Examples of Syntax Trees and Truth Tables

1.
$$\neg(L \lor L)$$



$$\begin{array}{c|c|c|c} L & L \lor L & \neg(L \lor L) \\ \hline T & T & F \\ F & F & T \\ \end{array}$$

2. $(M \lor Y) \lor M$



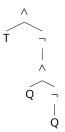
| М | Υ | $M \vee Y$ | $(M \lor Y) \lor M$ |
|----------------|---|------------|---------------------|
| \overline{T} | T | T | T |
| F | T | T | T |
| T | F | T | T |
| F | F | F | F |

3.
$$(Q \wedge Q) \wedge (Y \wedge Y)$$



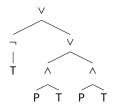
| Q | Υ | $Q \wedge Q$ | Y ^ Y | $(Q \wedge Q) \wedge (Y \wedge Y)$ |
|----------------|---|--------------|-------|------------------------------------|
| \overline{T} | T | T | T | T |
| F | T | F | T | F |
| T | F | T | F | F |
| F | F | F | F | F |

4.
$$T \wedge \neg (Q \wedge \neg Q)$$



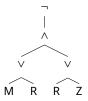
| Q | Т | $\neg Q$ | $Q \wedge \neg Q$ | $\neg (Q \land \neg Q)$ | $T \wedge \neg (Q \wedge \neg Q)$ |
|----------------|---|----------|-------------------|-------------------------|-----------------------------------|
| \overline{T} | T | F | F | T | T |
| F | T | T | F | T | T |
| T | F | F | F | T | F |
| F | F | T | F | T | F |

5. $\neg T \lor [(P \land T) \lor (P \land T)]$



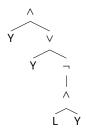
| Р | Т | $P\wedgeT$ | ¬Т | $(P \wedge T) \vee (P \wedge T)$ | $\neg T \lor [(P \land T) \lor (P \land T)]$ |
|----------------|---|------------|----|----------------------------------|--|
| \overline{T} | T | T | F | T | T |
| F | T | F | F | F | F |
| T | F | F | T | F | T |
| F | F | F | T | F | T |

6. $\neg[(M \lor R) \land (R \lor Z)]$



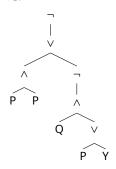
| М | R | Z | $M \vee R$ | $R \vee Z$ | $ (M \lor R) \land (R \lor Z) $ | $\neg [(M \lor R) \land (R \lor Z)]$ |
|----------------|---|---|------------|------------|-----------------------------------|--------------------------------------|
| \overline{T} | T | T | T | T | T | F |
| F | T | T | T | T | T | F |
| T | F | T | T | T | T | F |
| F | F | T | F | T | F | T |
| T | T | F | T | T | T | F |
| F | T | F | T | T | T | F |
| T | F | F | T | F | F | T |
| F | F | F | F | F | F | T |

7. $Y \wedge [Y \vee \neg(L \wedge Y)]$



| L | Υ | L∧Y | $\neg(L \land Y)$ | $\mid Y \lor \neg(L \land Y) \mid$ | $Y \wedge [Y \vee \neg(L \wedge Y)]$ |
|----------------|---|-----|-------------------|------------------------------------|--------------------------------------|
| \overline{T} | T | T | F | T | T |
| F | T | F | T | T | T |
| T | F | F | T | T | F |
| F | F | F | T | T | F |

8.
$$\neg \{(P \land P) \lor \neg [Q \land (P \lor Y)]\}$$



| Р | Q | Υ | P∨Y | P∧P | Q ∧ (P ∨ Y) | $\neg[Q \land (P \lor Y)]$ | $ (P \land P) \lor \neg [Q \land (P \lor Y)] $ | $\neg \{(P \land P) \lor \neg [Q \land (P \lor Y)]\}$ |
|---|---|---|-----|-----|-------------|----------------------------|--|---|
| T | T | T | T | T | T | F | T | F |
| F | T | T | T | F | T | F | F | T |
| T | F | T | T | T | F | T | T | F |
| F | F | T | T | F | F | T | T | F |
| T | T | F | T | T | T | F | T | F |
| F | T | F | F | F | F | T | T | F |
| T | F | F | T | T | F | T | T | F |
| F | F | F | F | F | F | T | T | F |