



# BenchmarkDotNet

## State of the art

Andrey Akinshin, Adam Sitnik



```
~/Work/BenchmarkDotNet master
> git show 6eda98ab | head -5
commit 6eda98ab1e83a0d185d09ff8b24c795711af8db1
Author: Andrey Akinshin <andrey.akinshin@gmail.com>
Date:   Sun Aug 18 13:20:56 2013 +0700
```

Initial commit

Version	Downloads	Last updated			
0.13.5	558,749	3 months ago			
0.13.4	361,393	4 months ago	0.9.8	119,312	06/07/2016
0.13.3	144,756	5 months ago	0.9.7	10,601	29/05/2016
0.13.2	1,342,245	9 months ago	0.9.7-beta	2,879	29/05/2016
0.13.1	4,552,884	11/08/2021	0.9.6	5,787	11/05/2016
0.13.0	765,889	19/05/2021	0.9.6-beta	1,652	11/05/2016
0.12.1	4,117,117	06/04/2020	0.9.5	3,206	02/05/2016
0.12.0	1,448,552	24/10/2019	0.9.5-beta	1,737	02/05/2016
0.11.5	1,770,183	02/04/2019	0.9.4	5,331	24/03/2016
0.11.4	367,495	15/02/2019	0.9.4-beta	1,599	24/03/2016
0.11.3	591,864	20/11/2018	0.9.3	3,052	13/03/2016
0.11.2	48,142	01/11/2018	0.9.3-beta	1,509	13/03/2016
0.11.1	292,134	22/08/2018	0.9.2	7,552	05/03/2016
0.11.0	212,211	23/07/2018	0.9.1	8,924	10/02/2016
0.10.14	336,850	09/04/2018	0.9.0	2,911	09/02/2016
0.10.13	624,061	02/03/2018	0.8.2	1,789	19/01/2016
0.10.12	152,128	14/01/2018	0.8.1	1,755	08/01/2016
0.10.11	65,790	01/12/2017	0.8.0	1,907	17/12/2015
0.10.10	121,065	03/11/2017	0.7.8	2,950	01/10/2015
0.10.9	117,363	28/07/2017	0.7.7	27,945	30/07/2015
0.10.8	58,163	09/06/2017	0.7.6	2,389	02/07/2015
0.10.7	4,354	05/06/2017	0.7.5	1,677	09/06/2015
0.10.6	21,643	12/05/2017	0.7.4	1,812	09/05/2015
0.10.5	33,593	26/04/2017	0.7.3	1,609	08/05/2015
0.10.4	3,500	21/04/2017	0.7.2	1,583	07/05/2015
0.10.3	118,033	01/03/2017	0.7.1	1,649	06/05/2015
0.10.2	154,226	21/01/2017	0.7.0	1,600	06/05/2015
0.10.1	19,623	04/12/2016	0.6.0	1,616	04/05/2015
0.10.0	52,033	10/11/2016	0.5.2	2,480	21/03/2014
0.9.9	33,543	17/08/2016	0.5.1	1,840	01/10/2013
			0.5.0	7,766	23/09/2013

