

# Applying the Regression Anatomy Formula

Open R and verify that the mtcars dataset is automatically loaded.

```
head(mtcars)
```

##	mpg	cyl	disp	hp	drat	wt	qsec	vs	am	gear	carb
## Mazda RX4	21.0	6	160	110	3.90	2.620	16.46	0	1	4	4
## Mazda RX4 Wag	21.0	6	160	110	3.90	2.875	17.02	0	1	4	4
## Datsun 710	22.8	4	108	93	3.85	2.320	18.61	1	1	4	1
## Hornet 4 Drive	21.4	6	258	110	3.08	3.215	19.44	1	0	3	1
## Hornet Sportabout	18.7	8	360	175	3.15	3.440	17.02	0	0	3	2
## Valiant	18.1	6	225	105	2.76	3.460	20.22	1	0	3	1

You are interested in the following model:

$$mpg = \beta_0 + \beta_1 hp + \beta_2 wt + u$$

Your task is to figure out what the ols estimate for  $\beta_1$  would be, *without* conducting a multiple regression in R, instead only relying on simple regressions.

Applying the regression anatomy formula,

$$\hat{\beta}_1 = \frac{cov(y, r_1)}{var(r_1)}$$

where  $r_1$  is the residual from a regression of  $hp$  on  $wt$ .

1. Use R to compute the residuals  $r_1$ , then compute the numerator of the regression anatomy formula.
2. Compute the denominator of the regression anatomy formula.
3. Explain, in a sentence or two, why this method works to compute  $\beta_1$ .