W203 Lab 3

Armand Kok, Adam Yang, James De La Torre

Introduction

Our team has been hired by a local political campaign to research North Carolina crime statistics and generate suggestions for policies for reducing crime.

The crime statistics data set being analyzed is a subset of the data used by Cornwell and W. Trumball in their 1994 study. The data set contains the output variable, crmrate, which is crimes committed per capita, and it also contains 24 other variables which will be treated as input variables and potential modulators of the crime rate.

We will attempt to build a linear model that regresses **crmrate** on some key variables in the data set. We hope to identify variables that can be reasonably assessed as causal with respect to the crime rate. From our model fidings, we will produce policy proposals which we believe can influence these variables and result in a decrease in crime.

It is important to note that just because a variable is found to correlate with the crime rate, it does not imply that the variable is useful from the perspective of a political campaign. We may find variables that cannot be influenced by any political policy or action. Such variables may improve the predictive ability of our model, but they will not be targeted for change by any policy proposals.

Exploratory Data Analysis

The data file, crime_v2.csv was opened and found to contain 97 rows. Each row represents data for a single county in North Carlolina. Immediate inspection of the data revealed a few data cleanup steps were required.

- The last 6 rows of the data set were blanks. These empty records were deleted.
- One row had values of 1 for both west and central, placing that county in two regions simultaneously. It is unknown whether this is possible, but currently there has been no reason to delete this particular row so the data will be kept for now, as evaluation of variable importance is still ongoing.
- The prbconv variable, representing the "probability of conviction" was read in as a factor (a cateogorical variable) instead of a numeric variable. This variable was converted to numeric.

```
library(car)
library(reshape2)
library(ggplot2)

# Adam's dir
mydir <- "/Users/adamyang/Desktop/w203/Lab3/w203-Lab3/"

# Armand's dir
# mydir<-'C:/Users/ak021523/Documents/GitHub/mids-repos/W203/Homework/w203-Lab3/'

# jim's directory mydir<-
# F:/users/jddel/Documents/DATA_SCIENCE_DEGREE_LAPTOP/W203_Stats/Lab_03/'

# read df
crime_df = read.csv(paste0(mydir, "crime_v2.csv"))</pre>
```

summarize all vars summary(crime_df)

```
##
                          year
                                                            prbarr
                                       crmrte
        county
##
           : 1.0
                             :87
                                           :0.005533
                                                               :0.09277
                     Min.
    1st Qu.: 52.0
                     1st Qu.:87
##
                                   1st Qu.:0.020927
                                                        1st Qu.:0.20568
##
    Median :105.0
                     Median:87
                                   Median: 0.029986
                                                        Median :0.27095
##
    Mean
           :101.6
                     Mean
                             :87
                                   Mean
                                           :0.033400
                                                        Mean
                                                               :0.29492
    3rd Qu.:152.0
                     3rd Qu.:87
                                   3rd Qu.:0.039642
                                                        3rd Qu.:0.34438
##
    Max.
           :197.0
                     Max.
                             :87
                                           :0.098966
                                                               :1.09091
                                   Max.
                                                        Max.
##
    NA's
            :6
                     NA's
                             :6
                                   NA's
                                                        NA's
                                                               :6
##
           prbconv
                         prbpris
                                             avgsen
                                                               polpc
##
                : 5
                      Min.
                              :0.1500
                                         Min.
                                               : 5.380
                                                           Min.
                                                                   :0.000746
##
    0.588859022: 2
                      1st Qu.:0.3648
                                         1st Qu.: 7.340
                                                           1st Qu.:0.001231
##
                : 1
                      Median :0.4234
                                         Median: 9.100
                                                           Median: 0.001485
##
    0.068376102: 1
                             :0.4108
                                         Mean
                                              : 9.647
                      Mean
                                                           Mean
                                                                  :0.001702
    0.140350997: 1
                      3rd Qu.:0.4568
                                         3rd Qu.:11.420
                                                           3rd Qu.:0.001877
##
    0.154451996: 1
                      Max.
                              :0.6000
                                         Max.
                                                :20.700
                                                           Max.
                                                                   :0.009054
##
    (Other)
                :86
                      NA's
                              :6
                                         NA's
                                                :6
                                                           NA's
                                                                   :6
##
       density
                            taxpc
                                               west
                                                               central
##
                              : 25.69
                                                 :0.0000
                                                                    :0.0000
    Min.
           :0.00002
                                         Min.
                                                            Min.
                       Min.
##
    1st Qu.:0.54741
                       1st Qu.: 30.66
                                          1st Qu.:0.0000
                                                            1st Qu.:0.0000
##
    Median : 0.96226
                       Median: 34.87
                                          Median :0.0000
                                                            Median :0.0000
    Mean
           :1.42884
                       Mean : 38.06
                                          Mean
                                                 :0.2527
                                                            Mean
                                                                   :0.3736
                       3rd Qu.: 40.95
##
    3rd Qu.:1.56824
                                          3rd Qu.:0.5000
                                                            3rd Qu.:1.0000
##
    Max.
           :8.82765
                       Max.
                              :119.76
                                          Max.
                                                 :1.0000
                                                            Max.
                                                                    :1.0000
    NA's
           :6
                       NA's
                                          NA's
                                                            NA's
##
                               :6
                                                 :6
                                                                    :6
                          pctmin80
##
        urban
                                               wcon
                                                                wtuc
##
    Min.
            :0.00000
                       Min.
                              : 1.284
                                          Min.
                                                 :193.6
                                                           Min.
                                                                   :187.6
    1st Qu.:0.00000
                       1st Qu.: 9.845
                                          1st Qu.:250.8
##
                                                           1st Qu.:374.6
##
    Median :0.00000
                       Median :24.312
                                          Median :281.4
                                                           Median :406.5
    Mean
           :0.08791
                       Mean
                             :25.495
                                          Mean
                                                 :285.4
                                                           Mean
                                                                 :411.7
##
    3rd Qu.:0.00000
                       3rd Qu.:38.142
                                          3rd Qu.:314.8
                                                           3rd Qu.:443.4
##
    Max.
           :1.00000
                       Max.
                               :64.348
                                          Max.
                                                 :436.8
                                                           Max.
                                                                  :613.2
            :6
                       NA's
                               :6
                                          NA's
                                                           NA's
##
    NA's
                                                 :6
                                                                   :6
##
         wtrd
                          wfir
                                            wser
                                                              wmfg
##
    Min.
            :154.2
                     Min.
                             :170.9
                                      Min.
                                            : 133.0
                                                         Min.
                                                                :157.4
##
    1st Qu.:190.9
                     1st Qu.:286.5
                                       1st Qu.: 229.7
                                                         1st Qu.:288.9
##
    Median :203.0
                     Median :317.3
                                      Median : 253.2
                                                         Median :320.2
##
    Mean
          :211.6
                     Mean
                            :322.1
                                      Mean
                                            : 275.6
                                                         Mean
                                                                :335.6
##
    3rd Qu.:225.1
                     3rd Qu.:345.4
                                       3rd Qu.: 280.5
                                                         3rd Qu.:359.6
                                              :2177.1
##
           :354.7
                             :509.5
    Max.
                     Max.
                                      Max.
                                                         Max.
                                                                 :646.9
                                                         NA's
##
    NA's
           :6
                     NA's
                             :6
                                       NA's
                                              :6
                                                                :6
##
         wfed
                          wsta
                                            wloc
                                                             mix
##
            :326.1
                             :258.3
                                              :239.2
                                                               :0.01961
    Min.
                     Min.
                                      Min.
                                                        Min.
                     1st Qu.:329.3
##
    1st Qu.:400.2
                                       1st Qu.:297.3
                                                        1st Qu.:0.08074
    Median :449.8
                     Median :357.7
                                      Median :308.1
                                                        Median : 0.10186
##
    Mean
           :442.9
                     Mean
                             :357.5
                                      Mean
                                              :312.7
                                                        Mean
                                                               :0.12884
##
    3rd Qu.:478.0
                     3rd Qu.:382.6
                                       3rd Qu.:329.2
                                                        3rd Qu.:0.15175
##
    Max.
            :598.0
                             :499.6
                                              :388.1
                                                               :0.46512
                     Max.
                                      Max.
                                                        Max.
                     NA's
                             :6
##
    NA's
            :6
                                      NA's
                                              :6
                                                        NA's
                                                               :6
##
       pctymle
##
    Min.
           :0.06216
    1st Qu.:0.07443
```