# The Contributors

 AndreyAkinshin 811 commits 90,630 ++ 64,602 --	 adamsitnik 797 commits 154,045 ++ 129,733 --	 mattwarren 108 commits 23,929 ++ 6,454 --	 WojciechNagorski 45 commits 5,067 ++ 2,759 --	 ig-sinicyn 34 commits 13,542 ++ 2,930 --
 alinasimrnova 30 commits 4,848 ++ 2,986 --	 YegorStepanov 24 commits 1,366 ++ 630 --	 Ky7m 24 commits 1,122 ++ 609 --	 naricc 22 commits 1,844 ++ 819 --	 mawosoft 12 commits 325 ++ 43 --
 Rizzen 12 commits 1,663 ++ 296 --	 radekdoulik 10 commits 689 ++ 586 --	 epeshk 10 commits 187 ++ 81 --	 radical 9 commits 157 ++ 157 --	 morgan-kn 9 commits 2,244 ++ 369 --
 kant2002 8 commits 204 ++ 181 --	 lukasz-pryzyk 8 commits 607 ++ 93 --	 redknightlois 8 commits 638 ++ 37 --	 martincostello 7 commits 637 ++ 41 --	 Teknikaali 7 commits 1,861 ++ 141 --
 YohDeadfall 6 commits 76 ++ 26 --	 dlemstra 6 commits 629 ++ 59 --	 lahma 6 commits 209 ++ 63 --	 gigi81 6 commits 272 ++ 43 --	 marcnet80 5 commits 225 ++ 100 --
 MichalStrehovsky 5 commits 84 ++ 55 --	 teboco 5 commits 36 ++ 25 --	 FransBouma 5 commits 15,786 ++ 14,580 --	 JohannesDemi 4 commits 257 ++ 52 --	 jonathananpeppers 4 commits 1,055 ++ 27 --
 svick 4 commits 83 ++ 72 --	 gsomix 4 commits 732 ++ 32 --	 mfilippov 4 commits 46 ++ 257 --	 AmadeusW 4 commits 436 ++ 63 --	 roji 4 commits 1,185 ++ 98 --
 ppanyukov 4 commits 228 ++ 63 --	 timcassell 3 commits 3,826 ++ 4,791 --	 leonvandermeer 3 commits 277 ++ 20 --	 mrsharm 3 commits 38 ++ 1 --	 am11 3 commits 58 ++ 12 --
 stanciadrian 3 commits 32 ++ 6 --	 Symbai 3 commits 34 ++ 27 --	 damageboy 3 commits 44 ++ 21 --	 CodeTherapist 3 commits 1,080 ++ 14 --	 MarekM25 3 commits 461 ++ 24 --
 Maximusya 3 commits 26 ++ 25 --	 SteveDesmond-ca 3 commits 71 ++ 10 --	 mtschnieders 3 commits 9 ++ 9 --	 KeterSCP 2 commits 70 ++ 2 --	 teo-tsirpanis 2 commits 212 ++ 253 --
 Serg046 2 commits 485 ++ 38 --	 fanyang-mono 2 commits 3 ++ 13 --	 MichalPetryka 2 commits 2 ++ 1 --	 jkotas 2 commits 144 ++ 117 --	 AndyAyersMS 2 commits 72 ++ 14 --
 workgroupengineering 2 commits 164 ++ 33 --	 pavelsavara 2 commits 16 ++ 18 --	 akoeplinger 2 commits 5 ++ 5 --	 kevinsalimi 2 commits 47 ++ 30 --	 ExceptionCaught 2 commits 189 ++ 69 --
 suslovk 2 commits 14 ++ 8 --	 sleemer 2 commits 111 ++ 66 --	 circularnet 2 commits 3 ++ 3 --	 glennawatson 2 commits 20 ++ 19 --	 frediel 2 commits 4 ++ 4 --
 bgrainger 2 commits 100 ++ 2 --	 facundofarias 2 commits 3 ++ 3 --	 Tornhoof 2 commits 2 ++ 2 --	 Itrzesinski 2 commits 785 ++ 255 --	 dmitry-ra 2 commits 71 ++ 71 --
 shoelzer 2 commits 48 ++ 70 --	 ENiKS 2 commits 21 ++ 11 --	 Chrisgozd 2 commits 186 ++ 3 --	 GeorgePlotnikov 2 commits 356 ++ 2 --	 ipjohnson 2 commits 666 ++ 40 --
 cdmihai 2 commits 20 ++ 10 --	 alexandromikitin 2 commits 154 ++ 2 --	 krk 2 commits 38 ++ 1 --	 onionhammer 1 commit 2 ++ 2 --	 erhardt 1 commit 4 ++ 1 --
 rolshevsky 1 commit 27 ++ 28 --	 jawn 1 commit 4 ++ 4 --	 pent 1 commit 1 ++ 1 --	 aidmsu 1 commit 1 ++ 1 --	 smit Patel 1 commit 3 ++ 2 --
 aarondandy 1 commit 6 ++ 6 --	 davkean 1 commit 2 ++ 2 --	 RichLinnell 1 commit 7 ++ 3 --	 mmayr-at 1 commit 2 ++ 2 --	 factormystic 1 commit 1 ++ 1 --
 arthrp 1 commit 2 ++ 2 --	 Denislstomin 1 commit 202 ++ 29 --	 russcam 1 commit 71 ++ 1 --	 JohanLarsson 1 commit 3 ++ 2 --	 goldshtn 1 commit 73 ++ 5,416 --
 cloudRoutine 1 commit 5 ++ 11 --	 ForNeVeR 1 commit 1 ++ 1 --	 vkkoshelev 1 commit 1 ++ 1 --	 NN--- 1 commit 2 ++ 2 --	 mijay 1 commit 173 ++ 0 --



