Oksendal 3.3

E) Example of stochastic process X+ satisfying

[E[X+]=E[X6] for all +2,0

and which is not a martinagle w.r.t. its own piltration.

Take Y+ with $Y_0=0$ and Y=0 uniform Y=0 independent from Y+. Then, Y=0 Y=0 Y=0 Y=0 Y=0

However,

E[UY+150]= E[U(Y++Y5-Y5)]50]

= E[U(Y+-Y6)]50]+ E[UY5]50]

= E[U[56]. E[Y+-Y5]56]+ E[UY5]55]

= Y6 E[U[56] = 0