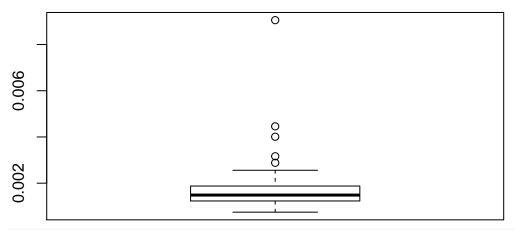
```
Median :0.07771
           :0.08396
##
   Mean
##
   3rd Qu.:0.08350
           :0.24871
  Max.
##
   NA's
str(crime_df)
   'data.frame':
                    97 obs. of 25 variables:
                    1 3 5 7 9 11 13 15 17 19 ...
   $ county
             : int
              : int 87 87 87 87 87 87 87 87 87 87 ...
##
   $ year
             : num 0.0356 0.0153 0.013 0.0268 0.0106 ...
##
   $ crmrte
##
   $ prbarr : num 0.298 0.132 0.444 0.365 0.518 ...
   $ prbconv : Factor w/ 92 levels "","`","0.068376102",..: 63 89 13 62 52 3 59 78 42 86 ...
   $ prbpris : num  0.436  0.45  0.6  0.435  0.443  ...
##
##
   $ avgsen : num
                    6.71 6.35 6.76 7.14 8.22 ...
##
   $ polpc
              : num
                    0.001828 0.000746 0.001234 0.00153 0.00086 ...
##
   $ density : num
                     2.423 1.046 0.413 0.492 0.547 ...
##
              : num
                     31 26.9 34.8 42.9 28.1 ...
##
                    0 0 1 0 1 1 0 0 0 0 ...
   $ west
              : int
##
   $ central : int
                    1 1 0 1 0 0 0 0 0 0 ...
##
             : int
                    0 0 0 0 0 0 0 0 0 0 ...
   $ urban
##
   $ pctmin80: num
                     20.22 7.92 3.16 47.92 1.8 ...
##
   $ wcon
              : num
                     281 255 227 375 292 ...
                     409 376 372 398 377 ...
##
   $ wtuc
              : num
##
                     221 196 229 191 207 ...
   $ wtrd
              : num
##
   $ wfir
                     453 259 306 281 289 ...
              : num
##
   $ wser
              : num
                    274 192 210 257 215 ...
##
   $ wmfg
              : num
                     335 300 238 282 291 ...
##
   $ wfed
              : num
                     478 410 359 412 377 ...
##
   $ wsta
                     292 363 332 328 367 ...
              : num
##
   $ wloc
              : num
                     312 301 281 299 343 ...
##
              : num 0.0802 0.0302 0.4651 0.2736 0.0601 ...
   $ mix
   $ pctymle : num
                     0.0779 0.0826 0.0721 0.0735 0.0707 ...
# get rid of rows with missing values (this only kills the 6
# blank rows)
crime_df <- crime_df[complete.cases(crime_df), ]</pre>
# convert prob of conviction to numeric
crime_df$prbconv <- as.numeric(as.character(crime_df$prbconv))</pre>
```

