

ROYAL HOLLOWAY, UNIVERSITY OF LONDON

# Enigma: Prime Numbers and Cryptosystems

by

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*“Anyone can design a security system that he cannot break. So when someone announces, Heres my security system, and I cant break it, your first reaction should be, Who are you? If hes someone who has broken dozens of similar systems, his system is worth looking at. If hes never broken anything, the chance is zero that it will be any good.”*

Bruce Schneier, *The Ethics of Vulnerability Research*

## *Abstract*

Modern cryptography allows us to perform many types of information exchange over insecure channels. One of these tasks is to agree on a secret key over a channel where messages can be overheard. This is achieved by Diffie-Hellman protocol. Other tasks include public key and digital signature schemes; RSA key exchange can be used for them. These protocols are of great importance for bank networks.

Most such algorithms are based upon number theory, namely, the intractability of certain problems involving prime numbers. The project involves implementing basic routines for dealing with prime numbers and then building cryptographic applications using them.

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# Abbreviations

**AES**   **A**dvanced **E**ncryption **S**tandard

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# Attacks and Flaws

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## Appendix A

# Enigma Application Specification

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## Appendix B

# Enigma Protocol Specification

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