

Strong correlations between text quality and complex networks features

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Abstract: Concepts of complex networks have been used to obtain metrics that were correlated to text quality established by scores assigned by human judges. Texts produced by high-school students in Portuguese were represented as scale-free networks (word adjacency model), from which typical network features such as the in/outdegree, clustering coefficient and shortest path were obtained. Another metric was derived from the dynamics of the network growth, based on the variation of the number of connected components. The scores assigned by the human judges according to three text quality criteria (coherence and cohesion, adherence to standard writing conventions and theme adequacy/development) were correlated with the network measurements. Text quality for all three criteria was found to decrease with increasing average values of outdegrees, clustering coefficient and deviation from the dynamics of network growth. Among the criteria employed, cohesion and coherence showed the strongest correlation, which probably indicates that the network measurements are able to capture how the text is developed in terms of the concepts represented by the nodes in the networks. Though based on a particular set of texts and specific language, the results presented here point to potential applications in other instances of text analysis.

1 Introduction

The area of complex networks [1, 2, 3], which can be viewed as an intersection between graph theory and statistical mechanics, has been marked by many theoretical advances and relevant applications over the last few years. New concepts such as the hubs, i.e. nodes with particularly high degree, had major impact for understanding and re-interpreting problems such as essentiality [4] and resilience to attacks [5]. Applications of complex networks have appeared in widely diverse areas, ranging from the Internet [6] to networks of Jazz artists [7]. Because of its special importance to human communication, culture, and even intelligence, the representation and analysis of written texts in terms of graphs and complex networks offers a promising (and challenging) research opportunity for the forthcoming years. The application of concepts and tools from mathematics, physics and computer science to the analysis of texts is not new and includes approaches generally associated with first-order statistics of words and other elements obtained from texts. With the availability of databases accessible through the Internet, unprecedented possibilities for such investigations are now open. For instance, considering first-order statistics, Gonçalves & Gonçalves have identified the works of renowned English writers [8], Montemurro & Zanette have grouped words based on their linguistic role in a corpus [9], and

Zhou & Slater have proposed a method to measure the relevance of words in a text [10]. Indeed, first-order analysis does provide valuable information about the global and specific features of most texts.

We believe that further insights can be obtained by using higher-order statistics in order to enhance the context representation, to which the concept of complex networks is closely related. More specifically, each word in a text can be represented as a node, while subsequent words define associations, or edges, between such nodes (this model is known as word adjacency/co-occurrence network). Typically, pairs of subsequent words, excluding articles and other connecting words, are considered, implying a Markov model with unity length memory. Larger Markov memory lengths can be obtained by considering tuples of subsequent words. Because the networks incorporate the most immediate associations between words and concepts, their topology - quantified by several measurements [11] such as node degree, clustering coefficient and shortest path - can provide information on some properties of the text, such as style and authorship. A series of studies indicate that word adjacency networks [12, 13, 14, 15], semantic networks [1, 16, 17, 18, 19, 20, 21], word association networks [16, 22, 23] and syntactic networks [24, 25] are graphs that show features present in classical examples of complex networks, such as the World Wide Web and social networks. One of the important consequences of such studies is the presence of hubs in linguistic networks.

In this study we investigate the possibility of automated evaluation of text quality using topological measurements extracted from the corresponding complex networks. We consider three criteria for scoring texts which are related to text quality, namely i) coherence and cohesion, (ii) adherence to standard writing conventions and (iii) theme adequacy/development. These are the criteria generally employed to mark essays for high-school students applying to enter the university in Brazil. Complex networks are obtained from such texts by considering the proximity between words, and the indegree and outdegree, the clustering coefficient and shortest path distributions are estimated for each text. Such measurements are estimated after the full construction of the networks, while the number of connected components is monitored during their growth, yielding a topological feature which is a function of the number of added word associations. All the mea-

surements are correlated with grades assigned by human experts. The results indicate that, despite the many parameters and unavoidable subjectivity of human language, such an approach presents potential to be used as a subsidy for a more objective and reproducible means to evaluate text quality.