Outlier Identification

After reviewing the distributions of the different variables, there were 4 variables had outliers, which is defined by anything that is more than Q3 + 1.5 IQR or Q1 - 1.5 IQR: - polpc - row 51 - prbarr - row 51 - wser - row 84 - taxpc row 25 After reviewing further, there was no reason for the extreme outliers to be removed from the data set. boxplots of the variables above are shown below.

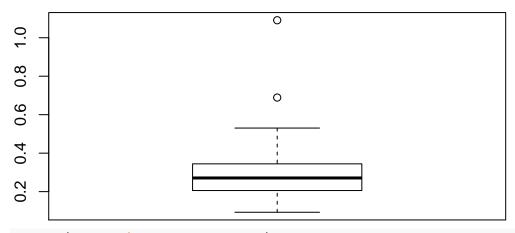
boxplot(crime_df\$polpc, main = "polpc")

polpc



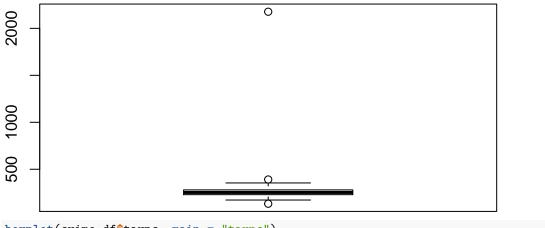
boxplot(crime_df\$prbarr, main = "prbarr")

prbarr



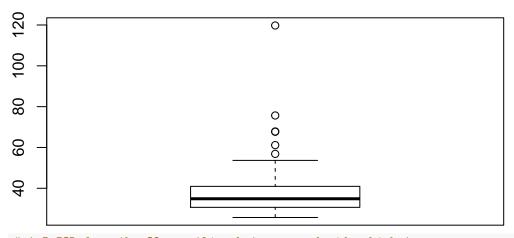
boxplot(crime_df\$wser, main = "wser")

wser



boxplot(crime_df\$taxpc, main = "taxpc")

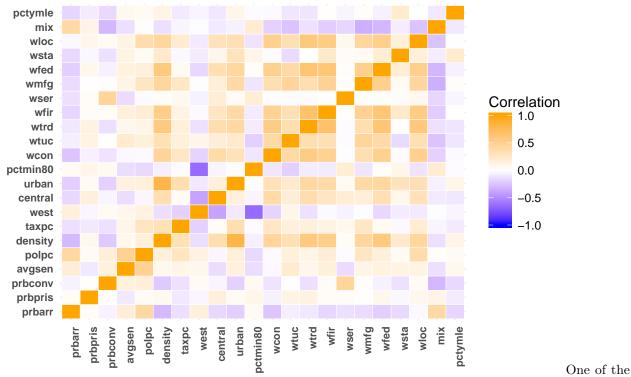
taxpc



1.5 IQR from the Q3 = outlier but we can decide which to # eliminate

Check for multicolinearity

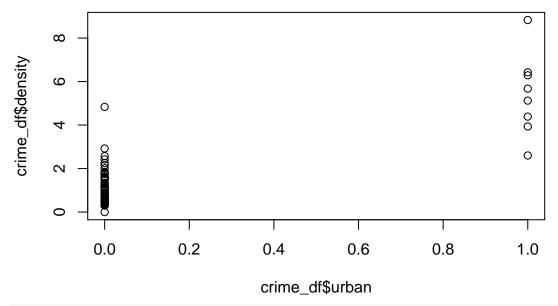
Build a correlation matrix. Identify input variables that correlate with one another. Choose only one variable from each correlated pair to include in model-building.



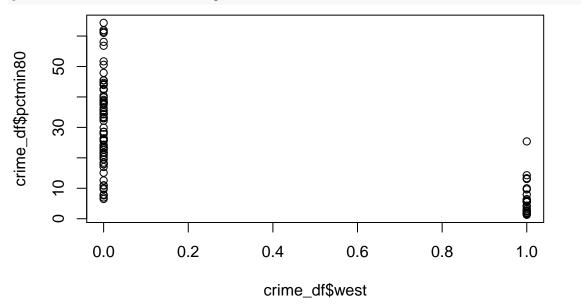
assumptions for multiple OLS regression is to avoid perfect multicollinearity between independent variables. This, however, is not common in practical cases. Less than perfect multicollinearity is a more common problem that will not cause bias in the OLS, but would introduce large variances and covariances. As a result, precise estimation would become difficult so it can be beneficial to remove certain imperfect multicollinearity variables.

