```
Oksendal 3.4
 i) X+ = B+ + 4+
    1. X+ 15 Fi-measurable for all + since B+ 15.
    2. E[[X+]] = E[B++4+1] < E[1B+]+E[14+1] < 00
since B+ is a martinagle and 14H is a constant.
    3. E[X+150]= X5, 5=+
      Notice that
         E[B++4+ | F6] = B5+4+ $ 1. Not a motragle
in Xt= Bt B2(1)= Juesi3 (w) (w) {= Ft
   1. X+ 15 Ft-measurable
   2. E[IX+1] = E[B] may not be finite
3. E[X+1F5] = X5 55+
      E[B][F6] = E[(B+-B6+B5)][F6]
  = E[(B+-B6)2/J=6]+2E[(B+-B6)B6/J=6]+E[B32/J=6]
  = 1-5+B62 + B5 (6<+)
                                      .. Not a mortuagle
111) Xx= +2B+ - 2 / 5B5 ds
   J. X+ 15 F+-meoardole.
2. E[IX+1] ≤ E[I+2B+1] + 2E[J+5B5d5] < ∞
   3 E[X+156] = E | +2B+-2 | +5B526 | 56
 = +2Bs-2 (5 sBsds-2E [ + rBrdr | Js
 - +2Bs - 2 | 3 3Bsds - 2 | + r E [Br | Fs] ds
 - 12B5-2 /5 sB5d5 - 2/1 rB5d5
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= +2B3-215 sB5d5-B5(+2-52)=52B5-215 sB5d5

: ls a mortingale

(1V.) X+=B,(4)B2(1) where (B,(4), B2(4)) 15 or 2-dim 3m.

- 1. Xt is Ft-measurable since Bilth and Balth is
- 2. E[1X+1]= E[1B1(4)1]. E[1B2(4)1] < 00
- 3. E[X+1F5]= B1(5).B2(5)= X5, 55+

i. Is a mortingale