$\begin{array}{c} {\rm COMP~550} \\ {\rm Algorithms~and~Analysis} \\ {\rm Spring~2020} \\ {\rm Pop~Quiz~3} \end{array}$

Don't forget to write your name on the quiz sheet.

1. Consider the recurrence relation $T(n) = 2T(n-1) + T(n-2)$ for $n \geq 2$, $T(0) = 1$, $T(1) = 2$. Compute $T(2)$, $T(3)$, $T(4)$, $T(5)$, and $T(6)$. Fill in the blanks a), b), c), d), e) with the values in order.
A fair die when tossed will give each of the values 1 through 6 with equal probability. The plural of die is $dice$.
2. Suppose two fair dice are tossed. What is the probability that they will produce equal values?
3. Suppose two fair dice, called A and B, are tossed. What is the probability that A will produce a larger value than B?
4. Suppose two fair dice are tossed. What is the probability that the sum of their values will equal 7?
5. Suppose two fair dice are tossed. What is the probability that the sum of their values will equal 6?
3. What is the expected number of heads if a fair coin is tossed 20 times?
7. What is the expected value for a single toss of a fair die?
8. What is the expected value for the sum of two tosses of a fair die?
9. Suppose someone tosses a fair coin 10 times. What is the probability that all tosses will result in the same outcome, that is, all tosses will be heads or all tosses will be tails?
10. What is the sum of the series $1/2 + 2/4 + 3/8 + 4/16 + \dots$?