In this example, we illustrate various unsupervised learning techniques (Clustering, PCA, SVD) using an example term-document matrix as the data.

```
In [1]:
         import numpy as np
          import pylab as pl
          import pandas as pd
          from sklearn.cluster import KMeans
In [2]: cd D:\Documents\Class\CSC478\Data
         D:\Documents\Class\CSC478\Data
In [4]: Data = pd.read_csv('term-doc-mat.csv', header=None)
          TD = Data.ix[:,1:]
          TD
Out[4]:
                2
                          5
                                  7
                                                        13
                                                               15
                    3
                        4
                              6
                                     8
                                         9
                                             10 11
                                                    12
                                                            14
          0
            24
                32
                    12
                        6
                          43
                              2
                                  0
                                      3
                                                 4
                                                    0
                                                        0
                                                            0
                                                               0
                                         1
                                             6
          1
             9
                5
                    5
                        2
                          20
                              0
                                  1
                                     0
                                         0
                                             0
                                                 27
                                                    14
                                                        3
                                                            2
                                                                11
          2
            0
                3
                    0
                        0
                          3
                              7
                                     4
                                         27
                                             4
                                                 0
                                                        0
                                                               0
                                  12
                                                    1
                                                            0
          3
            3
                    0
                              16
                                      2
                                                7
                                                        21
                                                               2
                0
                        0
                          0
                                  0
                                         25
                                             23
                                                    12
                                                            3
                    0
          4
             1
                0
                        0
                          0
                              33
                                  2
                                     0
                                         7
                                             12 | 14
                                                    5
                                                        12
                                                            4
                                                               0
          5
            12
                2
                    0
                        0 27
                              0
                                  0
                                      0
                                         0
                                             22 9
                                                    4
                                                        0
                                                            5
                                                               3
          6
            0
                0
                    0
                        0
                          0
                                 32
                                     22
                                         34
                                             17 0
                                                    0
                                                        0
                                                               0
                              18
                                                            0
                          2
             1
                0
                    0
                        0
                              0
                                      0
                                         3
                                             9
                                                 27
                                                    7
                                                        5
                                                               4
                                  0
                                                            4
                        7
            21
                          31
                              0
                                                        0
          8
                10
                    16
                                  0
                                     0
                                         0
                                             0
                                                 0
                                                    0
                                                            1
                                                               0
            2
                0
                    0
                        2
                          0
                              27
                                  4
                                      2
                                             8
                                                 33
                                                        14
                                                               3
                                         11
                                                    16
```

```
In [5]: terms = Data.ix[:,0]
    terms
```

```
Out[5]: 0
                 database
                    index
         1
         2
               likelihood
         3
                   linear
         4
                   matrix
         5
                    query
         6
               regression
         7
               retrieval
         8
                      sql
                   vector
         Name: 0, dtype: object
```

First, we want to do some document clustering. Since the data is in term-document format, we need to obtain the transpose of the TD matrix.

Now we have a document-term matrix:

In [8]: DT

Out[8]:

	0	1	2	3	4	5	6	7	8	9
1	24	9	0	3	1	12	0	1	21	2
2	32	5	3	0	0	2	0	0	10	0
3	12	5	0	0	0	0	0	0	16	0
4	6	2	0	0	0	0	0	0	7	2
5	43	20	3	0	0	27	0	2	31	0
6	2	0	7	16	33	0	18	0	0	27
7	0	1	12	0	2	0	32	0	0	4
8	3	0	4	2	0	0	22	0	0	2
9	1	0	27	25	7	0	34	3	0	11
10	6	0	4	23	12	22	17	9	0	8
11	4	27	0	7	14	9	0	27	0	33
12	0	14	1	12	5	4	0	7	0	16
13	0	3	0	21	12	0	0	5	0	14
14	0	2	0	3	4	5	0	4	1	7
15	0	11	0	2	0	3	0	4	0	3

In [12]: numTerms=len(terms) numTerms

Out[12]: 10

Next, we will transform the data to TFxIDF weights:

In [13]: # Find doucment frequencies for each term DF = np.array([(DT!=0).sum(0)])print DF

[[10 11 8 10 9 8 5 9 6 12]]