After reviewing the correlation matrix in detail, there were 5 pairs of variables that have a somewhat strong correlation to each other (i.e. has correlation > 0.6), which are plotted below. Based on the plots, then the following variables were removed from the final model: - urban - this is somewhat redundant with density. - west - west was removed because it is a dummy variable, and pctmin80 is a continuous one which may contain more information for the regression model. - wtrd, wfed, wfir - wages tend to be higher with density, so density was kept as it can succinctly represent the same information. Below are the scatterplots of the different correlated variables

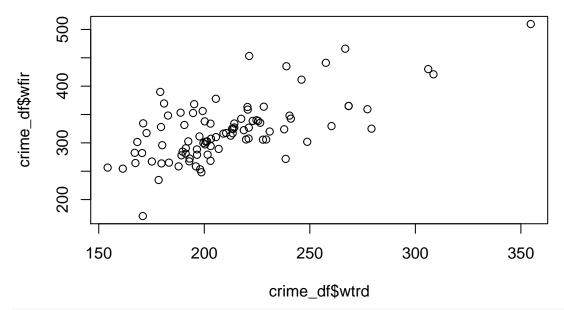
plot(crime_df\$urban, crime_df\$density)

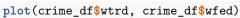


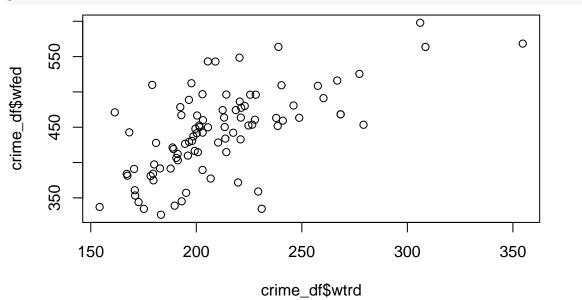
plot(crime_df\$west, crime_df\$pctmin80)



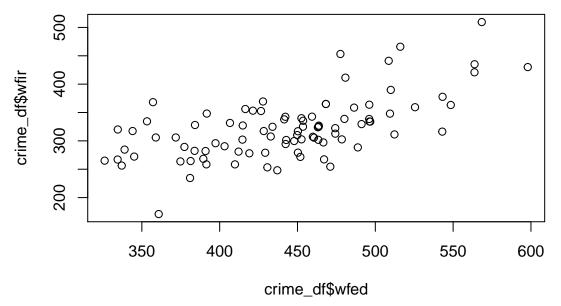
plot(crime_df\$wtrd, crime_df\$wfir)



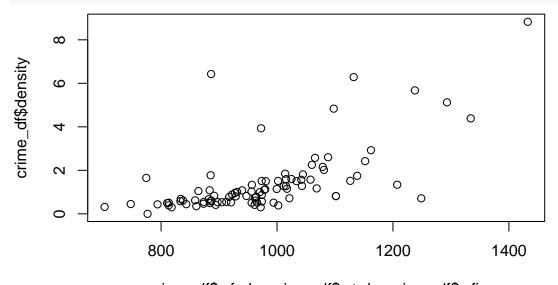




plot(crime_df\$wfed, crime_df\$wfir)



plot(crime_df\$wfed + crime_df\$wtrd + crime_df\$wfir, crime_df\$density)



