# A Predictive Model for Co-op / Condo Sales in Queens, New York

Final project for Math 342W Data Science at Queens College 5/25/2022

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#### Abstract

New York City remains one of the most desirable places to live in the United States. Access to high quality public education, robust public transit, top tier medical care and a wide range of employment opportunities continue to drive demand for homes in the five boroughs. Using data harvested from Zillow.com via Amazon's Mechanical Turk we will construct a predictive model for condo and co-op sale prices in mainland Queens as a first step towards modeling real estate sale prices across the entire city.

#### 1 Introduction

The specific problem being addressed by this project is as follows: can we accurately predict how much a co-op or condominium in main land Queens will sell for? Our phenomena of interest is the real estate market for condos and co-ops constrained to be within the above geographical region. The response value, typically denoted y, is the selling price of the real estate properties of interest and is a continuous value. We assumed stationarity at the outset, and employed four separate algorithms:  $\mathcal{A}_{\text{OLS}}$ ,  $\mathcal{A}_{\text{Step-OLS}}$ ,  $\mathcal{A}_{\text{CART}}$ ,  $\mathcal{A}_{\text{RandomForest}}$  to generated different models in an effort to accurately predict the response. Ultimately the Random Forest model built off an expanded set of features yielded the best results.

#### 2 The Data

The bulk of the training data was gathered from Zillow.com through Amazon's MTurk system. The original data frame consisted of 2230 individual observations across 56 distinct columns. Our population of interest is defined to be all condo and co-op's across mainland Queens and this data set appears to be fairly representative of that population.

Approximately 50 percent of the sale prices present were between \$175,000—\$435,250. There were outliers at both the top and bottom ends, specifically a Glen Oaks co-op which sold for \$999,999 and a co-op in Lindenwood which sold for \$55,000. We supplemented the original data set with additional information from the Google Places and Google Geocode API's as well as from the NYC historical crime data repository (via NYC open data).

Extrapolation is a possibility with our current model setup. New condo and co-ops are being constructed all the time, it is plausible that in the future newer properties will come up for sale with feature measurements outside those in the range of those in our training data. For example, provided real estate trends continue to trend upwards, it would not be difficult to see listing prices exceed the historical data or to have maintenance costs rise beyond the range of those the model was trained on.

#### 2.1 Featurization

After removing the junk columns associated with MTurk, a total of 26 features remained on 2230 observations in the original data set. A list of those features with basic summary statistics is below in Figure 1. We believe the names are self explanatory.

Data Summary												
	Values											
Name	housing_	data										
Number of rows	2230											
Number of columns	26											
Key	NULL											
Column type frequency:												
character	16											
numeric	10											
Group variables	None											
Variable type: characte	er											
skim variable	n i	nissing	comple	te_rate	min	max e	empty	n unio	que w	hites	pace	
1 cats allowed	_	0		1	1		0		3		0	
2 common_charges		1684		0.245	4	7	0		258		0	
3 coop_condo		0		1	5	5	0		2		0	
4 date_of_sale		1702		0.237	8		0		222		0	
5 dining room type		448		0.799	4		0		5		0	
6 dogs allowed		0		1	2		0		3		0	
7 fuel type		112		0.950	3		0		6		0	
8 full address or zip co	de	0		1	5		0	11	177		0	
9 garage exists		1826		0.181	1		0	_	6		0	
10 kitchen type		16		0.993	4		0		13		0	
11 maintenance_cost		623		0.721	5		0		509		0	
12 model type		40		0.982		-	0		B75		0	
13 parking_charges		1671		0.251			ø		89		0	
14 sale price		1702		0.237	8		0		315		0	
15 total taxes		1646		0.262	4	_	0		293		0	
15 total_taxes 16 listing price to neare:	+ 1000	534		0.761	4		9		292		0	
To IIsting_price_to_neare:	st_1000	334		0.761	4	,			232		0	
Variable type: numeric												
skim_variable	n_missing	comple	te_rate	mea	an	50	d p0	p25	p50	p75	p100	
1 approx year built	40		0.982	1963.		21.1		1950				
2 community_district_num	19		0.991	26.3		2.95	3	25	26	28	32	
3 num bedrooms	115		0.948	1.69	5	0.744	1 0	1	2	2	6	
4 num floors in building	650		0.709	7.79		7.52	1					
5 num_full_bathrooms	0		1	1.2		0.445			1			
6 num_half_bathrooms	2058		0.0771	0.95		0.302			1			
7 num_total_rooms	2		0.999	4.14		1.35	0	3	4	_		
8 pct_tax_deductibl	1754		0.213	45.4		6.95	20		50			
9 sq_footage	1210		0.457	955.	-	81.	100	743		1100		
10 walk score	1210		1	83.9		14.7	7	77	89	95		
TO MUTY PCOLG	0		1	05.9		14./	/	//	09	95	99	

Figure 1

The feature **model type** was dropped as it contained useless inconsistent information, while **num half bathrooms** was also dropped due to a high level of missingness with approximately 93% of the values missing. A total of 16 of the original 26 features were encoded as character type and needed to be converted to either numeric or factor with the appropriate levels. Several of the factor variables had duplicated levels which needed to be combined, for example **dogs allowed** had levels: "no", "yes", "yes89". Discrepancies like this were addressed during the cleaning process using common sense.

