Computation, learning, and typology Class 3: More formal limits

Adam Albright and Eric Baković CreteLing 2023 — July 2023



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Some other invocations of phonological simplicity

Simplicity in the face of phonetic motivation

Gordon (2002):51

The author proposes that syllable weight is driven by considerations of phonetic effectiveness and phonological simplicity, and that the phonetically best distinctions are those which divide syllables into groups that are phonetically most distinct from each other. Phonologically complex distinctions are those which exceed an upper threshold in the number of phonological predicates to which they refer. It is claimed that languages adopt weight distinctions that are phonetically most effective without being overly complex phonologically. Syllable weight thus reflects a compromise between phonetic and phonological factors.



Human learners and learning algorithms

- Moreton & Pater (2012); Pater & Moreton (2012): "... make predictions about skews toward simplicity in typology, in conjunction with a model of iterated learning."
- Durvasula & Liter (2020): "There is a simplicity bias when generalising from ambiguous data."
- Albright & Hayes (2002): Minimum Generalization Learner
- Barke et al. (2019): SyPном: separating out inferences
- Ellis et al. (2022): Bayesian Program Induction



Consistency of rule interactions

A fragment of the phonological grammar of Yokuts

	/mut+t/	/?uːt+ka/	/paxaːt+t/	/?uːt+hn/
$\varnothing \longrightarrow i/C _C \begin{Bmatrix} C \\ \# \end{Bmatrix}$	mut <u>i</u> t	?uːtka	paxaːti̯t	ʔuːthiౖn
$[\alpha \text{high}] \longrightarrow [\beta \text{round}] / \begin{bmatrix} \alpha \text{high} \\ \beta \text{round} \end{bmatrix} C_0 $	mut <u>u</u> t	?uːtka	paxaːtit	?uːth <u>u</u> n
$[+long] \longrightarrow [-high]$	mutut	? <u>o:</u> tka	paxaːtit	? <u>o:</u> thun
$V \longrightarrow [-long] / _C \begin{Bmatrix} C \\ \# \end{Bmatrix}$	mutut	? <u>o</u> tka	paxa:tit	? <u>o</u> thun
	[mutut]	[?otka]	[paxaːtit]	[?othun]
	'swear' (aor.pass.)	'steal' (fut.pass.)	'mourn' (aor.pass.)	'steal' (aorist)

epenthesis feeds harmony lowering counterxeeds harmony; shortening counterbleeds lowering epenthesis bleeds shortening everything everywhere all at once



Different strokes for different folks

- Anderson (1974): local ordering
 - A < B. B < C. but C < A
 - interaction markedness: feeding > neutral > bleeding
- Kiparsky (1985): cyclicity
 - A < B < C within a cycle, but C < A across cycles
 - must be independently motivated by the morphology

Consistency of rankings



A possible rule-based grammar

- Stop+liquid cluster simplification
 - liquid $\rightarrow \emptyset$ / stop #
- r+sonorant epenthesis
 - $\varnothing \rightarrow$ ə / r ___ sonorant
- Assume lexicon with a range of structures

UR	/mat/	/kab/	/patr/	/tabl/	/parl/	/tarm/
TR simpl.	_	_	pat	tab	_	_
rN epenth.	_	_	_	_	parəl	tarəm
SR	[mat]	[kab]	[pat]	[tab]	[parəl]	[tarəm]



OT translation: Stop+liquid cluster simplification

Constraints

• Markedness:
$$*\begin{bmatrix} -son \\ -cont \end{bmatrix} \begin{bmatrix} +cons \\ +son \\ +cont \end{bmatrix} = *TR$$

- Faithfulness 1: Max(C)
- Faithfulness 2: Dep(V)
- Ranking: *TR, Dep(V) ≫ Max(C)

/tabl/	M:*TR	F:DEP(V)	F:Max(C)
เ [tab]		 	*
[tabl]	*W	 	L
[tabəl]		*W	L



OT translation: r+sonorant epenthesis

Constraints

• Markedness:
$$*r\begin{bmatrix} -syl \\ +son \end{bmatrix} = *rN$$

- Faithfulness 1: MAX(C)
- Faithfulness 2: DEP(V)
- Ranking: *rN, Max(C) ≫ Dep(V)

/parl/	M:*rN	F:Max(C)	F:DEP(V)
☞ [parəl]		 	*
[parl]	*W	 	L
[par]		*W	L



A ranking contradiction!

