

1. Zoradte čísla od najmenšieho po najväčšie

- a.  $(0,85)^{-4}; (2,1)^{-4}; (-0,9)^{-4}; (6,1)^{-4}; (-2,3)^{-4}$   
 b.  $3^{500}; 3^{700}; 5^{300}; 5^{500}; 5^{700}; 7^{300}; 7^{500}$

2. Vypočítajte bez použitia kalkulačky

- a.  $\sqrt{0,0121} = \sqrt{121 \cdot 10^{-4}} = \sqrt{121} \cdot \sqrt{10^{-4}} = 11 \cdot 10^{-2} = 0,11$   
 b.  $\sqrt{160\,000} = \sqrt{16 \cdot 10^4} = 4 \cdot 10^2 = 400$   
 c.  $\sqrt{14\,400} = 120$   
 d.  $\sqrt{0,0064} = 0,08$   
 e.  $\sqrt{\frac{6^2-11}{\frac{20}{5}}} = \sqrt{\frac{25}{4}} = \frac{5}{2}$

3. Vypočítajte

- a.  $(\sqrt{12} \cdot \sqrt{24}) : \sqrt{8} = \sqrt{\frac{12 \cdot 24}{8}} = \sqrt{36} = 6$   
 b.  $\sqrt{9+3\sqrt{3}} \cdot \sqrt{9-3\sqrt{3}} = \sqrt{(9+3\sqrt{3})(9-3\sqrt{3})} = \sqrt{81-27} = \sqrt{54} = \sqrt{9 \cdot 6} = 3\sqrt{6}$   
 c.  $(\sqrt{2})^2 + (\sqrt{8})^2 = 2 + 8 = 10$   
 d.  $(\sqrt{5-\sqrt{3}} + \sqrt{5+\sqrt{3}})^2 = (\sqrt{5-\sqrt{3}} + \sqrt{5+\sqrt{3}}) \cdot (\sqrt{5-\sqrt{3}} + \sqrt{5+\sqrt{3}}) = 5 - \sqrt{3} + 5 + \sqrt{3} + 2\sqrt{(5-\sqrt{3})(5+\sqrt{3})} = 10 + 2\sqrt{25-3} = 10 + 2\sqrt{22}$   
 e.  $\left(\frac{\sqrt{5}+1}{2}\right)^{2000} \cdot \left(\frac{\sqrt{5}-1}{2}\right)^{2000} = \left(\frac{(\sqrt{5}+1)(\sqrt{5}-1)}{4}\right)^{2000} = \left(\frac{5-1}{4}\right)^{2000} = 1^{2000} = 1$   
 $a^2 \cdot b^2 = (a \cdot b)^2$

4. Vzorec  $a\sqrt{b} = \sqrt{a^2 b}$  pre kladné  $a, b$  použite v „obidvoch smeroch“, aby ste daný výraz vyjadrili druhou odmocninou z jediného prirodzeného čísla.

- a.  $6\sqrt{3} = \sqrt{6^2 \cdot 3} = \sqrt{36 \cdot 3} = \sqrt{108}$   
 b.  $\sqrt{8} + \sqrt{2} = \sqrt{4 \cdot 2} + \sqrt{2} = 2\sqrt{2} + \sqrt{2} = 3\sqrt{2} = \sqrt{3^2 \cdot 2} = \sqrt{18}$   
 c.  $\sqrt{18} - \sqrt{8} = \sqrt{2}$   
 d.  $3\sqrt{7} + \sqrt{112} = 3\sqrt{7} + \sqrt{16 \cdot 7} = 3\sqrt{7} + 4\sqrt{7} = 7\sqrt{7} = \sqrt{49 \cdot 7} = \sqrt{343}$   
 e.  $3\sqrt{18} + \sqrt{72} = \sqrt{450}$

5. Číselné výrazy upravte na súčet alebo rozdiel druhých odmocnín a prirodzených čísel.

- a.  $\sqrt{80} + \sqrt{75} - \sqrt{48} + \sqrt{125} - \sqrt{27} = 4\sqrt{5} + 5\sqrt{3} - 4\sqrt{3} + 5\sqrt{5} - 3\sqrt{3} = 9\sqrt{5} + 2\sqrt{3}$   
 b.  $(\sqrt{6} - 3\sqrt{3} + 5\sqrt{2} - \sqrt{8}) \cdot \sqrt{6} = 6 - 9\sqrt{2} + 10\sqrt{3} - 4\sqrt{3} = 6 - 9\sqrt{2} + 6\sqrt{3}$   
 c.  $(\sqrt{3} + \sqrt{5} + \sqrt{7}) + (\sqrt{3} - \sqrt{5} + \sqrt{7}) = 2\sqrt{3} + 2\sqrt{7} = 2(\sqrt{3} + \sqrt{7})$