The feature **full address or zip code** represented something of a challenge at the outset as it was a character string with no consistent formatting. We coded a simple function to extract the zip code to create a new feature **zip-codes**. In addition the full address string was fed through the Google Geocode API to create both features **lat** and **lon** which represented the latitude and longitude coordinates of each real estate property. After **zipcodes**, **lat** and **lon** were gathered **full address or zip code** was dropped as we now had numeric representations for location to be used later. The result of these data cleaning procedures can be seen below.

```
-- Data Summary -----
                                    Values
                                    housing_data
Number of columns
                                    NULL
Column type frequency:
   factor
                                    17
   numeric
Group variables
                                    None
-- Variable type: factor
  skim_variable
                         n_missing complete_rate ordered n_unique top_counts
                                                                             2 no: 1402, yes: 828
2 co-: 1661, con: 569
1 cats_allowed
2 coop condo
                                                         FALSE
                                                                            2 co: 1661, con: 569
5 com: 957, for: 620, oth: 201, din: 2
2 no: 1684, yes: 546
5 gas: 1348, oil: 664, ele: 62, oth: 41
2 NA: 1826, yes: 404
4 eat: 942, eff: 849, com: 399, non: 23
  dining_room_type
                                                 0.799 FALSE
4 dogs allowed
                                                         FALSE
5 fuel_type
6 garage_exists
                                 112
                                                 0.950 FALSE
7 kitchen_type
                                                 0.992 FALSE
                                  17
-- Variable type: numeric
                                            n_missing complete_rate
40 0.982
    skim_variable
                                                                                                                  p25
1950
   approx_year_built
                                                                                                                             1958
                                                                                                                                      1970
                                                                                                                                                   2017
 2 common_charges
3 community_district_num
                                                  1684
                                                                    0.245
                                                                                442
                                                                                             262.
                                                                                                           70
                                                                                                                   280
                                                                                                                              390
                                                                                                                                       552.
                                                                                                                                                   2499
                                                                                                                16947
 4 date of sale
                                                  1702
                                                                    0.237
                                                                             17035.
                                                                                             104.
                                                                                                        16847
                                                                                                                            17033
                                                                                                                                     17127
                                                                                                                                                 17212
                                                                    0.721
                                                                                                0.744
 6 num bedrooms
                                                    115
                                                                    0.948
 7 num_floors_in_building
8 num_full_bathrooms
                                                                    0.709
                                                                                                7 52
                                                                                                0.445
9 num_total_rooms
10 parking_charges
                                                                    0.999
                                                                                  4.14
                                                                                                1.35
                                                  1671
11 pct_tax_deductibl
12 sale_price
13 sq_footage
14 total_taxes
                                                  1754
                                                                    0.213
                                                                                 45.4
                                                                                                6.95
                                                                                                            20
                                                                                                                     40
                                                                                                                                50
                                                                                                                                         50
                                                                                                                                                     75
                                                                    0.237 314957.
                                                                                                        55000 171500
                                                                                                                                   428875
                                                                    0.457
                                                   1210
                                                                                955.
                                                                                             381.
                                                                                                          100
                                                                                                                   743
                                                                                                                              881
                                                                                                                                      1100
                                                                                                                                                  6215
                                                                    0.262
                                                                              2226
                                                                                            1850
                                                                                                                   281
                                                                                                                             2411
                                                                                                                                      3500
15 walk_score
                                                                                 83.9
                                                                                              14.7
                                                                                                                               89
16 listing_price_to_nearest_1000
17 zipcodes
                                                    534
                                                                    0.761 385641.
                                                                                         200258
                                                                                                        65000 229750
                                                                                                                          329500 525000
                                                                                                                                              1000000
                                                                             11353.
                                                                                              90.2
                                                                                                                11358
                                                                                                                                    11375
```

Figure 2

With the latitude and longitude available we employed the Google Places API to obtain data regarding the number of Long Island Rail Road train stations and number of liquor stores within a 1 mile radius of each property. In addition the Google Places API was used to assign the appropriate NYPD precinct number to each observation. These features were eventually added to the data set as **num train**, **num liq** and **prec num** respectively. Finally we accessed historical crime data by police precinct, through the New York City Open Data website. By downloading a csv of historical crime reports we were able to filter to the 2016-2017 time period and borough of Queens to get the total number of reported crimes by precinct number. This was ultimately joined with the cleaned historical data frame in the form of the final added feature **num crimes**.

#### 2.2 Errors and Missingness

Errors associated with the data were primarily limited to duplicate factor levels (probably as a result of data entry error) as previously explained in the **dogs** allowed example in subsection 2.1. There were also 6 features encoded as character which needed to be converted to numeric via the parse number function. Specifics can be seen in the attached code appendix lines 36 - 94.

Missingness represented a significant issue, as can be seen in Figure 3. To remedy this problem we first created a missingness matrix denoted M of dummy variables, to track all observations with missing measurements and their locations. We then employed the missForest package to impute the missing values. Ultimately the matrix M was not used during construction of the final models as it did not seem to result in improved performance.

