

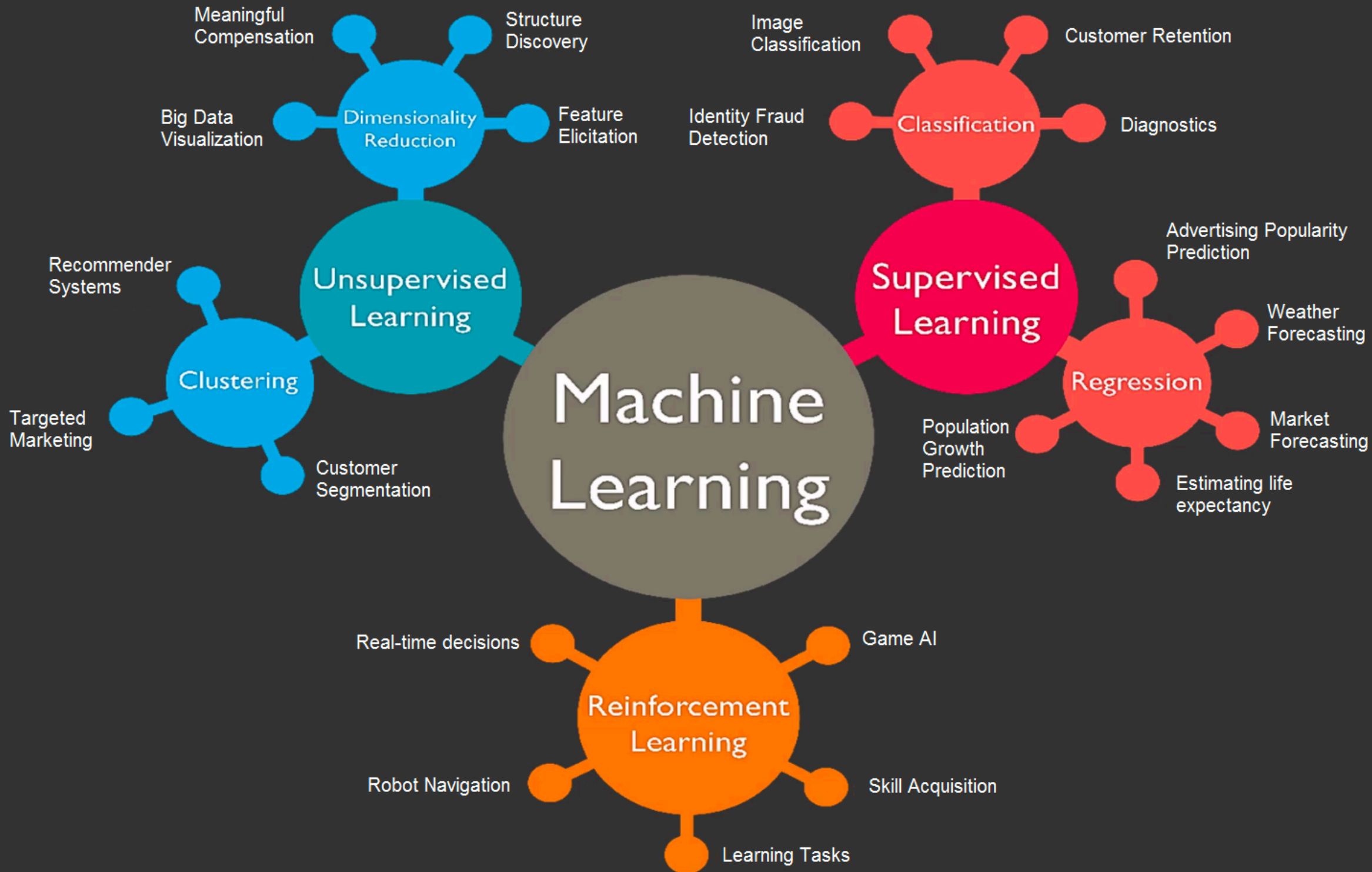
# INTRODUCTION TO LOGISTIC REGRESSION

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**OPENING**

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# INTRO TO CLASSIFICATION



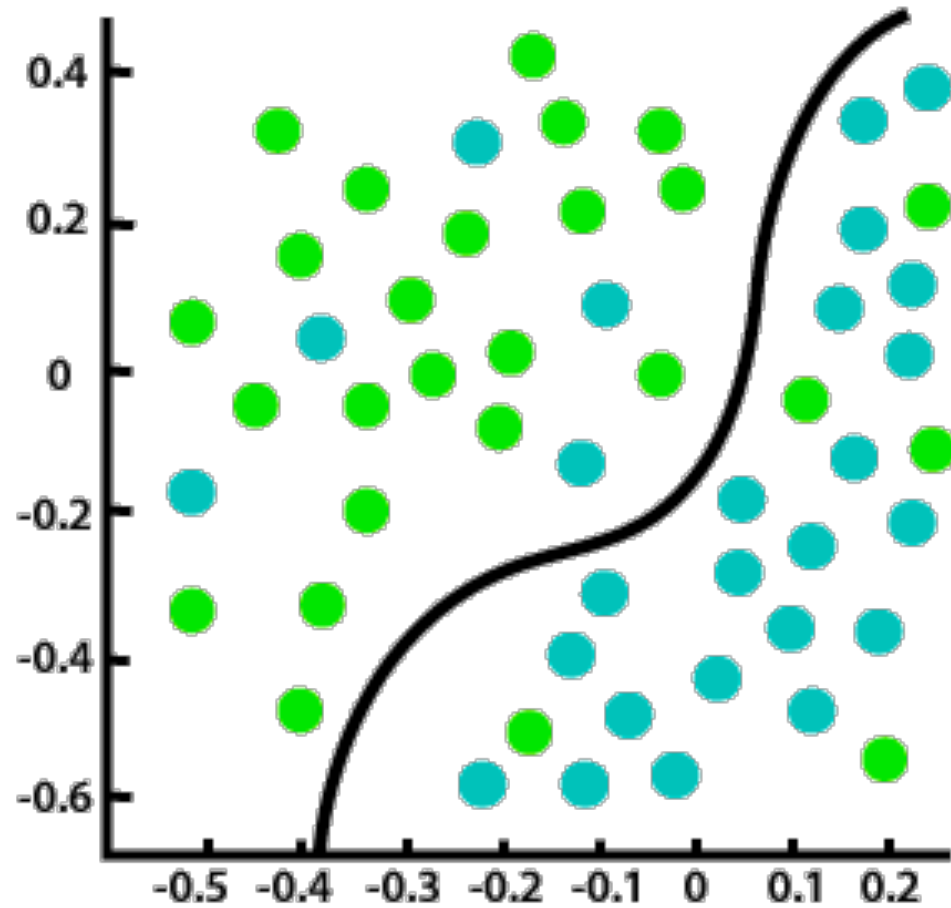