2 Text assessment by human subjects

One set of 40 pieces of text has been selected, which comprise essays on the same subject - influence from TV on our society - written in Brazilian Portuguese by high school students. All pieces of text have approximately the same size, with an average of 228 words. A panel of five human judges, all of which are computational linguists, analyzed the texts using three criteria to mark them, namely (i) coherence and cohesion, (ii) adherence to standard writing conventions and (iii) theme adequacy/development, henceforth referred to as *CC*, *SWC* and *TAD*, respectively. The judges assigned marks from 0 to 10 to each text for the three criteria, and did not receive any instruction as to reference values or how these criteria should be rated. Not surprisingly, there is large dispersion among the marks given, as illustrated in Fig. 1, where the five marks are shown in the vertical axes for each of the 40 texts (horizontal axes). The texts were sorted from left to right according to an increasing dispersion in the scores assigned by the judges. The numbering of the text may therefore vary from one figure to the other, as the different criteria were analyzed. Note also that for some texts less than five points may appear in the picture because equal scores could have been given. Because of the large dispersion of the marks, in this paper we shall concentrate on data obtained with the 20 texts with lowest score dispersion. The results obtained with the full set of 40 texts will be briefly commented upon in the Concluding section.

3 Measurements of text features using complex networks

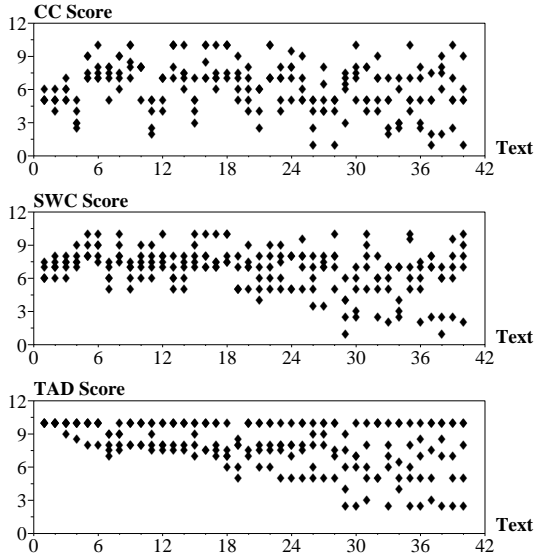


Figure 1: 40 texts vs. corresponding scores (from 0 to 10) according to the three quality criteria, identified as *CC* for coherence and cohesion, *SWC* for adherence to standard writing conventions and *TAD* for theme adequacy/development. The horizontal axes are ordered from the text with the lowest score dispersion between the five judges to the text with the highest dispersion. The sequences of texts in the horizontal axes are not necessarily equal for the different criteria.

Two word adjacency networks were obtained from a given text. In the first one, called NET-A, each different pair (w_1, w_2) of subsequent words (at distance one from each other) defines a directed weighted edge in the network, whose weight represents the frequency of the association from word w_1 to word w_2 . The association network was obtained similarly to that described in [22], i.e. each of the N different words was represented as a node and each connection between words as a weighted edge between the corresponding nodes representing those words. The stopwords have been removed and the remaining words have been lemmatized. Removing stopwords eliminates very common words, such as verb to be and some adverbs, and words from closed classes (articles, pronouns, prepositions and conjunctions). Lemmatization is the process of reducing a word into its base form, such as the verb “passed” to the infinitive “pass”. Therefore, different occurrences of meaning-related words are represented by the same node in the network. The second word adjacency network, called NET-B, is almost the same as NET-A, but also connects subsequent words at distance two, i.e. w_1 is also connected to w_3 , although there is a word w_2 between them. In other words, each sequence of three words $(\dots, w_1, w_2, w_3, \dots)$ implies a directed edge from w_1 to w_3 and another directed edge from w_2 to w_3 . Note that the two adopted types of networks, namely NET-A and NET-B, represent Markov models of memory one and two, respectively. The choice of these two models has been aimed at providing subsidies for investigating the effect of the extent of the considered context into the measurements and results.

All network measurements adopted were extracted from the weight matrix W representing the network. This $N \times N$ matrix was obtained by starting with all elements as zero and making $W(j, i) = W(j, i) + 1$ whenever there was the association $i \rightarrow j$. Because of the directed edges, the matrix W is not symmetric. It is also possible to obtain an adjacency matrix K from W by making $K(j, i) = 1$ whenever $W(j, i) > 0$. The measurements obtained from such networks are described in the remaining of this section.

3.1 Indegree and outdegree

The indegree and outdegree of node i are defined, respectively, as

$$ID(i) = \sum_{j=1}^N W(i, j) \quad (1)$$

and

$$OD(i) = \sum_{j=1}^N W(j, i). \quad (2)$$

We adopt the network outdegree OD as the arithmetic mean of every $OD(i)$ (the network indegree ID is obtained similarly). Because the average value of the indegrees coincides with that obtained for the outdegrees, only the latter will be considered henceforth.

