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[> with(*LinearAlgebra*)  
[&x, Add, Adjoint, BackwardSubstitute, BandMatrix, Basis, BezoutMatrix, BidiagonalForm, BilinearForm, CharacteristicMatrix, CharacteristicPolynomial, Column, ColumnDimension, ColumnOperation, ColumnSpace, CompanionMatrix, ConditionNumber, ConstantMatrix, ConstantVector, Copy, CreatePermutation, CrossProduct, DeleteColumn, DeleteRow, Determinant, Diagonal, DiagonalMatrix, Dimension, Dimensions, DotProduct, EigenConditionNumbers, Eigenvalues, Eigenvectors, Equal, ForwardSubstitute, FrobeniusForm, GaussianElimination, GenerateEquations, GenerateMatrix, Generic, GetResultDataType, GetResultShape, GivensRotationMatrix, GramSchmidt, HankelMatrix, HermiteForm, HermitianTranspose, HessenbergForm, HilbertMatrix, HouseholderMatrix, IdentityMatrix, IntersectionBasis, IsDefinite, IsOrthogonal, IsSimilar, IsUnitary, JordanBlockMatrix, JordanForm, KroneckerProduct, LA\_Main, LUdecomposition, LeastSquares, LinearSolve, LyapunovSolve, Map, Map2, MatrixAdd, MatrixExponential, MatrixFunction, MatrixInverse, MatrixMatrixMultiply, MatrixNorm, MatrixPower, MatrixScalarMultiply, MatrixVectorMultiply, MinimalPolynomial, Minor, Modular, Multiply, NoUserValue, Norm, Normalize, NullSpace, OuterProductMatrix, Permanent, Pivot, PopovForm, QRdecomposition, RandomMatrix, RandomVector, Rank, RationalCanonicalForm, ReducedRowEchelonForm, Row, RowDimension, RowOperation, RowSpace, ScalarMatrix, ScalarMultiply, ScalarVector, SchurForm, SingularValues, SmithForm, StronglyConnectedBlocks, SubMatrix, SubVector, SumBasis, SylvesterMatrix, SylvesterSolve, ToeplitzMatrix, Trace, Transpose, TridiagonalForm, UnitVector, VandermondeMatrix, VectorAdd, VectorAngle, VectorMatrixMultiply, VectorNorm, VectorScalarMultiply, ZeroMatrix, ZeroVector, Zip]

(1

[>  
[> logPCM := Matrix([[0, a12, a13, a14, a15 ], [-a12, 0, a23, a24, a25], [ -a13, -a23, 0, a34, a35], [ -a14, -a24, -a34, 0, a45 ], [ -a15, -a25, -a35, -a45, 0 ]]);

$$\log PCM := \begin{bmatrix} 0 & a_{12} & a_{13} & a_{14} & a_{15} \\ -a_{12} & 0 & a_{23} & a_{24} & a_{25} \\ -a_{13} & -a_{23} & 0 & a_{34} & a_{35} \\ -a_{14} & -a_{24} & -a_{34} & 0 & a_{45} \\ -a_{15} & -a_{25} & -a_{35} & -a_{45} & 0 \end{bmatrix}$$

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$$\left( \begin{array}{cccccccccc} 0 & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 0 & 1 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 1 & 0 & 0 & 0 & 1 & 1 \end{array} \right)$$

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WeightVectors := Matrix(125, 5, [[0, 0, 0, 0, 0]]):
for tindex from 1 to 125 do
AdjMatT := Matrix( [[0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0]]):
DEGR := Matrix( [[0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0], [0, 0, 0, 0, 0]]):
t := T[tindex]:
if t[1] = 1 then AdjMatT[1, 2] := 1: AdjMatT[2, 1] := 1: end if:
if t[2] = 1 then AdjMatT[1, 3] := 1: AdjMatT[3, 1] := 1: end if:
if t[3] = 1 then AdjMatT[1, 4] := 1: AdjMatT[4, 1] := 1: end if:
if t[4] = 1 then AdjMatT[1, 5] := 1: AdjMatT[5, 1] := 1: end if:
if t[5] = 1 then AdjMatT[2, 3] := 1: AdjMatT[3, 2] := 1: end if:
if t[6] = 1 then AdjMatT[2, 4] := 1: AdjMatT[4, 2] := 1: end if:
if t[7] = 1 then AdjMatT[2, 5] := 1: AdjMatT[5, 2] := 1: end if:
if t[8] = 1 then AdjMatT[3, 4] := 1: AdjMatT[4, 3] := 1: end if:
if t[9] = 1 then AdjMatT[3, 5] := 1: AdjMatT[5, 3] := 1: end if:
if t[10] = 1 then AdjMatT[4, 5] := 1: AdjMatT[5, 4] := 1: end if:

for indexi from 1 to 5 do
s := 0:
for indexj from 1 to 5 do
s := s + AdjMatT[indexi, indexj]:
end do:
DEGR[indexi, indexi] := s:
end do:
L := DEGR - AdjMatT:
Lti := DeleteRow(DeleteColumn(L, 1), 1):

logIPCM := logPCM ~ AdjMatT:
logRHS := Vector([0, 0, 0, 0]):
for indexi from 2 to 5 do
s := 0:
for indexj from 1 to 5 do
s := s + logIPCM[indexi, indexj]:
end do:
logRHS[indexi - 1] := s:
end do:
logwT := MatrixVectorMultiply(MatrixInverse(Lti), logRHS):
WeightVectors[tindex, 1 ..] := Transpose(Vector([0, logwT])):
end do:
interface(rtablesiz = 125):

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*WeightVectors*

0	$a_{25} - a_{15}$	$a_{35} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$a_{34} + a_{45} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$a_{35} - a_{15}$	$-a_{34} + a_{35} - a_{15}$	$-a_{15}$
0	$a_{24} + a_{45} - a_{15}$	$a_{35} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{24} + a_{45} - a_{15}$	$a_{34} + a_{45} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{24} - a_{34} + a_{35} - a_{15}$	$a_{35} - a_{15}$	$-a_{34} + a_{35} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$a_{35} - a_{15}$	$-a_{24} + a_{25} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$-a_{24} + a_{25} + a_{34} - a_{15}$	$-a_{24} + a_{25} - a_{15}$	$-a_{15}$
0	$a_{23} + a_{35} - a_{15}$	$a_{35} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{23} + a_{34} + a_{45} - a_{15}$	$a_{34} + a_{45} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{23} + a_{35} - a_{15}$	$a_{35} - a_{15}$	$-a_{34} + a_{35} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$-a_{23} + a_{25} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$-a_{23} + a_{25} - a_{15}$	$-a_{23} + a_{25} - a_{34} - a_{15}$	$-a_{15}$
0	$a_{24} + a_{45} - a_{15}$	$-a_{23} + a_{24} + a_{45} - a_{15}$	$a_{45} - a_{15}$	$-a_{15}$
0	$a_{23} + a_{35} - a_{15}$	$a_{35} - a_{15}$	$a_{23} - a_{24} + a_{35} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{15}$	$-a_{23} + a_{25} - a_{15}$	$-a_{24} + a_{25} - a_{15}$	$-a_{15}$
0	$a_{25} - a_{14} - a_{45}$	$a_{35} - a_{14} - a_{45}$	$-a_{14}$	$-a_{14} - a_{45}$
0	$a_{25} - a_{14} - a_{45}$	$a_{34} - a_{14}$	$-a_{14}$	$-a_{14} - a_{45}$
0	$a_{25} + a_{34} - a_{35} - a_{14}$	$a_{34} - a_{14}$	$-a_{14}$	$a_{34} - a_{35} - a_{14}$
0	$a_{24} - a_{14}$	$a_{35} - a_{14} - a_{45}$	$-a_{14}$	$-a_{14} - a_{45}$
0	$a_{24} - a_{14}$	$a_{34} - a_{14}$	$-a_{14}$	$-a_{14} - a_{45}$
0	$a_{24} - a_{14}$	$a_{34} - a_{14}$	$-a_{14}$	$a_{34} - a_{35} - a_{14}$
0	$a_{24} - a_{14}$	$a_{24} - a_{25} + a_{35} - a_{14}$	$-a_{14}$	$a_{24} - a_{25} - a_{14}$
0	$a_{24} - a_{14}$	$a_{34} - a_{14}$	$-a_{14}$	$a_{24} - a_{25} - a_{14}$
0	$a_{23} + a_{35} - a_{14} - a_{45}$	$a_{35} - a_{14} - a_{45}$	$-a_{14}$	$-a_{14} - a_{45}$

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