In [15]: NDocs = len(DT[0])
print NDocs

15

- In [16]: # Create a matrix with all entries = NDocs
 NMatrix=np.ones(np.shape(DT), dtype=float)*NDocs
- In [17]: # Convert each entry into IDF values
 # Note that IDF is only a function of the term, so all rows will be identical.
 DivM = np.divide(NMatrix, DF)
 IDF = np.log2(DivM)
- In [18]: np.set_printoptions(precision=2, suppress=True)
 print IDF[0:2,]

[[0.58 0.45 0.91 0.58 0.74 0.91 1.58 0.74 1.32 0.32] [0.58 0.45 0.91 0.58 0.74 0.91 1.58 0.74 1.32 0.32]]

- In [19]: # Finally compute the TFxIDF values for each document-term entry
 DT_tfidf = DT * IDF
- In [21]: DT_tfidf
- Out[21]:

	0	1	2	3	4	5	6	7
1	14.039100	4.027131	0.000000	1.754888	0.736966	10.882687	0.000000	0.7369
2	18.718800	2.237295	2.720672	0.000000	0.000000	1.813781	0.000000	0.0000
3	7.019550	2.237295	0.000000	0.000000	0.000000	0.000000	0.000000	0.0000
4	3.509775	0.894918	0.000000	0.000000	0.000000	0.000000	0.000000	0.0000
5	25.153388	8.949180	2.720672	0.000000	0.000000	24.486046	0.000000	1.4739
6	1.169925	0.000000	6.348234	9.359400	24.319865	0.000000	28.529325	0.0000
7	0.000000	0.447459	10.882687	0.000000	1.473931	0.000000	50.718800	0.0000
8	1.754888	0.000000	3.627562	1.169925	0.000000	0.000000	34.869175	0.0000
9	0.584963	0.000000	24.486046	14.624063	5.158759	0.000000	53.888725	2.2108
10	3.509775	0.000000	3.627562	13.454138	8.843587	19.951593	26.944363	6.6326
11	2.339850	12.081392	0.000000	4.094738	10.317518	8.162015	0.000000	19.898
12	0.000000	6.264426	0.906891	7.019550	3.684828	3.627562	0.000000	5.1587
13	0.000000	1.342377	0.000000	12.284213	8.843587	0.000000	0.000000	3.6848
14	0.000000	0.894918	0.000000	1.754888	2.947862	4.534453	0.000000	2.9478
15	0.000000	4.922049	0.000000	1.169925	0.000000	2.720672	0.000000	2.9478

Now we are ready for clustering

Let's take a look at the cluster centroids

```
print "\t\tCluster0\tCluster1\tCluster2"
In [26]:
          for i in range(len(terms)):
              print "%10s\t%.4f\t\t%.4f\t\t%.4f" %(terms[i],centroids tfidf[0][i],centro
          ids_tfidf[1][i],centroids_tfidf[2][i])
                           Cluster0
                                            Cluster1
                                                            Cluster2
            database
                                            1.4039
                                                             13.6881
                           0.4680
               index
                           5,1010
                                            0.0895
                                                             3,6692
          likelihood
                           0.1814
                                            9.7944
                                                             1.0883
              linear
                           5.2647
                                            7.7215
                                                            0.3510
                           5.1588
                                            7,9592
                                                            0.1474
              matrix
               query
                           3.8089
                                            3.9903
                                                            7.4365
                          0.0000
                                            38.9901
                                                            0.0000
          regression
           retrieval
                           6.9275
                                            1.7687
                                                            0.4422
                 sal
                           0.2644
                                            0.0000
                                                             22,4728
              vector
                           4.7002
                                            3.3481
                                                             0.2575
```