crime_df\$wfed + crime_df\$wtrd + crime_df\$wfir

Stan-

dardize Independent Variables

In order to compare the impacts of the different independent variables, the values of those variables needed to be standardized so that the slope coefficients are similar in scale (e.g. if the range of a variable is between 0 and 1, then the coefficient may be larger than that of a variable that ranges between 0-200). For the standardization, the variables were all scaled to range between 0 and 1, based on the min and max values.

```
# make a copy of crime_df for standardizing values
std_crime_df <- cbind(crime_df)

# a function to standardize values (fraction of range)
standardize_values <- function(x) {
        (x - min(x))/(max(x) - min(x))
}

# for all columns other than county number, year, and crime</pre>
```

```
# rate, standardize between 0 and 1
for (col in 4:ncol(std_crime_df)) {
    std crime df[, col] <- standardize values(std crime df[,
        coll)
}
summary(std_crime_df)
##
                                                           prbarr
        county
                          year
                                       crmrte
    Min. : 1.0
                                          :0.005533
                                                              :0.0000
##
                            :87
                                  Min.
                                                      Min.
                     Min.
    1st Qu.: 52.0
                     1st Qu.:87
                                   1st Qu.:0.020927
                                                       1st Qu.:0.1131
##
    Median :105.0
                     Median:87
                                  Median: 0.029986
                                                      Median :0.1785
    Mean
          :101.6
                     Mean
                            :87
                                   Mean
                                          :0.033400
                                                      Mean
                                                             :0.2025
##
    3rd Qu.:152.0
                     3rd Qu.:87
                                   3rd Qu.:0.039642
                                                       3rd Qu.:0.2521
##
    Max.
           :197.0
                     Max.
                            :87
                                  Max.
                                          :0.098966
                                                      Max.
                                                              :1.0000
##
       prbconv
                         prbpris
                                            avgsen
                                                              polpc
    Min.
           :0.0000
                      Min.
                            :0.0000
                                        Min.
                                              :0.0000
                                                          Min.
                                                                 :0.00000
##
    1st Qu.:0.1350
                      1st Qu.:0.4773
                                        1st Qu.:0.1279
                                                          1st Qu.:0.05837
##
    Median :0.1873
                      Median : 0.6076
                                        Median :0.2428
                                                          Median :0.08900
##
    Mean
           :0.2352
                      Mean
                            :0.5795
                                        Mean
                                               :0.2785
                                                          Mean
                                                                 :0.11510
    3rd Qu.:0.2535
                      3rd Qu.:0.6817
                                        3rd Qu.:0.3943
                                                          3rd Qu.:0.13611
##
##
    Max.
           :1.0000
                      Max.
                             :1.0000
                                        Max.
                                               :1.0000
                                                          Max.
                                                                 :1.00000
       density
##
                           taxpc
                                               west
                                                               central
    Min.
           :0.00000
                              :0.00000
                                          Min.
                                                 :0.0000
                                                            Min.
                                                                   :0.0000
                       Min.
    1st Qu.:0.06201
                       1st Qu.:0.05283
                                          1st Qu.:0.0000
                                                            1st Qu.:0.0000
##
    Median :0.10900
                       Median :0.09756
                                          Median :0.0000
                                                            Median :0.0000
##
    Mean
           :0.16186
                       Mean
                              :0.13142
                                          Mean
                                                 :0.2527
                                                            Mean
                                                                   :0.3736
    3rd Qu.:0.17765
                       3rd Qu.:0.16217
                                          3rd Qu.:0.5000
                                                            3rd Qu.:1.0000
           :1.00000
##
    Max.
                       Max.
                              :1.00000
                                          Max.
                                                 :1.0000
                                                            Max.
                                                                   :1.0000
##
        urban
                          pctmin80
                                              wcon
                                                                wtuc
##
           :0.00000
                       Min. :0.0000
                                                :0.0000
                                                                  :0.0000
    Min.
                                         Min.
                                                           Min.
                                         1st Qu.:0.2350
    1st Qu.:0.00000
                       1st Qu.:0.1358
                                                           1st Qu.:0.4394
    Median :0.00000
                                         Median :0.3611
##
                       Median : 0.3652
                                                           Median :0.5143
##
    Mean
           :0.08791
                       Mean
                              :0.3839
                                         Mean
                                                :0.3772
                                                           Mean
                                                                  :0.5264
    3rd Qu.:0.00000
                       3rd Qu.:0.5845
                                         3rd Qu.:0.4983
                                                           3rd Qu.:0.6011
##
    Max.
           :1.00000
                       Max.
                              :1.0000
                                         Max.
                                                :1.0000
                                                           Max.
                                                                  :1.0000
##
         wtrd
                           wfir
                                             wser
                                                                wmfg
                                               :0.00000
##
           :0.0000
                             :0.0000
    Min.
                      Min.
                                        Min.
                                                           Min.
                                                                  :0.0000
    1st Qu.:0.1828
                      1st Qu.:0.3414
                                        1st Qu.:0.04727
                                                           1st Qu.:0.2686
    Median : 0.2435
                      Median : 0.4324
##
                                        Median: 0.05880
                                                           Median : 0.3326
    Mean
           :0.2861
                      Mean
                             :0.4465
                                        Mean
                                               :0.06973
                                                           Mean
                                                                  :0.3640
##
    3rd Qu.:0.3538
                      3rd Qu.:0.5152
                                                           3rd Qu.:0.4131
                                        3rd Qu.:0.07216
##
    Max.
           :1.0000
                             :1.0000
                                               :1.00000
                                                           Max.
                                                                  :1.0000
                                        Max.
##
         wfed
                           wsta
                                             wloc
                                                               mix
##
           :0.0000
                             :0.0000
                                               :0.0000
                                                                 :0.0000
    Min.
                      Min.
                                        Min.
                                                          Min.
                      1st Qu.:0.2943
##
    1st Qu.:0.2727
                                        1st Qu.:0.3901
                                                          1st Qu.:0.1372
    Median : 0.4552
                      Median :0.4118
                                        Median: 0.4625
                                                          Median : 0.1846
##
           :0.4297
                             :0.4111
                                               :0.4936
                                                                 :0.2452
    Mean
                      Mean
                                        Mean
                                                          Mean
##
    3rd Qu.:0.5589
                      3rd Qu.:0.5150
                                        3rd Qu.:0.6049
                                                          3rd Qu.:0.2966
##
    Max.
           :1.0000
                      Max. :1.0000
                                        Max.
                                               :1.0000
                                                          Max.
                                                                 :1.0000
       pctymle
##
##
    Min.
           :0.00000
##
    1st Qu.:0.06579
```

Median : 0.08338

```
## Mean :0.11688
## 3rd Qu.:0.11439
## Max. :1.00000
```

Now that we have standardized the units of all input variables, we can compute model slope coefficients that will be in comparable units.

Standardized Regression Model

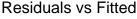
A multi variable regression model was created using the data set that has been standardized above.

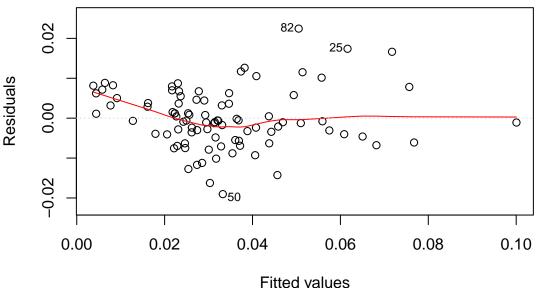
Then the model was evaluated for potential high leverage/influence data points as well as potential biases.