3.2 Clustering coefficient

The clustering coefficient of node i is calculated as follows. First, all nodes receiving an edge from node i are identified and included into the set R , with $N_c = |R|$. If B is the total number of edges between all the nodes in R (taking into account the edges directions, i.e. edge $i \rightarrow j$ is different from edge $j \rightarrow i$), the clustering coefficient of node i is obtained as (for an example, see Fig. 2)

$$CLC(i) = \frac{B}{N_c(N_c - 1)}. \quad (3)$$

In case N_c is smaller or equal to 1, then $CLC(i) = 0$. The network clustering coefficient CLC is the arithmetic mean of all individual clustering coefficients $CLC(i)$.

3.3 Network dynamics

We have taken measurements considering the dynamics of growth for the complex network as a given text was analyzed. The number of connected components (or clusters) was calculated after adding each word association to the network, yielding a topological feature which is a function of the number of associations and, consequently, of the evolution of the text construction. For each text, the network was initiated with all N words, each one representing a single component, and the connections were

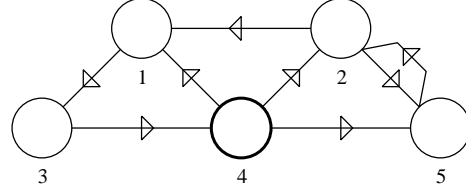


Figure 2: Computation of the clustering coefficient of node 4 ($CLC(4)$). In this particular case, $N_c = 3$, since node 4 is connected to the nodes belonging to the set $R = \{1, 2, 5\}$ (node 3 has an edge shared with node 4, but this edge does not come from node 4). If the nodes 1, 2 and 5 formed a fully connected subnetwork, there would be $N_c(N_c - 1) = 3(3 - 1) = 6$ edges between them, but in fact there is only $B = 3$. Finally, the clustering coefficient of node 4 is $CLC(4) = B/(N_c(N_c - 1)) = 3/6 = 0.5$. This definition of clustering coefficient does not take into account the edge weights.

established by each word association that occurred along the text. When a word association was read, a new edge was created in the network or the weight of an already existing edge was increased. As a consequence of the word adjacency model, the number of connected components always converged to one after all words had been introduced. Fig. 3 shows how the number of components evolves with the number of edges for three texts extracted from the selected corpus, being therefore representative of the evolution of connectivity in a given text. In each graph, the straight line was included to guide the eye, and represents the special case of uniform variation of the number of components, while the other curve indicates the real variation as the word associations were read. A quantitative treatment of the data in Fig. 3 was carried out by calculating the extent to which the real plot departed from the straight line. For short, this measurement will be referred to in the remainder of this article as “components dynamics deviation” (CDD). Let $f_a(x)$ be the actual function that associates the number of components with the number x of word associations already inserted into the network, $f_s(x)$ be the reference straight line, L be the total number of word associations in the text and N be the total number of vertices in the network. The deviation

in the network dynamics is calculated as

$$CDD = \frac{\sum_{x=1}^L |f_a(x) - f_s(x)|/N}{L}. \quad (4)$$

Texts A, B and C, whose dynamics are represented in Fig. 3, have CDD values of 0.014, 0.045 and 0.064, respectively. A visual inspection of these three texts in Fig. 3 corroborates these increasing values obtained for texts from A to C.

3.4 Shortest path

Distances between pairs of nodes, which also consider the edges directions, were calculated with the Floyd-Warshall algorithm [26]. We consider the complement of each weight, $W_{max} - W(j, i) + 1$, where W_{max} is the maximum edge weight present in the network, to compute the shortest paths $SP(i, j)$ between any two nodes i and j . SP is defined in this way because it is not desirable that the shortest paths algorithm gives low priority to the strongest edges, which are those that represent more frequent and possibly more important associations between words. Whenever there is no path between two nodes i and j , we take $SP(i, j) = NW_{mean}$, where N is the number of vertices and W_{mean} is the arithmetic mean of all edge weights. The SP measurement for a whole network is the arithmetic mean of every $SP(i, j)$, provided that $i \neq j$.

4 Results and discussion

In a previous report [27], we have shown that the measurements associated with complex networks could be used to distinguish between low-quality and high-quality texts, selected from two different sources. However, a limitation to that study was that the differences emerging from the analysis could arise from the source of the text, age and background of the writers and even subject of the essays. In order to avoid such possible interferences, in the present study we took texts from only one source, namely essays written by high-school students, with approximately the same age and academic background, on a single topic - influence from TV on our society. Firstly, we illustrate in Fig. 4 for three texts from the set that the distribution of outdegrees of the investigated data suggest

the scale-free property, indicated by the linear $\log \times \log$ plot for the outdegree, which is consistent with previous reports in the literature [12, 13]. Similar results were obtained for the indegree and for the other texts (not shown here).

