Complete the truth tables.

1.

| P | Q | $Q \wedge Q$ | $\neg Q$ | $P \wedge (Q \wedge Q)$ | $[P \land (Q \land Q)] \lor \neg Q$ | $\neg \{ [P \land (Q \land Q)] \lor \neg Q \}$ | $\neg\neg\{[P\land(Q\land Q)]\lor\neg Q\}$ |
|----------------|----------------|--------------|----------------|-------------------------|-------------------------------------|--|--|
| T | T | T | F | T | T | F | T |
| \overline{F} | \overline{T} | | \overline{F} | F | F | <u></u> | <u>F</u> |
| \overline{T} | \overline{F} | | | $\overline{\mathbb{F}}$ | T | \overline{F} | |
| \overline{F} | \overline{F} | | | | | $\overline{\mathbb{F}}$ | |

2.

| P = Q | $R \mid P \wedge Q$ | $R \wedge P$ | $(R \wedge P) \wedge Q$ | $[(R \land P) \land Q] \land (P \land Q)$ | $\neg\{[(R \land P) \land Q] \land (P \land Q)\}$ | $\neg\neg\{[(R \land P) \land Q] \land (P \land Q)\}$ |
|-----------|-------------------------------|--------------|-------------------------|--|---|---|
| (T) (T) (| ① ① | T | T | $\!$ | F | \bigcirc |
| F 7 | (T) - (F) | F - | \overline{F} | \overline{F} | <u> </u> | (F) |
| T F (| (T) - (F) | (T) | [E | F | | F |
| F (F) | (T) - (F) | (F) | [E | F | | F |
| T T | $\bar{F} = \bar{T} = \bar{T}$ | F | \overline{F} | <i>F</i> | \overline{T} | \overline{F} |
| F 7 | \widehat{F} | (F) | \mathbb{F}^{-} | \overline{F} | <u> </u> | \mathbb{P}^{-} |
| T F | \widehat{F} | F - | \mathbb{F}^{-} | \overline{F} | <u> </u> | \mathbb{P}^{-} |
| | $\mathbb{E}[\mathbb{E}]$ | | | <u></u> | $oxed{\mathbb{D}}$ | (F) |

3.

| Q = R | $Q \vee R$ | $\neg Q$ | $\neg(Q \lor R)$ | $\neg \neg Q$ | $\neg\neg(Q\lor R)$ | $\neg\neg(Q\lor R)\lor\neg\neg Q$ |
|----------------|------------|----------------|---|----------------|---------------------|-----------------------------------|
| | T | F | F | \bigcirc | T | T |
| \overline{E} | | | <u>-</u> | \overline{F} | | |
| \overline{T} | | \overline{F} | - - - - | | T | |
| \overline{F} | | | | \overline{F} | \overline{F} | |

4.

| $P Q R \mid Q \lor P \mid R \lor Q \mid Q \land (Q \lor P) \mid \neg (R \lor Q) \mid [Q \land (Q \lor P)] \land Q \parallel \{[Q \land (Q \lor P)] \land Q\} \lor Q \land Q \lor Q$ | $\checkmark \neg (R \lor Q)$ |
|--|------------------------------|
| | |
| $egin{array}{c c c c c c c c c c c c c c c c c c c $ | |
| | |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
| | |
| \overline{F} \overline{T} \overline{F} \overline{T} \overline{T} \overline{T} \overline{T} \overline{T} | |
| | |
| \overline{F} | |

5.

| P | Q | R | $P \wedge R$ | $Q \wedge P$ | $R \wedge P$ | $(Q \land P) \land (P \land R)$ | $ \neg(R \land P) $ | $ \neg (R \land P) \lor [(Q \land P) \land (P \land R)] $ |
|----------------|----------------|-------------------------|----------------|----------------|----------------|---|---------------------|---|
| \overline{T} | \bigcirc | \bigcirc | T | T | T | T | F | \bigcirc |
| \overline{F} | \bar{T} | \overline{T} | \overline{F} | \overline{F} | \overline{F} | \overline{F} | | $\overline{\mathbb{T}}$ |
| T^{-} | \overline{F} | | T | \overline{F} | | \overline{F} | \overline{F} | $\overline{\mathbb{F}}$ |
| \bar{F} | \overline{F} | | \overline{F} | \overline{F} | - F - | $\overline{\mathbb{F}}$ | | <u> </u> |
| T | \overline{T} | \overline{F} | \overline{F} | T - T | | [<u>F</u> | [<u>T</u> | <u> </u> |
| \bar{F} | \bar{T} | \overline{F} | F | \overline{F} | F | \overline{F} | | <u> </u> |
| T^{-} | \overline{F} | \overline{F} | \overline{F} | \overline{F} | <u>F</u> | [<u>F</u> | | <u> </u> |
| \overline{F} | <u></u> | $\overline{\mathbb{E}}$ | | | | $\left[egin{array}{cccccccccccccccccccccccccccccccccccc$ | | |

| P | Q | R | $Q \lor P$ | $P \wedge P$ | $P \wedge Q$ | $(Q \vee P) \vee R$ | $(P \wedge P) \vee (P \wedge Q)$ | $[(P \land P) \lor (P \land Q)] \land [(Q \lor P) \lor R]$ |
|----------------|----------------|----------------|-------------------------|---------------|----------------|--|----------------------------------|--|
| \overline{T} | \bigcirc | \bigcirc | T | T | T | T | T | T |
| F | \bar{T} | \bar{T} | $ \bar{T} \bar{T} $ | $ \bar{F} $ | \overline{F} | T | F | \overline{F} |
| \overline{T} | \overline{F} | \overline{T} | - T | - T | (F) | | | |
| F | \overline{F} | \bar{T} | $ \bar{F} $ | F | \overline{F} | T = T = T | F | \overline{F} |
| \overline{T} | \overline{T} | \overline{F} | - T | - T | <u> </u> | | | |
| F | T^{-} | \bar{F} | $ \bar{T} - \bar{T} $ | $ \bar{F} $ | \overline{F} | T | $\lceil F \rceil$ | \overline{F} |
| \overline{T} | | \overline{F} | - T | - T | <u> </u> | | [<u></u> | |
| \overline{F} | \overline{F} | | | | | $egin{bmatrix} egin{bmatrix} \egn{bmatrix} \e$ | | |

| P | Q | $P \vee Q$ | $Q \wedge P$ | $\neg P$ | $\neg P \lor (Q \land P)$ | $\neg(P \lor Q)$ | $\left \left[\neg P \lor (Q \land P) \right] \land \neg (P \lor Q) \right.$ |
|----------------|----------------|----------------|----------------|----------------|---------------------------|------------------|---|
| T | \bigcirc | T | T | F | T | F | F |
| \bar{F} | \bar{T} | \bar{T} | \overline{F} | \bar{T} | T = T = T | \overline{F} | \overline{F} |
| T^{-} | \overline{F} | T | \overline{F} | \overline{F} | \overline{F} | \overline{F} | \overline{F} |
| \overline{F} | \overline{F} | \overline{F} | \overline{F} | T | \overline{T} | \bar{T} | T |