Because the centroids are based on TFxIDF weights, they are not as descriptive as raw term frequencies or binary occurrence data. Let's redo the clustering with the original raw term frequencies.

```
In [27]: DT = np.array(DT)
    centroids, clusters = kMeans.kMeans(DT, 3, kMeans.distCosine, kMeans.randCent)

Iteration   1
    Iteration   2
    Iteration   3
    Iteration   4
    Iteration   5
```

```
In [28]:
          print "\t\tCluster0\tCluster1\tCluster2"
          for i in range(len(terms)):
              print "%10s\t%.4f\t\t%.4f\t\t%.4f" %(terms[i],centroids[0][i],centroids[1]
          [i],centroids[2][i])
                           Cluster0
                                             Cluster1
                                                              Cluster2
            database
                           1.7143
                                             23.4000
                                                               1.3333
               index
                           8.1429
                                             8.2000
                                                              0.3333
          likelihood
                           1.7143
                                             1.2000
                                                               14.3333
              linear
                           12.0000
                                             0.6000
                                                              9.0000
              matrix
                           11.4286
                                             0.2000
                                                               3.0000
                           6.1429
                                             8,2000
                                                              0.0000
               query
          regression
                           5.0000
                                             0.0000
                                                               29.3333
           retrieval
                           8.0000
                                             0.6000
                                                               1.0000
                           0.1429
                                             17.0000
                                                              0.0000
                  sql
                           15.4286
                                             0.8000
                                                               5.6667
              vector
In [29]:
          print clusters
          [[ 1.
                    0.
           [ 1.
                    0.01]
             1.
                    0.01]
             1.
                    0.01]
             1.
                    0.
                    0.03]
             0.
             2.
                    0.
             2.
                    0.
                        ]
             2.
                    0.
                    0.051
             0.
             0.
                    0.02]
                    0.01]
             0.
             0.
                    0.01]
                    0.01]
             0.
           [ 0.
                    0.14]]
In [30]:
          print centroids
             1.71
                      8.14
                              1.71
                                    12.
                                            11.43
                                                     6.14
                                                            5.
                                                                    8.
                                                                            0.14
                                                                                  15.43]
          ΓΓ
             23.4
                      8.2
                              1.2
                                     0.6
                                             0.2
                                                     8.2
                                                            0.
                                                                    0.6
                                                                           17.
                                                                                   0.8 ]
              1.33
                      0.33
                            14.33
                                     9.
                                             3.
                                                     0.
                                                           29.33
                                                                            0.
                                                                                   5.67]]
                                                                    1.
```

Next, let's use principal component analysis to reduce the dimensionality of the data:

```
In [31]: from sklearn import decomposition
```

We'll perform PCA to obtain the top 5 components and then transform the DT matrix into the lower dimensional space of 5 components:

```
In [32]: pca = decomposition.PCA(n_components=5)
DTtrans = pca.fit(DT).transform(DT)
```

```
In [33]:
         np.set printoptions(precision=2, suppress=True)
         print DTtrans
         [[-25.45
                   -1.8
                           4.02
                                 -3.12
                                         -0.24]
          [-23.78]
                   -7.29 -0.53
                                 -4.77
                                          6.321
                   -5.44 -10.09
                                 -3.46
                                          2.87]
          [-15.03
                   -4.39 -14.84
                                          0.44]
          [ -6.75
                                 -3.08
          [-46.7
                    0.01
                          21.78
                                  3.11
                                        -0.29]
          [ 27.41
                    7.93
                          12.27 -15.16
                                        13.47]
            15.67 -21.74
                          -1.33 11.4
                                          5.81]
             8.28 -16.54
                          -6.94
                                  5.39
                                         1.47]
            29.51 -18.64
                          16.68
                                  4.82
                                        -1.69]
            11.41
                    0.44
                          15.03
                                 -3.03 -17.19]
             6.98 37.69
                                         5.5 ]
                           4.5
                                 14.83
             5.97 13.91
                          -6.64
                                  2.12
                                        -3.321
          [ 12.36 10.4
                          -4.93 -11.5
                                        -5.51]
             1.67
                    2.69 -13.18 -2.04
                                        -3.72]
          [ -1.53
                    2.79 -15.8
                                  4.49
                                        -3.94]]
In [34]: print(pca.explained_variance_ratio_)
         [ 0.45 0.23 0.15 0.07 0.05]
```

Looking at the above, it can be observed that the first 5 components capture (explain) 95% of the variance in the data.