We now attempt to correlate the measurements using complex networks concepts with the scores assigned by the human judges. Because of the large score dispersion for some texts, we perform the analysis taking only the 20 texts with the lowest dispersion for each criterion. This analysis results in a set of 24 plots (Figs. 5–8) which correlate the four network measurements with the three types of scores for each of the two types of networks. Figs. 5–8 are organized with the measurements distributed along the horizontal axes, while the scores assigned by the human judges are positioned in the vertical axes. The labels A and B refer to the measurements taken from the networks constructed following the models NET-A and NET-B, respectively. The values from both the measurements and scores were standardized into a standard normal distribution $N(0, 1)$ and a linear regression was performed for each correlation plot. The corresponding straight line, the Pearson correlation coefficient and the p-value are also given in the figure as a guide for the strength of the linear correlations [28].

Figs. 5A and 5B indicate that the scores assigned by the human judges - for the three criteria - decrease with increasing number of outdegrees. Most significant are the results for the cohesion and coherence (CC) and adherence to standard writing conventions (SWC). Large Pearson coefficients were obtained with very low p-values, which indicates that the linear correlations were not obtained by chance. The scores corresponding to the theme adequacy/development (TAD) are less sensitive to the number of outdegrees, though they also tend to decrease. It appears then that an analysis of the number of outdegrees allows one to capture the quality of the text, with a large number of outdegrees causing the text to lose quality. There is practically no difference in behavior in the results using NET-A and NET-B, i.e. considering a larger context in NET-B did not affect the results significantly. It should be mentioned that we have also calculated the indegrees for all of the texts separately. Because averages were taken, the results were identical to those of the outdegrees and were therefore omitted.

Similar conclusions can be drawn from Figs. 6A and

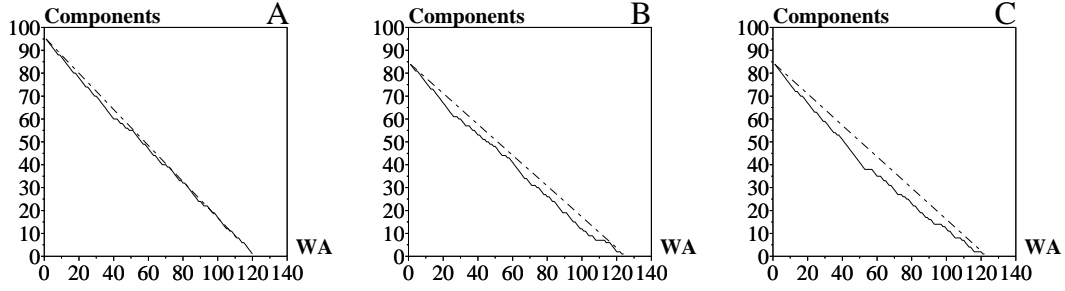


Figure 3: Dynamics of the network for three texts extracted from the selected set of 40 pieces of text. In the horizontal axes, WA stands for the number of word associations already inserted into the network. The straight dotted line is a reference that assumes uniform variation of the number of components as the edges are inserted or as their corresponding weights are modified in the network. The other curve is the real one, which reflects the actual variation of the number of components. The deviation in the network dynamics, according to Equation 4, for the three texts above are 0.014 (A), 0.045 (B) and 0.064 (C).

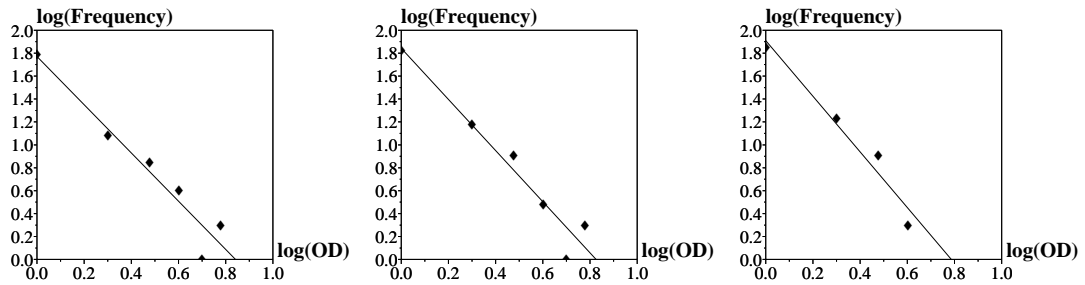


Figure 4: Log×log outdegree (OD) distributions for three texts extracted from the corpus of 40 texts. A scale-free behavior is suggested by these examples.