8.

| P | Q | R | $P \wedge Q$ | $Q \wedge R$ | $\neg R$ | $(Q \wedge R) \vee (P \wedge Q)$ | $\neg \neg R$ | $\neg\neg R \lor [(Q \land R) \lor (P \land Q)]$ |
|----------------|----------------|-------------------------|----------------|----------------|----------------|----------------------------------|------------------|--|
| \overline{T} | \overline{T} | \overline{T} | T | T | F | \bigcirc{T} | | T |
| \overline{F} | \overline{T} | \overline{T} | \overline{F} | T^{-} | \overline{F} | <u></u> | | \overline{T} |
| T^{-} | \overline{F} | $\overline{\mathbb{T}}$ | \overline{F} | \overline{F} | \overline{F} | <u>- F</u> | | \overline{T} |
| \overline{F} | \overline{F} | \overline{T} | F | \overline{F} | \overline{F} | <u>-</u> | | |
| T^{-} | \overline{T} | \overline{F} | T | \overline{F} | T^{-} | | $ \overline{F} $ | |
| \bar{F} | \bar{T} | \overline{F} | F | _F | T^{-} | <u> </u> | Ē | \overline{F} |
| T^{-} | \overline{F} | \overline{F} | F | \overline{F} | T^{-} | | $ \overline{F} $ | \overline{F} |
| \overline{F} | \overline{F} | \overline{F} | \overline{F} | \overline{F} | T^{-} | | $ \overline{F} $ | \overline{F} |

9.

| P | Q | R | $P \lor Q$ | $Q \wedge Q$ | $\neg R$ | $\neg \neg R$ | $\neg \neg R \land (P \lor Q)$ | $ (Q \land Q) \land [\neg \neg R \land (P \lor Q)] $ |
|----------------|----------------|----------------|--|----------------|----------|---------------|--------------------------------|--|
| T | \bigcirc | \bigcirc | T | T | F | T | T | T |
| \overline{F} | \overline{T} | \overline{T} | T = T | | | T | | |
| T | \overline{F} | \overline{T} | \bar{T} | \overline{F} | | T - | | \overline{F} |
| \overline{F} | \overline{F} | \overline{T} | \bar{F} | - F | (F) | T T | F | F |
| \overline{T} | \overline{T} | \overline{F} | $ - \bar{T} - \bar{T} $ | - T | (T) | F - | F | F |
| \overline{F} | \overline{T} | \overline{F} | $ - \bar{T} - \bar{T} $ | T - T | (T) | F - | F | F |
| \overline{T} | \overline{F} | \overline{F} | $ - \bar{T} - \bar{T} $ | - Ē | (T) | F - | [<u>F</u> | F |
| \overline{E} | \overline{F} | | $\begin{bmatrix} - & -\bar{F} & - & - \\ - & -\bar{F} & - & - \end{bmatrix}$ | | | | | |

10.

| P | Q | R | $R \wedge Q$ | $\neg P$ | $\neg(R \land Q)$ | $\neg \neg P$ | $\neg \neg (R \land Q)$ | $\neg \neg (R \land Q) \land \neg \neg P$ |
|----------------|----------------|----------------|--------------|----------------|-------------------|---------------|---|---|
| \overline{T} | \bigcirc | \bigcirc | T | F | F | T | T | T |
| \overline{F} | \overline{T} | \bar{T} | | | \overline{F} | | | \overline{F} |
| \overline{T} | \overline{F} | \overline{T} | F | | | | [- - - | F |
| \overline{F} | \overline{F} | \overline{T} | - <u>-</u> F | | <u>-</u> | (F) | [- - - - | F |
| \overline{T} | \overline{T} | \overline{F} | - F | \overline{F} | <u>-</u> | | \overline{F} | F |
| \overline{F} | \overline{T} | \overline{F} | - <u>-</u> F | \overline{T} | <u>T</u> | (F) | [- - - - | F |
| \overline{T} | \overline{F} | \overline{F} | - F | \overline{F} | <u>-</u> | | [- - - - | F |
| \overline{F} | \overline{F} | | | | | | | |

| P | Q | R | $P \lor P$ | $\neg P$ | $\neg R$ | $(P \lor P) \lor Q$ | $\neg P \land \neg R$ | $ (\neg P \land \neg R) \land [(P \lor P) \lor Q] $ |
|----------------|----------------|----------------|--------------|----------------|----------------|---------------------|-----------------------|---|
| T | T | T | T | F | F | T | F | F |
| \overline{F} | T^{-} | \bar{T} | $ \bar{F} $ | \bar{T} | \overline{F} | \bar{T} | \overline{F} | \overline{F} |
| T | \overline{F} | \bar{T} | $ -\bar{T} $ | \bar{F} | \bar{F} | \overline{T} | \overline{F} | \overline{F} |
| \overline{F} | \overline{F} | \bar{T} | $ \vec{F} $ | \bar{T} | \bar{F} | \overline{F} | \overline{F} | \overline{F} |
| \overline{T} | \overline{T} | \overline{F} | <u>T</u> | \overline{F} | \overline{T} | | \overline{F} | \overline{F} |
| \overline{F} | \bar{T} | \bar{F} | $ \bar{F} $ | \bar{T} | T^{-} | \bar{T} | T - T - T | $ \bar{T} $ |
| \overline{T} | \overline{F} | \overline{F} | <u>(T)</u> | \overline{F} | | | \overline{F} | \overline{F} |
| \overline{F} | \overline{F} | | | | | | | |

| P | R | $R \vee R$ | $P \wedge P$ | $(R \vee R) \vee R$ | $(P \wedge P) \wedge R$ | $\neg[(R \lor R) \lor R]$ | $\neg [(R \lor R) \lor R] \land [(P \land P) \land R]$ |
|----------------|--|------------|---------------------------------------|---------------------|-------------------------|---------------------------|--|
| \overline{T} | \bigcirc | \bigcirc | T | T | T | F | F |
| $\bigcirc F$ | | | | | \overline{F} | $oxed{\mathbb{F}}$ | <u> </u> |
| \bigcirc | (F) | | | (F) | <u> </u> | | (F) |
| \overline{F} | $_{-}$ | | $\lfloor \underline{\hat{F}} \rfloor$ | | | | $oxed{\mathbb{F}}$ |

