

# HW1 High Dynamic Range Imaging

Appendix

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# Outline

- Grading
  - Implementation
  - Experiment & Free Study
- Additional Implementation Details
  - Response Calibration
  - Construct Radiance

# Grading

Items		Score
<b>Implementation</b> <b>(65%)</b>	Camera Response Calibration	20%
	Global Tone Mapping	10%
	Local Tone Mapping	15%
	Edge-Preserving Filter	15%
	White Balance	5%
<b>Experiment&amp; Free Study</b> <b>(35%)</b>	Experiments	20%
	Free Study	15%

# Grading: Implementation

- You will get full score if your result pass the bar
  - same result with TA's implementation

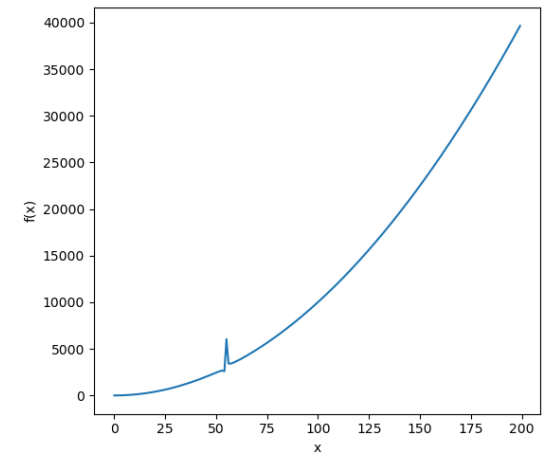
Complete function `globalTM()` in `tm.py`. Your result for `/TestImg/memorial.hdr` should be similar to `/ref/p2_gtm.png` (PSNR>45dB), under the default setting `s=1.0` to get a full score.

# Grading: Experiment& Free Study

- Experiment
  - Finish an asked Figure/Curve/Image
  - Discussion
- Free Study
  - Select *Two* topics you want
  - Research and discuss on it
- What should be included in Report?
  - i. Assumption
  - ii. Justification

# Example: Do not

- For variable  $x$ , sweep from 0.1 ~ 200
- Describe the trend ( $f(x)$  v.s.  $x$ )
  - which maybe already mentioned in class
- Notice something weird around  $x$  in (50~60)
- I guess xxx so, xxx ...



# Example: Do

- Keep you sweep for observation
  - Describe the trend if it's important to you
- Assume that:  $f(x) = f_{ideal}(x) + \frac{g(y)}{x-55}$ 
  - Design a experiment to justify your assumption
    - ex1. sweep  $y$
    - ex2. Design a special experiment to eliminate unideal part
- Describe
  - Where the assumption comes from?
  - Why you design the experiment in this way?
  - How your experiment prove your assumption?

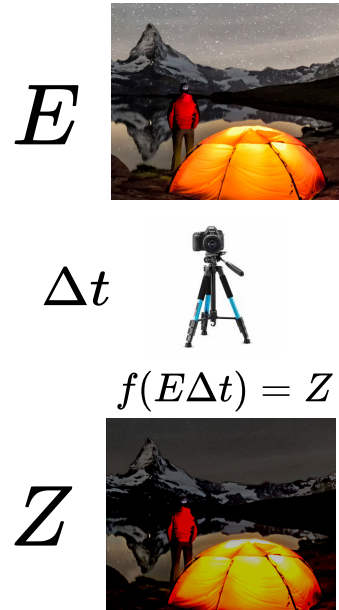
# You don't need to be "correct"

- It's ok to provide an assumption that fits reality imperfectly
- We will grade the report based on :
  - Correctness of reasoning
  - Rigorousness of justification



# Response Calibration

- We want  $E$  (radiance) of a scene
- What do we have?
  - $Z$  (Pixel value) and  $\Delta t$  (Exposure time)
- What do we know (or assume)?
  - $Z$  has one-to-one mapping with exposure  $E\Delta t$ 
    - Other setting unchanged
  - The mapping:
    - $g(Z) = \ln E + \ln \Delta t$
- If we have  $g(Z)$  for all possible  $Z$  ( $[0:1:256]$ )
  - and exposure time  $\Delta t_j$  for a taken image  $j$
  - We can obtain  $\ln E = g(Z) - \ln \Delta t$



