Laboratorium #9. Teoria optymalizacji.

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Poniższy program służy do rozwiązywania problemów geometrycznych.

Dokument zawiera rozwiązanie 11 zadań na dwa sposoby

```
cvx_gp = zeros(11,1);
cvx_log = zeros(11,1);
WynikiZgodne = strings(11,1);
```

Zadanie 1

```
total len = 2400;
 cvx begin gp quiet
                               variables x y
                               \texttt{maximize} \ \mathbf{x}^{\star}\mathbf{y}
                                subject to
                                                           2*x + y <= total_len;
 cvx end
 cvx_begin quiet
                                maximize(logx + logy)
                                subject
                                                            log(2*exp(logx) + exp(logy)) <= log(total_len);</pre>
 cvx_end
proba = 1;
   cvx_gp(proba,1) = x;
 cvx_gp(proba, 2) = y;
 cvx_log(proba,1) = exp(logx);
 cvx_log(proba,2) = exp(logy);
  \textbf{if} \ (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, \texttt{1}))) \ \texttt{==} \ \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, \texttt{1}))) \ \texttt{\&\&} \ (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, \texttt{2}))) \ \texttt{==} \ \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, \texttt{2}))) \\ \textbf{==} \ \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, \texttt{2}))) \ \texttt{==} \ \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, \texttt{2}))) \\ \textbf{==} \ \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, \texttt{2})) 
                               WynikiZgodne(proba) = string('Tak');
                                WynikiZgodne(proba) = string('Nie');
```

Zadanie 2

```
total_len = 500;
cvx_begin gp quiet
     variables x y
     maximize x*v
     subject to
          x + 2 * y <= total_len;
cvx_end
cvx begin quiet
     variables logx logy
     maximize(logx + logy)
          log(2*exp(logy) + exp(logx)) \le log(total_len);
cvx end
cvx_gp(proba, 1) = x;
cvx_gp(proba,2) = y;
cvx_log(proba,1) = exp(logx);
cvx_log(proba,2) = exp(logy);
 \text{if } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 1)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 1))) \text{ && } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 2)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 2))) \\ \end{aligned} 
      WynikiZgodne(proba) = string('Tak');
else
     WynikiZgodne(proba) = string('Nie');
end
```

Zadanie 3

```
total_vol = 50;
cvx_begin gp quiet
     variables h w
     minimize( 60*w*w + 48 * w * h )
     subject to
         3*w*w*h == total_vol;
cvx_end
% 2 część
total_vol = 50;
cvx_begin quiet
     variables logh logw
     \label{eq:minimize} \texttt{minimize(60*exp(logw)*exp(logw)*+48*exp(logw)*exp(logh))} \ )
     subject to
          log(3)+2*logw + logh == log(total_vol) ;
proba = 3;
cvx_gp(proba,1) = w;
cvx_gp(proba, 2) = h;
cvx_log(proba,1) = exp(logw);
cvx\_log(proba,2) = exp(logh);
 \text{if } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 1)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 1))) \text{ && } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 2)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 2))) \\ \end{aligned} 
     WynikiZgodne(proba) = string('Tak');
     WynikiZgodne(proba) = string('Nie');
end
```

Zadanie 4

```
% 1 wersia
total material = 10;
cvx_begin gp quiet
     variables w h
     maximize w^2*h
     subject to
         2*w^2+4*w*h <= total_material;
cvx_end
     .
wersja
cvx_begin quiet
     variables logw logh
     maximize log(exp(logw)^2*exp(logh))
     subject t
          log(2*exp(logw)^2+4*exp(logw)*exp(logh)) <= log(total_material);</pre>
cvx_end
proba = 4;
cvx_gp(proba, 1) = w;
cvx\_gp(proba, 2) = h;
cvx_log(proba,1) = exp(logw);
cvx_log(proba,2) = exp(logh);
 \text{if } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 1)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 1))) \text{ && } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 2)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 2))) \\ \end{aligned} 
     WynikiZgodne(proba) = string('Tak');
else
     WynikiZgodne(proba) = string('Nie');
end
```

Zadanie 5

1 wersja

```
total_amount = 1500;
cvx begin gp quiet
      variables r h
      minimize 2*pi()*r^2 + 2*pi()*r*h
      subject to
          pi()*r^2*h == total_amount;
cvx end
cvx_begin quiet
      {\tt variables} \ {\tt logr} \ {\tt logh}
     \label{eq:minimize} \mbox{minimize (2*pi()*exp(logr)^2+2*pi()*exp(logr)*exp(logh))}
      subject t
          log(pi()*exp(logr)^2*exp(logh)) == log(total_amount)
cvx_end
proba = 5;
cvx_gp(proba,1) = r;
cvx_gp(proba, 2) = h;
cvx_log(proba,1) = exp(logr);
cvx_log(proba,2) = exp(logh);
 \text{if } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 1)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 1))) \text{ && } (\texttt{round}(\texttt{cvx\_gp}(\texttt{proba}, 2)) = \texttt{round}(\texttt{cvx\_log}(\texttt{proba}, 2))) \\ \end{aligned} 
      WynikiZgodne(proba) = string('Tak');
     WynikiZgodne(proba) = string('Nie');
end
```

cvx begin gp quiet variables h % maximize(140*h-48*h^2+4*h^3) maximize(140*h-0-96*h+12*h^2) subject to % h >= 0 % h <= 5 % 140-96*h+12*h^2 <= 0 24*h-96 == 0 cvx end h