# BenchmarkDotNet

## Powerful .NET library for benchmarking

stars 8964

used by 15745

downloads 18624834

# Introduction



# Sample

```
public class ParsingBenchmarks
{
    [Benchmark]
    public int ParseInt() => int.Parse("123456789");
}

void Main(string[] args)
=> BenchmarkRunner.Run<ParsingBenchmarks>();
```

# Demo

```
PS D:\projects\BdnDemo> dotnet run -c Release -f net7.0 --filter *ParsingBenchmarks*
```



# How does it work?



# BenchmarkSwitcher

```
void Main(string[] args)
=> BenchmarkSwitcher
    .FromAssembly(typeof(Program).Assembly)
    .Run(args, config: null);
```

```
PS D:\projects\BenchmarkDotNet\samples\BenchmarkDotNet.Samples> dotnet run -c Release -f net7.0
Available Benchmarks:
#0 Algo_Md5VsSha256
#1 IntroArguments
#2 IntroArgumentsPriority
#3 IntroArgumentsSource
#4 IntroArrayParam
#5 IntroBasic
You should select the target benchmark(s). Please, print a number of a benchmark (e.g. '0') or a contained benchmark
caption (e.g. 'Algo_Md5VsSha256').
If you want to select few, please separate them with space ' ' (e.g. '1 2 3').
You can also provide the class name in console arguments by using --filter. (e.g. '--filter *Algo_Md5VsSha256*').
Enter the asterisk '*' to select all.
```

# Configuration

- [Attributes]
- Fluent API
- Command line arguments
- Every filtered benchmark is executed for every Job defined in the Config.

```
var config = DefaultConfig.Instance  
    .AddJob(Job.Default.WithAbc())  
    .AddJob(Job.Default.WithXyz());
```

# Jitting

```
OverheadJitting 1: 1 op, 264100.00 ns, 264.1000 us/op
WorkloadJitting 1: 1 op, 221800.00 ns, 221.8000 us/op
```

```
OverheadJitting 2: 16 op, 369400.00 ns, 23.0875 us/op
WorkloadJitting 2: 16 op, 336500.00 ns, 21.0312 us/op
```

# Pilot stage – perfect invocation count

```
WorkloadPilot 1: 16 op, 1500.00 ns, 93.7500 ns/op
WorkloadPilot 2: 32 op, 2000.00 ns, 62.5000 ns/op
WorkloadPilot 3: 64 op, 3800.00 ns, 59.3750 ns/op
WorkloadPilot 4: 128 op, 4700.00 ns, 36.7188 ns/op
WorkloadPilot 5: 256 op, 11600.00 ns, 45.3125 ns/op
WorkloadPilot 6: 512 op, 17000.00 ns, 33.2031 ns/op
WorkloadPilot 7: 1024 op, 30400.00 ns, 29.6875 ns/op
WorkloadPilot 8: 2048 op, 59100.00 ns, 28.8574 ns/op
WorkloadPilot 9: 4096 op, 115400.00 ns, 28.1738 ns/op
WorkloadPilot 10: 8192 op, 230600.00 ns, 28.1494 ns/op
WorkloadPilot 11: 16384 op, 461500.00 ns, 28.1677 ns/op
WorkloadPilot 12: 32768 op, 980300.00 ns, 29.9164 ns/op
WorkloadPilot 13: 65536 op, 1839400.00 ns, 28.0670 ns/op
WorkloadPilot 14: 131072 op, 3709500.00 ns, 28.3012 ns/op
WorkloadPilot 15: 262144 op, 7258600.00 ns, 27.6894 ns/op
WorkloadPilot 16: 524288 op, 14538400.00 ns, 27.7298 ns/op
WorkloadPilot 17: 1048576 op, 28773500.00 ns, 27.4405 ns/op
WorkloadPilot 18: 2097152 op, 62435200.00 ns, 29.7714 ns/op
WorkloadPilot 19: 4194304 op, 93930900.00 ns, 22.3949 ns/op
WorkloadPilot 20: 8388608 op, 136373100.00 ns, 16.2569 ns/op
WorkloadPilot 21: 16777216 op, 267919300.00 ns, 15.9692 ns/op
WorkloadPilot 22: 33554432 op, 530501600.00 ns, 15.8102 ns/op
```