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# WHERE ARE WE?

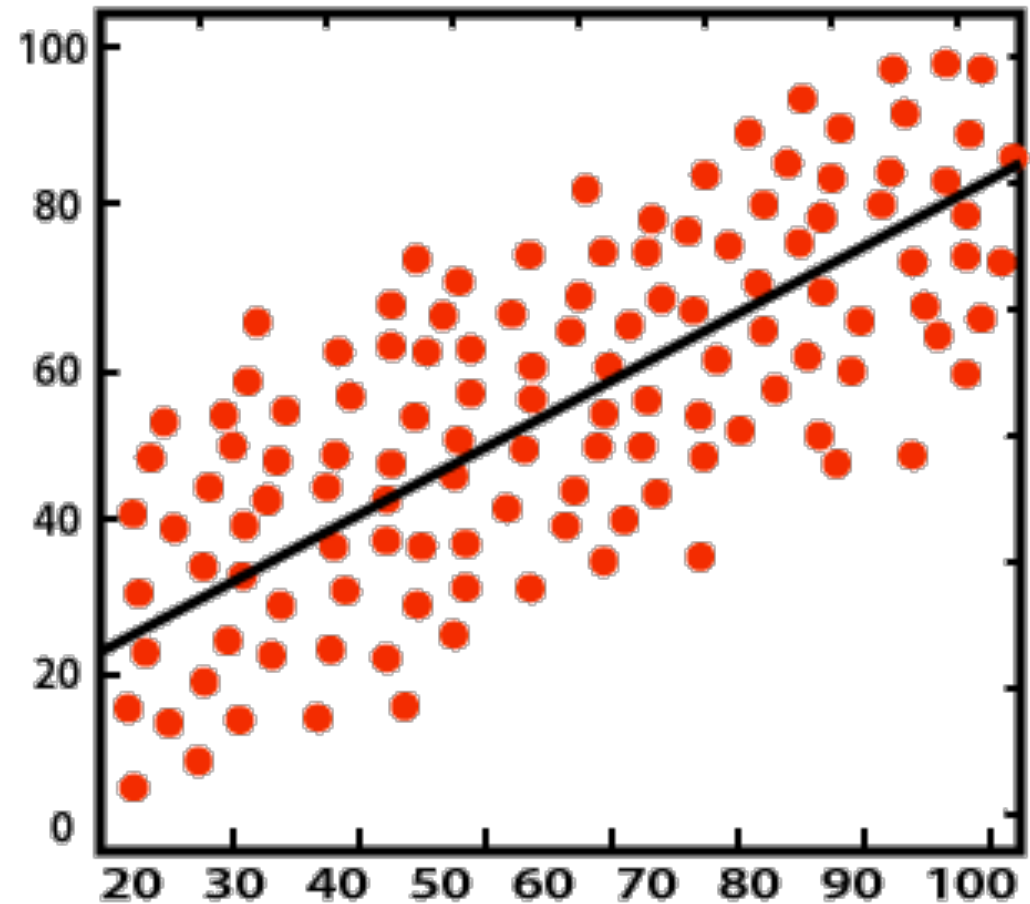
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	<i>Supervised Learning</i>	<i>Unsupervised Learning</i>
<i>Discrete</i>	classification or categorization	clustering
<i>Continuous</i>	regression	dimensionality reduction