13.

| P | Q | R | $P \wedge P$ | $R \wedge Q$ | $(R \land Q) \lor (P \land P)$ | $\neg(R \land Q)$ | $\neg (R \land Q) \lor [(R \land Q) \lor (P \land P)]$ |
|----------------|----------------|----------------|----------------|--------------|--------------------------------|-------------------|--|
| \overline{T} | \bigcirc | \bigcirc | T | T | T | F | \bigcirc |
| \overline{F} | \overline{T} | \bar{T} | \overline{F} | | | \overline{F} | |
| T | \overline{F} | \overline{T} | - T | - <u>-</u> | | T T | |
| \overline{F} | \overline{F} | \overline{T} | - <u>F</u> | - Ē | F | | |
| T | \overline{T} | \overline{F} | - T | - Ē | T T | | |
| \overline{F} | \overline{T} | \overline{F} | - F | - <u>F</u> | F | | |
| T | \overline{F} | \overline{F} | - T | - Ē | | | |
| \overline{F} | \overline{F} | | | | | | |

14.

| P | R | $R \wedge P$ | $\neg P$ | $\neg(R \land P)$ | $\neg \neg P$ | $\neg \neg (R \wedge P)$ | $\neg\neg(R \land P) \land \neg\neg P$ |
|----------------|----------------|--------------|----------------|-------------------|----------------|--------------------------|--|
| \overline{T} | \bigcirc | \bigcirc | F | F | T | T | T |
| \overline{F} | \overline{T} | | | | \overline{F} | $ \widehat{F} $ | F |
| \overline{T} | \overline{F} | | \overline{F} | | | [E] | F |
| \overline{F} | \overline{F} | | | | \overline{F} | <u>F</u> | F |

15.

| P | Q | R | $R \wedge P$ | $\neg R$ | $\neg R \wedge (R \wedge P)$ | $Q \wedge [\neg R \wedge (R \wedge P)]$ | $\neg \{Q \land [\neg R \land (R \land P)]\}$ | $\neg \neg \{Q \land [\neg R \land (R \land P)]\}$ |
|----------------|----------------|----------------|--------------|-----------|------------------------------|---|---|--|
| \overline{T} | | \bigcirc | _ | F | F | F | \bigcirc | F |
| | \overline{T} | \overline{T} | | \bar{F} | \overline{F} | $\overline{\mathbb{F}}$ | $\overline{\mathbb{T}}$ | \overline{F} |
| | \overline{F} | _(T)_ | | \bar{F} | \overline{F} | F | $\overline{\mathbb{T}}$ | \overline{F} |
| \overline{F} | \overline{F} | \overline{T} | <u>F</u> | \bar{F} | <u>F</u> | F | | \overline{F} |
| | | | | \bar{T} | <u>F</u> | F | | \overline{F} |
| \overline{F} | | | | \bar{T} | <u>F</u> | F | $\overline{\mathbb{T}}$ | <u> </u> |
| | \overline{F} | \overline{F} | - Ē | \bar{T} | <u>F</u> | F | | \overline{F} |
| \overline{F} | \overline{F} | \bar{F} | | \bar{T} | | | | $\overline{\mathbb{F}}$ |

| P | R | $P \lor P$ | $\neg R$ | $P \wedge \neg R$ | $\neg(P \lor P)$ | $(P \land \neg R) \lor \neg (P \lor P)$ | $\neg[(P \land \neg R) \lor \neg(P \lor P)]$ |
|----------------|-----------|----------------|----------------|-------------------|------------------|---|--|
| T | T | T | F | F | F | F | T |
| \overline{F} | \bar{T} | \overline{F} | \overline{F} | (F) | T | T | \overline{F} |
| T^{-} | \bar{F} | T^{-} | T | | \overline{F} | T | \overline{F} |
| \overline{F} | \bar{F} | | T | | T | $\begin{bmatrix} & & & & & & & & & & & & & & & & & & &$ | |

| P | R | $P \vee R$ | $R \vee R$ | $R \wedge P$ | $(R \wedge P) \vee (P \vee R)$ | $ \neg[(R \land P) \lor (P \lor R)] $ | $\neg[(R \land P) \lor (P \lor R)] \lor (R \lor R)$ |
|----------------|----------------|------------|----------------|----------------|--------------------------------|---------------------------------------|---|
| \overline{T} | \bigcirc | T | \bigcirc | \bigcirc | T | F | T |
| \overline{F} | \overline{T} | | | \overline{F} | | \overline{F} | $\overline{\mathbb{T}}$ |
| \overline{T} | \overline{F} | | \overline{F} | \overline{F} | \overline{T} | $\overline{\mathbb{F}}$ | \overline{F} |
| \overline{E} | \overline{F} | | | | <u> </u> | | |

18.

| P | Q | R | $P \vee R$ | $\neg Q$ | $(P \lor R) \lor R$ | $P \wedge \neg Q$ | $\neg[(P \lor R) \lor R]$ | $\neg[(P \lor R) \lor R] \lor (P \land \neg Q)$ |
|----------------|----------------|----------------|--------------------------|----------------|---------------------|-------------------|---------------------------|---|
| \overline{T} | \bigcirc | \bigcirc | T | F | T | F | F | F |
| \overline{F} | \overline{T} | \overline{T} | | \overline{F} | | <u>F</u> | [<u>F</u> | \overline{F} |
| T | \overline{F} | \bar{T} | $ -\bar{T} - \bar{T} $ | \bar{T} | T | _T | \overline{F} | \overline{T} |
| \overline{F} | \overline{F} | \overline{T} | - T | \overline{T} | <u> </u> | <u>F</u> | [<u>F</u> | \widehat{F} |
| \overline{T} | \overline{T} | \overline{F} | - T | (F) | T | <u>F</u> | [<u>F</u> | \widehat{F} |
| \overline{F} | \overline{T} | \overline{F} | - Ē | \overline{F} | F | <u>F</u> | <u>T</u> | |
| \overline{T} | \overline{F} | \overline{F} | | (T) | T | <u>T</u> | F | |
| \overline{F} | \overline{F} | | | | | \overline{F} | | |

19.