In review the following findings were noted: - row 84 and 25 have a high Cook's distance and high standardized residuals, which means the data point can be problematic for the regression model. - row 25 and 84 were also noted earlier to be an extreme outier for the wser variable. Thus based on this finding the point will be removed and the regression will be redone. - Judging from the residuals vs. fitted plot the model may have some bias when the predicted value crmrte is between 0 to 0.04. Particularly the model tend to underpredict lower crmrates, and overpredict medium crmrte. - From the Normal Q-Q line, it looks like that majority of predictions follow the line, indicating a normal and independent distribution.

```
# TODO clean out the warning
std_model <- lm(crmrte ~ . - county - year - crmrte - urban -
    west - wtrd - wfed - wfir, data = std_crime_df)

plot(std_model, 1)</pre>
```

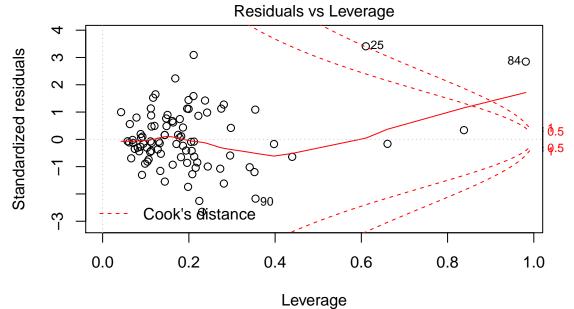




Im(crmrte ~ . - county - year - crmrte - urban - west - wtrd - wfed - wfir)

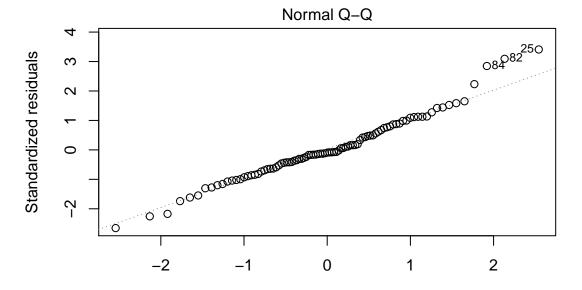
```
## Warning in sqrt(crit * p * (1 - hh)/hh): NaNs produced
## Warning in sqrt(crit * p * (1 - hh)/hh): NaNs produced
```

plot(std_model, 5)



Im(crmrte ~ . - county - year - crmrte - urban - west - wtrd - wfed - wfir)

plot(std_model, 2)



Theoretical Quantiles

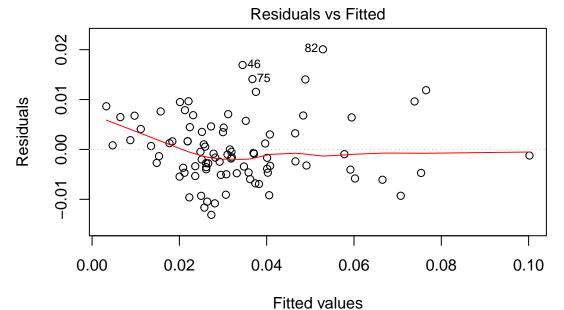
Im(crmrte ~ . - county - year - crmrte - urban - west - wtrd - wfed - wfir)

```
# summary(std_model)$r.squared

std_crime_df2 <- std_crime_df[-c(84, 25), ]

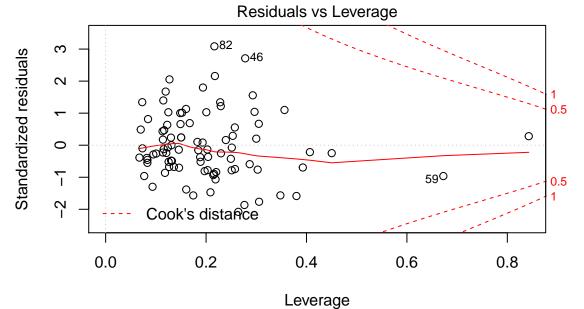
std_model2 <- lm(crmrte ~ . - county - year - crmrte - urban -
    west - wtrd - wfed - wfir, data = std_crime_df2)

plot(std_model2, 1)</pre>
```



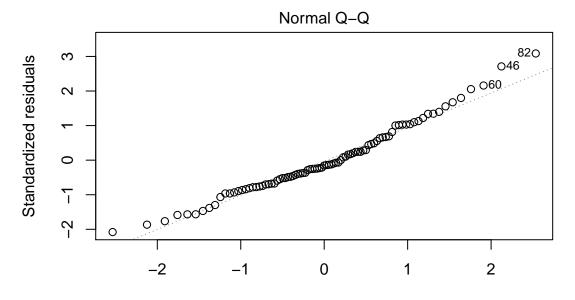
Im(crmrte ~ . - county - year - crmrte - urban - west - wtrd - wfed - wfir)

plot(std_model2, 5)



Im(crmrte ~ . - county - year - crmrte - urban - west - wtrd - wfed - wfir)

plot(std_model2, 2)



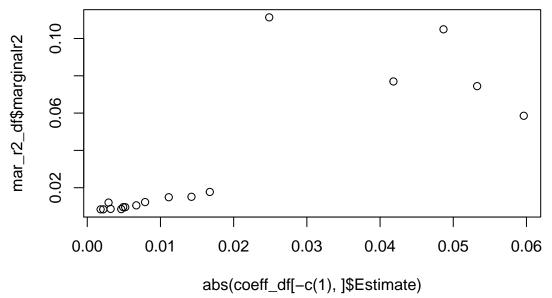
Theoretical Quantiles

Im(crmrte ~ . – county – year – crmrte – urban – west – wtrd – wfed – wfir)

