

CS5200 Homework 5 Theory

Adam McNeil

Question 1

Calories:  $300 = 60X + 60Y$

Vitamin A:  $36 = 12X + 6Y$

Vitamin C:  $90 = 6X + 30Y$

Cost =  $1.2X + 1.5Y$  Solution:

$X = 2.5$  cups

$Y = 2.5$  cups

Question 2

$$P = 20x_1 + 10x_2 + 15x_3$$

$$3x_1 + 2x_2 + 5x_3 \leq 55$$

$$2x_1 + x_2 + x_3 \leq 26$$

$$x_1 + x_2 + 3x_3 \leq 30$$

$$5x_1 + 2x_2 + 4x_3 \leq 57$$

$$x_1, x_2, x_3 \geq 0$$

$$P = 20x_1 + 10x_2 + 15x_3$$

$$55 - 3x_1 - 2x_2 - 5x_3 = s_1$$

$$26 - 2x_1 - x_2 - x_3 = s_2$$

$$30 - x_1 - x_2 - 3x_3 = s_3$$

$$57 - 5x_1 - 2x_2 - 4x_3 = s_4$$

$$x_1, x_2, x_3, s_1, s_2, s_3, s_4 \geq 0$$

$$x_1 = 0, x_2 = 0, x_3 = 0, s_1 = 55, s_2 = 26, s_3 = 30, s_4 = 57$$

$$P = 0$$

Non-basic set:  $\{x_1, x_2, x_3\}$

Basic set:  $\{s_1, s_2, s_3, s_4\}$

$$P = 20x_1 + 10x_2 + 15x_3$$

$$55 - 3x_1 - 2x_2 - 5x_3 = s_1; x_1 = 55/3$$

$$26 - 2x_1 - x_2 - x_3 = s_2; x_1 = 13$$

$$30 - x_1 - x_2 - 3x_3 = s_3; x_1 = 30$$

$$57 - 5x_1 - 2x_2 - 4x_3 = s_4; x_1 = 57/5 < -tightest$$

$$x_1 = 11.4, x_2 = 0, x_3 = 0, s_1 = 55, s_2 = 26, s_3 = 30, s_4 = 0$$

$$P = 228$$

Non-basic set:  $\{x_2, x_3, s_4\}$

Basic set:  $\{x_1, s_1, s_2, s_3\}$

$$55 - 3x_1 - 2x_2 - 5x_3 = s_1; x_2 = 55/2$$

$$26 - 2x_1 - x_2 - x_3 = s_2; x_2 = 26 < -tightest$$

$$30 - x_1 - x_2 - 3x_3 = s_3; x_2 = 30$$

$$57 - 5x_1 - 2x_2 - 4x_3 = s_4; x_2 = 57/2$$

$x_1 = 0, x_2 = 26, x_3 = 0, s_1 = 55, s_2 = 26, s_3 = 30, s_4 = 0$   
 $P = 260$   
Non-basic set:  $\{s_2, x_1, x_3\}$   
Basic set:  $\{x_2, s_1, s_3, s_4\}$

Question 3

Since we are given the nodes one at a time we can sort the nodes as we get them. It would only take  $n$  time to insert a node into a sorted list. Since it only takes  $n$  manipulations after that, for each new node we could find the convex hull in  $n^2$  steps.

Question 4

Yes A is in P.

Yes A is in NP.

He should not get the million dollar reward because all he showed was that P is a subset of NP problems. In order to get the prize he would need to show that a np complete problem could be reduced to a problem in P.