Now, we can redo the clustering, but this time in the lower dimensional space:

```
In [35]: centroids_pca, clusters_pca = kMeans.kMeans(DTtrans, 3, kMeans.distCosine, kMe
ans.randCent)

Iteration 1
Iteration 2
Iteration 3
Iteration 4
Iteration 5
Iteration 6
```

```
In [36]:
          print clusters pca
                     0.
           [[ 0.
                         1
            [ 0.
                     0.
                         ]
            Γ
              0.
                     0.061
              2.
                     0.12]
              0.
                     0. ]
              1.
                     0.03]
              2.
                     0.12]
            [ 2.
                     0.021
              1.
                     0.21]
            [ 1.
                     0.14]
                     0.2 1
             1.
            [ 1.
                     0.21]
            [ 1.
                     0.1 ]
            [ 2.
                     0.16]
            [ 2.
                     0.12]]
```

Next, let's actually derive the principal components manaually using linear algebra rather than relying on the PCA package from sklearn:

First step is to obtain the covariance matrix:

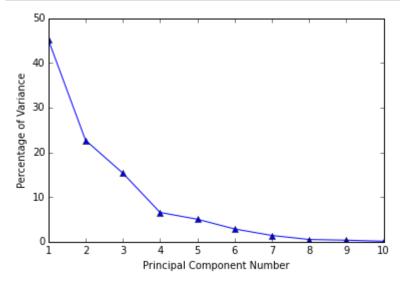
```
meanVals = np.mean(DT, axis=0)
In [38]:
          meanRemoved = DT - meanVals #remove mean
          covMat = np.cov(meanRemoved, rowvar=0)
          np.set printoptions(precision=2, suppress=True, linewidth=100)
          print covMat
          [[ 179.7
                      38.44
                             -17.06
                                      -50.7
                                               -40.93
                                                         66.87
                                                                -60.9
                                                                         -19.62
                                                                                 116.32
                                                                                          -5
          9.49]
                              -21.54
                                      -19.81
                                                -6.5
                                                         31.83
                                                                -55.7
                                                                                           2
           [ 38.44
                      67.26
                                                                          38.13
                                                                                  27.67
          7.04]
                                                       -11.61
           [ -17.06
                     -21.54
                               51.78
                                        31.1
                                                 9.36
                                                                 77.41
                                                                          -8.72
                                                                                 -16.2
          4.67]
                                       85.97
                                                51.43
                                                         2.54
                                                                 45.59
                                                                          15.13
                                                                                 -41.97
           [ -50.7
                     -19.81
                               31.1
                                                                                           4
          7.47]
           [ -40.93
                      -6.5
                                9.36
                                        51.43
                                                80.57
                                                         -4.43
                                                                 25.86
                                                                          17.64
                                                                                 -35.07
                                                                                           7
          4.14]
                                        2.54
           [ 66.87
                      31.83
                              -11.61
                                                -4.43
                                                         72.97
                                                                -22.49
                                                                          15.7
                                                                                  45.17
          8.391
                     -55.7
                               77.41
                                       45.59
                                                25.86
                                                       -22.49
                                                                162.03
                                                                                 -50.37
           [ -60.9
                                                                         -18.1
          7.87]
                                                         15.7
                                                                -18.1
                                                                                 -19.18
           [ -19.62
                      38.13
                               -8.72
                                       15.13
                                                17.64
                                                                          48.12
                                                                                           4
          9.06]
           [ 116.32
                      27.67
                              -16.2
                                       -41.97
                                               -35.07
                                                         45.17
                                                                -50.37
                                                                         -19.18
                                                                                  93.92
                                                                                          -4
          8.33]
           [ -59.49
                      27.04
                                4.67
                                       47.47
                                                74.14
                                                         -8.39
                                                                  7.87
                                                                          49.06
                                                                                 -48.33
                                                                                         10
          2.26]]
```

```
In [48]:
         import numpy.linalg as la
         eigVals,eigVects = la.eig(np.mat(covMat))
In [49]: print eigVals
                                                                            3.25
         [ 426.77 214.24 144.96
                                    61.87
                                           47.51
                                                   26.97
                                                           13.24
                                                                    1.06
         4.71]
In [50]: print eigVects
         [[-0.57 -0.09 0.46 -0.14 -0.26 -0.15 0.58 0.05 -0.1 -0.02]
                             0.51 -0.12 -0.19 -0.22 -0.3 -0.35 -0.49]
          [-0.18 0.39 0.1
          [ 0.18 -0.26 0.3
                             0.19 -0.11 -0.48 -0.11 -0.06 0.69 -0.2
                        0.36 -0.35 0.53 -0.49 -0.02 -0.03 -0.36 0.03]
          [ 0.29 0.1
          [ 0.26  0.27  0.31 -0.47 -0.33  0.34 -0.05 -0.53  0.14 -0.11]
          [-0.21 0.13 0.43 0.13 0.56 0.51 -0.09 0.2
                                                           0.27 - 0.21
          [ 0.4 -0.51 0.42 0.37 -0.17 0.28 0.01 -0.01 -0.38 0.12]
          [ 0.06  0.38  0.08  0.41  0.14 -0.05  0.28 -0.33  0.17
                                                                0.661
          [-0.42 -0.08 0.23 -0.11 -0.14 -0.07 -0.72 -0.01 -0.05
                                                                 0.461
          [ 0.28  0.51  0.21  0.03  -0.37  -0.04  -0.04  0.69  0.01  0.07]]
In [51]: eigValInd = np.argsort(eigVals) #sort, sort goes smallest to largest
         eigValInd = eigValInd[::-1]
                                     #reverse
         sortedEigVals = eigVals[eigValInd]
         print sortedEigVals
         total = sum(sortedEigVals)
         varPercentage = sortedEigVals/total*100
         print varPercentage
         [ 426.77 214.24 144.96
                                    61.87
                                           47.51
                                                   26.97
                                                           13.24
                                                                    4.71
                                                                            3.25
         1.06]
         [ 45.18 22.68 15.35
                                6.55
                                        5.03
                                              2.86
                                                     1.4
                                                            0.5
                                                                   0.34
                                                                          0.11]
```