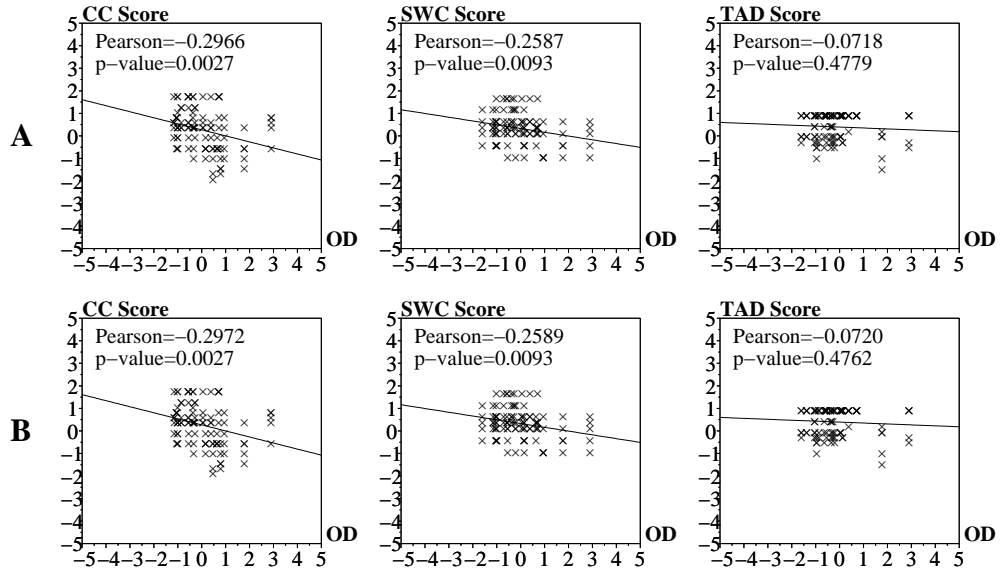


Figure 5: Correlations between the outdegrees (OD , horizontal axes) and the scores (vertical axes) for the 20 texts with the lowest score dispersion. In the vertical axes, SWC stands for standard writing conventions, TAD for theme adequacy/development and CC for coherence and cohesion. Both axes are standardized into a standard normal distribution $N(0, 1)$. Measurements obtained from the two types of networks, NET-A and NET-B, are discriminated by the labels A and B, respectively.

6B, which show that text quality decreases with an increasing clustering coefficient (*CLC*). Now correlations appeared stronger for the data with NET-A than for NET-B, particularly for the *CC* and *SWC* scores. In fact, from all measurements those of *CLC* gave the highest correlations (cf. Pearson coefficient) with text quality. From a linguistic point of view, one may infer that texts lose quality if the concepts are highly interconnected, probably excessively interconnected.

As for the deviation from a linear dynamics for the network growth (*CDD*), an inspection of Figs. 7A and 7B points to the text quality decreasing with increasing deviations, with little difference between data for NET-A and NET-B. This corroborates our earlier finding with texts from two different sources (see first version of this paper [27]). In the latter study, a threshold in the *CDD* value was used to distinguish between low- and high-quality texts. A large deviation indicates that the concepts were first introduced at an early stage of the text construction, thus causing the total number of components to decrease fast. As a result, the writer probably kept repeating the arguments in the remainder of the writing process, leading to a low quality text. As an example of this correlation, consider the texts whose dynamics are illustrated in Fig. 3. These texts received average scores of 7.9 (A), 5.2 (B) and 3.7 (C), according to the coherence and cohesion criterion, while the *CDD* values were 0.014 (A), 0.045 (B) and 0.064 (C), respectively. From a linguistic point of view, *CDD* appears to capture whether the flow of the prose is adequate, which is reflected especially in the cohesion and coherence.

The correlation between the scores used to assess quality and the measurements of shortest paths is weaker than for the other measurements obtained with NET-A and NET-B, as shown in Figs. 8A and 8B. There is a slight increase in the quality scores with increasing shortest paths, especially with the *SWC*. The reason for a weaker correlation may be found in the results from our previous work with texts of different sources [27]. There, we found that text quality appeared to increase slightly with the shortest path when all texts were considered. However, when analyzing only the low-quality texts, we observed text quality to decrease with increasing shortest paths. We interpreted the latter result as being due to the difficulties faced by poor writers in establishing long sequences of connections among different concepts. This discrepancy between low

and high-quality texts calls for further, more detailed research into the possible correlation between shortest paths and quality.