# CLASSIFICATION VS REGRESSION



Classification



Regression

# COMMON ALGORITHMS

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## Regression

Simple Linear Regression

Multiple Linear Regression

Polynomial Linear Regression

Support Vector Regression

Decision Tree Regression

Random Forest Regression

Neural Network

## Classification

Logistic Regression

K Nearest Neighbors

Support Vector Machine

Naïve Bayes

Decision Tree Classification

Random Forest Classification

Neural Network

# WHAT IS THE OUTCOME VARIABLE?

Regression

Age	Income	Loan Amount
21	20000	0
37	55000	150000
29	35000	120000
23	17000	550000
34	70000	250000
47	84000	0
25	30000	90000

Classification

Age	Income	Loan Status
21	20000	Rejected
37	55000	Approved
29	35000	Approved
23	17000	Rejected
34	70000	Approved
47	84000	Rejected
25	30000	Approved



# CLASSIFICATION vs REGRESSION



Student Profile



*Predicting Student*  
**Pass Or Fail**



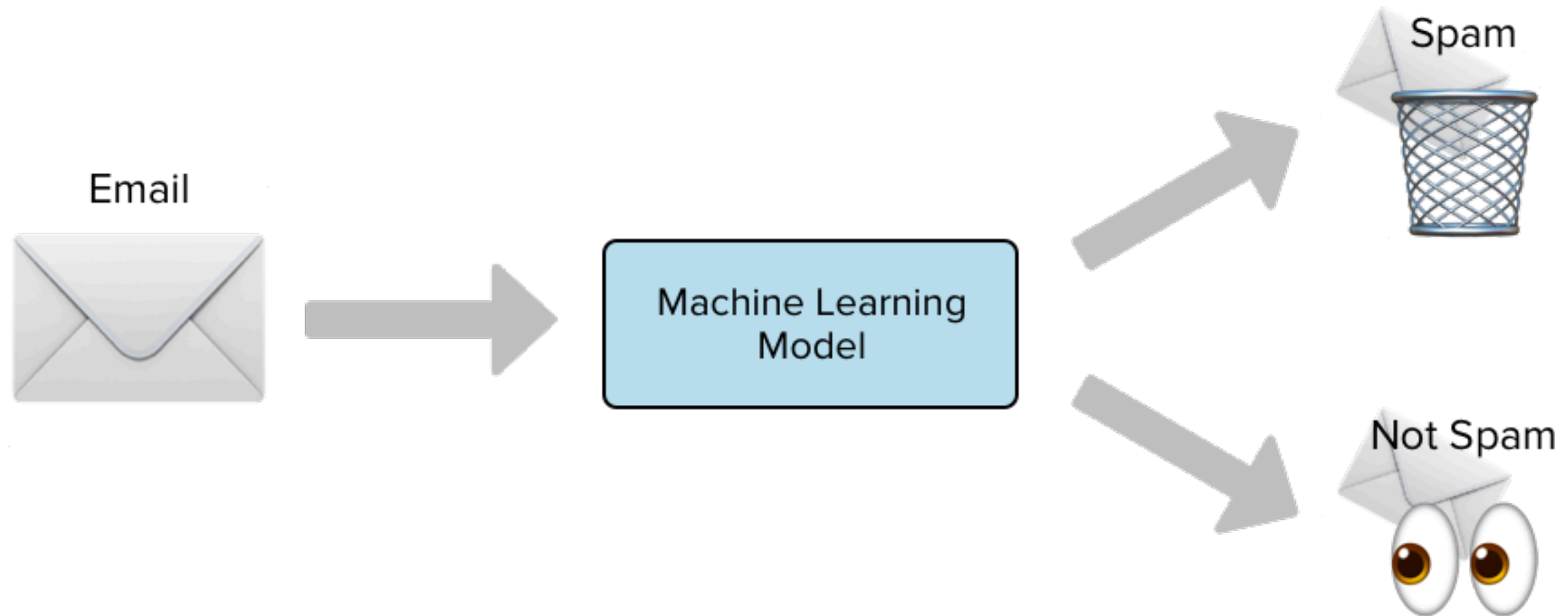
Student Profile



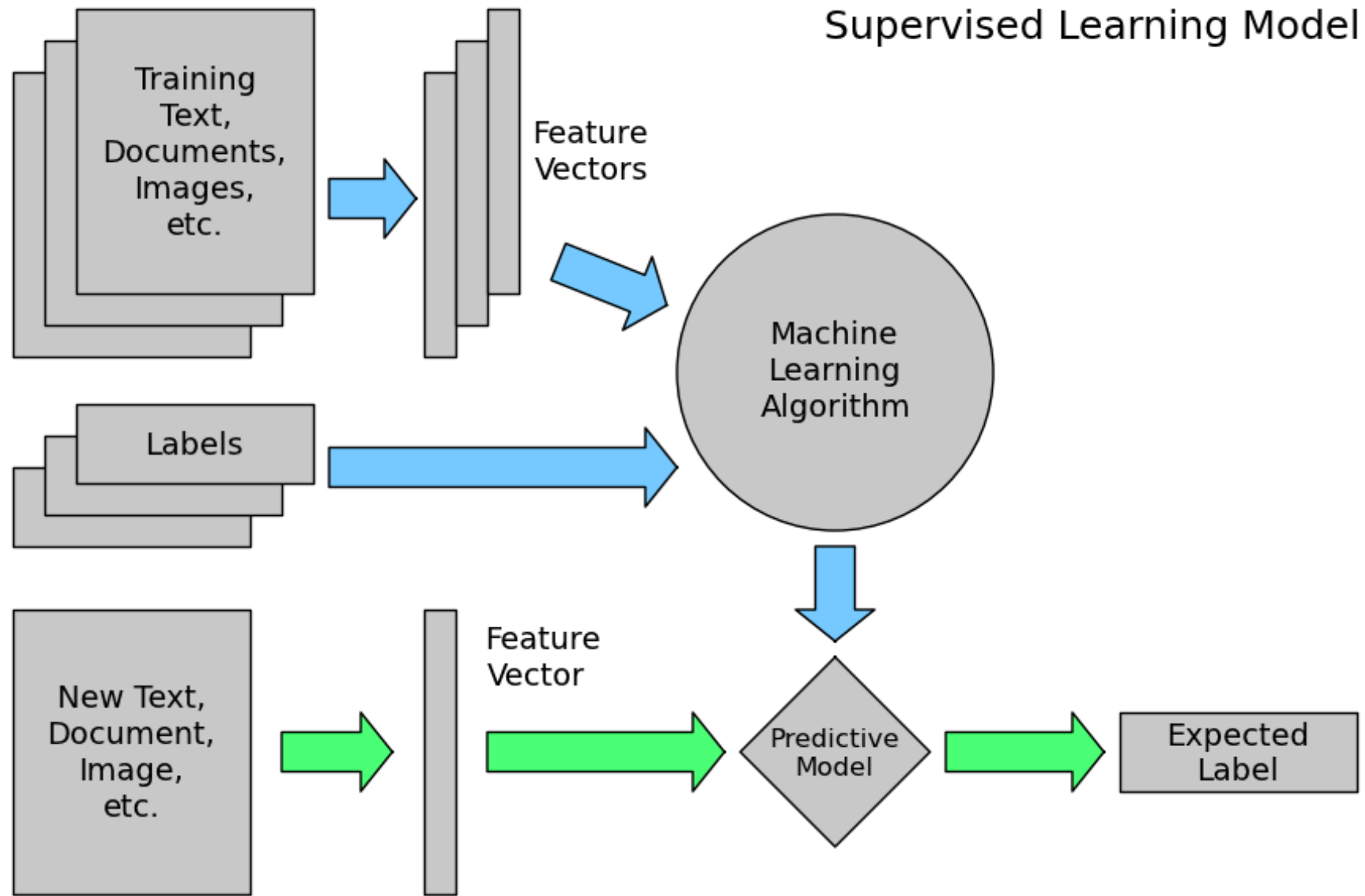
*Predicting Student Marks*  
**Percentage**



# CLASSIFICATION



# CLASSIFICATION



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## INTRODUCTION

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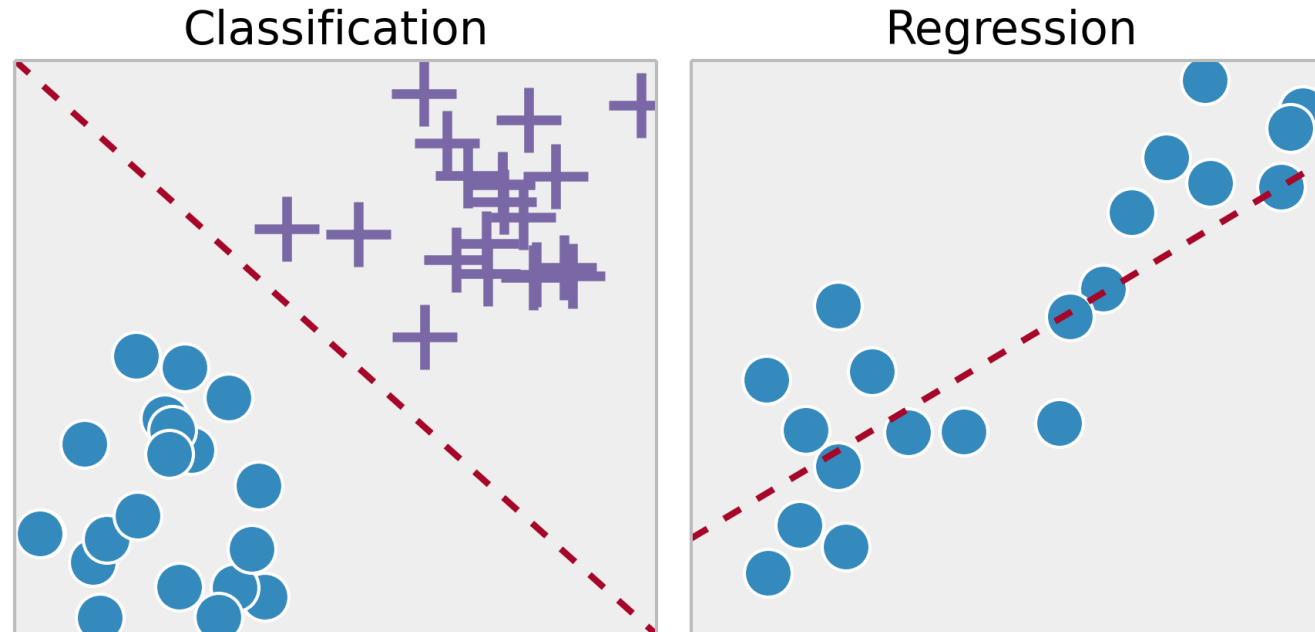
# LOGISTIC REGRESSION