We can plot the principal components based on the percentage of variance they capture:

```
In [53]: import matplotlib.pyplot as plt
%matplotlib inline

fig = plt.figure()
    ax = fig.add_subplot(111)
    ax.plot(range(1, 11), varPercentage[:10], marker='^')
    plt.xlabel('Principal Component Number')
    plt.ylabel('Percentage of Variance')
    plt.show()
```



```
[[-25.45
          -1.8
                  4.02
                        -3.12
                                 0.24]
[-23.78
          -7.29
                -0.53
                        -4.77
                                -6.32]
[-15.03
         -5.44 -10.09
                                -2.87]
                        -3.46
[ -6.75
         -4.39 -14.84
                        -3.08
                                -0.44]
 [-46.7
          0.01
                21.78
                         3.11
                                 0.291
 [ 27.41
           7.93
                 12.27 -15.16 -13.47]
  15.67 -21.74
                 -1.33
                        11.4
                                -5.81]
   8.28 -16.54
                 -6.94
                               -1.47]
                         5.39
  29.51 -18.64
                 16.68
                         4.82
                                1.69]
                               17.19]
  11.41
          0.44
                 15.03
                        -3.03
   6.98 37.69
                  4.5
                        14.83
                                -5.5 ]
   5.97
         13.91
                 -6.64
                         2.12
                                 3.321
  12.36 10.4
                 -4.93 -11.5
                                 5.51]
           2.69 -13.18
                        -2.04
                                 3.72]
   1.67
  -1.53
           2.79 -15.8
                         4.49
                                 3.94]]
```