| Q | R | $\neg R$ | $\neg R \land Q$ | $\neg \neg R$ | $\neg\neg\neg R$ | $\neg \neg \neg R \land (\neg R \land Q)$ |
|----------------|----------------|----------------|------------------|---------------|------------------|---|
| \overline{T} | \bigcirc | F | F | T | F | F |
| \overline{F} | \overline{T} | \overline{F} | <u>F</u> | | \overline{F} | F |
| T | \overline{F} | | <u> </u> | | | <u> </u> |
| \overline{F} | \overline{F} | | | | | |

20.

| Q | R | $Q \vee R$ | $Q \wedge R$ | $R \wedge R$ | $(Q \vee R) \vee (Q \wedge R)$ | $(R \wedge R) \vee Q$ | $ [(Q \lor R) \lor (Q \land R)] \land [(R \land R) \lor Q] $ |
|----------------|-----------|----------------|----------------|--------------|--------------------------------|-----------------------|--|
| \overline{T} | T | T | T | T | T | T | T |
| \overline{F} | \bar{T} | T | \overline{F} | | T | T | |
| T^{-} | \bar{F} | T^{-} | <u>F</u> | | T | T | |
| \overline{F} | \bar{F} | \overline{F} | \overline{F} | - Ē | \overline{F} | \overline{F} | F |

21.

| P | Q | R | $R \wedge P$ | | | $\neg P \lor (R \land P)$ | $Q \wedge [\neg P \vee (R \wedge P)]$ | $ \neg Q \lor \{Q \land [\neg P \lor (R \land P)]\} $ |
|----------------|----------------|----------------|---|----------------|--|---------------------------|--|---|
| \overline{T} | \bigcirc | \bigcirc | \bigcirc | F | F | T | T | \bigcirc |
| \overline{F} | \overline{T} | \overline{T} | \overline{F} | \overline{T} | \overline{F} | T T | | $ \overline{\mathcal{T}} $ |
| \overline{T} | \overline{F} | \overline{T} | - T | \overline{F} | \overline{T} | $\overline{\mathbb{T}}$ | \overline{F} | $\overline{\mathcal{T}}$ |
| F | \overline{F} | \bar{T} | \bar{F} | \bar{T}^{-} | \bar{T} | T | \bar{F} | T |
| \overline{T} | \overline{T} | \overline{F} | <u>F</u> | \overline{F} | \overline{F} | F | F | \widehat{F} |
| \overline{F} | \overline{T} | \overline{F} | - Ē | \overline{T} | \overline{F} | T | | |
| T | \overline{F} | \bar{F} | \bar{F} | \bar{F} | \bar{T} | \overline{F} | \overline{F} | \overline{T} |
| F_{-} | \overline{F} | \bar{F} | $\begin{bmatrix} - & - & \overline{F} & - & - \\ - & F & - & - \end{bmatrix}$ | \bar{T} | $\begin{bmatrix} T \\ T \end{bmatrix}$ | T | $egin{bmatrix}ar{F} & \ ar{F} & \ \end{bmatrix}$ | $ \overline{T} $ |

| P | R | $P \vee P$ | $P \wedge P$ | $\neg P$ | $(P \lor P) \land R$ | $(P \wedge P) \wedge \neg P$ | $ [(P \land P) \land \neg P] \lor [(P \lor P) \land R] $ |
|----------------|----------------|------------|----------------|----------------|----------------------|------------------------------|--|
| \overline{T} | \bigcirc | \bigcirc | T | F | \bigcirc | F | T |
| \overline{F} | \overline{T} | | <u>F</u> | | F | \overline{F} | F |
| \overline{T} | \overline{F} | | | \overline{F} | <u>F</u> | \overline{F} | F |
| \overline{F} | \overline{F} | | \overline{F} | | | \overline{F} | \overline{F} |

| P | Q | R | $P \lor P$ | $R \vee Q$ | $R \wedge R$ | $(R \wedge R) \vee (R \vee Q)$ | $Q \lor (P \lor P)$ | $ [(R \land R) \lor (R \lor Q)] \land [Q \lor (P \lor P)] $ |
|----------------|----------------|----------------|-----------------------|--------------|----------------|--------------------------------|-----------------------------|---|
| \overline{T} | T | <u>T</u> | | | | <u></u> | (T) | <u></u> |
| \overline{F} | \overline{T} | \bar{T} | \bar{F} | $ \bar{T} $ | T | \overline{T} | \bar{T} | T |
| \overline{T} | \overline{F} | \overline{T} | | - T | | T | | |
| | \overline{F} | | | - T | | | $\overline{\mathbb{F}}^{-}$ | \mathbb{F}^{-} |
| | | | - T | | | <u> </u> | | |
| \overline{F} | \overline{T} | \overline{F} | - F | | | | | |
| T | \overline{F} | \bar{F} | $ \bar{T} - \bar{T} $ | \bar{F} | \overline{F} | \overline{F} | \bar{T} | \overline{F} |
| \overline{F} | \overline{F} | \bar{F} | \bar{F} | \bar{F} | \overline{F} | \overline{F} | \overline{F} | \overline{F} |

| $P Q R R \vee P \neg Q (R \vee P) \wedge Q \neg Q \vee [(R \vee P) \wedge Q] \{\neg Q \vee [(R \vee P) \wedge Q]\} \wedge Q \neg \{\neg$ | 11 1 1) // 6 |
|---|----------------|
| | F |
| | \overline{F} |
| | |
| $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$ | |
| | |
| \overline{F} \overline{T} \overline{F} \overline{F} \overline{F} \overline{F} \overline{F} \overline{F} \overline{F} \overline{F} \overline{F} | T^{-} |
| \overline{T} \overline{F} \overline{F} \overline{T} \overline{T} \overline{T} \overline{T} | T^{-} |
| \overline{F} \overline{F} \overline{F} \overline{F} \overline{T} \overline{T} \overline{T} \overline{T} | \overline{T} |

25.

| P | Q | R | $P \vee R$ | $\neg P$ | $Q \vee \neg P$ | $\neg (P \lor R)$ | $\neg(Q \lor \neg P)$ | $\neg (Q \lor \neg P) \lor \neg (P \lor R)$ |
|----------------|-----------|----------------|----------------|----------------|-----------------|-------------------|---|---|
| \overline{T} | T | T | T | F | T | F | F | F |
| \overline{F} | \bar{T} | T | T^{-} | T | \bar{T} | \overline{F} | \overline{F} | $ar{F}$ |
| T | \bar{F} | T | T | \overline{F} | \overline{F} | <u>F</u> | T = T = T | \overline{T} |
| \overline{F} | | T | T | T | T T T | <u>F</u> | \overline{F} | \overline{F} |
| \overline{T} | | \overline{F} | T | \overline{F} | T - T - T | - | \overline{F} | \overline{F} |
| \overline{F} | | \overline{F} | \overline{F} | T | T - T - T | <u>-</u> | \overline{F} | T |
| \overline{T} | \bar{F} | \overline{F} | T | \overline{F} | \overline{F} | <u>F</u> | T - T - T | \overline{T} |
| \overline{F} | _ F _ | F | \overline{F} | T | T = T | | $\left[egin{array}{cccccccccccccccccccccccccccccccccccc$ | $oxed{ egin{bmatrix}$ |

