

Sheet 1

① $n = 2048$

PE adding 2 numbers = 1 millisecond

PE sending m numbers = $2 + \frac{m}{1024}$ milliseconds

PE from 1 to 1024, power of 2

PE = 1 :-

$$\begin{aligned} \text{Adding numbers time} &= n - 1 \\ &= \underline{\underline{2047}} \end{aligned}$$

~~Step 1~~

Step 1:- Transfer to other PEs

~~Step 2~~ Summation of numbersStep 3:- Send once add once until
Reaching first PE

$$\boxed{\text{PE} = 1} \quad \text{Time} = 2047 \text{ milliseconds}$$

$$\boxed{\text{PE} = 2} \quad \text{Step 1:- } 1024 \text{ from PE 1 to PE 2}$$

$$2 + \frac{m}{1024} = 2 + \frac{1024}{1024} = 3$$

Step 2:- 1024

$$\text{Step 3:- } \left(2 + \frac{1}{1024}\right) + \left(1\right)$$

Transfer adding

/ 1

general rule ~~3.9~~ ~~1024~~

Data Distribution

PE = 4

Step 1: $2 + \frac{1024}{1024} = 3$

PE#0 → PE#2

Step 2: $2 + \frac{512}{1024} = 2.5$

PE#0 PE#1
↓ ↓
#2 #3

Step 3:

Addition: ~~5~~ 11

#0 #1
↑ ↑
#2 #3

Step 4: $2 + \frac{1}{1024} \approx 2.001$

Step 5: Add 1

Step 6: $2 + \frac{1}{1024} \approx 2.001$

Step 7: 1

Total = 522.502

General formula:-

$$P = 2^9, n = 2^k = 2048 = 2^{11} \text{ NOTES}$$

- Data Distribution: $\sum_{n=1}^9 2 + \frac{2^{k-n}}{1024} = \sum_{n=1}^9 2 + 2^{k-n-10}$

- Addition: $n_p - 1 = 2^{k-9} - 1$

- Collecting & Adding: $9(2 + \frac{1}{1024} + 1)$

$$\text{Total} = \sum_{n=1}^9 (2 + 2^{k-n-10}) + 2^{11-9} - 1 + 9(2 + \frac{1}{1024} + 1)$$

q	PE	$\Sigma(2 + 2^{k-n-10})$	Total	Speedup	Efficiency
0	1	//	2048	1	100%
1	2	3	1029	1.989	99.45%
2	4	5.5	522.5	3.918	97.95%
3	8	7.75	271.75	7.533	94.9875%
4	16	9.875	148.88	13.75	85.9375%
5	32	11.9375	89.94	22.76	71.125%
6	64	13.96875	62.97	32.50	50.78125%
7	128	15.984375	51.99	39.37	30.75%
8	256	17.9921875	49	41.78	16.32%
9	512	19.99609375	50	40.94	7.99%
10	1024	21.99804688	53	38.62	3.77%

2) @ Every Processor only computes the slot of Histogram offered to it but there will be redundant pixels that will not be counted per slot

① The image will be processed faster but there will be a chance of racing conditions to access & write in the histogram.

③ Strong Scalability: Number of cores is changing but input is fixed

Weak Scalability: Both cores & input are changing

④ Distributed Memory:- Each Node ~~has~~ have its own private memory and only communicate explicitly by sending across a network

Shared Memory:- All cores access a common memory space through a shared bus + local cache for each core.

⑤ Typical Considerations

- Partitioning:- Decomposing the problem into pieces.
like Data parallelism, task parallelism, model parallelism.
- Communication:- Depending on the partitioning scheme, the amount of communication & the type of communication is ~~also~~ determined.
- Synchronization:- In order to operate in an appropriate way, threads or processes may need to be synchronized.
- Load Balancing:- Work needs to be equally divided among threads or processes in order to balance the ~~load~~ load and minimize idle times.