Next, let's look at an application of Singular Value Decomposition. This time, we'll foucs on the term-document matrix in order to find themes based on combinations of terms.

```
In [56]: u, s, vt = la.svd(TD, full matrices=False)
In [57]:
          print u
                                                               0.07 -0.07
           [[ 0.39 -0.6
                            0.22
                                   0.17
                                          0.22 -0.1
                                                       -0.59
                                                                             0.041
                                          0.06 -0.17
              0.3
                    -0.2
                           -0.33 -0.5
                                                        0.21 -0.08 -0.57 -0.31]
              0.2
                            0.33 -0.16
                                          0.04 - 0.4
                                                              -0.76 0.23 -0.02]
                     0.16
                                                        0.
                                   0.42 -0.49 -0.53
              0.37
                     0.27
                            0.
                                                        0.04
                                                               0.27 -0.16 -0.05]
              0.32
                     0.23 - 0.19
                                   0.49 0.31
                                                 0.38
                                                        0.03 -0.22
                                                                      0.
                                                                            -0.521
              0.29 -0.23 -0.02
                                         -0.66
                                                        0.07 -0.31 -0.03
                                   0.
                                                 0.53
              0.36
                     0.38
                            0.62 -0.35
                                          0.08
                                                 0.3
                                                        0.02
                                                               0.34 - 0.1
                                                                           -0.031
              0.21
                     0.05 -0.34 -0.38 -0.2
                                                -0.02 -0.28
                                                               0.21
                                                                      0.65 - 0.331
                                                               0.18
              0.23 - 0.44
                           0.15
                                  0.11
                                          0.15 -0.09
                                                        0.72
                                                                      0.38 -0.021
              0.42
                    0.25 -0.42 -0.03 0.33
                                               0.
                                                        0.02
                                                               0.01
                                                                      0.07
                                                                             0.68]]
In [58]:
           print s
           [ 93.97 77.25 54.14
                                     29.74
                                             26.27
                                                      19.76
                                                              13.75
                                                                       9.41
                                                                               7.88
                                                                                        3.88]
In [60]:
           print np.diag(s)
           [[ 93.97
                               0.
                                        0.
                                                0.
                       0.
                                                        0.
                                                                0.
                                                                        0.
                                                                                 0.
                                                                                         0.
                                                                                              1
               0.
                      77.25
                               0.
                                        0.
                                                0.
                                                        0.
                                                                0.
                                                                        0.
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                                                                                              ]
               0.
                       0.
                               54.14
                                        0.
                                                0.
                                                        0.
                                                                0.
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                                                                                         0.
                                                                                              ]
                               0.
                                       29.74
               0.
                       0.
                                                0.
                                                        0.
                                                                0.
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                                                                                 0.
                                                                                         0.
                                                                                              1
               0.
                       0.
                                0.
                                        0.
                                               26.27
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                                                                        0.
                                                                                 0.
                                                                                              1
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               0.
                       0.
                                0.
                                        0.
                                                0.
                                                       19.76
                                                                0.
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                                                                                 0.
                                                                                         0.
                                                                        0.
               0.
                       0.
                                0.
                                        0.
                                                0.
                                                        0.
                                                               13.75
                                                                                 0.
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                       0.
                                0.
                                                0.
                                                                0.
                                                                        9.41
                                                                                         0.
               0.
                                        0.
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               0.
                       0.
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                                        0.
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                                                        0.
                                                                0.
                                                                        0.
                                                                                 7.88
                                                                                         0.
                                                                                              ]
            0.
                       0.
                                0.
                                        0.
                                                0.
                                                        0.
                                                                0.
                                                                        0.
                                                                                 0.
                                                                                         3.88]]
In [64]:
          originalTD = np.dot(u, np.dot(np.diag(s), vt))
           print originalTD
                                                 -0.
                    32.
                          12.
                                                                               0.
                                                                                     0.
                                                                                           0.
                                                                                                 0.]
           [[ 24.
                                 6.
                                      43.
                                             2.
                                                        3.
                                                              1.
                                                                    6.
                                                                          4.
                     5.
                           5.
                                                  1.
                                                       -0.
               9.
                                 2.
                                      20.
                                           -0.
                                                             -0.
                                                                    0.
                                                                        27.
                                                                              14.
                                                                                     3.
                                                                                           2.
                                                                                                11.]
                     3.
                          -0.
                                -0.
                                       3.
                                            7.
                                                 12.
                                                        4.
                                                             27.
                                                                    4.
                                                                         -0.
                                                                               1.
                                                                                    -0.
                                                                                                -0.]
              -0.
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                                                        2.
               3.
                    -0.
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                                      -0.
                                           16.
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                                                             25.
                                                                   23.