	Value	S		
Name	housi	ng data		
Number of rows	2230	0_		
Number of columns	24			
Key	NULL			
Column type frequency:	=			
factor	7			
numeric	17			
Group variables	None			
Variable type: fact	tor			
skim variable n n	missing com	nlete rate		
1 cats_allowed	0	1		
2 coop_condo	0	1		
3 dining_room_type	448	0.799		
4 dogs_allowed	0	1		
5 fuel_type	112	0.950		
6 garage_exists	0	1		
7 kitchen_type	17	0.992		
Variable type: nume	eric			
		n missing	complete_rate	
skim_variable				
1 approx_year_built		40	0.982	
1 approx_year_built 2 common_charges		40 1684	0.245	
1 approx_year_built 2 common_charges 3 community_district	_num	40 1684 19	0.245 0.991	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale	_num	40 1684 19 1702	0.245 0.991 0.237	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost	_num	1684 19 1702 623	0.245 0.991 0.237 0.721	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms		1684 19 1702 623 115	0.245 0.991 0.237 0.721 0.948	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build		1684 19 1702 623 115 650	0.245 0.991 0.237 0.721 0.948 0.709	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build 8 num_full_bathrooms		40 1684 19 1702 623 115 650	0.245 0.991 0.237 0.721 0.948 0.709	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_buil 8 num_full_bathrooms 9 num_total_rooms		40 1684 19 1702 623 115 650 0	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999	
1 approx_year_built 2 common_charges 3 community_district_4 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges		40 1684 19 1702 623 115 650 0 2	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999	
1 approx_year_built 2 common_charges 3 community_district, 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges 11 pct_tax_deductibl		40 1684 19 1702 623 115 650 0 2 1671 1754	0.245 0.991 0.237 0.721 0.948 0.709 1 0.999 0.251	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_built 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges 11 pct_tax_deductibl 1 sale_price		- 40 1684 19 1702 623 115 650 0 2 1671 1754	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999 0.251 0.213	
1 approx_year_built 2 common_charges 3 community_district, 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build 8 num_full_bathrooms 9 num total_rooms 10 parking_charges 11 pct_tax_deductibl 12 sale_price 13 sq_footage		- 40 1684 19 1702 623 115 650 0 2 1671 1754 1702	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999 0.251 0.213 0.237	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_built 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges 11 parking_charges 12 sale_price 13 sq_footage 14 total_taxes		- 40 1684 19 1702 623 115 650 0 2 1671 1754 1702 1210	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999 0.251 0.213 0.237 0.457	
1 approx year built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_build 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges 11 pct_tax_deductibl 12 sale_price 13 sq_footage 14 total_taxes 15 walk score	ding	1684 199 1702 623 115 650 0 2 1671 1754 1702 1210 1646	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999 0.251 0.213 0.237 0.457 0.262	
1 approx_year_built 2 common_charges 3 community_district 4 date_of_sale 5 maintenance_cost 6 num_bedrooms 7 num_floors_in_built 8 num_full_bathrooms 9 num_total_rooms 10 parking_charges 11 parking_charges 12 sale_price 13 sq_footage 14 total_taxes	ding	1684 199 1702 623 115 650 0 2 1671 1754 1702 1210 1646	0.245 0.991 0.237 0.721 0.948 0.709 1   0.999 0.251 0.213 0.237 0.457	

Figure 3

After the imputation process was completed rows 1-529 were taken as these were the only observations from the original data set which included actual sale prices (i.e. not those which were imputed by missForest). Our additional features described above in 2.1 were also attached to create  $\mathbb{D}$ , summarized below in figure 4.

