You can think of a normal inverse gamma as first sampling from an InverseGamma((n-1)/2, (n-1)s^2/2) to get a sigsor and then you use that value of sigsq to draw a theta from N(xbar, sigsq/n) and return the two-dimensional point [then
$$\theta$$
) θ θ θ θ θ θ θ

Norm Inv Gamma $(\cdot,\cdot,\cdot)=N(\mathbb{X},\frac{\sigma^n}{n})$ · Invham $(\frac{1-1}{2},\frac{G-D_2^n}{2})$

 $\frac{\mathcal{P}(\mathcal{P}, 6^{\alpha} | X)}{\mathcal{P}(\mathcal{P}, 6^{\alpha} | X)} = \mathcal{P}(\mathcal{P} | X, 6^{\alpha}) \underbrace{\mathcal{P}(6^{\alpha} | X)}_{\text{probability}} \quad \text{By Def of cond.}$

If we decompose the first way, we draw theta from N(xbar, sigsq/n) and thus sigsq must be known. What if we break this by instead of using the Jeffrey's prior, use

P(0) = N(mo, th) and P(0) = Inv Gram (10 10 10) These were the two priors we began with when we started investigating the normal likelihood model. However, it's important to note we are not allowing $\tau^{t} = \sigma^{2}/h_{p}$ $P(\theta, \sigma^{a}) = P(\theta) P(\sigma^{a}) \text{ not } P(\theta | \sigma^{a}) P(\sigma^{a})$

What happens? The two priors are disconnected completely. Let's derive the posterior under this two-dimensional prior. $P(\theta, \sigma^2 | x) \propto P(x | \theta, \sigma^2) P(\theta, \sigma^2) = P(x | \theta, \sigma^3) P(\theta) P(\sigma^2)$

 $= \left(0^{2}\right)^{\frac{1}{2} - \frac{1}{2} - \frac{1}{2}} e^{-\frac{1}{2} \frac{1}{2} - \frac{1}{2}} \left(\left(\frac{L-1}{2}\right)^{\frac{2}{2}L} + \frac{1}{2} 0 0^{\frac{1}{2}L} + \frac{1}{2} 0^{\frac{1}{2}L}\right) \frac{1}{2} - \left(\frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{2} 0^{\frac{1}{2}L}\right) \frac{1}{2} e^{-\frac{1}{2} \frac{1}{2} \frac{1}{2}} \left(\frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{1}{2} \frac{1}{2} \frac{1}{2} + \frac{1}{2} \frac{$ $= \left(\sigma^{3}\right)^{\frac{3}{4}} e^{-\frac{1}{16\pi}\left(\left(h-1\right)5^{2} + h_{0} \cdot \sigma_{+}^{2} + h_{0}\overline{\nu}^{2}\right)\int_{b}^{\infty} e^{3\sqrt[3]{4}}} N$

Is this kernel $k(sigsq \mid x)$ proportional to any distribution you know? NO!!! This means we can't sample from it using the table you've seen. Get a bigger table? No... this is not a known distribution! So we're in trouble... because we can't sample from $P(\text{sigsq} \mid x)$ thus we can't sample from the posterior.

We need a general way to sample from kernels of unknown

distributions.