

```
In[1]:= (* 1: Adams-Bashforth 2 *)
```

```
In[2]:= p[r_, z_] := r^2 - (r + 3 z / 2 * r - z / 2);
```

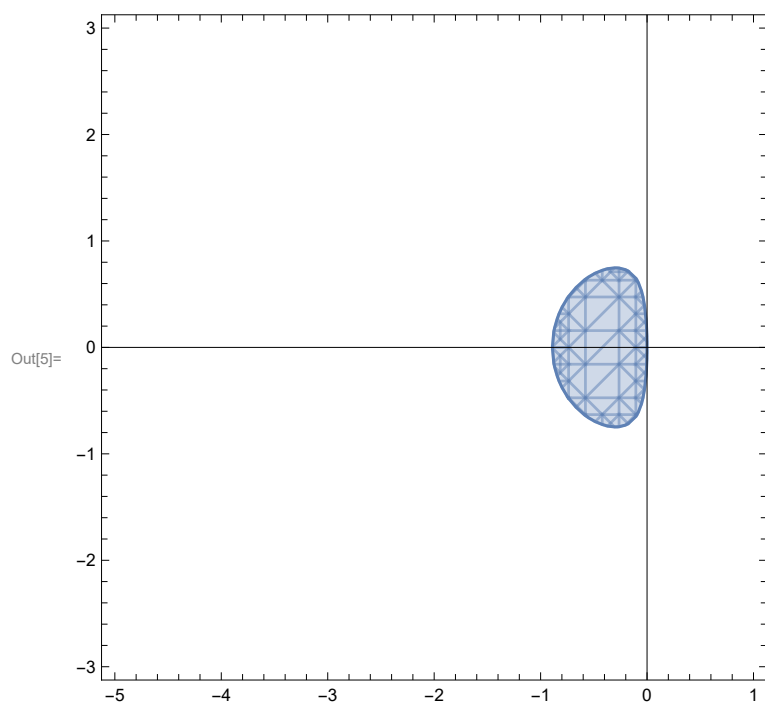
```
In[3]:= p[r, z]
```

$$\text{Out[3]} = -r + r^2 + \frac{z}{2} - \frac{3 r z}{2}$$

```
In[4]:= equns = Solve[p[r, z] == 0, r]
```

$$\text{Out[4]} = \left\{ \left\{ r \rightarrow \frac{1}{4} \left(2 + 3 z - \sqrt{4 + 4 z + 9 z^2} \right) \right\}, \left\{ r \rightarrow \frac{1}{4} \left(2 + 3 z + \sqrt{4 + 4 z + 9 z^2} \right) \right\} \right\}$$

```
In[5]:= RegionPlot[Norm[Evaluate[r /. equns /. z -> x + i y]] < 1, {x, -5, 1}, {y, -3, 3}, Axes -> True]
```



```
In[6]:= (* 2 Runge Kutta 4 *)
```

```
Clear[p, r, z];
```

```
k1[z_] := z;
```

```
k2[z_] := z (1 + k1[z] / 2);
```

```
k3[z_] := z (1 + k2[z] / 2);
```

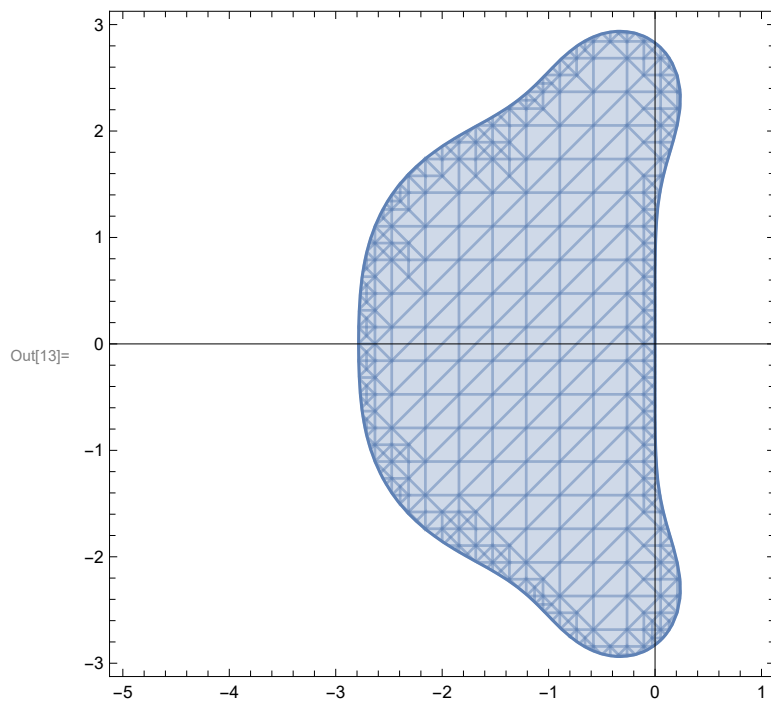
```
k4[z_] := z (1 + k3[z]);
```

```
In[11]:= p[r_, z_] := r - (1 + 1 / 6 * (k1[z] + 2 k2[z] + 2 k3[z] + k4[z]))
```

```
In[12]:= eq = Solve[p[r, z] == 0, r]
```

$$\text{Out[12]} = \left\{ \left\{ r \rightarrow \frac{1}{24} \left(24 + 24 z + 12 z^2 + 4 z^3 + z^4 \right) \right\} \right\}$$

In[13]:= **RegionPlot**[**Norm**[**r /. eq /. z** \rightarrow $x + \text{i} y$] < 1 , {**x**, -5, 1}, {**y**, -3, 3}, **Axes** \rightarrow **True**]



In[14]:= **(* 3 Backwards Euler *)**

In[15]:= **Clear**[**p**, **z**, **r**, **eq**];

In[16]:= **p**[**r_**, **z_**] := **r**² - (**r** + **z** * **r**²)

In[17]:= **eq** = **Solve**[**p**[**r**, **z**] == 0, **r**]

Out[17]= $\left\{ \left\{ r \rightarrow 0 \right\}, \left\{ r \rightarrow \frac{1}{1-z} \right\} \right\}$

In[18]:= **RegionPlot**[**Norm**[**r** /. **eq** /. **z** \rightarrow **x** + **i** **y**] < 1, {**x**, -5, 5}, {**y**, -5, 5}, **Axes** \rightarrow **True**]