- Violations of both *TR and *rN could be repaired by either epenthesis or deletion
- Epenthesis requires Max ≫ DEP
- Deletion requires DEP ≫ Max
- Without further stipulations, expect the same repair for both configurations



A typological consequence of OT

- Consistency of ranking makes predictions about what combinations of processes a grammar contains
- Surprisingly, this prediction has not been tested extensively
- Perhaps promising that even with this limitation, OT has been as successful as it has been so far?



A caveat

- Example assumes a single relevant Max(C) constraint, and a single relevant DEP(V) constraint
- Several maneuvers available to tackle different repairs for different configurations
 - Generally preferred repair violates different M
- Example chosen to involve C₂=/I/ in both cases, similar contexts, etc., but even so one might imagine augmenting the constraint set to accommodate it
- Nonetheless, expect typological bias for unified repairs



"Simplicity" of rankings

Evaluation metrics in learning

The use of the evaluation metric in SPE

- · Given two grammars that are consistent with the data
- Choose the one that is 'valued' more highly by the evaluation metric

Is there an equivalent of this for OT constraint rankings?



Simplicity of rankings

One intuitive idea

- Grammars with fewer crucial rankings are simpler than grammars with more crucial rankings
 - A, B, C
 - A, B ≫ C
 - A ≫ B ≫ C

But: recall that we assume that all OT grammars are total rankings Tesar & Smolensky (2000)



Reinterpretation in terms of learning

- Learners use data to establish rankings, by adjusting the "strength" of constraints
 - · Crucial rankings demanded by the data
 - Perhaps additional rankings that happen to emerge during the course of learning, due to the way in which constraint strengths are adjusted
- Rankings between other constraints are arbitrary, and could differ from speaker to speaker, since data doesn't require/guarantee them
- Question: if the data is ambiguous between two grammars, does the learning procedure end up favoring one interpretation?
 - If so, this bias could shape the typology

An example: Stanton (2016)

- Data about stress placement may be ambiguous
 - Two analyses agree for short words, but make different predictions for (unseen) longer words
- Learning procedure may prefer one analysis over the other
- This analysis also corresponds to the typologically preferred pattern



Assigning stress without feet

 Constraints on position of stresses and intervals between them

Assign one * for each σ separating stress from the L/R ALIGN-L. ALIGN-R edge of the word NonFinality Assign one * for stress on the final σ *CLASH Assign one * for each sequence of two stressed σ 's *LAPSE Assign one * for each sequence of two stressless σ 's *LAPSE-L/R Assign one * if neither of the initial/final two σ 's is stressed *EXTENDLAPSE Assign one * for each sequence of three stressless σ 's *EXTLAPSE-L/R Assign one * if none of the initial/final three σ 's is stressed



Assigning stress without feet (cont.)

• E.g., antepenultimate stress

/σσσσσσ/	*ExtLapse(R)	*ExtLapse(L)	Align(L)	Align(R)
а. боооооо	*! W		L	***** W
b. σάσσσσσ	*! W		* L	**** W
с. σσόσσσσ	*! W		** L	**** W
d.	*! W	*	*** L	*** W
🖙 e. σσσσόσσ		*	****	**
f. σσσσσόσ		*	****! W	* L
д. σσσσσσσ		*	****!* W	L

- · The insight behind the analysis
 - Stress as far left as possible $(ALIGN(L) \gg ALIGN(R))$
 - But not more than 3σ from the end (ExtLapse(R) \gg ALIGN(L))

The midpoint pathology (Kager, 2012; Stanton, 2016)

 Short words: can satisfy both *(Extended)Lapse(L) and *(Extended)Lapse(R), by keeping stress towards the middle of the word

/σσ	σσσ	1	*ExtLapse(L)	*ExtLapse(R)
RF	a.	σσόσσ		I
	b.	σσσσσ	*! W	
	C.	σσσσσ		*! W

 Longer words: can't satisfy both, so satisfy the higher-ranked one with stress at the relevant edge

/σσσσσσσ/		σσ/	*ExtLapse(L)	*ExtLapse(R)
	a.	σσσόσσσ	*! W	*
IS .	b.	σσσσσσσ		*
	C.	σσσσσσσ	*! W	L

Example: a 'midpoint-stress' language

 $*ExtLapse(L) \gg *ExtLapse(R) \gg Align(L) \gg Align(R)$

- *ExtLapse(L/R) ≫ ALIGN(L/R): stress can move inside word to avoid extended lapse
- *ExtLapse(L) >> *ExtLapse(R): when too long to satisfy both, it moves to the left side of the word
- ALIGN(L) >> ALIGN(R): when on the left side of the word, it falls on the very first syllable



Comparing the grammars

- Antepenultimate (AP) stress
 - *ExtLapse(R) >> Align(L) >> Align(R)
 - *ExtLapse(R) ≫ *ExtLapse(L), but ranking of *ExtLapse(L) w.r.t. other constraints does not matter
- AP midpoint stress
 - *ExtLapse(L) \gg *ExtLapse(R) \gg Align(L) \gg Align(R)
 - Midpoint grammar requires additional crucial rankings
 - Question: if learners receive ambiguous data, would they favor a ranking consistent with AP stress?