Heuristic

`job.WithInvocationCount(count) or --invocationCount`

# Result = (Result + Overhead) - Overhead

OverheadActual	1:	33554432 op,	51447100.00 ns,	1.5332 ns/op
OverheadActual	2:	33554432 op,	50752900.00 ns,	1.5126 ns/op
OverheadActual	3:	33554432 op,	50577000.00 ns,	1.5073 ns/op
OverheadActual	4:	33554432 op,	51037700.00 ns,	1.5210 ns/op
OverheadActual	5:	33554432 op,	51601500.00 ns,	1.5378 ns/op
OverheadActual	6:	33554432 op,	52445000.00 ns,	1.5630 ns/op
OverheadActual	7:	33554432 op,	51899400.00 ns,	1.5467 ns/op
OverheadActual	8:	33554432 op,	51600300.00 ns,	1.5378 ns/op
OverheadActual	9:	33554432 op,	51092800.00 ns,	1.5227 ns/op
OverheadActual	10:	33554432 op,	51463500.00 ns,	1.5337 ns/op
OverheadActual	11:	33554432 op,	50651700.00 ns,	1.5095 ns/op
OverheadActual	12:	33554432 op,	52135700.00 ns,	1.5538 ns/op
OverheadActual	13:	33554432 op,	51307100.00 ns,	1.5291 ns/op
OverheadActual	14:	33554432 op,	50521000.00 ns,	1.5056 ns/op
OverheadActual	15:	33554432 op,	52331800.00 ns,	1.5596 ns/op

# The Overhead

```
[Benchmark](Description = "Interlocked.Increment(ref int)")  
[Arguments(10)]  
public int Increment(ref int arg) => Interlocked.Increment(ref arg);  
  
[Benchmark]  
[Arguments(10)]  
public int Overhead(ref int arg) => 0;  
  
DefaultConfig.Instance  
.AddJob(Job.Default.WithId("NO Overhead"))  
.AddJob(Job.Default.WithEvaluateOverhead(false).WithId("With Overhead"))
```

# The difference

Method	Job	EvaluateOverhead	arg	Mean	Error	StdDev
'Interlocked.Increment(ref int)'	NO Overhead	Default	10	2.876 ns	0.0269 ns	0.0251 ns
'Interlocked.Increment(ref int)'	With Overhead	False	10	4.341 ns	0.0230 ns	0.0215 ns

# Warmup stage

```
WorkloadWarmup    1: 33554432 op, 537440800.00 ns, 16.0170 ns/op
WorkloadWarmup    2: 33554432 op, 535354700.00 ns, 15.9548 ns/op
WorkloadWarmup    3: 33554432 op, 521823300.00 ns, 15.5515 ns/op
WorkloadWarmup    4: 33554432 op, 530491200.00 ns, 15.8099 ns/op
WorkloadWarmup    5: 33554432 op, 525622600.00 ns, 15.6648 ns/op
WorkloadWarmup    6: 33554432 op, 526581400.00 ns, 15.6933 ns/op
WorkloadWarmup    7: 33554432 op, 521130400.00 ns, 15.5309 ns/op
```

