

$$T = 10 \text{ cms}$$

$$f = 2 \text{ cms} = 20 \text{ pixels}$$

$$Z = \frac{T \cdot f}{[33, 20, 25]} = \frac{200}{d} \approx [6.06, 10, 8]$$

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②

a)  $E = [T_x] R = \begin{bmatrix} 0 & -10 & 0 \\ -10 & 0 & -10 \\ 0 & 10 & 0 \end{bmatrix}$

$$S = E^T E = \begin{bmatrix} 400 & 0 & 100 \\ 0 & 200 & 0 \\ 100 & 0 & 100 \end{bmatrix} \rightarrow (S - S^T) = 0$$

P. K. 11  $U = \begin{bmatrix} 0 & -s_{21} & s_{13} \\ s_{21} & 0 & -s_{32} \\ -s_{13} & s_{32} & 0 \end{bmatrix} = \begin{bmatrix} 0 & 0 & 100 \\ 0 & 0 & 0 \\ -100 & 0 & 0 \end{bmatrix}$

$$U(S - S^T) = 0$$

b)  $e_l = [0]$ ,  $e_r = [0]$

c)  $l_r = E \cdot [X, Y, Z]^T$

$$l_r = \begin{bmatrix} -30 \\ 50 \\ 30 \end{bmatrix}$$

d)  $F = K_r^{-T} E K_l^{-1}$

$$= \begin{bmatrix} 0 & -1/4000 & 1/25 \\ -1/4000 & 0 & 1/50 \\ 3/40 & 3/20 & -1/2 \end{bmatrix}$$

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$$e) e'_i \cdot K_i \cdot e_i = [0]$$

$$e'_r \cdot K_r \cdot e_r = [0]$$

$$f) l_i = F \cdot x_r$$

$$= F \cdot \begin{bmatrix} 100 \\ 50 \\ 1 \end{bmatrix} = \begin{bmatrix} a \\ b \\ c \end{bmatrix} = \begin{bmatrix} 25500 \\ 12875 \\ 1 \end{bmatrix}$$

$$25500x + 12875y + 1 = 0$$

$$m \approx -1.98, \quad b = -c/b = -0.0000774$$

③

$$F = \begin{bmatrix} 0 & -t_z & b \\ t_z & 0 & -t_x \\ 0 & t_x & 0 \end{bmatrix}$$

$$[x_r \ y_r \ 1] \cdot F \cdot \begin{bmatrix} x_l \\ y_l \\ 1 \end{bmatrix} = 0$$

$$= -t_z \cdot x_r \cdot x_l - t_x \cdot y_r x_l + t_z x_r \cdot y_l + t_x \cdot y_r \cdot y_l = 0$$

only need 1 point from r & one from l

④ Center Right =  $[75, 50]^T$

Center left =  $[100, 70]^T$

Average distance = 20 pixel in left & 50 in right

$$a) T = \begin{bmatrix} 1 & 0 & -c_x \\ 0 & 1 & -c_y \\ 0 & 0 & 1 \end{bmatrix}, \quad S = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$T_l = \begin{bmatrix} 1/20 & 0 & -100 \\ 0 & 1/20 & -70 \\ 0 & 0 & 1 \end{bmatrix}, \quad T_r = \begin{bmatrix} 1/50 & 0 & -75 \\ 0 & 1/50 & -80 \\ 0 & 0 & 1 \end{bmatrix}$$

$$b) F = T_r^T \cdot f_i \cdot T_l$$

$$F = \begin{bmatrix} 0 & -7.5 \times 10^{-5} & 0.1245 \\ -7.5 \times 10^{-5} & 0 & 0.15 \\ 0.378 & 0.37 & -1290 \end{bmatrix}$$

⑤ Left Scan-line: 100, 150, 90, 140, 200  
Right Scan-line: 90, 105, 145, 130, 210

⑥

Index left	1	2	3	4	5
Intensity left	100	150	90	140	200
Matched Intensity	105	145	90	145	210
Matched Index	2	3	1	3	5
Disparity	1	1	-2	-1	0

Pixel 3 in Right is matched to 2 points

b)

I left	1	2	3	4	5
I <sub>r</sub> left	100	150	90	140	200
Matched I <sub>r</sub>	105	145	/	130	210
Matched I	2	3	/	4	5
Disparity	0	0	/	0	0

Smaller solution