26.

| Q | R | $R \wedge Q$ | $\neg Q$ | $\neg R$ | $\neg R \vee \neg Q$ | $(R \wedge Q) \wedge R$ | $ (\neg R \lor \neg Q) \land [(R \land Q) \land R] $ |
|----------------|----------------|--------------|----------------|----------------|----------------------|-------------------------|--|
| \overline{T} | T | T | F | F | F | T | F |
| \overline{F} | T^{-} | \bar{F} | \bar{T} | \overline{F} | \overline{T} | F | \overline{F} |
| \overline{T} | \overline{F} | - Ē | \overline{F} | \overline{T} | | F = F | \widehat{F} |
| \overline{F} | \overline{F} | \bar{F} | \bar{T} | T^{-} | \overline{T} | F | \overline{F} |

27.

| Q | $Q \wedge Q$ | $\neg(Q \land Q)$ |
|----------------|--------------|-------------------|
| | T | F |
| \overline{F} | | |

| Q | R | $Q \vee Q$ | $R \wedge R$ | $\neg Q$ | $(R \wedge R) \vee \neg Q$ | $\neg(Q \lor Q)$ | $\neg (Q \lor Q) \lor [(R \land R) \lor \neg Q]$ |
|----------------|----------------|----------------|----------------|----------------|----------------------------|------------------|--|
| \overline{T} | \bigcirc | \bigcirc | T | F | T | F | <u>(T)</u> |
| \overline{F} | \overline{T} | \overline{F} | | | | | |
| \overline{T} | \overline{F} | | \overline{F} | \overline{F} | <u>F</u> | <u>F</u> | \overline{F} |
| \overline{F} | \overline{F} | \overline{F} | | | | | |

| Q | R | $R \vee Q$ | $\neg Q$ | $\neg(R \lor Q)$ | $\neg Q \land \neg (R \lor Q)$ | $\neg[\neg Q \land \neg(R \lor Q)]$ | $\neg\neg[\neg Q \land \neg(R \lor Q)]$ |
|----------------|-----------|------------|-----------------------------------|------------------|--------------------------------|-------------------------------------|---|
| \overline{T} | T | T | F | F | F | T | F |
| \overline{F} | \bar{T} | T^{-} | T^{-} | \overline{F} | F | T = T | F F |
| T^{-} | \bar{F} | T | \overline{F} | \overline{F} | F | T | F F |
| \overline{F} | \bar{F} | F | $\begin{bmatrix} T \end{bmatrix}$ | T | | | |

30.

| P | R | $\neg P$ | $\neg R$ | $\neg P \vee R$ | $\neg \neg R$ | $\neg (\neg P \lor R)$ | $\neg(\neg P \lor R) \land \neg \neg R$ |
|----------------|----------------|----------------|----------------|-----------------|---------------|-----------------------------------|---|
| \overline{T} | \bigcirc | F | F | T | T | F | F |
| \overline{F} | \overline{T} | \overline{T} | \overline{F} | | - T | \overline{F} | <u>F</u> |
| T | \overline{F} | \overline{F} | T | F | [F | | F F |
| \overline{F} | \overline{F} | \overline{T} | T | | (F) | $ \overline{F} - \overline{F} $ | <u>F</u> <u>F</u> |

31.

| Q | R | $\neg Q$ | $\neg R$ | $\neg Q \lor \neg R$ | $\neg \neg R$ | $\neg \neg R \land (\neg Q \lor \neg R)$ |
|----------------|-----------|----------------|----------------|--|----------------|--|
| \bigcirc | T | F | F | F | T | F |
| \overline{F} | \bar{T} | | \overline{F} | T | | T |
| \overline{T} | \bar{F} | \overline{F} | | T | \overline{F} | F |
| $\bigcirc F$ | \bar{F} | | | $\begin{bmatrix} - & - & - & T & - & - & - \\ - & & & T & & - & - \end{bmatrix}$ | | |

32.

| Q | R | $R \vee Q$ | $Q \wedge R$ | $R \wedge Q$ | $(Q \wedge R) \vee (R \wedge Q)$ | $Q \lor (R \lor Q)$ | $ [(Q \land R) \lor (R \land Q)] \lor [Q \lor (R \lor Q)] $ |
|----------------|----------------|------------|---|--------------------|----------------------------------|---------------------|---|
| T | T | T | T | T | T | T | T) |
| \overline{F} | \bar{T} | T^{-} | \overline{F} | \overline{F}^{-} | \overline{F} | | |
| T | \bar{F} | T | \overline{F} | | [<u>F</u> | | |
| \overline{F} | \overline{F} | F | Γ \overline{F} $\overline{\Gamma}$ | | | | |

33.

| P | Q | R | $R \vee Q$ | $P \wedge P$ | $\neg Q$ | $(P \wedge P) \vee \neg Q$ | $R \wedge (R \vee Q)$ | $[(P \land P) \lor \neg Q] \lor [R \land (R \lor Q)]$ |
|----------------|----------------|----------------|--|---|--|--|--|---|
| \overline{T} | T | T | T | T | F | T | T | T |
| \overline{F} | T^{-} | \bar{T} | \bar{T} | \overline{F} | \bar{F} | $ \overset{-}{F} \overset{-}{F} \overset{-}{-} \overset{-}{-} $ | T | \overline{T} |
| T | \overline{F} | \bar{T} | \bar{T} | \bar{T} | \bar{T} | | T | \overline{T} |
| \overline{F} | \overline{F} | \bar{T} | T - T | \overline{F} | \bar{T} | T - T - T | T | \overline{T} |
| T | T^{-} | \bar{F} | $ -\bar{T} $ | \bar{T} | \bar{F} | - $ T$ $ -$ | F | \overline{T} |
| \overline{F} | \overline{T} | \overline{F} | | | \overline{F} | F | [- F | \overline{F} |
| T | \overline{F} | \bar{F} | \bar{F} | \bar{T} | \bar{T} | $ \overline{T} $ | F | \overline{T} |
| F | _ <i>F</i> _ | \bar{F} | $\begin{bmatrix} - & -\bar{F} & - & - \\ - & -\bar{F} & - & - \end{bmatrix}$ | $\begin{bmatrix} - & -F & - & - & - & - & - & - & - & - $ | $\begin{bmatrix} -\overline{T} & -\overline{T} \\ -\overline{T} & -\overline{T} \end{bmatrix}$ | $ig egin{array}{cccccccccccccccccccccccccccccccccccc$ | $\begin{bmatrix} - & - & - & - & - & - & - & - & - & - $ | \overline{T} |