In order to find which variables are most impactful to crmrte, the marginal R-squared against the standardized coefficients were reviewed. Based on the plots, the following variables were found to have the highest marginal R-squared and absolute slope coefficient: -prbarr -prbconv -polpc -density -pctmin80

```
coeff_df = data.frame(summary(std_model)$coefficients)
# summary(std_model)$r.squared
# base R-Squared
base_model <- lm(crmrte ~ . - county - year - crmrte, data = std_crime_df)</pre>
base_r2 <- summary(base_model)$r.squared</pre>
# create list of variables for the for-loop
var_names <- colnames(std_crime_df)</pre>
remove <- c("county", "year", "crmrte", "urban", "west", "wtrd",</pre>
    "wfed", "wfir")
var_names <- var_names[!var_names %in% remove]</pre>
# initiate an empty vector to store the marginal R-Squared
var_r2_delta = c()
# loop through the variable names and store the marginal
# R-Squared
for (i in var_names) {
    fmla <- as.formula(paste("crmrte ~ - crmrte +", paste(var_names[!var_names %in%)</pre>
        i], collapse = "+")))
    delta_model <- lm(fmla, data = crime_df)</pre>
    r2_delta <- base_r2 - summary(delta_model)$r.squared
    var_r2_delta <- c(var_r2_delta, r2_delta)</pre>
}
\# put the variable and marginal R-squared in a dataframe
mar r2 df <- data.frame(v1 = var names, v2 = var r2 delta)</pre>
colnames(mar_r2_df) <- c("variable", "marginalr2")</pre>
```

```
# sort dataframe by marginal R-squared in a descending order
# mar_r2_df <- mar_r2_df[rev(order(mar_r2_df$marginalr2)),]
plot(abs(coeff_df[-c(1), ]$Estimate), mar_r2_df$marginalr2)</pre>
```



```
subset(mar_r2_df, marginalr2 > 0.04)
```

```
## variable marginalr2
## 1 prbarr 0.07445392
## 2 prbconv 0.07695649
## 5 polpc 0.05856302
## 6 density 0.10492397
## 9 pctmin80 0.11132549
```

Non-Standardized Regressions

The following is the model that contains almost all available variables as explanatory variables with the exception of variables we excluded due to potential multi-collinearity.

```
crime_df2 <- crime_df[-c(84, 25), ]

model1 <- lm(crmrte ~ . - county - year - crmrte - urban - west -
    wtrd - wfed - wfir, data = crime_df2)

summary(model1)$r.squared</pre>
```

[1] 0.8688977

summary(model1)\$coefficients

```
##
                    Estimate
                               Std. Error
                                             t value
                                                         Pr(>|t|)
## (Intercept)
               3.097640e-02 1.561081e-02
                                          1.9842914 5.108937e-02
               -5.078247e-02 8.704418e-03 -5.8341022 1.478721e-07
## prbarr
## prbconv
               -1.962352e-02 3.293124e-03 -5.9589361 8.903946e-08
## prbpris
                4.754774e-03 1.048442e-02 0.4535087 6.515656e-01
## avgsen
               -3.961756e-04 3.497705e-04 -1.1326727 2.611624e-01
```

```
## polpc
                6.460940e+00 1.346144e+00 4.7995886 8.534766e-06
               6.845704e-03 7.973078e-04 8.5860246 1.369694e-12
## density
## taxpc
               -7.103721e-05 1.021711e-04 -0.6952767 4.891513e-01
## central
               -3.517708e-03 1.926533e-03 -1.8259265 7.206619e-02
## pctmin80
                3.898315e-04 5.176540e-05 7.5307361 1.236934e-10
## wcon
                4.081808e-05 2.373695e-05 1.7196007 8.986184e-02
## wtuc
               4.373842e-06 1.324754e-05 0.3301626 7.422493e-01
## wser
               -6.293562e-05 2.794740e-05 -2.2519307 2.742112e-02
## wmfg
               4.568252e-06 1.208881e-05 0.3778909 7.066390e-01
## wsta
               -4.273992e-05 2.105298e-05 -2.0301130 4.609284e-02
## wloc
               4.531803e-05 4.143979e-05 1.0935875 2.778324e-01
               -2.294321e-02 1.269191e-02 -1.8077035 7.488831e-02
## mix
                9.580106e-02 3.779334e-02 2.5348663 1.345432e-02
## pctymle
The following is the model that contains a transformed explanatory variable.
model_transform <- lm(crmrte ~ prbarr + log(prbconv) + density,</pre>
    data = crime_df2)
summary(model_transform)$r.squared
## [1] 0.6570935
summary(model_transform)$coefficients
                                             t value
                                                         Pr(>|t|)
                    Estimate
                               Std. Error
## (Intercept)
                 0.025420503 0.0035106022 7.241066 1.857260e-10
## prbarr
                -0.028710438 0.0089889944 -3.193954 1.969045e-03
## log(prbconv) -0.006276946 0.0022761837 -2.757662 7.125235e-03
## density
                 0.007903815 0.0008331222 9.486981 5.580124e-15
The following is the model that contains only variables that were identified to be most relevant to crmrte
based on their marginal R-squared and standardized slope coefficient values.
model_key <- lm(crmrte ~ prbarr + prbconv + polpc + density +</pre>
   pctmin80, data = crime_df2)
summary(model_key)$r.squared
## [1] 0.8204393
summary(model_key)$coefficients
##
                    Estimate
                               Std. Error
                                             t value
                                                         Pr(>|t|)
## (Intercept) 0.0300488820 3.494735e-03 8.598328 4.156915e-13
## prbarr
               -0.0555832603 8.317408e-03 -6.682763 2.515871e-09
## prbconv
               -0.0179293179 3.139371e-03 -5.711118 1.698543e-07
## polpc
                6.1601721055 1.204450e+00 5.114512 1.989594e-06
                0.0063705861 6.966292e-04 9.144873 3.349488e-14
## density
## pctmin80
                0.0003808799 5.212093e-05 7.307620 1.527153e-10
```