Interpreting ambiguous data

AP stress		"AP" midpoi	nt
2 syl	σσ	2 syl	σσ
3 syl	σσσ	3 syl	σσσ
4 syl	σόσσ	4 syl	σόσσ
5 syl	σσόσσ	5 syl	σσόσσ
6 syl	σσσόσσ	6 syl	σσσσσσ
7 syl	σσσσόσσ	7 syl	σσσσσσσ



Interpreting ambiguous data

AP stress		"AP" midpoin	t
2 syl	σσ	2 syl	σσ
3 syl	σσσ	3 syl	σσσ
4 syl	σόσσ	4 syl	σόσσ
5 syl	σσόσσ	5 syl	σσόσσ

- The two patterns are ambiguous in words $<6\sigma$
- Question: what grammar would a learning algorithm prefer, given ambiguous data of this sort?
- We try first with Recursive Constraint Demotion
 - All constraints start out ranked equally
 - At each step, demote constraints that favor losers (L's)



Learning from short words: constraint demotion

/σσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
ເ ≅ a. όσ		İ	İ	*
b. σ ớ		 	* W	L
/σσσ/	*EVTL ADSE(L)	*ExtLapse(R)	ALICN(L)	ALICN(B)
70007	LATLAPSE(L)	LATEAPSE(IX)	ALIGN(L)	` '
☞ a. όσσ		l.	I	**
b. σόσ		I I	* W	* L
ς. σσό		1	** W	L
	II .=			
/σσσσ/	*EXTLAPSE(L)	· *ExtLapse(R)	ALIGN(L)	· ALIGN(R)
a.		* W	L	*** W
🖙 b. σόσσ		I I	*	**
ς. σσόσ		I L	** W	* L
d. σσσσ	* W	I	*** W	L
//	*[*\=\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	*Evel +===(D)	A / L \	Δ(D)
/σσσσσ/	EXTLAPSE(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
a. σσσσσ		* W	L	**** W
b. σόσσσ		* W	' * L	' *** W
🖙 c. σσόσσ		I I	**	**
d. σσσόσ	* W	I	*** W	* L
е. σσσσό	* W	l I	**** W	L

Learning from short words: constraint demotion

/σσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
🖙 a. όσ		l		*
b. σό		! !	* W	L
/σσσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
🖙 a. όσσ		I		**
b. σόσ		I I	* W	* L
ς. σσό		I	** W	L
	II			
/σσσσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
a. σσσσ		* W	L	*** W
🖙 b. σόσσ		l I	*	**
ς. σσόσ		I I	** W	* L
d. σσσό	* W	I	*** W	L
	II			
/σσσσσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
а. боооо		* W	L	**** W
b. σόσσσ		* W	* L	*** W
🖙 c. σσόσσ		I I	**	**
d. σσσόσ	* W	I	*** W	* L
е. σσσσσ	* W	l	**** W	L

Learning from short words: constraint demotion

/σσ/	*ExtLapse(L)	*ExtLapse(R)	ALIGN(L)	ALIGN(R)
🖙 a. όσ		İ		*
b. σό		 	* W	L
	+=			. (5)
/σσσ/	*EXTLAPSE(L)	*ExtLapse(R)	Align(L)	Align(R)
🖙 a. όσσ		ı		**
b. σόσ		I I	* W	* L
ς. σσό		I	** W	L
, ,	+F 1 (1)	' +E (D)	A (1)	A (D)
/σσσσ/	*EXTLAPSE(L)	*ExtLapse(R)	Align(L)	Align(R)
a. όσσσ		* W	L	*** W
🖙 b. σόσσ		I I	*	**
ς. σσόσ		1	** W	* L
d. σσσό	* W	! !	*** W	L
/σσσσσ/	*ExtLapse(L)	*ExtLapse(R)	Align(L)	ALIGN(R)
а. боооо		* W	L	**** W
b. σόσσσ		* W	* L	*** W
🖙 c. σσόσσ		I I	**	**
d. σσσόσ	* W		*** W	* L
е. σσσσό	* W	l I	**** W	L