# What do we want again?

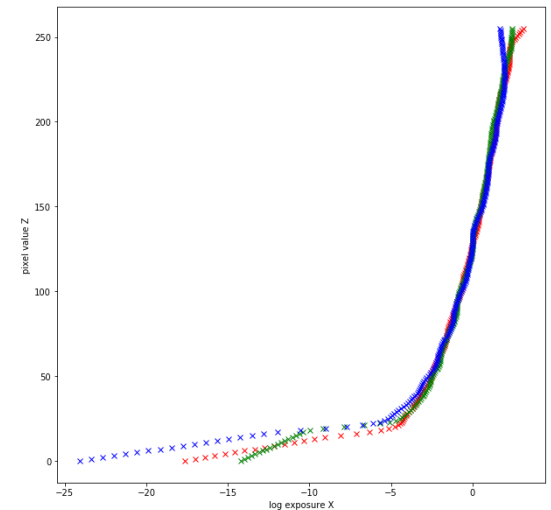
- $g(Z)$  for all possible  $Z$  ([0:1:256])
  - 256 variables
- What relation do we have?
  - Exposure Mapping

$$g(Z) - \ln E = \ln \Delta t$$

- Smoothness Constraint

$$g''(Z) = 0$$

- How to find out  $g(z)$ ?
  - Measuring a lot of samples
  - Measure  $Z_{ij}$  on  $E_i$  and  $\Delta t_j$

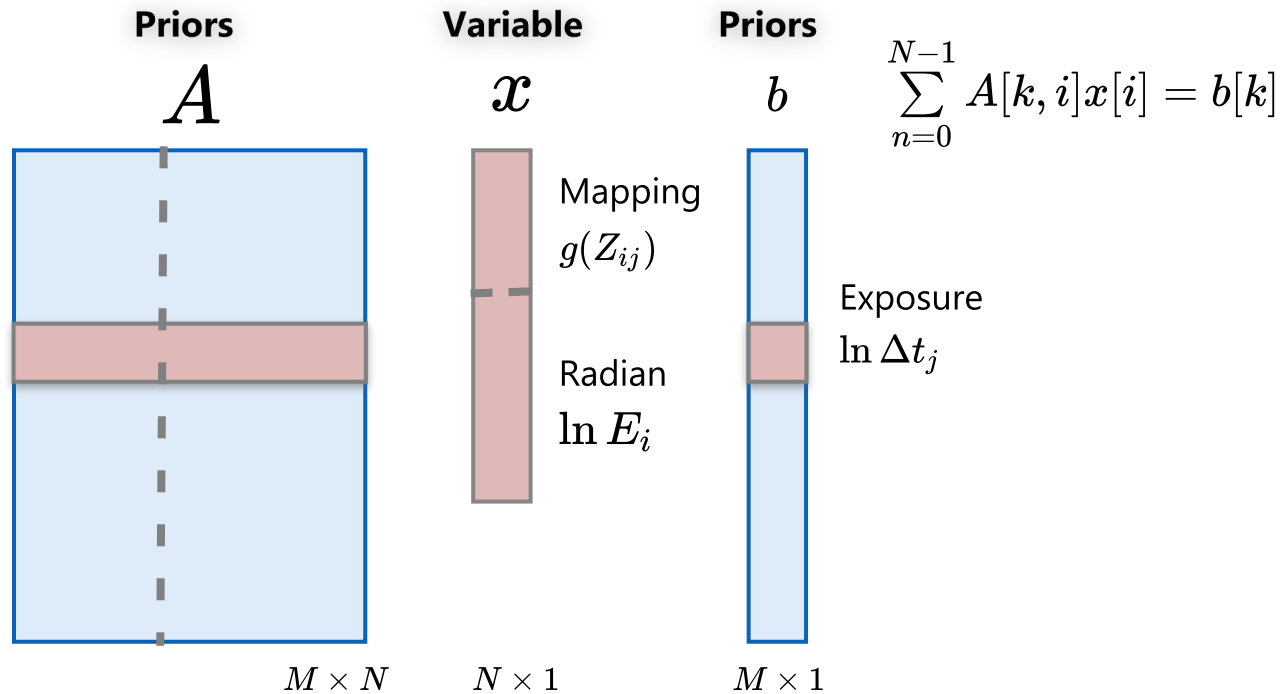


# Solving Objective Function

$$O = \sum_i \sum_j [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]^2 + \lambda \sum_z [g''(z)]^2$$

- The objective function describes a relation (we want) between
  - **variables** and **measurements**
- What are variables?
  - The unknown terms  $g(z)$  and  $\ln E_i$
- What are measurements?
  - The known terms  $Z_{ij}$  and  $\Delta t_j$

# Objective Function in Matrix Form



- $M$  {#(equations)}: number of measurements  $(\Delta t_j, Z_{ij}) \rightarrow I \times J$
- $N$  {#(variables)}:  $256 + \#(E_i) \rightarrow 256 + I$

# Data Term Assignment

$$\sum_i \sum_j [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]^2$$

That's say in  $k$ -th measurement, image 3 ( $\Delta t_3 = 2$ ),  
pixel 12 has intensity  $Z_{12,3} = 127$ .