5 Conclusions and perspectives

We have applied the concepts of complex networks to one set of texts which comprises essays of variable quality (as confirmed by human judges) written by high-school students on the same topic. A correlation could be established between the measurements, i.e. outdegrees, clustering coefficient and deviation from a linear dynamics in the network growth, and the scores assigned by the human judges. The influence of shortest paths on text quality could not be established unequivocally, probably because the effects may differ for low and high-quality texts. Among the criteria employed, cohesion and coherence was the one showing strongest correlation between the scores and the network measurements. One may argue that this correlation indicates that the measurements are able to capture how the text is developed in terms of the concepts represented by the nodes in the networks. We should not expect these measurements to capture the text quality in terms of the adherence to standard writing conventions (*SWC*), as there is no deep analysis of the texts. Essays performing well in this criterion were those with small or negligible number of spelling and grammatical mistakes. However, writers that produce good-quality texts in terms of cohesion and coherence normally write grammatically correct texts. We believe this to be the reason for the good correlation between the scores of *SWC* and the network measurements. The third criterion, theme adequacy/development (*TAD*) is a more subjective because human judges assess whether the writer addressed the expected issues for the given topic. It is not uncommon that the score assigned be related to whether the examiner agrees with the ideas put forward in the essay. Not surprisingly then, the correlation between the network measurements and the scores was weak.

The conclusions above hold for the 2 types of analysis performed, both with NET-A and NET-B. Therefore, the context captured with only adjacent words appears to be sufficient to correlate with text quality. In addition, in subsidiary experiments we observed that essentially the same conclusions and trends apply for the full set of 40 texts,

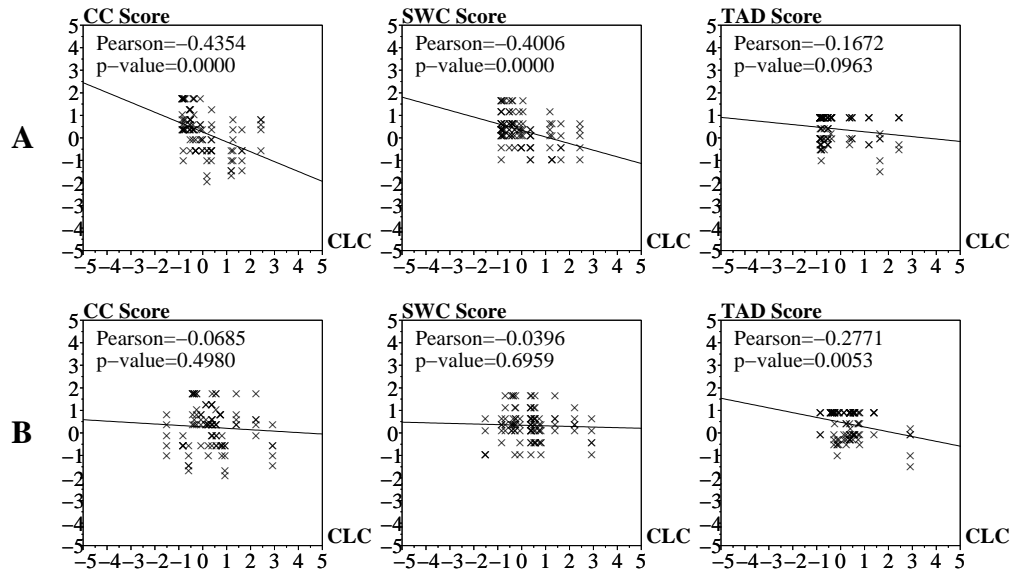


Figure 6: Correlations between the clustering coefficients (CLC , horizontal axes) and the scores (vertical axes) for the 20 texts with the lowest score dispersion. In the vertical axes, SWC stands for standard writing conventions, TAD for theme adequacy/development and CC for coherence and cohesion. Both axes are standardized into a standard normal distribution $N(0, 1)$. Measurements obtained from the two types of networks, NET-A and NET-B, are discriminated by the labels A and B, respectively.

