## A. Problems to Submit

- 1. BE Exercise: 8.15 (not part (j)).
  - For BE 8.15, you must justify each result using a theorem(s) and/or definition(s); that is, you will NOT get full credit for just listing the distribution.
  - Do skip BE 8.15(j) as this distribution was not covered in class (or you could do a little Googling to figure it out (before looking in the back of the book)!).
- 2. Let  $X_i$  for i = 1, 2, 3 be independent random variables with  $N(i, i^2)$  distributions. For each of the following situations, use the  $X_i$ 's to construct a statistic with the indicated distribution. That is, your solution to each part below should be a function of **ALL THREE**  $X_i$ 's.
  - (a) Chi-square distribution with 3 degrees of freedom.
  - (b) Student t distribution with 2 degrees of freedom.
  - (c) F distribution with 1 and 2 degrees of freedom.
- 3. BE Exercises: 8.13, 8.18.
  - For the BE exercises listed above, you may use R or statistical tables to find the probabilities. However, you are encouraged to do it both ways for practice.

## **B.** Additional Practice Problems

- 1. BE Exercises: 8.1, 8.11.
  - For the BE exercises listed above, you may use R or statistical tables to find the probabilities. However, you are encouraged to do it both ways for practice.
- 2. Suppose that  $Z_1, \ldots, Z_n$  is an iid sample from N(0,1). Using the MGF approach ...
  - (a) Show that  $\mathbb{Z}_1^2$  follows a chi-square distribution with 1 degree of freedom.
  - (b) Show that  $Z_1^2 + \ldots + Z_n^2$  follows a chi-square distribution n degrees of freedom.
- 3. Prove the following theorems given in the course text (before looking in the text)!).
  - (a) **Theorem 8.3.1**.
  - (b) **Theorem 8.3.3**.
  - (c) **Theorem 8.3.4**.
- 4. BE Exercise: 8.4.