Data Summary										
	Values									
Name	Dat									
Number of rows	529									
Number of columns	29									
Column type frequency:										
factor	7									
numeric	22									
Group variables	None									
Variable type: factor										
skim variable n miss:				top counts						
cats_allowed	0	1 FALSE	2	no: 286, yes	: 243					
coop_condo	0	1 FALSE	2	co-: 399, co	n: 130					
dining_room_type	0	1 FALSE		com: 333, fo		oth: 54, d	din: 2			
dogs_allowed	0	1 FALSE	2	no: 382, yes	: 147					
fuel type	0	1 FALSE	5	gas: 321, oi	1: 185,	ele: 11, d	oth: 9			
garage_exists	0	1 FALSE	2	NA: 434, yes	: 95					
kitchen_type	0	1 FALSE	3	eff: 233, ea	t: 213,	com: 83, r	non: 0			
Variable type: numeric										
	n_missing co		mean			p25	p50			
1 prec_num	0			2.23	103	109	109	109	115	
2 approx_year_built	0		1962.	20.5	1915	1950	1957.	1968	2016	
3 common_charges	0		560.	190.	70	426	563.	695.	1135.	
4 community_district_num		1		2.98	3	25	26	28	30	
5 date_of_sale	0		17035.	104.	16847	16947	17035	17127	17212	
6 maintenance_cost	0		808.	358.	155	612	724	885	4659	
7 num_bedrooms	0	1		0.748	0	1	1	2	3	
<pre>8 num_floors_in_building</pre>		1		6.26	1	3	6	7	34	
9 num_full_bathrooms	0	1		0.423		1	1	1	3	
0 num_total_rooms	0	1		1.20	1	3	4	5	8	
1 parking_charges	0	1		54.2	9	68.6	106.	141.	500	
.2 pct_tax_deductibl	0	1	43.5	6.57	20	38.6	45	49.5		
3 saie_price	0	1	315504.	179797.	55000	172000	260000	430000	999999	
			897.			706.	260000 826.	998	6215	
4 sq_footage 5 total_taxes	0 0	1 1 1	897. 2458.	179797. 361. 1189.	55000 375 11	706. 1806.	826. 2464.	998 3132.	6215 9300	
4 sq_footage 5 total_taxes	0	1	897.	179797. 361. 1189. 13.1	55000 375	706.	826.	998 3132. 94	6215	
4 sq_footage 5 total_taxes 6 walk_score	0 0	1 1 1	897. 2458.	179797. 361. 1189.	55000 375 11	706. 1806.	826. 2464.	998 3132.	6215 9300	
4 sq_footage 5 total_taxes 6 walk_score 7 zipcodes 8 lat	0 0 0 0	1 1 1 1 1	897. 2458. 83.1 11356. 40.7	179797. 361. 1189. 13.1 86.2 0.0299	55000 375 11 15 11004 40.7	706. 1806. 76 11360 40.7	826. 2464. 85 11368 40.7	998 3132. 94 11375 40.8	6215 9300 99 11435 40.8	
4 sq_footage 5 total_taxes 6 walk_score 7 zipcodes 8 lat	0 0 0 0	1 1 1 1	897. 2458. 83.1 11356.	179797. 361. 1189. 13.1 86.2	55000 375 11 15 11004 40.7	706. 1806. 76 11360	826. 2464. 85 11368 40.7	998 3132. 94 11375	6215 9300 99 11435 40.8	
4 sq_footage 5 total_taxes 6 walk_score 7 zipcodes 8 lat 9 lon	0 0 0 0	1 1 1 1 1 1 1 1	897. 2458. 83.1 11356. 40.7 -73.8 0.711	179797. 361. 1189. 13.1 86.2 0.0299 0.0533	55000 375 11 15 11004 40.7 -74.0	706. 1806. 76 11360 40.7 -73.9	826. 2464. 85 11368 40.7 -73.8	998 3132. 94 11375 40.8	6215 9300 99 11435 40.8 -73.7	
13 sale_price 14 sq_footage 15 total_taxes 16 walk_score 17 zipcodes 18 lat 19 lon 20 num_train 21 num_liq 22 num_crimes	0 0 0 0 0	1 1 1 1 1 1	897. 2458. 83.1 11356. 40.7 -73.8 0.711 14.2	179797. 361. 1189. 13.1 86.2 0.0299 0.0533	55000 375 11 15 11004 40.7 -74.0	706. 1806. 76 11360 40.7 -73.9	826. 2464. 85 11368 40.7 -73.8	998 3132. 94 11375 40.8 -73.8	6215 9300 99 11435 40.8 -73.7	

Figure 4

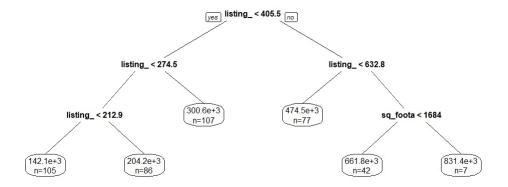
## 3 Modeling

To construct our predictive models,  $\mathbb{D}$  was partitioned into  $\mathbb{D}_{train}$  and a hold out set  $\mathbb{D}_{test}$  with approximately 20% of the observations allocated at random to the hold out. Using this split on  $\mathbb{D}$  we constructed several models.

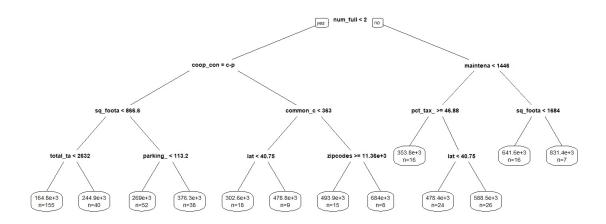
First, we explored regression trees, constructed using the R package rpart and all of  $\mathbb{D}_{train}$  and a subsection of  $\mathbb{D}_{train}$ . We then moved on to OLS based solutions and built several linear models using the lm package. Finally a random forest model was also fit on all of  $\mathbb{D}_{train}$  using the R package randomForest.

#### 3.1 Regression Tree Modeling

The initial regression tree model found the most important features to be: listing price to nearest 1000 and sq footage. An image of the tree is included below.



This result is somewhat strange. Given the number of features existing in training data one would expect more than the listing price and square footage to be a driving factor in predicting the sale price. On the other hand it makes sense that knowing the listing price can be useful in predicting the ultimate selling price as the two quantities should be relatively close in value. When the tree model is fit on all features except the listing price we obtain the following:



This is much closer to expectations. When the listing price feature is excluded, the CART algorithm finds that 12 different features are needed vs. only the two used in the initial tree. We have a hypothesis for why this is the case.