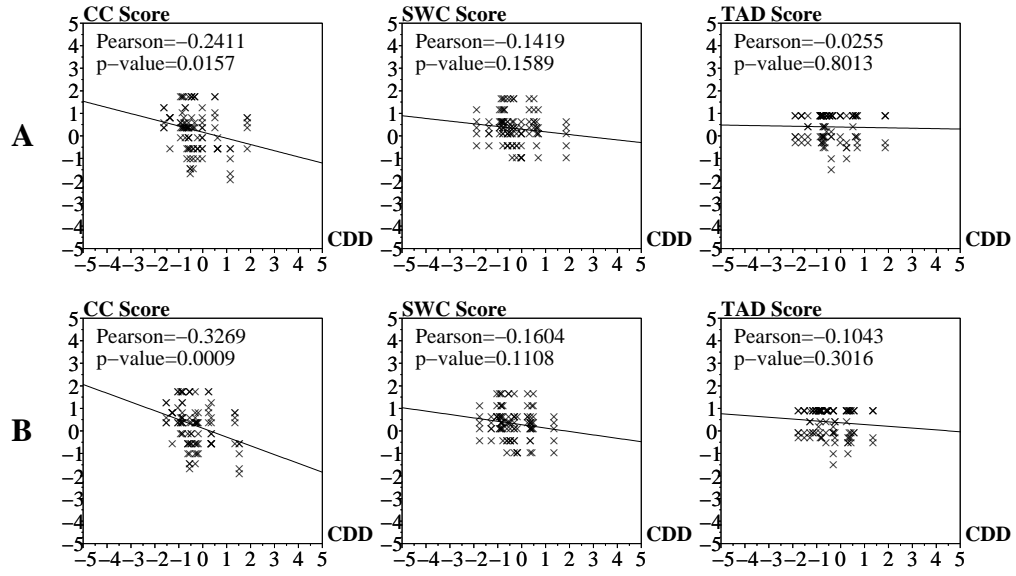


Figure 7: Correlations between the components dynamics deviations (CDD , horizontal axes) and the scores (vertical axes) for the 20 texts with the lowest score dispersion. In the vertical axes, SWC stands for standard writing conventions, TAD for theme adequacy/development and CC for coherence and cohesion. Both axes are standardized into a standard normal distribution $N(0, 1)$. Measurements obtained from the two types of networks, NET-A and NET-B, are discriminated by the labels A and B, respectively.

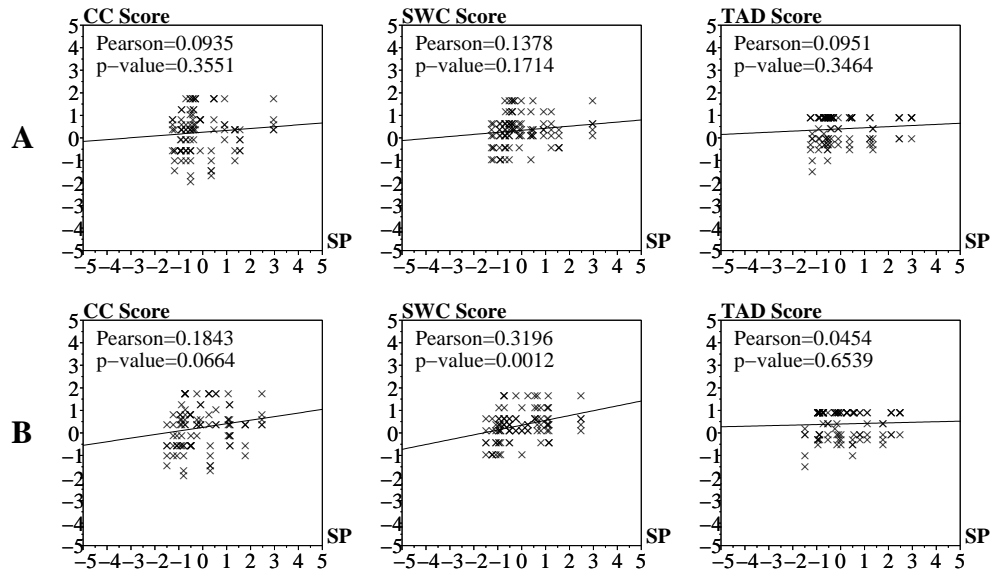


Figure 8: Correlations between the shortest paths (SP , horizontal axes) and the scores (vertical axes) for the 20 texts with the lowest score dispersion. In the vertical axes, SWC stands for standard writing conventions, TAD for theme adequacy/development and CC for coherence and cohesion. Both axes are standardized into a standard normal distribution $N(0, 1)$. Measurements obtained from the two types of networks, NET-A and NET-B, are discriminated by the labels A and B, respectively.

which also included those with large dispersions in the scores assigned by the human judges (results not shown here). The trend toward decreasing scores with the number of outdegrees and clustering coefficient suggests that text lose quality if the concepts are highly interconnected. With the analysis of the network dynamics, one infers that the faster and closer a writer introduces new concepts not seen so far in a text, the worse the text is.