`job.WithWarmupCount(count)`

or

- `--warmupCount`
- `--minWarmupCount`
- `--maxWarmupCount`

# Actual Workload

```
WorkloadActual 1: 33554432 op, 527246200.00 ns, 15.7132 ns/op
WorkloadActual 2: 33554432 op, 527950500.00 ns, 15.7342 ns/op
WorkloadActual 3: 33554432 op, 532592300.00 ns, 15.8725 ns/op
WorkloadActual 4: 33554432 op, 541320100.00 ns, 16.1326 ns/op
WorkloadActual 5: 33554432 op, 537627700.00 ns, 16.0226 ns/op
WorkloadActual 6: 33554432 op, 533328400.00 ns, 15.8944 ns/op
WorkloadActual 7: 33554432 op, 533828300.00 ns, 15.9093 ns/op
WorkloadActual 8: 33554432 op, 530525400.00 ns, 15.8109 ns/op
WorkloadActual 9: 33554432 op, 531167800.00 ns, 15.8300 ns/op
WorkloadActual 10: 33554432 op, 531245100.00 ns, 15.8323 ns/op
WorkloadActual 11: 33554432 op, 530232900.00 ns, 15.8022 ns/op
WorkloadActual 12: 33554432 op, 530643500.00 ns, 15.8144 ns/op
WorkloadActual 13: 33554432 op, 530398200.00 ns, 15.8071 ns/op
WorkloadActual 14: 33554432 op, 533226500.00 ns, 15.8914 ns/op
WorkloadActual 15: 33554432 op, 529635800.00 ns, 15.7844 ns/op
```

`job.WithIterationCount(count)`

# Results

```
WorkloadResult 1: 33554432 op, 475799100.00 ns, 14.1799 ns/op
WorkloadResult 2: 33554432 op, 476503400.00 ns, 14.2009 ns/op
WorkloadResult 3: 33554432 op, 481145200.00 ns, 14.3392 ns/op
WorkloadResult 4: 33554432 op, 486180600.00 ns, 14.4893 ns/op
WorkloadResult 5: 33554432 op, 481881300.00 ns, 14.3612 ns/op
WorkloadResult 6: 33554432 op, 482381200.00 ns, 14.3761 ns/op
WorkloadResult 7: 33554432 op, 479078300.00 ns, 14.2776 ns/op
WorkloadResult 8: 33554432 op, 479720700.00 ns, 14.2968 ns/op
WorkloadResult 9: 33554432 op, 479798000.00 ns, 14.2991 ns/op
WorkloadResult 10: 33554432 op, 478785800.00 ns, 14.2689 ns/op
WorkloadResult 11: 33554432 op, 479196400.00 ns, 14.2812 ns/op
WorkloadResult 12: 33554432 op, 478951100.00 ns, 14.2739 ns/op
WorkloadResult 13: 33554432 op, 481779400.00 ns, 14.3581 ns/op
WorkloadResult 14: 33554432 op, 478188700.00 ns, 14.2511 ns/op
```

```
WorkloadActual 1: 33554432 op, 527246200.00 ns, 15.7132 ns/op
WorkloadActual 2: 33554432 op, 527950500.00 ns, 15.7342 ns/op
WorkloadActual 3: 33554432 op, 532592300.00 ns, 15.8725 ns/op
WorkloadActual 4: 33554432 op, 541320100.00 ns, 16.1326 ns/op
WorkloadActual 5: 33554432 op, 537627700.00 ns, 16.0226 ns/op
WorkloadActual 6: 33554432 op, 533328400.00 ns, 15.8944 ns/op
WorkloadActual 7: 33554432 op, 533828300.00 ns, 15.9093 ns/op
WorkloadActual 8: 33554432 op, 530525400.00 ns, 15.8109 ns/op
WorkloadActual 9: 33554432 op, 531167800.00 ns, 15.8300 ns/op
WorkloadActual 10: 33554432 op, 531245100.00 ns, 15.8323 ns/op
WorkloadActual 11: 33554432 op, 530232900.00 ns, 15.8022 ns/op
WorkloadActual 12: 33554432 op, 530643500.00 ns, 15.8144 ns/op
WorkloadActual 13: 33554432 op, 530398200.00 ns, 15.8071 ns/op
WorkloadActual 14: 33554432 op, 533226500.00 ns, 15.8914 ns/op
WorkloadActual 15: 33554432 op, 529635800.00 ns, 15.7844 ns/op

// AfterActualRun
WorkloadResult 1: 33554432 op, 475799100.00 ns, 14.1799 ns/op
WorkloadResult 2: 33554432 op, 476503400.00 ns, 14.2009 ns/op
WorkloadResult 3: 33554432 op, 481145200.00 ns, 14.3392 ns/op
WorkloadResult 4: 33554432 op, 486180600.00 ns, 14.4893 ns/op
WorkloadResult 5: 33554432 op, 481881300.00 ns, 14.3612 ns/op
WorkloadResult 6: 33554432 op, 482381200.00 ns, 14.3761 ns/op
WorkloadResult 7: 33554432 op, 479078300.00 ns, 14.2776 ns/op
WorkloadResult 8: 33554432 op, 479720700.00 ns, 14.2968 ns/op
WorkloadResult 9: 33554432 op, 479798000.00 ns, 14.2991 ns/op
WorkloadResult 10: 33554432 op, 478785800.00 ns, 14.2689 ns/op
WorkloadResult 11: 33554432 op, 479196400.00 ns, 14.2812 ns/op
WorkloadResult 12: 33554432 op, 478951100.00 ns, 14.2739 ns/op
WorkloadResult 13: 33554432 op, 481779400.00 ns, 14.3581 ns/op
WorkloadResult 14: 33554432 op, 478188700.00 ns, 14.2511 ns/op
```