Going back to the original housing data set, all 500+ observations which had an actual selling price (those which actually made it to the training data set) where missing the listing price for whatever reason. This means that the listing price feature in our  $\mathbb D$  is an imputed value across all 529 observations. We believe that the imputed listing price actually encodes the predictive information contained in other features in some way, which is why the CART algorithm finds it to be the only necessary feature in the initial build. By imputing the listing price we were in effect predicting what the selling price should be in an indirect way. This may explain why the CART algorithm found just that feature (along with square footage) as necessary when looking for splits. As such, our selected tree model, will be the one fit to the entire data set excluding the listing price feature.

#### 3.2 Linear Modeling

First, the linear model using only **listing price to nearest 1000** and **sq footage** as predictors was fit. The coefficients for each feature are as follows:

One can interpret the coefficient on square footage as: given the feature measurements on two properties with the exact same listing price, assuming the linear model accurately represents the relationship between selling price and included features, then a unit increase in square footage will result in a average change in predicted selling price by approximately 11 dollars and 4 cents. The "meaning" of the listing price coefficient is similar however square footage is assumed to be measured the same and the average unit change in prediction would be around 1006 dollars.

Second, a linear model was fit using the features in the second regression tree given by:

```
lm(formula = sale_price ~ num_full_bathrooms + coop_condo + maintenance_cost +
    sq_footage + common_charges + pct_tax_deductib1 + total_taxes +
parking_charges + lat + zipcodes, data = D_train)
Coefficients:
       (Intercept) num_full_bathrooms
                                                coop_condocondo
                                                                      maintenance cost
         -3.123e+07
                                7.827e+04
                                                       2.018e+05
                                                                             1.056e+02
                                                                                                     3.955e+01
    common_charges pct_tax_deductibl
                                                     total taxes
                                                                       parking charges
                                                       1.671e+01
                                                                                                     8.176e+05
                                -6.693e+03
           zincodes
         -1.806e+02
```

A third OLS model, was fit using a step-wise algorithm to determine feature selection. The predictors used and coefficients found are summarized in the below image:

```
lm(formula = sale_price ~ listing_price_to_nearest_1000 + common_charges +
date_of_sale + zipcodes + maintenance_cost + total_taxes +
     approx_year_built + prec_num + dogs_allowed + num_train +
     sq footage + walk score + num full bathrooms, data = D train)
Coefficients:
                     (Intercept) listing_price_to_nearest_1000
                                                                                          common_charges
                                                            1.036e+03
                                                                                                3.761e+01
                       2.820e+06
                    date of sale
                                                             zipcodes
                                                                                        maintenance cost
                      -1.189e+02
                                                           -3.409e+01
                                                                                                2.922e+01
                                                  approx_year_built
-3.761e+02
                     total taxes
                                                                                                 prec_num
                      -8.938e+00
                                                                                                2.622e+03
                 dogs_allowedyes
                                                            num train
                       9.208e+03
                                                            3.898e+03
                                                                                                -1.182e+01
                                                 num_full_bathrooms
                      walk score
                      -2.389e+02
                                                           -
-3.186e+03
```

The forward step-wise algorithm found a different variety of features to be useful in constructing a linear model.

#### 3.3 Random Forest Modeling

Finally a random forest model was fit on  $\mathbb{D}_{\text{train}}$ . The random forest is similar to the original CART algorithm in that it is searching for the best orthogonal-to-axis splits among the available predictors, however it has two additional properties that make it superior. First it uses a randomized subset of the features to explore at each split instead of the entire set, netting a reduction in correlation. Second it constructs many trees in this way, instead of just 1 and the resulting prediction is the average result across all of them. Our random forest model is actually a collection of many regression trees.

The random forest model employed in this project used a nodesize parameter equal to 1 and the forest was composed of 2000 trees with a default mtry value (total features divided by 3). This non-parametric model had an in-sample RMSE of \$44,414. This model should be the one chosen to make predictions about the future selling price of condos and co-ops in mainland Queens.

First, it is highly unlikely that a linear relationship accurately explains the underlying relationship between the features and selling price. This rules out the constructed OLS models. Second, by intentionally overfitting (by setting node size to 1) we can take advantage of the model averaging aspect of the random forest to yield a more accurate model. Although this model averaging will lead to a reduction in "interpret-ability", that is it will be more difficult to explain how the model is generating it's predictions compared to a simpler algorithm like OLS or a single regression tree.

We believe that there are several features which are actually causal to the selling price of condos and co-ops including the number of crimes occurring in the area, taxes, whether it is a co-op or condo, size of the co-op / condo, and different costs (maintenance / common charges). These predictors consistently provided value across all the algorithms we employed. How to prove this relationship would require a more extensive validation process, probably something along the lines of nested k-fold cross-validation, further work to more scientifically

select the hyper-parameters used in the model construction (mtry, nodesize and num trees), and an expanded set of training data to work with.

