**4.6.** a) For 
$$c, \alpha$$
 constants,  $B_t \in \mathbf{R}$  define

$$X_t = e^{ct + \alpha B_t} \ .$$

$$dX_t = (c + \frac{1}{2}\alpha^2)X_t dt + \alpha X_t dB_t .$$

$$\therefore dX_{+} = (c + \alpha^{2}) X_{+} dA_{+} \propto X_{+} dB_{+}$$

b) For  $c, \alpha_1, \dots, \alpha_n$  constants,  $B_t = (B_1(t), \dots, B_n(t)) \in \mathbf{R}^n$  define

$$X_t = \exp\left(ct + \sum_{j=1}^n \alpha_j B_j(t)\right).$$

Prove that

$$dX_t = \left(c + \frac{1}{2} \sum_{j=1}^n \alpha_j^2\right) X_t dt + X_t \left(\sum_{j=1}^n \alpha_j dB_j\right).$$

By the multidimensional Hos formula, let g(+, x) = ettex

and

Hance,

$$dX_{+} = \left(c + \frac{1}{2} \sum_{j=1}^{n} \alpha_{j}^{2}\right) X_{+} dt + X_{+} \left(\sum_{j=1}^{n} \alpha_{j} d\beta_{j}\right)$$