Two possible refinements

* $ExtLapse(R) \gg *ExtLapse(L)$

/000000/	EXILAPSE(R)	EXILAPSE(L)	ALIGN(L)	ALIGN(R)
a. σσσσσσσσ	*! W		L	***** W
b. σάσσσσσ	*! W		* L	**** W
с. σσόσσσσ	*! W		** L	**** W
d. σσσόσσσ	*! W	*	*** L	*** W
^{ва} е. σσσσόσσ		*	****	**
f. σσσσσόσ		*	****! W	* L
д. σσσσσσσ		*	****!* W	L
, ,	*E!(D)	*F(1)	A /L)	A (D)
/σσσσσσσσ/	*ExtLapse(R)	*ExtLapse(L)	Align(L)	Align(R)
a. σσσσσσσσ	*! W	EXILAPSE(L)	ALIGN(L)	****** W
	` '	EXILAPSE(L)	* L	
a. σσσσσσσσ	*! W	EXILAPSE(L)		****** W
a. όσσσσσσσ b. σόσσσσσσ	*i W	*	* L	****** W
a. όσσσσσσσ b. σόσσσσσσ c. σσόσσσσσ	*i W *i W *i W		* L ** L	****** W ***** W ***** W
a. όσσσσσσσ b. σόσσσσσσ c. σσόσσσσσ d. σσσόσσσσ	*! W *! W *! W	*	* L ** L *** L	****** W ***** W ***** W
a. όσσσσσσσ b. σόσσσσσσ c. σσόσσσσσ d. σσσόσσσσ e. σσσσόσσσ	*! W *! W *! W	*	* L ** L *** L **** L	****** W ***** W **** W *** W

*Evel apos(B) *Evel apos(L) Augu(L) Augu(D)

Antepenultimate stress

$*ExtLapse(L) \gg *ExtLapse(R)$

	/σσσσσσ/	*ExtLapse(L)	*ExtLapse(R)	Align(L)	Align(R)
	ва: a. о́оооооо	« a. боооооо			*****
	b. σόσσσσσ		*	* W	***** L
	с. σσόσσσσ		*	** W	**** L
ı	d. σσσόσσσ	*! W	*	*** W	*** L
	е. σσσσόσσ	*! W	L	**** W	** L
	f. σσσσσόσ	*! W	L	**** W	* L
	д. σσσσσσσ	*! W	L	***** W	L
	/σσσσσσσ/	*ExtLapse(L)	*ExtLapse(R)	Align(L)	ALIGN(R)
	🖼 а. обооооооо		*		*****
	b. σόσσσσσσ		*	* W	***** L
ı	с. σσόσσσσσ		*	** W	***** L
	d. σσσόσσσσ	*! W	*	*** W	**** L
ı	e. σσσσόσσσ	*! W	*	**** W	*** L

Midpoint system

*I W

*! W

f. σσσσσόσσ a. σσσσσσόσ

h. σσσσσσσσά

2 syl σσ 5 syl σσσσσσ 3 syl σσσ 6 syl σσσσσσ 4 syl σσσσσ 7 syl σσσσσσσ



****** W

Ambiguity in short words

- Using RCD, learners exposed to ambiguous ($\leq 5\sigma$) data have no reason to prefer either consistent AP or AP midpoint stress
- Where does the antepenultimate bias come from?



The learning algorithm matters

- RCD doesn't explain antepenultimate bias, because in short words, *ExtLapse(L) and *ExtLapse(R) are 'W-only' constraints => remain highly ranked
- Stanton's conjecture: human learners actually use a ranking algorithm that doesn't just demote L's, but also promotes W's (??)



The learning algorithm matters (cont.)

- · Why this will help:
 - Short words give lots of evidence for ALIGN(L) ≫ ALIGN(R)
 - If the learner demotes ALIGN(R) and promotes ALIGN(L), then ALIGN(L) will end up above other markedness constraints
 - Similarly, 4–5σ provide evidence for *ExtLapse(R) »
 ALIGN(L), causing it to be promoted
 - Consequence: *ExtLapse(L) is 'left in the dust' (not promoted unless you get 6+ syllable words)