| P | Q | R | $P \lor Q$ | $P \vee R$ | $\neg R$ | $(P \vee R) \wedge (P \vee Q)$ | $[(P \lor R) \land (P \lor Q)] \land \neg R$ | $\neg \{ [(P \lor R) \land (P \lor Q)] \land \neg R \}$ |
|----------------|-----------|----------------|----------------|------------|---------------|--------------------------------|---|---|
| \bigcirc | T | T | T | \bigcirc | F | T | F | T |
| \overline{F} | \bar{T} | \overline{T} | T^{-} | | \bar{F} | | \overline{F} | T |
| T | \bar{F} | \bar{T} | T^{-} | - T | \bar{F} | | F | |
| \overline{F} | \bar{F} | \bar{T} | \overline{F} | - T | \bar{F} | | F | |
| T | \bar{T} | \overline{F} | T^{-} | - T | \bar{T}^{-} | | \mid | \overline{F} |
| \overline{F} | \bar{T} | \bar{F} | T^{-} | - Ē | \bar{T}^{-} | | F | |
| T | \bar{F} | \overline{F} | T^{-} | - T | \bar{T}^{-} | | \mid | \overline{F} |
| \overline{F} | \bar{F} | \overline{F} | \overline{F} | | \bar{T} | F | $egin{array}{cccccccccccccccccccccccccccccccccccc$ | |

| P | Q | R | $P \wedge P$ | $R \wedge P$ | $R \wedge Q$ | $(R \wedge P) \vee P$ | $(P \wedge P) \wedge (R \wedge Q)$ | $[(P \land P) \land (R \land Q)] \lor [(R \land P) \lor P]$ |
|----------------|----------------|----------------|----------------|--|--|-----------------------|------------------------------------|---|
| \overline{T} | \bigcirc | T | T | T | T | T | T | T |
| \bar{F} | \bar{T} | \bar{T} | \overline{F} | \bar{F} | T T | \overline{F} | \overline{F} | \mathbb{P}^{-} |
| T^{-} | \overline{F} | T | | T | $ F ^{-}$ | T | <u>F</u> | |
| \bar{F} | \overline{F} | T^{-} | \overline{F} | \bar{F} | $ \vec{F} $ | F | \overline{F} | \mathbb{F} |
| T^{-} | \overline{T} | \bar{F} | | \bar{F} | $ \vec{F} $ | T | \overline{F} | |
| \overline{F} | \overline{T} | \overline{F} | F - F | \bar{F} | $ F ^{-}$ | F | <u>F</u> | \widehat{F} |
| T^{-} | \overline{F} | \overline{F} | | \bar{F} | $ \vec{F} $ | T | \overline{F} | |
| \overline{F} | \overline{F} | F | | $\begin{bmatrix} - & - & \overline{F} & - & - \\ - & \overline{F} & - & - & - \end{bmatrix}$ | $\begin{bmatrix} - & - & - & - & - & - & - & - & - & - $ | | | \mathbb{P} |

| Q | R | $\neg Q$ | $\neg R$ | $\neg Q \wedge \neg R$ | $(\neg Q \land \neg R) \land \neg Q$ | $\neg [(\neg Q \land \neg R) \land \neg Q]$ |
|----------------|----------------|----------------|----------------|------------------------|--------------------------------------|---|
| T | T | F | F | F | F | T |
| \overline{F} | | \overline{T} | \overline{F} | F (F) | <u>F</u> | Ţ Ţ |
| T | \overline{F} | \overline{F} | T | \overline{F} | \overline{F} | T |
| \overline{F} | \overline{F} | T | T | T - T - T | | \overline{F} |

37.

| P | Q | $P \wedge P$ | $\neg P$ | $\neg Q$ | $\neg P \land (P \land P)$ | $\neg \neg Q$ | $[\neg P \land (P \land P)] \lor \neg \neg Q$ |
|----------------|----------------|----------------|----------------|---|---|---|---|
| T | \bigcirc | \bigcirc | F | F | F | T | T |
| \overline{F} | T^{-} | \overline{F} | T^{-} | \overline{F} | \overline{F} | \bar{T} | T |
| \overline{T} | \overline{F} | | \overline{F} | | F F | $\lceil \widehat{F} \rceil$ | F |
| \overline{F} | \overline{F} | \overline{F} | | | $\overline{\mathbb{F}}$ | | |
| | | | | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ | $\begin{array}{c ccccccccccccccccccccccccccccccccccc$ |

38.

| - | | | | | | | | |
|---|-------------------------|-----------|----------------|----------------|----------------|--------------------------|-------------------|--|
| | Q | R | $R \vee Q$ | $Q \wedge R$ | $\neg R$ | $\neg R \lor (R \lor Q)$ | $\neg(Q \land R)$ | $\left \left[\neg R \lor (R \lor Q) \right] \lor \neg (Q \land R) \right $ |
| | \overline{T} | T | T | T | F | T | F | T |
| | \overline{F} | \bar{T} | T | \overline{F} | \overline{F} | T T | T = T = T | \overline{T} |
| | $\overline{\mathbb{T}}$ | \bar{F} | T | \overline{F} | T | T T | T - T - T | \overline{T} |
| | \overline{F} | \bar{F} | \overline{F} | | T | | T | \overline{T} |

39.