                                                                          7.
                                                                              12.
                                                                                    21.
                                                                                           3.
                                                                                                 2.]
               1.
                    -0.
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                                -0.
                                      -0.
                                           33.
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                                                       -0.
                                                              7.
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                                                                        14.
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                                      27.
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              12.
                     2.
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                                                        0.
                                                              0.
                                                                   22.
                                                                               4.
                                                                                    -0.
                                                                                           5.
                                                                                                 3.1
              -0.
                    -0.
                           0.
                                 0.
                                      -0.
                                           18.
                                                 32.
                                                       22.
                                                             34.
                                                                   17.
                                                                         -0.
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                                                                    9.
                                                                               7.
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                     0.
                                      2.
                                            0.
                                                 -0.
                                                        0.
                                                              3.
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                                                                                                 4.1
               1.
                          -0.
                                 0.
                                                                                           4.
              21.
                                 7.
                                           -0.
                                      31.
                                                  0.
                                                              0.
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                                                                               0.
                                                                                     0.
                    10.
                          16.
                                                        0.
                                                                                           1.
                                                                                                 0.]
               2.
                    -0.
                           0.
                                 2.
                                      -0.
                                           27.
                                                  4.
                                                        2.
                                                             11.
                                                                    8.
                                                                        33.
                                                                              16.
                                                                                    14.
                                                                                           7.
           3.]]
In [66]:
           numDimensions = 3
           u ld = u[:, :numDimensions]
           sigma = np.diag(s)[:numDimensions, :numDimensions]
           vt ld = vt[:numDimensions, :]
           lowRankTD = np.dot(u ld, np.dot(sigma, vt ld))
```

```
In [67]:
          np.set printoptions(precision=2, suppress=True, linewidth=120)
          print lowRankTD
          [[ 25.33
                     22.89
                             13.5
                                      6.13
                                            45.48
                                                    -1.98
                                                             1.99
                                                                     2.79
                                                                            1.9
                                                                                    7.87
                                                                                            4.6
          1.34
                -1.82
                         1.01
                                 2.14]
                      7.37
                              4.79
                                      2.6
           [ 10.71
                                            18.7
                                                     6.82
                                                            -5.26
                                                                    -3.14
                                                                           -3.04
                                                                                    6.47
                                                                                           21.6
          9.52
                  6.96
                         4.02
                                 4.41]
                      2.05
                              0.6
                                      0.29
                                                    10.24
                                                            12.93
                                                                     8.54
                                                                           19.25
                                                                                    9.57
              1.46
                                             2.07
                                                                                           -2.7
             -0.
                      2.18
                              0.08
                                     -0.94]
              1.25
                     -0.19
                             -0.45
                                      0.22
                                                    20.3
                                                            10.26
                                                                     6.46
                                                                           20.37
                                                                                   14.86
                                                                                           15.4
                                             1.03
                     10.26
              8.63
                              3.55
                                      2.17]
           Γ
              0.3
                     -1.69
                             -1.06
                                      0.02
                                            -0.57
                                                    18.19
                                                             4.81
                                                                     2.78
                                                                           13.17
                                                                                   12.03
                                                                                           19.7
             10.15
                     10.88
                              4.12
                                      3.051
          1
           [ 12.74
                                            22.51
                     10.59
                              6.33
                                      3.07
                                                             0.76
                                                                     1.09
                                                                            3.03
                                                                                    7.25
                                                                                           10.8
                                                     4.64
          1
              4.81
                      3.12
                              2.17
                                      2.49]
                                            -0.06
              0.58
                      1.9
                             -0.08
                                      0.01
                                                    20.55
                                                            25.06
                                                                    16.42
                                                                           37.57
                                                                                   18.2
                                                                                           -5.2
          3
              0.13
                      4.68
                              0.16
                                     -1.94]
                     -0.13
                                      0.54
              2.26
                              0.23
                                             3.39
                                                     9.93
                                                            -3.09
                                                                    -2.23
                                                                                    5.95
                                                                                           19.6
                                                                            0.62
                                      3.5]
              9.17
                      8.18
                              3.73
           [ 17.34
                     15.78
                              9.34
                                      4.21
                                                                           -0.65
                                                                                    4.05
                                            31.25
                                                    -3.21
                                                             0.35
                                                                     1.28
                                                                                            1.8
              0.19
                     -2.16
                              0.39
                                      1.3 ]
           Γ
              1.34
                     -2.11
                             -1.07
                                      0.26
                                             0.94
                                                    23.19
                                                             1.78
                                                                     0.66
                                                                           11.78
                                                                                   14.65
                                                                                           31.6
             15.6
                                      5.21]]
                     15.57
                              6.33
```

