- **3.12.** As in Exercise 3.9 we let $\circ dB_t$ denote Stratonovich differentials.
 - (i) Use (3.3.6) to transform the following Stratonovich differential equations into Itô differential equations:

(a)
$$dX_t = \gamma X_t dt + \alpha X_t \circ dB_t$$

(b)
$$dX_t = \sin X_t \cos X_t dt + (t^2 + \cos X_t) \circ dB_t$$

(ii) Transform the following Itô differential equations into Stratonovich differential equations:

(a)
$$dX_t = rX_t dt + \alpha X_t dB_t$$

(b)
$$dX_t = 2e^{-X_t}dt + X_t^2dB_t$$

$$X_{t} = X_{0} + \int_{0}^{t} b(s, X_{s})ds + \frac{1}{2} \int_{0}^{t} \sigma'(s, X_{s})\sigma(s, X_{s})ds + \int_{0}^{t} \sigma(s, X_{s})dB_{s}, \quad (3.3.6)$$

i.a.,
$$dX_t = b(t, x)dt + L \tau'(t, x) \tau(t, x) ds + \tau(t, x) dB_t$$

$$2$$

$$dX_t = \delta X_t dt + L \alpha^2 X_t dt + \alpha X_t dB_t$$

$$\tau(t, x) = \alpha X_t dB_t$$

$$\tau'(t, x) = \alpha X_t dB_t$$

i.b)
$$\sigma(t,x) = t^2 + \cos x$$

$$\times$$
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