# 4 Performance Results for your Random Forest Model

Below is a summary of the performance results for the Random Forest and OLS models:

Model	In-Sample RMSE	In-Sample R2	OOS RMSE	OOS R2
OLS C2	\$79,412	81%	\$69,332	84%
OLS Stepwise	\$36,906	96%	\$28,095	97%
Random Forest	\$44,414	93%	\$31,522	97%

OLS C2 refers to the linear model built on the predictors the second regression tree model (that which excluded listing price) found most meaningful:

num full bathrooms	coop condo	maintenance cost	common charges
pct tax deductibl	total taxes	parking charges	lat
zipcodes	sq footage		

OLS Stepwise refers to the linear model where the forward step-wise algorithm selected the subset of features:

listing price	common charges	maintenance cost	approx year built
date of sale	dogs allowed	prec num	walk score
zipcodes	sq footage	num full bathrooms	num train
total taxes			

Both OLS models and Random Forest performed better out of sample vs in sample, and since we assumed stationarity the results should be a good indication of how each will perform in the future. Random Forest clearly beat the OLS C2, however, OLS Stepwise performed just slightly better than Random Forest. As stated earlier we feel it is unlikely that a linear model can accurately capture the relationship between our predictors and response, but a linear model is easier to explain, even one constructed using a forward step-wise procedure. We feel this merits further investigation in the future. It is possible, since our validation process consisted only of a train and test set, that the randomization of the data into each set led to the above results. In other words a more thorough model validation might show that the step-wise model is likely better than OLS C2 but perhaps not as good as Random Forest.

#### 5 Discussion

Unfortunately our random forest model did not beat Zillow.com, below is a table comparing the performance:

Predictions within x\% of sale price

Name	Med Error	5%	10%	20%
Zillow.com	2.3%	80.2%	94.1%	98.4%
QC RF	6.0%	46.7%	70.4%	92.3%

There is clearly some room for improvement in our approach. Adding more informative features might yield better performance. For instance, information regarding the schools in the area might provide value as it is known, in general, that better schools drive up surrounding property values. Additionally, it is plausible that expanded listing / selling price histories for each property exist on the web and could have been appended to our data set. We also neglected potential feature interactions and transformations, these could easily be explored using the model matrix function in R.

Further, if we return to section Figure 3 in section 2.2, it is clear that there was a significant amount of missingness in our data set, which was resolved with the missForest package. The use of missForest is a prediction exercise itself and subject to variance and error just like our final predictive models. It is likely we could have found actual data to use to fill some the gaps, in place of trying to impute, perhaps through a web scraping type exercise.

We previously mentioned using model selection techniques to find the optimal hyper parameter settings used by random forest, this is definitely worth exploring as well. While using a more thorough cross validation procedure will give us a better handle on future predictive accuracy and allow us to expand our set of actual models to test.

Finally, the feature **listing price** is also something of a open question. We would like to understand definitively why the original CART model selected it as the only useful predictor along with square footage.