`job.WithOutlierMode(mode)`  
or `--outliers`

IsOutlier

# The trap

```
public class ListBenchmarks
{
    private List<int> list = new List<int>();

    [Benchmark]
    public void Add() => list.Add(1234);

    [Benchmark]
    public void AddLoop()
    {
        list.Clear();

        for (int i = 0; i < 1000; i++)
            list.Add(1234);
    }
}
```

# OOM

```
WorkloadActual 50: 33554432 op, 323008800.00 ns, 9.6264 ns/op
WorkloadActual 51: 33554432 op, 374477100.00 ns, 11.1603 ns/op
WorkloadActual 52: 33554432 op, 377470000.00 ns, 11.2495 ns/op
WorkloadActual 53: 33554432 op, 367711400.00 ns, 10.9587 ns/op
WorkloadActual 54: 33554432 op, 311676900.00 ns, 9.2887 ns/op
```

OutOfMemoryException!

BenchmarkDotNet continues to run additional iterations until desired accuracy level is achieved. It's possible only if the benchmark method doesn't have any side-effects.

If your benchmark allocates memory and keeps it alive, you are creating a memory leak.

You should redesign your benchmark and remove the side-effects. You can use 'OperationsPerInvoke', 'IterationSetup' and 'IterationCleanup' to do that.

System.Reflection.TargetInvocationException: Exception has been thrown by the target of an invocation.

```
---> System.OutOfMemoryException: Array dimensions exceeded supported range.
   at System.Collections.Generic.List`1.set_Capacity(Int32 value)
   at System.Collections.Generic.List`1.AddWithResize(T item)
```

# Strategies

- Throughput – default, perfect for microbenchmarks with a steady state
- Monitoring
  - no Pilot stage
  - no Overhead evaluation
  - Outliers remain untouched
  - 1 iteration = 1 benchmark invocation
- ColdStart – no warmup, no pilot stage

# How it works: Summary

- Using statistics to get stable results
- Users don't need to worry about specifying invocation count
- Results don't contain overhead
- **It takes time to do all of that**
- User can specify invocation/iteration/warmup/target count
- User can customize the heuristic
- Benchmarks should not have side-effects

# Architecture



# Architecture

- Host Process (console app)
  - Generates a project file with C# source file (Console App)
  - Builds (Roslyn/dotnet cli)
  - Executes Child Process
- Child Process (console app)
  - **Executes benchmark**
  - Signals events to Host
  - Reports results to Host