$$\begin{aligned} \text{d. } (2\sqrt{5} + 5\sqrt{2})^2 - (10 + \sqrt{10})^2 &= (2\sqrt{5} + 5\sqrt{2})(2\sqrt{5} + 5\sqrt{2}) - (10 + \sqrt{10})(10 + \sqrt{10}) = \\ &= 20 + 20\sqrt{10} + 50 - 100 - 20\sqrt{10} - 10 = -40. \\ \text{e. } \sqrt{40 \cdot 15 \cdot 96} - \sqrt{12 \cdot 108} &= \sqrt{2^3 \cdot 5 \cdot 3 \cdot 5 \cdot 2^5 \cdot 3} - \sqrt{2^2 \cdot 3 \cdot 3^3 \cdot 2} = \sqrt{2^8 \cdot 3^2 \cdot 5^2} - \sqrt{2^4 \cdot 3^4} = 2^4 \cdot 3 \cdot 5 - 2^2 \cdot 3^2 = \\ &= 204. \end{aligned}$$

6. Usmernite zlomky

$$\begin{aligned} \text{a. } \frac{\sqrt{2}}{1+\sqrt{2}} \cdot \frac{1-\sqrt{2}}{1-\sqrt{2}} &= \frac{\sqrt{2}-2}{1-2} = \frac{\sqrt{2}-2}{-1} = 2-\sqrt{2}; \\ \text{b. } \frac{4}{\sqrt{5}-1} \cdot \frac{\sqrt{5}+1}{\sqrt{5}+1} &= \frac{4(\sqrt{5}+1)}{5-1} = \frac{4(\sqrt{5}+1)}{4} = \sqrt{5}+1; \\ \text{c. } \frac{\sqrt{6}}{\sqrt{3}+\sqrt{2}} \cdot \frac{\sqrt{3}-\sqrt{2}}{\sqrt{3}-\sqrt{2}} &= \frac{\sqrt{18}-\sqrt{12}}{3-2} = \frac{3\sqrt{2}-2\sqrt{3}}{1} = 3\sqrt{2}-2\sqrt{3}; \\ \text{d. } \frac{(1+\sqrt{2}+\sqrt{3})}{(1+\sqrt{2})+\sqrt{3}} \cdot \frac{(1+\sqrt{2})+\sqrt{3}}{(1+\sqrt{2})+\sqrt{3}} &= \frac{(1+\sqrt{2}+\sqrt{3})^2}{(1+\sqrt{2})^2 + 2\sqrt{2} + 3} = \frac{6+2\sqrt{2}+2\sqrt{3}+2\sqrt{6}}{1+2\sqrt{2}+2-3} = \\ &= \frac{6+2\sqrt{2}+2\sqrt{3}+2\sqrt{6}}{2\sqrt{2}} = \frac{\sqrt{2}(3+\sqrt{2}+\sqrt{3}+\sqrt{6})}{2\sqrt{2}} = \frac{3+\sqrt{2}+\sqrt{3}+\sqrt{6}}{2} \cdot \frac{\sqrt{2}}{\sqrt{2}} = \\ &= \frac{\sqrt{2}(3+\sqrt{2}+\sqrt{3}+\sqrt{6})}{2} = \frac{3\sqrt{2}+2+\sqrt{6}+\sqrt{12}}{2} = \frac{3\sqrt{2}+2+\sqrt{6}+2\sqrt{3}}{2} \end{aligned}$$

7. Porovnajte, ktoré číslo je väčšie  $A = \frac{6\sqrt{5}}{\sqrt{12}} \cdot \frac{\sqrt{10}}{\sqrt{12}}$   $B = \frac{15\sqrt{2}}{\sqrt{30}} \cdot \frac{\sqrt{10}}{\sqrt{12}}$

8. Vypočítajte

$$\begin{aligned} \text{a. } \left(\frac{2}{\sqrt{3}} - 1\right) : \left(2 - \frac{\sqrt{3}}{3}\right) \\ \text{b. } (\sqrt{7} + 4) \cdot \left(\frac{21}{2\sqrt{7}} - \frac{12}{\sqrt{7}+1}\right) \\ \text{c. } (\sqrt{5})^{-4} \\ \text{d. } (2 - \sqrt{2})^{-2} \\ \text{e. } (1 + \sqrt{2})^{-4} \cdot (3 + 2\sqrt{2})^{-3} \end{aligned}$$

$$A = \sqrt{15} = B = \sqrt{15}$$

$$\begin{aligned} &= \frac{\sqrt{2}(3+\sqrt{2}+\sqrt{3}+\sqrt{6})}{2} \\ &= \frac{\sqrt{2} \cdot \sqrt{30}}{2} = \frac{\sqrt{60}}{2} = \sqrt{\frac{60}{4}} = \sqrt{15} \\ &= \sqrt{30} \cdot \sqrt{30} = \sqrt{900} = 30 \\ &= (\sqrt{30})^2 = 30 \end{aligned}$$

9. Ako vieme usmerniť výraz  $\frac{1}{\sqrt{x}-\sqrt{y}}$ ,  $x > 0, y > 0, x \neq y$ ?

10. Ako vieme upraviť výraz  $(\sqrt{x} + \sqrt{y})^{-1}$ ?