Stargazer Regression Table for Model Specifications

```
library(stargazer)
##
## Please cite as:
```

```
## Hlavac, Marek (2018). stargazer: Well-Formatted Regression and Summary Statistics Tables.
```

R package version 5.2.2. https://CRAN.R-project.org/package=stargazer

```
stargazer(model_transform, model_key, model1, title = "Linear Models Parameters Predicting Crime Rate",
    type = "text", report = "vc", keep.stat = c("rsq", "n"),
    omit.table.layout = "n")
```

Linear Models Parameters Predicting Crime Rate

Dependent variable:

crmrte (1) (2) (3)

> prbarr -0.029 -0.056 -0.051 log(prbconv) - 0.006prbconv -0.018 -0.020 prbpris 0.005 avgsen -0.0004 polpc 6.160 6.461 density 0.008 0.006 0.007 taxpc -0.0001 central -0.004 pctmin80 0.0004 0.0004 wcon 0.00004wtuc 0.00000 wser -0.0001wmfg 0.00000 wsta -0.00004 wloc 0.00005mix - 0.023pctymle 0.096 Constant $0.025 \ 0.030 \ 0.031$

Observations 89 89 89 R2 0.657 0.820 0.869

Recommendation

For interpretability purposes, the model was re-done using non-standardized variables: -prbarr - prbconv - polpc - density - pctmin 80

Recommendation for political campaign: - police per capita has a positive slope coefficient with crmrte, and this may be due to more police are present in areas with high crmrte. This suggests that purely hiring more police officers may not be an impactful solution. - However probability of arrest and conviction both have a negative slope coefficients. The model suggests that perhaps a zero tolerance policy towards crime is needed to increase arrests and convictions and thus deter crimes from happening. - In terms areas with large minority population and high density, since these variable cannot be changed that much, perhaps a community outreach (e.g. job training program, afterschool programs, tutor/mentor program) to educate areas with a lot of minority can be done, so that crimes can be reduced in those areas.

Omitted Variables

Potential Omitted Variable #1: poverty_rate

$$crmrte = \beta_0 + \beta_1 * density + \beta_2 * poverty_rate + u$$

poverty
$$rate = \alpha_0 + \alpha_1 * density + u$$

- One thing that was noticeable in the data is that crmrate was higher in dense areas and large minority population, however this may be due to an omitted variable that is not available in the data set.
- For example: in dense areas the cost of living may be much higher, which can explain why higher wages are correlated with dense areas, but because of the higher cost of living. Because of this, there may be a lot more people living under the poverty line, which would encourage them to commit crimes and hence why dense areas have higher crimte.
- so the density slope coefficient in this instance is probably higher than it should be β_2 and α_1 would be positive.
- Maybe tax revenue or wages can help proxy this omitted variable.

Potential Omitted Variable #2: discrimination

$$crmrte = \beta_0 + \beta_1 * pctmin80 + \beta_2 * discrimination$$

$$discrimination = \alpha_0 + \alpha_1 * pctmin80$$

- Similarly minorities may be arrested for crimes more often than necessary due to discrimination. - in this scenario β_2 and $alpha_1$ would be a positive value.

Potential Omitted Variable #3: raised_in_oneparent_hh

$$crmrte = \beta_0 + \beta_1 * pctmin80 + \beta_2 * raised_in_2parents_hh$$

$$raised_in_2parents_hh = \alpha_0 + \alpha_1 * pctmin80$$

- In this scenario, minorities may be more likely to be raised in a single parent house hold. Thus making them more likely to commit crimes. - β_2 would be positive and α_1 would be negative.

Potential Omitted Variable #4: unemployment

$$crmrte = \beta_0 + \beta_1 * density + \beta_2 * unemployment$$

$$unemployment = \alpha_0 + \alpha_1 * density$$

- Higher umployment = higher crime rate (beta 2 > 0)
- Higher density = higher unemployment (alpha1 > 0)
- beta1 was positive, therefore, it might be higher than it should've been.

Potential Omitted Variable #5: years_of_education

$$crmrte = \beta_0 + \beta_1 * pctmin80 + \beta_2 * years_of_education$$

$$years of education = \alpha_0 + \alpha_1 * pctmin80$$

- Higher avg years of education for a county would result in lower crime rate, beta 2 < 0 - Higher percentage of minorities = lower average years of education for a county, alpha 1 < 0 - $\beta_2 * \alpha_1 > 0$, beta 1 > 0, therefore, it might be higher than it should've been.