We want the variables  $\ln E_{12}$  and  $g(127)$  has the following relationship

$$g(127) - \ln E_{12} = \ln 2$$

Then we should set row  $k$  as

- $A(k, 127) = 1$
- $A(k, 256 + 12) = -1$
- $b(k) = \ln 2$

# Smoothness Term Assignment

$$g''(z) = g(z - 1) - 2g(z) + g(z + 1) = 0$$

That's say in  $k$ -th experiments

Intensity  $z = 16$  should have 0 second order derivatives

$$g''(16) = g(15) - 2g(16) + g(17) = 0$$

Then we should set row  $k$  as

- $A(k, 15) = 1$
- $A(k, 16) = -2$
- $A(k, 17) = 1$
- $b(k) = 0$

# Bring back Reliability Weight

$$O = \sum_i \sum_j w(Z_{ij}) [g(Z_{ij}) - \ln E_i - \ln \Delta t_j]^2 + \lambda \sum_z [w(z) g''(z)]^2$$

That's say in  $k$ -th measurement, image 3 ( $\Delta t_3 = 2$ ),  
pixel 12 has intensity  $Z_{12,3} = 127$ .

We want the variables  $\ln E_{12}$  and  $g(127)$  has the following relationship

$$w(127)g(127) - w(127) \ln E_{12} = w(127) \ln 2$$

# Bring back Reliability Weight

We want the variables  $\ln E_{12}$  and  $g(127)$  has the following relationship

$$w(127)g(127) - w(127) \ln E_{12} = w(127) \ln 2$$

Then we should set row  $k$  as

- $A(k, 127) = w(127)$
- $A(k, 256 + 12) = -w(127)$
- $b(k) = w(127) \ln 2$



# Solve Least Square Problems

- $\|Ax - b\|^2$
- $A$  is usually not square matrix
  - We want more measurements(equations) to reduce the measurement error
- If we can find  $A^\dagger$  (pseudo inverse of  $A$ )
- We can obtain
  - $x = A^\dagger b$
  - Which minimize the square error  $\|Ax - b\|^2$

# Solve Least Square Problems

- $\|Ax - b\|^2$
- In Numpy, we can solve the least square problem with
  - `linalg.lstsq(a, b, rcond='warn')`
  - `a` : (M, N) array\_like "Coefficient" matrix.
  - `b` : {(M,), (M, K)} array\_like
- Returns: `x` {(N,), (N, K)} ndarray
  - Least-squares solution. If `b` is two-dimensional, the solutions are in the K columns of `x`.

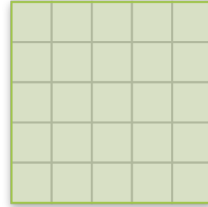
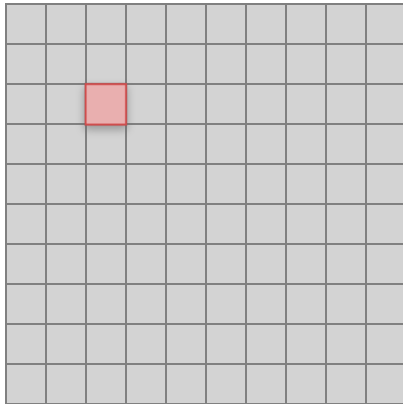
# Construct Radiance

- For an image  $j$  with exposure time ( $\Delta t_j$ )
- The radiance is simply
  - $E_i = \exp(g(Z_{ij}) - \ln \Delta t_j)$
- But why don't we use all available images?
  - $\ln E_i = \frac{\sum_j w(Z_{ij})[g(Z_{ij}) - \ln \Delta t_j]}{\sum_j w(Z_{ij})}$
  - $E_i = \exp(\ln E_i)$

# Image Filtering

- Covolution between  $w_{K \times L}$  and  $L_{I \times J}$
- LTI, Symmetric Filter

$$L'(i, j) = \sum_{k, l} w(k, l) L(i + k, j + l)$$



$$k, l \in [-N/2, N/2]$$