/σσ/	*ExtLapse(L)	*ExtLapse(R)	⊢ALIGN(L)	ALIGN(R)→
🖼 a. όσ		I	i	*
b. σ ớ		 	! * W	L
11	*[]	*F(D)		Λ(D)
/σσσ/	EXTLAPSE(L)	*ExtLapse(R)	! ←ALIGN(L)	I ALIGN(R)→
☞ a. όσσ		ı	ı	**
b. σόσ		I I	* W	' * L
ς. σσό		I	** W	L
	1 +=	· += .		(5)
/σσσσ/	*EXTLAPSE(L)	· *ExtLapse(R)	. ←ALIGN(L)	! ALIGN(R)→
a. όσσσ		* W	L	*** W
🖙 b. σόσσ		I I	*	**
ς. σσόσ		I I	** W	* L
d. σσσσ	* W	!	*** W	L
/σσσσσ/	*EVTLABOR(L)	*EXTLAPSE(R)	ALICN(L)	ALICN(P)
7000007	LATLAPSE(L)	<u> </u>	←ALIGN(L)	` ′
а. боооо		* W	L	**** W
b. σάσσσ		* W	* L	*** W
🖙 c. σσόσσ		I I	** !	! ** !
d. σσσόσ	* W	I I	*** W	* L
e. σσσσό	* W	i I	**** W	i 1

/σσ/	Align(L)←	*ExtLapse(L)	*ExtLapse(R)	\rightarrow Align(R)
🖙 a. όσ			I	*
b. σσ	* W		 	L
/σσσ/	ALIGN(L)←	*ExtLapse(L)	*ExtLapse(R)	\rightarrow Align(R)
🖙 a. όσσ			I	**
b. σόσ	* W		 	* L
ς. σσσ	** W		I	L
/σσσσ/	Align(L)←	*ExtLapse(L)	*ExtLapse(R)	\rightarrow Align(R)
a. σσσσ	L		* W	*** W
🖙 b. σόσσ	*		 	**
c. σσόσ	** W		 	* L
d. σσσό	*** W	* W	!	L
/σσσσσ/	ALIGN(L)←	*ExtLapse(L)	*ExtLapse(R)	→ALIGN(R)
a. σσσσσ	L		* W	**** W
b. σάσσσ	* L		* W	*** W
🖙 c. σσόσσ	**		I I	**
d. σσσόσ	*** W	* W	1	* L
e. σσσσσ	**** W	* W	i I	L

/σσ/	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	←*ExtLapse(R)	\leftarrow ALIGN(R) \rightarrow
🖙 a. όσ			I	*
b. σό	* W		 	L
/σσσ/	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	←*ExtLapse(R)	\leftarrow ALIGN(R) \rightarrow
🖙 a. όσσ			l	**
b. σόσ	* W		 	* L
ς. σσό	** W		I	L
/σσσσ/	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	←*ExtLapse(R)	\leftarrow Align(R) \rightarrow
a. σσσσ	L		* W	*** W
🖙 b. σόσσ	*		 	**
ς. σσόσ	** W		 	* L
d. σσσό	*** W	* W	I	L
/σσσσσ/	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	←*ExtLapse(R)	\leftarrow ALIGN(R) \rightarrow
a. σσσσσ	L		* W	**** W
b. σόσσσ	* L		* W	*** W
🖙 c. σσόσσ	**		I I	**
d. σσσόσ	*** W	* W	1	* L
е. σσσσσ	**** W	* W	i I	L

/σσ/	*ExtLapse(R)←	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	\leftarrow Align(R) \rightarrow
🖙 a. όσ				*
b. σớ		* W		L
/σσσ/	*ExtLapse(R)←	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	\leftarrow Align(R) \rightarrow
🖙 α. όσσ				**
b. σόσ		* W		* L
ς. σσό		** W		L
/σσσσ/	*ExtLapse(R)←	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	\leftarrow Align(R) \rightarrow
a. σσσσ	* W	L		*** W
🖙 b. σόσσ		*		**
ς. σσόσ		** W		* L
d. σσσό		*** W	* W	L
/σσσσσ/	*ExtLapse(R)←	\leftarrow Align(L) \rightarrow	*ExtLapse(L)	\leftarrow Align(R) \rightarrow
а. боооо	* W	L		**** W
b. σόσσσ	* W	* L		*** W
🖙 c. σσόσσ		**		**
d. σσσόσ		*** W	* W	* L
е. σσσσό		**** W	* W	L



Stepping back: the approach, more generally

- Some unattested systems may be possible to capture grammatically, but are difficult to learn
- Goal: theory of grammatical learning that predicts that learners, when exposed to typical input from a 'difficult' pattern, systematically misacquire it as a different, more commonly attested pattern
- Potential to explain not only unattested systems, but also rare systems (which we can't exclude as impossible grammars, anyway)
- Converging evidence: acquisition data, learning in the lab?

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