

COMP 550  
Algorithms and Analysis  
Spring 2020  
Pop Quiz 5

Don't forget to write your name on the quiz sheet.

1. Suppose  $X$  is an indicator variable for the occurrence of an event  $e$  and  $Y$  is an indicator variable for the event that  $e$  does not occur. Express  $Y$  in terms of  $X$ . Suppose  $Y = aX + b$ . Fill in the blanks with the values of  $a$  and  $b$ .

- a) Value of  $a$ : -1  
b) Value of  $b$ : 1

2. Suppose  $X$  is a random variable and the probability that  $X = 0$  is .2, the probability that  $X = 0.5$  is .5, and the probability that  $X = 1$  is .3. What is  $E[X]$ , the expected value of  $X$ ? .55

3. If  $X$  and  $Y$  are random variables, is it always true that  $E[X + Y] = E[X] + E[Y]$ ?  
true

4. If  $X$  and  $Y$  are random variables, is it always true that  $E[X * Y] = E[X] * E[Y]$ ?  
false

5. If  $X$  is a random variable and  $c$  is a real number, is it always true that  $E[cX] = cE[X]$ ?  
true

6. If  $X$  and  $Y$  are independent random variables, is it always true that  $E[X * Y] = E[X] * E[Y]$ ? true

7. Suppose  $X$  is an indicator variable for an event  $e$  and the probability that  $e$  will happen is 0.6. What is  $E[X]$ ? .6

8. Suppose  $X_i$  for  $1 \leq i \leq 10$  are indicator variables for the  $i^{th}$  toss of a coin yielding "heads." Let  $Y$  be a random variable for the number of times heads will occur on the even tosses, that is, tosses number 2,4,6,8,10. Express  $Y$  in terms of the indicator variables  $X_i$ . Choose the best answer.

- a)  $Y = X_1 + X_2 + \dots + X_{10}$   
b)  $Y = X_1 + X_3 + X_5 + X_7 + X_9$   
**c)  $Y = X_2 + X_4 + X_6 + X_8 + X_{10}$**   
d)  $Y = X_2 - X_1 + X_3 - X_2 + \dots + X_{10} - X_9$