# Why Process-level Isolation?

- We want to have stable and repeatable results
- Order of executing benchmarks should not affect the results
  - Benchmarks can have side effects
  - GC is self-tuning (generation size can change over time)
  - JIT is also self-tuning (Tiered JIT + PGO)
  - .NET Runtime can apply some optimizations
- [[InProcessToolchain](#)] does **not** spawn new process

# How to prevent inlining?

```
[Benchmark(Baseline = true)]  
public void OneWay() { /* one way to solve the problem */ }  
[Benchmark]  
public void AnotherWay() { /* another way to solve the problem */ }
```

What if one of the methods get inlined?

How to prevent inlining without modifying the code?

```
public delegate Span<byte> TargetDelegate();  
  
private TargetDelegate targetDelegate = BenchmarkedMethod;
```

# How to minimize loop overhead?

```
private void MainMultiAction(long invokeCount)
{
    for (long i = 0; i < invokeCount; i++)
        targetDelegate();
}

private void MainMultiAction(long invokeCount)
{
    for (long i = 0; i < invokeCount / unrollFactor; i++)
    {
        targetDelegate(); targetDelegate(); targetDelegate(); targetDelegate();
        targetDelegate(); targetDelegate(); targetDelegate(); targetDelegate();
        targetDelegate(); targetDelegate(); targetDelegate(); targetDelegate();
        targetDelegate(); targetDelegate(); targetDelegate(); targetDelegate();
    }
}
job.WithUnrollFactor(count) or --unrollFactor
```

More info

# How to prevent from Out-of-order execution?

```
private void MainMultiAction(long invokeCount)
{
    for (long i = 0; i < invokeCount / unrollFactor; i++)
    {
        consumer.Consume(targetDelegate()); consumer.Consume(targetDelegate());
        consumer.Consume(targetDelegate()); consumer.Consume(targetDelegate());
    }
}
```

# Consumer

```
public class Consumer
{
    private volatile byte byteHolder;
    // (more types skipped for brevity)
    private string stringHolder;
    private object objectHolder;

    [MethodImpl(MethodImplOptions.AggressiveInlining)]
    public void Consume(ulong ulongValue)
        => Volatile.Write(ref ulongHolder, ulongValue);
}
```

# Generating new project

- Benchmark.notcs (customized for every benchmark)
- Benchmark.csproj
  - Architecture (Job.Env.Platform)
  - Optimizations: ALWAYS on
- Benchmark.config - derives from Host.config file, except of:
  - GC Mode (Job.Env.Gc)
  - JIT: Legacy/RyuJIT/LLVm (Job.Env.Jit, \*LLVM only for Mono)
    - & more: GCCpuGroup, gcAllowVeryLargeObjects
- Use [KeepBenchmarkFiles] to see what is generated

# Different GC modes

```
[Config(typeof(GcConfig))]
public class GcBenchmarks
{
    private class GcConfig : ManualConfig
    {
        public GcConfig()
        {
            AddJob(Job.Default.WithGcMode(new GcMode { Server = true, Concurrent = true }).WithId("Background Server"));
            AddJob(Job.Default.WithGcMode(new GcMode { Server = true, Concurrent = false }).WithId("Server"));
            AddJob(Job.Default.WithGcMode(new GcMode { Server = false, Concurrent = true }).WithId("Background
Workstation"));
            AddJob(Job.Default.WithGcMode(new GcMode { Server = false, Concurrent = false }).WithId("Workstation"));

            AddDiagnoser(MemoryDiagnoser.Default);
        }
    }

    [Benchmark(Description = "new byte[10kB]")]
    public byte[] Allocate() => new byte[10000];
}
```

# Different GC modes: sample results

Method	Job	Concurrent	Server	Mean	Error	StdDev	Gen0	Allocated
'new byte[10kB]'	Background Server	True	True	798.5 ns	14.09 ns	13.18 ns	0.0486	9.79 KB
'new byte[10kB]'	Background Workstation	True	False	213.8 ns	4.31 ns	4.03 ns	1.1976	9.79 KB
'new byte[10kB]'	Server	False	True	776.7 ns	2.47 ns	2.31 ns	0.0486	9.79 KB
'new byte[10kB]'	Workstation	False	False	213.8 ns	4.14 ns	3.23 ns	1.1976	9.79 KB

