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In[1]:= $Assumptions = {(fd * t + fk * t * t * 0.5) > 0}
Integrate[(cd + ck * t) (fd + fk * t) Exp[-(fd * t + fk * t * t * 0.5)], {t, ti, tipd}]
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Out[1]= {fd t + 0.5 fk t^2 > 0}
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Out[2]= $Aborted
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In[20]:= Integrate[(cd + ck * t) (fd + fk * t) Exp[-(fd * t + fk * t * t) / 2], {t, ti, tipd},
Assumptions -> {(fd * t + fk * t * t) / 2 > 0, Element[{t, fd, fk, cd, ck, ti, tipd}, Reals]}]
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Out[20]=
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$$\left( e^{-\frac{fd^2 + 4 fd fk (ti + tipd) + 4 fk^2 (ti^2 + tipd^2)}{8 fk}} \left( -e^{-\frac{fd^2 + 2 fd fk (ti + tipd) + 2 fk^2 (ti^2 + tipd^2)}{4 fk}} \sqrt{\frac{1}{fk}} (-ck fd^2 + 4 ck fk + 2 cd fd fk) \right. \right. \\ \left. \sqrt{\pi} (fd + 2 fk tipd) Abs[fd + 2 fk ti] \operatorname{Erf}\left[\frac{\sqrt{\frac{1}{fk}} Abs[fd + 2 fk ti]}{2 \sqrt{2}}\right] + \right. \\ \left. (fd + 2 fk ti) \left( -2 \sqrt{2} (fd + 2 fk tipd) \left( 2 cd \left( e^{\frac{(fd + 2 fk ti)^2}{8 fk}} - e^{\frac{(fd + 2 fk tipd)^2}{8 fk}} \right) fk - \right. \right. \right. \\ \left. \left. ck e^{\frac{(fd + 2 fk tipd)^2}{8 fk}} (fd + 2 fk ti) + ck e^{\frac{(fd + 2 fk ti)^2}{8 fk}} (fd + 2 fk tipd) \right) \right) + \\ \left. e^{\frac{fd^2 + 2 fd fk (ti + tipd) + 2 fk^2 (ti^2 + tipd^2)}{4 fk}} \sqrt{\frac{1}{fk}} (-ck fd^2 + 4 ck fk + 2 cd fd fk) \sqrt{\pi} \right. \\ \left. Abs[fd + 2 fk tipd] \operatorname{Erf}\left[\frac{\sqrt{\frac{1}{fk}} Abs[fd + 2 fk tipd]}{2 \sqrt{2}}\right] \right) \Bigg) \Bigg) \Bigg) / \\ (4 \sqrt{2} fk (fd + 2 fk ti) (fd + 2 fk tipd))$$

In[21]:= % // Simplify

Out[21]=

$$\left( e^{-\frac{fd^2 + 4 fd fk (ti + tipd) + 4 fk^2 (ti^2 + tipd^2)}{8 fk}} \left( -e^{-\frac{fd^2 + 2 fd fk (ti + tipd) + 2 fk^2 (ti^2 + tipd^2)}{4 fk}} \sqrt{\frac{1}{fk}} (-ck fd^2 + 4 ck fk + 2 cd fd fk) \right. \right. \\ \left. \sqrt{\pi} (fd + 2 fk tipd) \text{Abs}[fd + 2 fk ti] \text{Erf}\left[\frac{\sqrt{\frac{1}{fk}} \text{Abs}[fd + 2 fk ti]}{2 \sqrt{2}}\right] + \right. \\ \left. (fd + 2 fk ti) \left( -2 \sqrt{2} (fd + 2 fk tipd) \left( 2 cd \left( e^{\frac{(fd + 2 fk ti)^2}{8 fk}} - e^{\frac{(fd + 2 fk tipd)^2}{8 fk}} \right) fk - \right. \right. \right. \\ \left. \left. ck e^{\frac{(fd + 2 fk tipd)^2}{8 fk}} (fd + 2 fk ti) + ck e^{\frac{(fd + 2 fk ti)^2}{8 fk}} (fd + 2 fk tipd) \right) + \right. \\ \left. \left. e^{\frac{fd^2 + 2 fd fk (ti + tipd) + 2 fk^2 (ti^2 + tipd^2)}{4 fk}} \sqrt{\frac{1}{fk}} (-ck fd^2 + 4 ck fk + 2 cd fd fk) \sqrt{\pi} \right. \right. \\ \left. \left. \left. \left. \left. \text{Abs}[fd + 2 fk tipd] \text{Erf}\left[\frac{\sqrt{\frac{1}{fk}} \text{Abs}[fd + 2 fk tipd]}{2 \sqrt{2}}\right] \right] \right] \right] \right] \right) / \\ (4 \sqrt{2} fk (fd + 2 fk ti) (fd + 2 fk tipd))$$