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# LOGISTIC REGRESSION

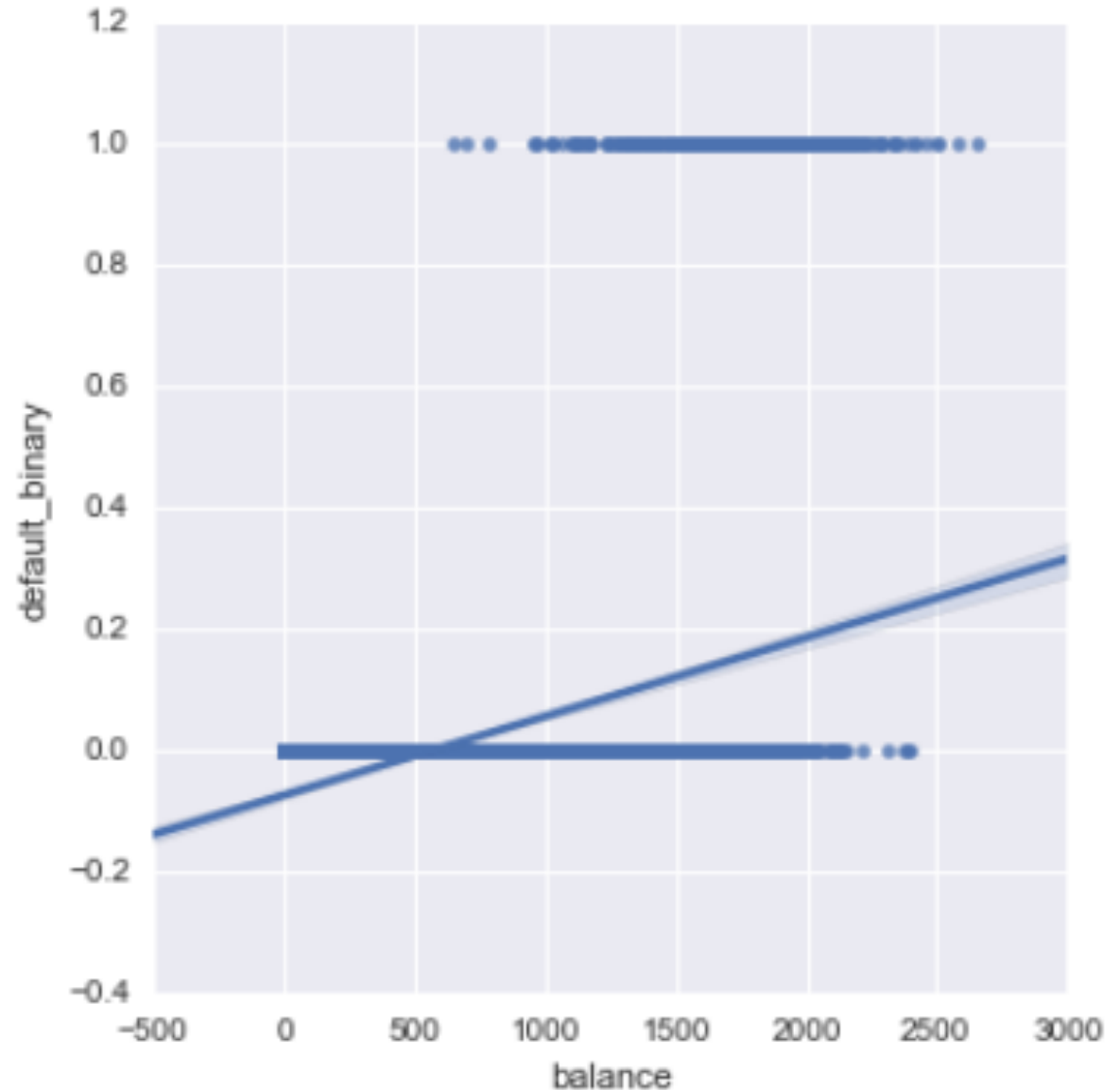
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- ▶ Logistic regression is a linear approach to solving a classification problem. It will use a linear regression *style* approach to predict the class of an item, but retain the interpretability of linear regression model.