The VT matrix can be viewed as the new representation of documents in the lower dimensional space.

```
In [68]:
         print vt_ld
                              0.06
                                          0.39
                                                0.18
                                                      0.12
                                                            0.37
                                                                  0.35
         [[ 0.24 0.18 0.1
                                    0.41
                                                                        0.41
                                                                              0.21
                                                                                    0.
            0.09 0.07]
          [-0.34 -0.32 -0.2
                             -0.08 -0.63
                                                0.2
                                                      0.11
                                                            0.36
                                                                  0.13
                                                                        0.06
                                                                              0.07
                                          0.33
                                                                                    0.
            0.02 -0.021
            0.07 0.14 0.06 0.02 0.13 -0.06
                                                0.4
                                                      0.27
                                                            0.43 0.08 -0.62 -0.26 -0.
            -0.1
                  -0.12]]
```

In information retrieval, a query is compared to documents using vector-space similarity between the query vector and document vectors. In the lower dim. space, this can be achieved by first mapping the query to lower dim. space, and then comparing it to docs in the lower dim. space.

```
In [72]: queryVector = np.array([0,0,1,5,4,0,6,0,0,2])
    lowDimQuery = np.dot(la.inv(sigma), np.dot(u_ld.T, queryVector))
    print lowDimQuery

[ 0.07  0.07  0.05]

In [74]: # Compute Cosine sim between the query and docs in the Lower dimensional space
    qNorm = lowDimQuery / la.norm(lowDimQuery)
```

```
In [77]: docNorm = np.array([vt ld[:,i]/la.norm(vt ld[:,i]) for i in range(len(vt ld[0
         1))1)
         print docNorm
         [[ 0.57 -0.81 0.16]
          [ 0.47 -0.8
                        0.371
            0.45 -0.85 0.27]
          [ 0.55 -0.82 0.15]
            0.54 -0.83 0.17]
          [ 0.75 0.64 -0.12]
          [ 0.37 0.41 0.83]
          [ 0.38  0.33  0.86]
          [ 0.55 0.54 0.64]
            0.92 0.33 0.2 1
          [ 0.55 0.08 -0.83]
          [ 0.61 0.2 -0.77]
          [ 0.64 0.47 -0.61]
          [ 0.64 0.16 -0.75]
          [ 0.53 -0.13 -0.84]]
         sims = np.dot(qNorm, docNorm.T)
In [78]:
         # return indices of the docs in decending order of similarity to the query
         simInds = sims.argsort()[::-1]
         for i in simInds:
             print "Cosine similarity between Document %d and the query is: %.4f" %(i,s
         ims[i])
         Cosine similarity between Document 8 and the query is: 0.9693
         Cosine similarity between Document 9 and the query is: 0.8843
         Cosine similarity between Document 6 and the query is: 0.8604
         Cosine similarity between Document 5 and the query is: 0.8362
         Cosine similarity between Document 7 and the query is: 0.8309
         Cosine similarity between Document 12 and the query is: 0.4358
         Cosine similarity between Document 13 and the query is: 0.1840
         Cosine similarity between Document 11 and the query is: 0.1767
         Cosine similarity between Document 10 and the query is: 0.0404
         Cosine similarity between Document 1 and the query is: -0.0555
         Cosine similarity between Document 0 and the query is: -0.0810
         Cosine similarity between Document 3 and the query is: -0.1039
         Cosine similarity between Document 14 and the query is: -0.1097
         Cosine similarity between Document 4 and the query is: -0.1119
         Cosine similarity between Document 2 and the query is: -0.1375
In [79]:
         centroids svd, clusters svd = kMeans.kMeans(vt ld.T, 3, kMeans.distCosine, kMe
         ans.randCent)
         Iteration 1
         Iteration
         Iteration 3
```

```
In [80]: print clusters_svd
          [[ 0.
                   0.
           [ 0.
                   0.
           [ 0.
                   0.
                       ]
             0.
                   0.
            0.
                   0.
                   0.05]
             2.
           [ 2.
                   0.01]
           [ 2.
                   0.01]
            2.
                   0.
           [ 2.
                   0.01]
            1.
                   0.
           [ 1.
                   0.
           [ 1.
                   0.
           [ 1.
                   0.
                       ]]
           [ 1.
In [81]:
         print "\t\tCluster0\tCluster1\tCluster2"
          for i in range(numDimensions):
              print "Theme %d\t\t%.4f\t\t%.4f\t" %(i,centroids_svd[0][i],centroids
          _svd[1][i],centroids_svd[2][i])
                          Cluster0
                                           Cluster1
                                                            Cluster2
         Theme 0
                          0.1994
                                           0.1982
                                                            0.2813
         Theme 1
                          -0.3141
                                           0.0570
                                                            0.2243
         Theme 2
                                                            0.2239
                          0.0844
                                           -0.2611
In [ ]:
```