Though based on a particular set of texts and specific language, the results presented here point to potential applications in other instances of text analysis. Indeed, the relatively high correlations obtained between human assessment and network measurements are to some extent surprising because of the potential complexity and subjectivity underlying text quality and human language. One can now envisage, for instance, an expert system that automatically marks essays, based on machine learning methods. This will require golden standards, with a panel of human judges agreeing on scores for a given set of texts (say 100 texts), with very little dispersion. If the network measurements are taken for these manually-marked essays and associated with the corresponding scores, machine learning algorithms may be used to classify the remaining texts. This is an interesting scenario for exams involving thousands of essays. Moreover, for essays with a pre-defined specific topic the expert system could be further sophisticated to consider the use of expected concepts and associations among these concepts. Finally, the approach presented here paves the way for the concepts of complex networks to be applied to other types of text, as in the identification of text genres and authorships, in addition to systems of information retrieval and automatic summarization. This may have a large impact in areas such as natural language processing [29], in particular, and linguistic studies in general.

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References

- [1] R. Albert, A.L. Barabási, *Rev. Mod. Phys.* **74**, 47 (2002)
- [2] S.N. Dorogovtsev, J.F.F. Mendes, *Adv. Complex. Syst.* **51**(4), 1079 (2002)
- [3] M.E.J. Newman, *SIAM Rev.* **45**, 167 (2003)
- [4] H. Jeong, S. Mason, A.L. Barabási, Z.N. Oltvai, *Nature* **411**, 41 (2001)
- [5] N. Schwartz, R. Cohen, D. ben Avraham, A.L. Barabási, S. Havlin, *Phys. Rev. E* **66**, 015104 (2002)
- [6] R. Albert, H. Jeong, A.L. Barabási, *Nature* **401**, 130 (1999)
- [7] P. Gleiser, L. Danon, *Adv. Complex. Syst.* **6**(4), 565 (2003)
- [8] L.L. Gonalves, L.B. Gonalves (2005), *cond-mat/0501361*
- [9] M.A. Montemurro, D.H. Zanette, *Adv. Complex. Syst.* **5**(1), 7 (2002)
- [10] H. Zhou, G.W. Slater, *Physica A* **329**, 309 (2003)
- [11] L.F. Costa, F.A. Rodrigues, G. Travieso, P.R.V. Boas (2005), *cond-mat/0505185*
- [12] R. Ferrer i Cancho, R.V. Solé, P. Roy. Soc. Lond. B Bio. **268**, 2261 (2001)
- [13] S.N. Dorogovtsev, J.F.F. Mendes, P. Roy. Soc. Lond. B Bio. **268**, 2603 (2001)
- [14] P. Allegrini, P. Grigolini, L. Palatella (2003), *cond-mat/0310648*
- [15] R. Milo, S. Itzkovitz, N. Kashtan, R. Levitt, S. Shen-Orr, I. Ayzenshtat, M. Sheffer, U. Alon, *Science* **303**, 1538 (2004)
- [16] M. Steyvers, J.B. Tenenbaum (2001), *cond-mat/0110012*
- [17] O. Kinouchi, A.S. Martinez, G.F. Lima, G.M. Loureno (2001), *cond-mat/0110217*

- [18] M. Sigman, G.A. Cecchi, PNAS **99**(3), 1742 (2002)
- [19] A.E. Motter, A.P.S. Moura, Y.C. Lai, P. Dasgupta, Phys. Rev. E **65**, 065102 (2002)
- [20] A.J. Holanda, I.T. Pisa, O. Kinouchi, A.S. Martinez, E.E.S. Ruiz, Physica A **344**, 530 (2004)
- [21] B. Dorow, D. Widdows, K. Ling, J.P. Eckmann, D. Sergi, E. Moses, *Using Curvature and Markov Clustering in Graphs for Lexical Acquisition and Word Sense Discrimination*, in *2nd Workshop organized by the MEANING Project (MEANING-2005)* (Trento, Italy, 2005)
- [22] L.F. Costa, Int. J. Mod. Phys. C **15**, 371 (2004)
- [23] A. Capocci, V.D.P. Servedio, G. Caldarelli, F. Colaiori (2004), cond-mat/0402499
- [24] R. Ferrer i Cancho, R.V. Solé, R. Khler, Phys. Rev. E **69**, 051915 (2004)
- [25] R. Ferrer i Cancho, A. Capocci, G. Caldarelli (2005), cond-mat/0504165
- [26] T.H. Cormen, C.E. Leiserson, R.L. Rivest, C. Stein, *Introduction to Algorithms* (The MIT Press, New York, 2001)
- [27] L. Antigueira, M.G.V. Nunes, O.N.O. Jr., L.F. Costa (2005), physics/0504033
- [28] J. Neter, M.H. Kutner, C.J. Nachtsheim, W. Wasserman, *Applied Linear Statistical Models* (Irwin, Chicago, 1996)
- [29] A.K. Joshi, Science **253**, 1242 (1991)