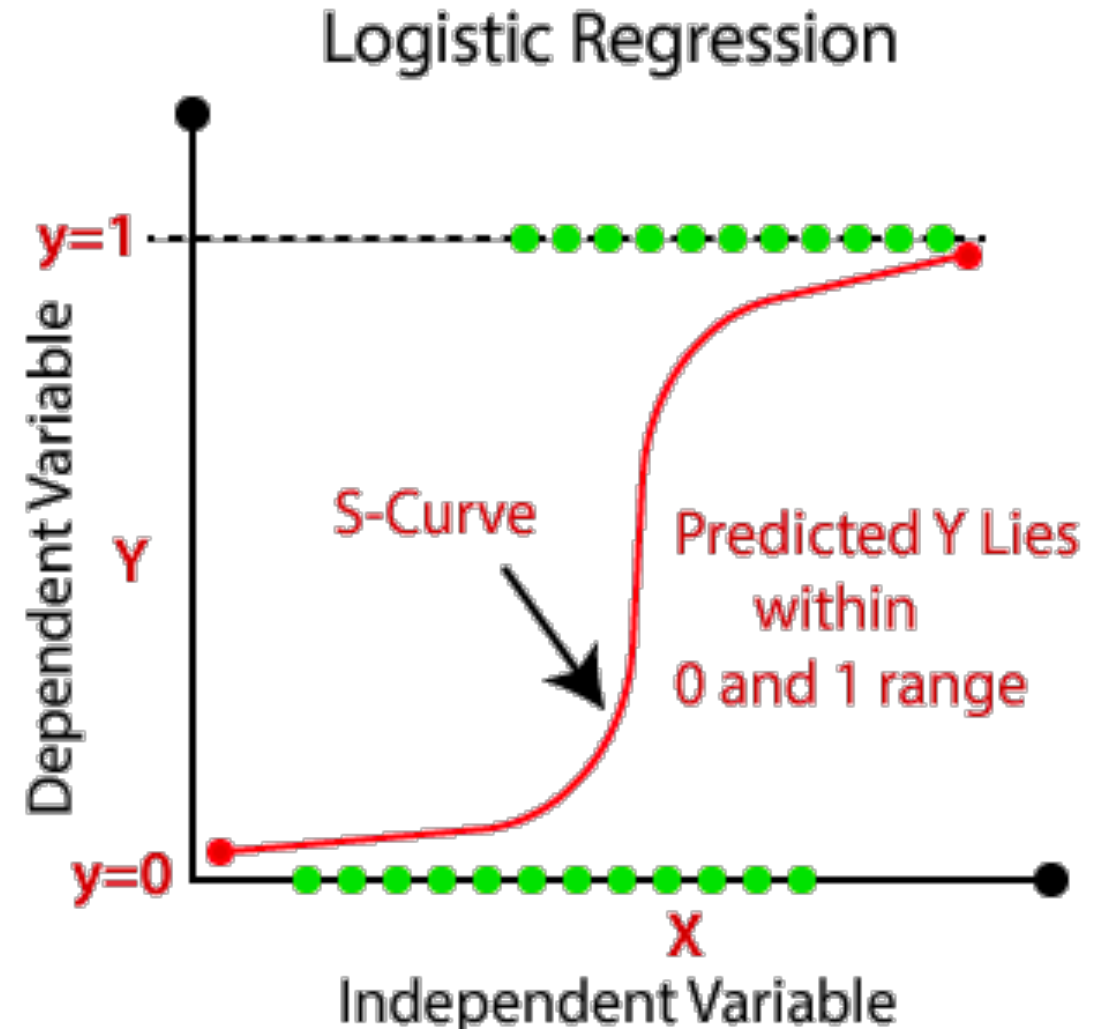
