**4.15.** Let x > 0 be a constant and define

$$X_t = (x^{1/3} + \frac{1}{3}B_t)^3$$
;  $t \ge 0$ .

Show that

$$dX_t = \frac{1}{3}X_t^{1/3}dt + X_t^{2/3}dB_t$$
;  $X_0 = x$ .

Let 
$$g(t,y) = \left(x^{1/3} + \frac{1}{3}y\right)^3$$
 and compute

• 
$$\frac{\partial}{\partial y} = 3\left(x^{1/3} + \frac{1}{3}y\right)^{2} \cdot \frac{1}{3} = \left(x^{1/3} + \frac{1}{3}y\right)^{3 \cdot \frac{2}{3}}$$

$$\frac{2a}{3} = 2\left(x^{1/3} + \frac{1}{3}y\right) \cdot \frac{1}{3} = \frac{2}{3}\left(x^{1/3} + \frac{1}{3}y\right)^{3.1}$$

$$dX_{+} = \left(x^{1/3} + \frac{1}{3}y\right)^{3 \cdot \frac{2}{3}} dB_{+} + \frac{1}{2} \frac{2}{3} \left(x^{1/3} + \frac{1}{3}y\right)^{3 \cdot \frac{1}{3}} dA_{+}$$

$$= X_{+}^{2/3} dB_{+} + 1 X_{+}^{1/3} d+$$