### 6 Code Appendix

```
setwd("C:/Users/Antonio/Desktop/650W/final_project")
housing_data<- read.csv("housing_data_2016_2017.csv", stringsAsFactors = FALSE)
 library (data.table)
library (data.table)
library (dplyr)
library (ggplot2)
library (randomForest)
library (rpart)
library (rpart)
library (readr)
library (readr)
library (skimr)
library (ggmap)
library (ggmap)
library (googleway)
# replace "api_key" with your API key
register_google(key = '')
  register_google(key =
#load as data.table
#10ad as data.table housing_data \( - \) data.table(housing_data) #throw out garbage columns related to MTurk housing_data \( - \) housing_data[,29:54] #review data type of each of the remaining relevant columns str(housing_data)
str (nousing_data)
skim(housing_data)
#D is going to be rows 1:529
#model_type looks like a junk column, either the data is duplicated elsewhere or not relevant so we drop it
housing_data[, model_type:=NULL]
 # maintenance_cost -> convert from $ABC to double
# maintenance_cost -> convert from $ABC to doubte # parking charges same as costs/ common charges # sale_price need to convert to double # total_taxes convert to double # listing price convert to double # convert common charges from $ABC to double housing_data[,c('common_charges','maintenance_c
                                                                                                                  'maintenance_cost', 'parking_charges', 'sale_price', 'total_taxes', 'listing_price_to_nearest_1000')] <-
# Factorize the character predictors — that have a reasonable number of unique levels.

cols <- c('cats_allowed','coop_condo', 'dining_room_type','dogs_allowed','fuel_type', 'garage_exists','kitchen_type')

housing_data[, (cols):= lapply(.SD, factor), .SDcols=cols]
#check levels
 Hereta levels (housing_data$cats_allowed) levels (housing_data$coop_condo) levels (housing_data$dining_room_type)
levels (housing_data$doming_loun_ty)
levels (housing_data$fuel_type)
levels (housing_data$fuel_type)
levels (housing_data$garage_exists)
levels (housing_data$gtitchen_type)
#some problems with the unique levels need to be cleaned up particularly: garage_exists, kitchen_type, cats_allowed, dogs_allowed housing_data$dogs_allowed = "yes89")] <- 'yes' housing_data$cats_allowed [which (housing_data$cats_allowed == "y")] <- 'yes' housing_data$fuel_type [which (housing_data$fuel_type == 'Other')] <- 'other'
 housing_data$garage_exists [which(housing_data$garage_exists ==1 | housing_data$garage_exists =='eys' | housing_data$garage_exists ==
housing\_data\$garage\_exists <- \ as.character(housing\_data\$garage\_exists) \\ housing\_data\$garage\_exists[which(is.na(housing\_data\$garage\_exists))] <- \ 'NA'
housing_data$kitchen_type[which(housing_data$kitchen_type == 1955)] <- NA
housing_data$kitchen_type[which(housing_data$kitchen_type == 'Combo')] <- 'combo'
housing_data$kitchen_type[which(housing_data$kitchen_type == 'Eat in' | housing_data$kitchen_type == 'Eat In' | housing_data$kitchen_type == 'efficiency' | housing_data$kitchen_type == 'efficiency kitchen' | housing_data$kitchen_type | efficiency kitchen' | efficiency
 \verb|housing_data[, (cols):= lapply(.SD, factor), .SDcols=cols]|
#data with date of sale housing_data$date_of_sale - as.numeric(as.Date(housing_data$date_of_sale, "%m/%d/%Y")) # if we need to convert back to date objects use as.Date(housing_data$date_of_sale,"1970-01-01")
# full_address_or_zip_code has a lot of useful information, extract just the zip code first
# extract zip code from address column vector
address <- housing_data$full_address_or_zip_code
result = substr(address, (nchar(address)+1)-18, nchar(address))
zipcodes <-parse_number(result)</pre>
\# looks like there was a problem with rows 2,600,1189,1322,1347 lets fix those now address [c(2,600,1189,1322,1347)] zipcodes [c(2,600,1189,1322,1347)] <- c(11354,11375,11375,11418,11418)
# parse_number returned some incomplete zips
probs <- which(nchar(zipcodes) < 5)</pre>
```

```
zipcodes [probs]
address [probs]
# appears to be data missing in the source file , we could try and impute or just look up the correct zipcodes and correct manually zipcodes [probs] <- c(11355,NA,11369,11372,11375,11364,11427) housing_data <- cbind (housing_data, zipcodes) rm (result,probs, address, zipcodes)
\# we can use google maps API to convert the full addresses to lat/long data (numeric) and save to a seperate csv file. I will leave t \# and will provide the csv file to prevent having to query the API every time the code is run
# housing_data$lon <- NA
# housing_data$lat <- NA
\pi # address_as_char <- as.character(housing_data$full_address_or_zip_code) #
# b <- matrix (NA, ncol=2, nrow=nrow (housing_data))
# # colnames(b) <- c('lat', 'lon')
# for (i in 1:nrow(housing_data)){
       \begin{array}{l} b \left[ i\;,2 \right] \; <- \; as.numeric \left( geocode \left( address\_as\_char \left[ \; i \; \right) \right) \left[ \; 1 \right] \right) \\ b \left[ \; i\;,1 \right] \; <- \; as.numeric \left( geocode \left( address\_as\_char \left[ \; i \; \right) \right) \left[ \; 2 \right] \right) \end{array}
# }
# write.matrix(b,file="latlong.csv")
# #Take these lines when ready to attached lat lon — wait until D_train is created and we add more features #b <— read.csv("latlong2.csv", stringsAsFactors = FALSE) #housing_data$lat <— b[,1] #housing_data$lon <— b[,2]
# High levels of missing in the data set will be dropped out right num_half_bathrooms has 93% of the rows missing housing_data<-housing_data[,num_half_bathrooms:=NULL]
# We will use the lat / lon and zipcode features in place of the full address housing_data<-housing_data[,full_address_or_zip_code:=NULL]
#write.csv(M, file='M-missing.csv')