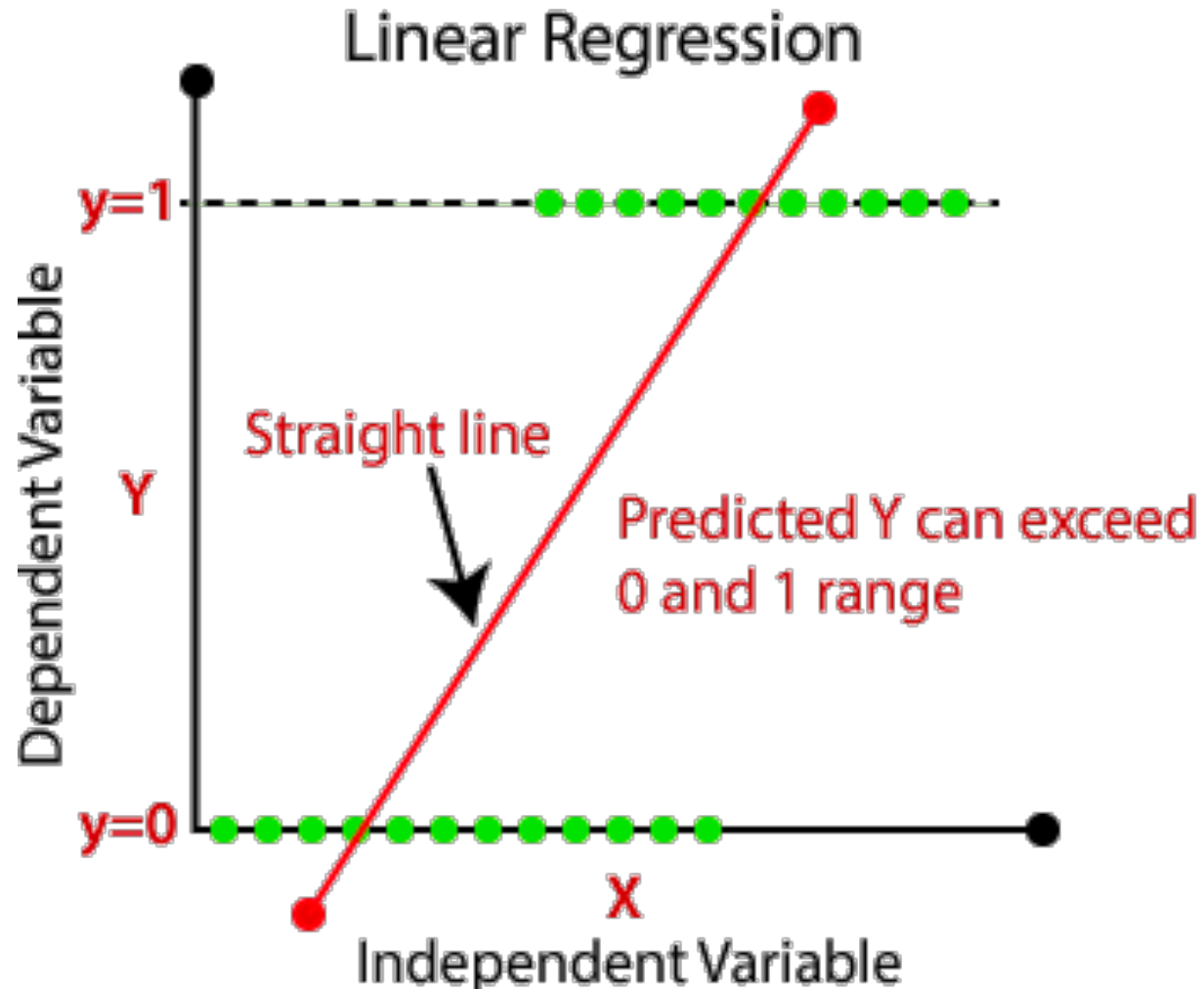