| P | Q | R | $\neg P$ | $\neg Q$ | $\neg P \wedge R$ | $\neg Q \wedge P$ | $(\neg Q \land P) \land (\neg P \land R)$ | $\neg[(\neg Q \land P) \land (\neg P \land R)]$ |
|----------------|----------------|----------------|---|----------------|-------------------|--|---|---|
| T | \bigcirc | \bigcirc | F | F | F | F | F | T |
| \overline{F} | \overline{T} | _(T)_ | | \overline{F} | | \overline{F} | \overline{F} | |
| \overline{T} | \overline{F} | \bar{T} | \overline{F} | | F - F | | \overline{F} | |
| \overline{F} | \overline{F} | \bar{T} | | | | \overline{F} | \overline{F} | |
| T | \overline{T} | \overline{F} | \overline{F} | \overline{F} | F - F | \overline{F} | \overline{F} | |
| \overline{F} | T^{-} | \bar{F} | \bar{T} | \overline{F} | \overline{F} | $ F ^{-}$ | \overline{F} | \overline{T} |
| T | \overline{F} | \bar{F} | \bar{F} | T^{-} | \overline{F} | T^{-} | \overline{F} | T |
| \overline{F} | \overline{F} | \bar{F} | $\begin{bmatrix} \overline{T} & \overline{T} \end{bmatrix}$ | T | \overline{F} | $\begin{bmatrix} - & - & F $ | $\left[\begin{array}{cccccccccccccccccccccccccccccccccccc$ | |

| P | Q | R | $Q \wedge Q$ | $\neg R$ | $\neg R \vee R$ | $(Q \wedge Q) \wedge P$ | $(\neg R \lor R) \land R$ | $[(Q \land Q) \land P] \land [(\neg R \lor R) \land R]$ |
|----------------|----------------|----------------|--------------|----------------|-----------------|-------------------------|---------------------------|---|
| T | \overline{T} | \bigcirc | T | F | T | T | T | T |
| \overline{F} | \overline{T} | \overline{T} | - T | \overline{F} | | F | T | \overline{F} |
| T | \overline{F} | \overline{T} | - F | \overline{F} | T | \overline{F} | T | \overline{F} |
| \overline{F} | \overline{F} | \overline{T} | - Ē | \overline{F} | T | F | [<u>T</u> | \overline{F} |
| \overline{T} | \overline{T} | \overline{F} | - T | \overline{T} | _T | | \overline{F} | \overline{F} |
| \overline{F} | \overline{T} | \overline{F} | - T | \overline{T} | _T | F | [<u>F</u> | F |
| \overline{T} | \overline{F} | \overline{F} | - Ē | \overline{T} | T | - | [<u>F</u> | F |
| \overline{F} | \overline{F} | \overline{F} | - Ē | \overline{T} | _T | F | F | <u>F</u> |

| P | Q | R | $Q \vee R$ | $R \vee R$ | $\neg P$ | $\neg P \lor (Q \lor R)$ | $P \lor (R \lor R)$ | $ [\neg P \lor (Q \lor R)] \land [P \lor (R \lor R)] $ |
|----------------|-----------|----------------|------------|----------------|----------------|--------------------------|------------------------------|--|
| T | T | \bigcirc | T | T | F | T | (T) | T |
| \overline{F} | \bar{T} | | | | | T T | | $\overline{\mathbb{T}}$ |
| T | \bar{F} | \overline{T} | | | \overline{F} | T T | | $\overline{\mathbb{T}}$ |
| \overline{F} | \bar{F} | \overline{T} | | | \overline{T} | T T | | $\overline{\mathbb{T}}$ |
| T | \bar{T} | \overline{F} | | \overline{F} | \overline{F} | T T | | T |
| \sim | \bar{T} | \overline{F} | | \overline{F} | \overline{T} | T T | $\lceil \overline{F} \rceil$ | \overline{F} |
| T | \bar{F} | \overline{F} | (F) | \overline{F} | \overline{F} | \overline{F} | | \overline{F} |
| \overline{F} | \bar{F} | <u>F</u> | | | | | | <u></u> |

42.

| P | Q | $P \wedge P$ | $\neg Q$ | $\neg \neg Q$ | $Q \land \neg \neg Q$ | $(Q \land \neg \neg Q) \lor (P \land P)$ | $\neg[(Q \land \neg \neg Q) \lor (P \land P)]$ |
|----------------|-----------|----------------|----------------|----------------|-----------------------|--|--|
| T | T | T | F | T | T | T | F |
| \overline{F} | \bar{T} | \overline{F} | \overline{F} | T | T | T | \overline{F} |
| T | \bar{F} | T | \bar{T} | \overline{F} | F | T | |
| \overline{F} | \bar{F} | \overline{F} | \bar{T} | \overline{F} | F | F = F | |

43.

| Q - R | $R \vee R$ | $R \wedge Q$ | $(R \vee R) \vee R$ | $[(R \vee R) \vee R] \wedge (R \wedge Q)$ | $\{[(R \lor R) \lor R] \land (R \land Q)\} \lor R$ | $ \neg (\{[(R \lor R) \lor R] \land (R \land Q)\} \lor R) $ |
|---------|------------|--------------|---------------------|---|--|---|
| (T) (T) | T | T | T | T | T | F |
| F (T) | T - T | - F | T | F | | |
| (T) (F) | F - | [| F | \overline{F} | \overline{F} | - |
| <u></u> | | | [| F | \mathbb{F} | |

44.

| P | Q | R | $P \vee R$ | $\neg Q$ | $\neg R$ | $(P \lor R) \land \neg R$ | $\neg \neg Q$ | $\neg\neg Q \land [(P \lor R) \land \neg R]$ |
|----------------|----------------|----------------|------------|--|----------------|---------------------------|---|--|
| T | T | T | T | F | F | F | T | (F) |
| \bar{F} | \bar{T} | \bar{T} | | \bar{F} | \overline{F} | \overline{F} | \bar{T} | \overline{F} |
| T | \overline{F} | T | | \bar{T} | \overline{F} | \overline{F} | \overline{F} | \overline{F} |
| \overline{F} | \bar{F} | T^{-} | | \bar{T} | \overline{F} | \overline{F} | \bar{F} | F |
| T^{-} | T | \overline{F} | | \bar{F} | | T | \bar{T} | T |
| \overline{F} | \bar{T} | \overline{F} | | \bar{F} | | \overline{F} | \bar{T} | \overline{F} |
| T^{-} | \bar{F} | \overline{F} | | \bar{T} | | T | \bar{F} | \overline{F} |
| F | \bar{F} | \overline{F} | | $\begin{bmatrix} -\overline{T} & -\overline{T} \\ -\overline{T} & -\overline{T} \end{bmatrix}$ | | | $\begin{bmatrix} -\overline{F} \\ -\end{bmatrix}$ | |

45.