#write.csv(X-imp, file='X-imputed.csv')
\# #number of train stations within a 1 mile radius \# num_train <- c()
# for (j in 1:529) {
       df_places <- google_places(
  location = b[j,],
  radius = 1700,
  place_type = 'train_station',
  key = key)</pre>
       num_train <- append(num_train,length(df_places$results$name))
# }
# #number of liquor stores within a 1 mile radius # num_liq <- c() #
# for (j in 1:529) {
       df_places <- google_places(
location = b[j,],
radius = 1700,
place_type = 'liquor_store',</pre>
           kev = kev)
#
#
#
# }
       num_liq <- append(num_liq,length(df_places$results$name))</pre>
\# #total fast food locations within 1 mile radius?
# ##we want to add in crime statistics gather from historic NYPD data. First we need to connect each address via lat lon to it's corresponding police precinct # police_prec <- c() # for(j in 1:529){
       df_places <- google_places(
  location = b[j,],</pre>
```

```
\begin{array}{lll} {\rm radius} & = 5000\,, \\ {\rm keyword} & = {\rm 'police \ precinct'}\,, \\ {\rm key} & = {\rm key}\,) \end{array}
             police_prec <- append(police_prec, df_places$results$name[1])
#
#
# }
# unique(police_prec)
# unique(police_prec)
# #some of the lat / lon returned police precincts outside of queens (midtown south and 75th). They are cases where south Queens boar
# which(police_prec=="Midtown Precinct South")
# which(police_prec=="New York City Police Department - 75th Precinct")
# police_prec[which(police_prec=="Midtown Precinct South")] <- 'New York City Police Department - 108th Precinct'
# police_prec[which(police_prec=="New York City Police Department - 75th Precinct")] <- 'New York City Police Department - 106th Precinct"
# #police_prec is actually a character vector, we just require the number.
# matches <- regmatches(police_prec, gregexpr("[[:digit:]]+", police_prec))
# prec_num <- as.numeric(unlist(matches))
#Create D
Dat <- X_imp[1:529,]
Dat$lat <- b[,1]
Dat$lon <- b[,2]
Dat$prec_num <- prec_num
Dat$num_train <- num_tra
                                                     num_train
Dat$num.train <- num.train
Dat$num.liq <- num.liq
#load historical crime data
#crime.dat3 <- read.csv("crime-qns.csv", stringsAsFactors = FALSE)
#left join the crime data
Dat <- merge(Dat, crime.dat3, by = "prec_num", all.x = TRUE)
Dat$listing_price_to_nearest_1000 <- Dat$listing_price_to_nearest_1000 / 1000
 #save to D to csv
#write.csv(Dat, file='D_final.csv')
 #Create D_train and hold-out set
 n <- nrow(Dat)
K <- 5
 test_indices \leftarrow sample (1:n, 1 / K * n)
train_indices \leftarrow setdiff (1:n, test_indices)
D_train <- Dat[train_indices , ]
y_train <- Dat[train_indices , "sale_price"]
 D_test <- Dat[test_indices, ]
y_test <- Dat[test_indices,"sale_price"]
D_test$sale_price <- NULL
#dim (D_train)
#dim (D_test)
 #length(y_train)
#length(y_test)
 #fit the different models
 #build tree mod
\label{eq:bound} \begin{tabular}{ll} \# build & tree_mod1 <- & rpart(sale_price & $\tilde{\ }$. & , & data=D_train , & method = 'anova') \\ \# summary(tree_mod) & \# printcp(tree_mod) \\ \# rsq . rpart(tree_mod) & \# prp(tree_mod1 , & digits = 4 , & extra = 1) \\ \end{tabular}
 #check on the hold out
#check on the hold out
yhat_oos <- predict(tree_mod1, D_test)
tree_oos_residuals <- y_test - yhat_oos
tree_rsq <- 1 - sum(tree_oos_residuals^2) / sum((y_test - mean(y_test))^2)
tree_rmse <- sd(tree_oos_residuals)
tree_med <- median(abs((y_test - yhat_oos)/y_test))</pre>
\label{eq:build tree without listing tree_mod2} $$ \text{tree_mod2} < - \text{rpart}(\text{sale_price }^-., \text{ data=D_train}[,-24], \text{ method } = \text{'anova'}) $$ \text{yhat\_oos} < - \text{ predict}(\text{tree\_mod2}, \text{ D_test}) $$ \text{tree2\_oos\_residuals} < - \text{ y-test } - \text{ yhat\_oos} $$ \text{tree2\_rsq} < -1 - \text{sum}(\text{tree2\_oos\_residuals}^2) / \text{sum}((\text{y\_test} - \text{mean}(\text{y\_test}))^2) $$ \text{tree2\_rmse} < - \text{sd}(\text{tree2\_oos\_residuals}) $$ \text{tree2\_med} < - \text{ median}(\text{abs}((\text{y\_test} - \text{yhat\_oos})/\text{y\_test})) $$ \text{\#prp}(\text{tree\_mod2}, \text{ digits} = 4, \text{ extra} = 1) $$
 #stock linear model based on CART1
 ## linear_mod_cart1 <- lm(formula = sale_price ~ listing_price_to_nearest_1000 + sq_footage, data = D_train) summary(linear_mod_cart1)$sigma summary(linear_mod_cart1)$r.squared
#how well does it do on the hold out?
yhat_oos <- predict(linear_mod_cart1, D_test)
lmc1_oos_residuals <- y_test - yhat_oos</pre>
```

```
lmc1\_rsq <-\ 1 \ -\ sum(lmc1\_oos\_residuals^2) \ /\ sum((y\_test \ -\ mean(y\_test))^2)
lmc1_rmse <-sd(lmc1_oos_residuals)
lmc1_med <- median(abs((y_test - yhat_oos)/y_test))</pre>
#linear model based on CART2
linear_mod_cart2 <- lm(formula = sale_price ~ num_full_bathrooms +
coop_condo + maintenance_cost + sq_footage +
common_charges + pct_tax_deductibl + total_taxes + parking_charges + lat + zipcodes, data = D_train)
summary(linear_mod_cart2)$sigma
summary(linear_mod_cart2)$r.squared</pre>
#use forward step-wise to do feature selection for lm
# fitall <- lm(sale-price ~ ., data=D_train)
# fit_start <- lm(sale_price ~ 1 , data=D_train)
# step(fit_start , direction='forward', scope=formula(fitall))</pre>
# median percent error
# median
tree_med
tree2_med
lmc1_med
_{\rm lmc2\_med}
linear_med
rf_med
# OUT OF SAMPLE RMSE
tree_rmse
tree2_rmse
lmc1 rmse
lmc2_rmse
linear_rmse
rf_rmse
```