# LINEAR REGRESSION can't model a binary outcome

- ▶ We need a way to *transform* our regression model so that its range changes from  $[-\infty, \infty]$  to  $[0, 1]$ .

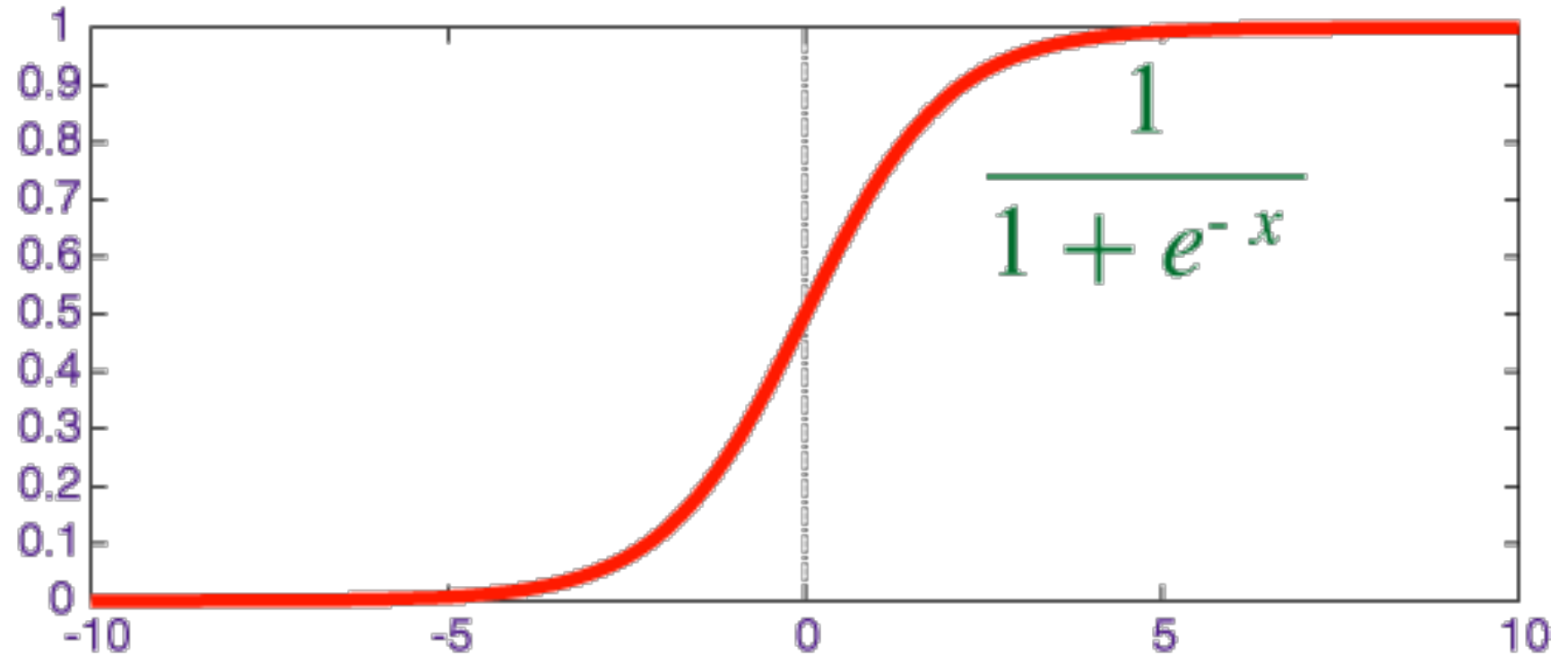


# LINEAR REGRESSION can't model a binary outcome



# LOGISTIC REGRESSION

- ▶ To do this, we'll use a log-based transformation called the **logit function**.
- ▶ It will limit our range to  $[0,1]$  and create the right shape for our regression line to match the categorical outcome variable.





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# EQUATIONS

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► Linear regression equation:

$$y = \beta_1 X + \beta_0$$

► Logistic regression equation:

$$p = P(y \mid X) = \frac{1}{1 + e^{-\beta_1 X + \beta_0}}$$

$$\text{logit}(p) = \beta_0 + \beta_1 x_1 + \beta_2 x_2$$

# Multinomial Logistic Regression



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## INTRODUCTION

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# INTERPRETING COEFFICIENTS

# COEFFICIENTS

- ▶ Coefficients are expressed as logodds
- ▶ Positive coefficients increase the log odds of the response (and thus increase the probability)
- ▶ Negative coefficients decrease the log odds of the response (and thus decrease the probability).

	probability	odds	logodds
<b>0</b>	0.10	0.1111111	-2.197225
<b>1</b>	0.20	0.250000	-1.386294
<b>2</b>	0.25	0.3333333	-1.098612
<b>3</b>	0.50	1.000000	0.000000
<b>4</b>	0.60	1.500000	0.405465
<b>5</b>	0.80	4.000000	1.386294
<b>6</b>	0.90	9.000000	2.197225

# LOGISTIC REGRESSION COEFFICIENTS

► The intercept is the log of the odds when all predictors are zero

► Coefficients are the log of the odds of each predictor

## Binary Logit: Churn

	Estimate	Standard Error	<i>z</i>	<i>p</i>
(Intercept)	-1.41	0.16	-8.73	< .001
Senior Citizen: Yes	0.41	0.11	3.60	< .001
Tenure	-0.03	0.00	-11.38	< .001
Internet Service: DSL	0.92	0.21	4.39	< .001
Internet Service: Fiber optic	1.82	0.32	5.66	< .001
Contract: One year	-0.88	0.14	-6.25	< .001
Contract: Two year	-1.68	0.24	-7.02	< .001
Monthly Charges	0.00	0.00	1.11	.266

*n* = 3,522 cases used in estimation (Training sample); R-squared: 0.1898; Correct predictions: 79.05%; McFadden's rho-squared: 0.2564; AIC: 3,065.1; multiple comparisons correction: None

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# COEFFICIENTS EXAMPLE: TITANIC SURVIVAL

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- ▶ These coefficients are "log odds"
- ▶ log odds = 0 indicates even probability
- ▶ log odds < 0 indicates less likely to occur
- ▶ log odds > 0 indicates more likely to occur

	Log Odds	odds_ratios
<b>Pclass</b>	-0.796128	0.451072
<b>Sex_male</b>	-0.637771	0.528469
<b>Sex_female</b>	0.637771	1.892258
<b>Age</b>	-0.441080	0.643341
<b>SibSp</b>	-0.324210	0.723098
<b>Parch</b>	-0.109567	0.896222
<b>Fare</b>	0.165687	1.180204
<b>Embarked_S</b>	-0.094984	0.909388
<b>Embarked_C</b>	0.093482	1.097991
<b>Embarked_Q</b>	0.022137	1.022384

# INTERPRET THE COEFFICIENTS

Changing the  $\beta_0$  value shifts the curve horizontally, whereas changing the  $\beta_1$  value changes the slope of the curve.