Zadanie 7

```
surface = 200;
cvx begin gp quiet
    variables w
    maximize( 207-3.5*w-400/w )
    subject to
  w*h == surface
       w >= 2;
        w \le 200/3.5
cvx_end
% 2 sposób
surface = 200;
cvx begin quiet
    variables logw logh
    maximize( 207-3.5*exp(logw)-400/exp(logw) )
    subject t
        logw+logh == log(surface)
       logw >= log(2);
        logw <= log(200/3.5)
cvx_end
proba = 7;
cvx_gp(proba,1) = w;
cvx_gp(proba, 2) = h;
cvx_log(proba,1) = exp(logw);
cvx_log(proba, 2) = exp(logh);
if (round(cvx_gp(proba,1)) == round(cvx_log(proba,1))) && (round(cvx_gp(proba,2)) == round(cvx_log(proba,2)))
    WynikiZgodne(proba) = string('Tak');
else
    WynikiZgodne(proba) = string('Nie');
end
```


cvx_begin gp quiet variables r h maximize(12-(4+pi)*r) %12*r - (2 + 0.5 * pi)*r^2) subject to % 2*h+2*r+pi*r 12 r=0 r<=12/(2+pi) cvx_end r h


```
cvx_begin quiet
     variables 1
    maximize( 256*v-16*v*v )
     subject to
cvx_end
cvx begin quiet
     variables logu logv
       maximize (256*exp(logv)-16*exp(logv)*exp(logv))
    minimize (16*(exp(logu) + exp(logv)))
     subject t
         log(exp(logu) + exp(logv)) \le log(16)
cvx_end
proba = 9;
cvx_gp(proba, 1) = u;
cvx_gp(proba, 2) = v;
cvx_log(proba, 1) = exp(u);
cvx_log(proba,2) = exp(v);
 \text{if } (\texttt{round}(\texttt{cvx}\_\texttt{gp}(\texttt{proba},1)) \ = \ \texttt{round}(\texttt{cvx}\_\texttt{log}(\texttt{proba},2))) \ \&\& \ (\texttt{round}(\texttt{cvx}\_\texttt{gp}(\texttt{proba},2)) \ = \ \texttt{round}(\texttt{cvx}\_\texttt{log}(\texttt{proba},2))) \\ \end{aligned} 
    WynikiZgodne(proba) = string('Tak');
     WynikiZgodne(proba) = string('Nie');
end
% cvx begin qp
       variables x y
       maximize x*y
       subject to
            2*x + y <= total_len;
% cvx_end
% cvx_begin
       variables logx logy
       maximize(logx + logy)
       subject to
            log(2*exp(logx) + exp(logy)) <= log(total len);</pre>
% cvx_end
```


cvx_begin gp quiet variables x y minimize sqrt($y^2 - 3^*y + 3$) % minimize($x^2 + (y-2)^2$) subject to $2^*y - 3 == 0$; % $y >= x^2 + 1$ cvx_end x y

 $cvx_begin gp quiet variables x minimize(<math>sqrt(x^2 + 9)$) subject to $x/(6*sqrt(x^2 + 9))-1/8 == 0 cvx_end$

proba = 4; cvx_gp(proba,1) = x; cvx_gp(proba,2) = NaN;

cvx_log(proba,1) = NaN; cvx_log(proba,2) = NaN;

 $if \ (round(cvx_gp(proba,1)) == round(cvx_log(proba,1))) \ WynikiZgodne(proba) = string('Tak'); \ else \ WynikiZgodne(proba) = string('Nie'); \ end \ which is the property of the property$

```
NrZadania = {'Zadanie 1';'Zadanie 2';'Zadanie 3';'Zadanie 4';'Zadanie 5';'Zadanie 6';'Zadanie 7';'Zadanie 8';'Zadanie 9';'Zadanie 10';'Zadanie 11'};

T = table(cvx_gp,cvx_log,WynikiZgodne,'RowNames',NrZadania)
```

T =

		cvx_gp		CVX	_log	WynikiZgodne
Zadanie	1	600	1200	600	1200	"Tak"
Zadanie	2	250	125	250	125	"Tak"
Zadanie	3	1.8821	4.7051	1.8821	4.705	"Tak"
Zadanie	4	1.291	1.2909	1.291	1.2909	"Tak"
Zadanie	5	6.2036	12.407	6.2036	12.407	"Tak"
Zadanie	6	0	0	0	0	""
Zadanie	7	10.69	18.708	10.69	18.708	"Tak"
Zadanie	8	0	0	0	0	""
Zadanie	9	8	8	2981.1	2980.8	"Nie"
Zadanie	10	0	0	0	0	11 11
Zadanie	11	0	0	0	0	""

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