| P | Q | R | $Q \lor P$ | $Q \lor Q$ | $\neg R$ | $P \wedge (Q \vee Q)$ | $\neg R \lor [P \land (Q \lor Q)]$ | $(Q \lor P) \lor \{\neg R \lor [P \land (Q \lor Q)]\}$ |
|----------------|----------------|----------------|--|--|---|--------------------------------------|------------------------------------|--|
| \overline{T} | T | T | T | T | F | T | T | T |
| \overline{F} | T^{-} | \bar{T} | $ - \bar{T} - $ | $ - \bar{T} - \bar{T} $ | \bar{F} | \overline{F} | \overline{F} | T |
| T | \bar{F} | \bar{T}^{-} | $ - \bar{T} - \bar{T} $ | $ \vec{F} $ | \bar{F} | F | \overline{F} | T |
| \overline{F} | \overline{F} | \overline{T} | - Ē | - Ē | \overline{F} | <u>F</u> | \overline{F} | F |
| T | T^{-} | \overline{F} | $ \bar{T} $ | T T | \bar{T} | T | \overline{T} | \overline{T} |
| \overline{F} | T^{-} | \bar{F} | $ - \bar{T} - $ | $ - \bar{T} - \bar{T} $ | \bar{T} | F | \overline{T} | T |
| T | \overline{F} | | | | | [| | |
| F | \overline{F} | \bar{F} | $oxed{\left[\begin{array}{ccccccccccccccccccccccccccccccccccc$ | $oxed{\left[\begin{array}{cc} - & ar{F} \end{array}\right]}$ | $\begin{bmatrix} \bar{T} \end{bmatrix}$ | $egin{bmatrix}F &F &F &F &F &F &F &$ | | T |

| P | Q | R | $P \lor Q$ | $R \wedge R$ | $(P \lor Q) \lor R$ | $(R \wedge R) \vee [(P \vee Q) \vee R]$ | $\neg \{(R \land R) \lor [(P \lor Q) \lor R]\} \mid$ | $\neg\neg\{(R \land R) \lor [(P \lor Q) \lor R]\}$ |
|----------------|----------------|-----------|--------------|----------------|---|--|--|--|
| T | T | T | T | T | T | T | F | T |
| \overline{F} | T^{-} | \bar{T} | \bar{T} | T^{-} | T | $ar{T}$ | \overline{F} | T |
| 1 | \overline{F} | | @ | | | | \overline{F} | |
| \overline{F} | \overline{F} | \bar{T} | \bar{F} | T | T | $ \overset{-}{T} \overset{-}{T} \overset{-}{-} \overset{-}{-} \overset{-}{T}$ | \overline{F} | T |
| T | \bar{T} | \bar{F} | \bar{T} | \overline{F} | T | $ar{T}$ | \overline{F} | T |
| \overline{F} | T^{-} | \bar{F} | \bar{T} | \overline{F} | T | $ar{T}$ | \overline{F} | T |
| T | \overline{F} | \bar{F} | $ -\bar{T} $ | \overline{F} | T | $ar{T}$ | \overline{F} | T |
| \overline{F} | | | | | $egin{bmatrix} ar{E} & ar{E} & ar{E} \end{bmatrix}$ | \mathbb{E}^{-} | | |

| P | Q | $\neg P$ | $\neg Q$ | $\neg P \land \neg Q$ |
|----------------|-----------|--|---|---|
| \overline{T} | _(T)_ | _(F)_ | _(F)_ | (F) |
| F | \bar{T} | \bar{T} | \overline{F} | \overline{F} |
| T^{-} | \bar{F} | \bar{F} | \bar{T} | \bar{F} |
| F_{-} | \bar{F} | $\begin{bmatrix} - & \overline{T} & - \\ - & \overline{T} & - \end{bmatrix}$ | $\begin{bmatrix} \overline{T} & \overline{T} \end{bmatrix}$ | $oxed{ egin{bmatrix} ar{T} & ar{T} & ar{T} \end{bmatrix} }$ |

48.

| R | $\neg R$ | $\neg \neg R$ | $\mid \neg \neg \neg R \mid$ | $\neg\neg\neg\neg R$ |
|----------------|----------|----------------|------------------------------|----------------------|
| \overline{T} | F | \bigcirc | F | T |
| \overline{F} | | \overline{F} | | F - F |

49.

| • | | | | | | | | | |
|---|----------------|----------------|----------------|------------|----------------|----------------|--------------------------------|---------------------|---|
| | P | Q | R | $P \lor Q$ | $Q \lor Q$ | $R \vee Q$ | $ (Q \lor Q) \lor (P \lor Q) $ | $(R \lor Q) \lor Q$ | $[(Q \lor Q) \lor (P \lor Q)] \lor [(R \lor Q) \lor Q]$ |
| | T | \bigcirc | \bigcirc | T | T | T | T | T | T |
| | \overline{F} | \bar{T} | \overline{T} | | | | | | |
| | T^{-} | \overline{F} | \overline{T} | | \overline{F} | | | | T |
| | \overline{F} | \overline{F} | \overline{T} | (F) | \overline{F} | | F | | T |
| | T^{-} | \overline{T} | \overline{F} | T T | | | | | T |
| | \overline{F} | \overline{T} | \overline{F} | T T | | | | | T |
| | T^{-} | \overline{F} | \overline{F} | T T | F - F | \overline{F} | <u></u> | <u>-</u> | |
| | \overline{F} | \overline{F} | \overline{F} | (F) | (F) | \overline{F} | F | <u>F</u> | \mathbb{F} |
| | | $- \simeq -$ | | l~ | | | L <u>~</u> | <u> </u> | u |

| P | Q | R | $P \vee R$ | $P \wedge P$ | $P \wedge Q$ | $(P \wedge Q) \vee (P \wedge P)$ | $\neg (P \lor R)$ | $ [(P \land Q) \lor (P \land P)] \lor \neg (P \lor R) $ |
|----------------|----------------|----------------|----------------|-------------------|---------------------------|----------------------------------|-------------------|---|
| \overline{T} | T | \bigcirc | T | T | T | T | F | T |
| \overline{F} | \bar{T} | \overline{T} | T^{-} | \bar{F} | \overline{F} | F | \overline{F} | F |
| T^{-} | \bar{F} | \overline{T} | T^{-} | $-\bar{T}$ | \bar{F} | T | \overline{F} | \overline{T} |
| \overline{F} | \overline{F} | \overline{T} | T | \bar{F} | \bar{F} | <u>-</u> | \overline{F} | F |
| T^{-} | \bar{T} | \overline{F} | T^{-} | $ - \bar{T} - $ | $ - \bar{T} - \bar{T} $ | T | F^{-} | T |
| \overline{F} | \bar{T} | \overline{F} | - F | \bar{F} | \bar{F} | \overline{F} | T | \overline{T} |
| T^{-} | \bar{F} | \overline{F} | T^{-} | $-\bar{T}$ | \bar{F} | T | \overline{F} | \overline{T} |
| \overline{F} | \overline{F} | \overline{F} | \overline{F} | \bar{F} | \bar{F} | <u>-</u> | T - T - T | T |
| | | | | | | | | |