In[22]:= % // CForm

Out[22]//CForm=

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(- (Power(E, (Power(fd,2) + 2*fd*fk*(ti + tipd) +
2*Power(fk,2)*(Power(ti,2) + Power(tipd,2))))/(4.*fk))*Sqrt(1/fk)*
(-(ck*Power(fd,2)) + 4*ck*fk + 2*cd*fd*fk)*Sqrt(Pi)*(fd + 2*fk*tipd)*
Abs(fd + 2*fk*ti)*Erf((Sqrt(1/fk)*Abs(fd + 2*fk*ti))/(2.*Sqrt(2)))) +
(fd + 2*fk*ti)*(-2*Sqrt(2)*(fd + 2*fk*tipd)*
(2*cd*(Power(E,Power(fd + 2*fk*ti,2)/(8.*fk)) -
Power(E,Power(fd + 2*fk*tipd,2)/(8.*fk)))*fk -
ck*Power(E,Power(fd + 2*fk*tipd,2)/(8.*fk))*(fd + 2*fk*ti) +
ck*Power(E,Power(fd + 2*fk*ti,2)/(8.*fk))*(fd + 2*fk*tipd)) +
Power(E, (Power(fd,2) + 2*fd*fk*(ti + tipd) +
2*Power(fk,2)*(Power(ti,2) + Power(tipd,2))))/(4.*fk))*Sqrt(1/fk)*
(-(ck*Power(fd,2)) + 4*ck*fk + 2*cd*fd*fk)*Sqrt(Pi)*Abs(fd + 2*fk*tipd)*
Erf((Sqrt(1/fk)*Abs(fd + 2*fk*tipd))/(2.*Sqrt(2)))))/
(4.*Sqrt(2)*Power(E, (Power(fd,2) + 4*fd*fk*(ti + tipd) +
4*Power(fk,2)*(Power(ti,2) + Power(tipd,2))))/(8.*fk))*fk*(fd + 2*fk*ti)*
(fd + 2*fk*tipd))
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In[23]:= % // TeXForm

Out[23]//TeXForm=

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\frac{\exp \left(-\frac{\text{fd}^2+4 \text{fd} \text{fk} (\text{ti}+\text{tipd})}{\text{fk}^2 \left(\text{ti}^2+\text{tipd}^2\right)}\right)^{8 \text{fk}}}{\left((\text{fd}+2 \text{fk} \text{ti}) \sqrt{\pi} \sqrt{\frac{1}{\text{fd}+2 \text{fk} \text{tipd}}}\right) \left(2 \text{cd} \text{fd} \text{fk}-\text{te} \text{fd}^2+4 \text{ck} \text{fk}\right) \text{erf}\left(\frac{\sqrt{\frac{1}{\text{fk}}}}{\text{fd}+2 \text{fk} \text{ti}}\right)^{2 \sqrt{2}} \exp \left(\frac{\text{fd}^2+2 \text{fd} \text{fk} (\text{ti}+\text{tipd})+2 \text{fk}^2 \left(\text{ti}^2+\text{tipd}^2\right)}{\text{fk}}\right)-2 \sqrt{2} (\text{fd}+2 \text{fk} \text{tipd}) \left(2 \text{fd} \text{fk} \left(e^{\frac{\text{fd}+2 \text{fk} \text{ti}}{2}}\right)^8 \text{fk}-e^{\frac{(\text{fd}+2 \text{fk} \text{tipd})^2}{8 \text{fk}}}\right)-\text{ck} (\text{fd}+2 \text{fk} \text{ti}) e^{\frac{(\text{fd} \text{fk} \text{tipd})^2}{8 \text{fk}}}+\text{ck} e^{\frac{(\text{fd}+2 \text{fk} \text{ti})^2}{8 \text{fk}}}\right) \sqrt{\pi} \sqrt{\frac{1}{\text{fk}}} (\text{fd}+2 \text{fk} \text{tipd})} \left(\text{fd}+2 \text{fk} \text{ti}\right) \left(2 \text{cd} \text{fk}-\text{ck} \text{fd}^2+4 \text{ck} \text{fk}\right) \text{erf}\left(\frac{\sqrt{\frac{1}{\text{fk}}}}{\text{fd}+2 \text{fk} \text{ti}}\right)^{2 \sqrt{2}} \exp \left(\frac{\text{fd}^2+2 \text{fd} \text{fk} (\text{ti}+\text{tipd})+2 \text{fk}^2 \left(\text{ti}^2+\text{tipd}^2\right)}{\text{fk}}\right)-4 \sqrt{2} \text{fk} (\text{fd}+2 \text{fk} \text{tipd})}
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