# Compare frameworks

```
public class Algo_Md5VsSha256
{
    private readonly byte[] data;
    private readonly MD5 md5 = MD5.Create();
    private readonly SHA256 sha256 = SHA256.Create();

    public Algo_Md5VsSha256()
    {
        data = new byte[10000];
        new Random(42).NextBytes(data);
    }

    [Benchmark]
    public byte[] Md5() => md5.ComputeHash(data);

    [Benchmark]
    public byte[] Sha256() => sha256.ComputeHash(data);
}
```

```
dotnet run -c Release -f net48 --filter *Algo* --runtimes net48 mono net7.0 nativeaot7.0
```

BenchmarkDotNet=v0.13.5, OS=Windows 11 (10.0.22621.1702/22H2/2022Update/SunValley2)  
AMD Ryzen Threadripper PRO 3945WX 12-Cores, 1 CPU, 24 logical and 12 physical cores  
[Host] : .NET Framework 4.8.1 (4.8.9139.0), X64 RyuJIT VectorSize=256  
Job-BQVMTG : .NET 7.0.5 (7.0.523.17405), X64 RyuJIT AVX2  
Job-XTPWQX : .NET Framework 4.8.1 (4.8.9139.0), X64 RyuJIT VectorSize=256  
Job-XIDDXQ : Mono 6.12.0 (Visual Studio), X64 VectorSize=128  
Job-WJMMJF : .NET 7.0.5-servicing.23174.5, X64 NativeAOT SSE4.2

Method	Runtime	Mean	Error	StdDev	Ratio
Md5	.NET 7.0	16.016 us	0.1510 us	0.1412 us	0.94
Md5	.NET Framework 4.8	17.083 us	0.0995 us	0.0931 us	1.00
Md5	Mono	26.781 us	0.2750 us	0.2297 us	1.57
Md5	NativeAOT 7.0	15.995 us	0.1232 us	0.1092 us	0.94
Sha256	.NET 7.0	4.915 us	0.0364 us	0.0304 us	0.03
Sha256	.NET Framework 4.8	146.356 us	1.0191 us	0.9533 us	1.00
Sha256	Mono	96.385 us	0.2082 us	0.1947 us	0.66
Sha256	NativeAOT 7.0	4.855 us	0.0364 us	0.0322 us	0.03

# Architecture: Summary

- Host process generates, builds and runs .exe per benchmark
- It helps us to get repeatable results
- It allows the users to compare different settings:
  - GC Workstation vs GC Server
  - .NET Framework vs Mono vs .NET vs NativeAOT
- It limits us to only known frameworks
- InProcessToolchain runs in process (-i)

# Features



# Exporters

- HTML
- Markdown: GitHub, StackOverflow
- CSV
- RPlot (requires R)
- XML
- JSON

```
[AsciiDocExporter]
[CsvExporter]
[CsvMeasurementsExporter]
[HtmlExporter]
[PlainExporter]
[RPlotExporter]
[JsonExporterAttribute.Brief]
[JsonExporterAttribute.BriefCompressed]
[JsonExporterAttribute.Full]
[JsonExporterAttribute.FullCompressed]
[MarkdownExporterAttribute.Default]
[MarkdownExporterAttribute.GitHub]
[MarkdownExporterAttribute.StackOverflow]
[MarkdownExporterAttribute.Atlassian]
[XmlExporterAttribute.Brief]
[XmlExporterAttribute.BriefCompressed]
[XmlExporterAttribute.Full]
[XmlExporterAttribute.FullCompressed]
public class IntroExporters
```

# .\BenchmarkDotNet.Artifacts\results

The screenshot shows a file explorer window and a code editor window. The file explorer is displaying a folder structure under 'BenchmarkDotNet.Artifacts > results'. The code editor window is showing assembly code for 'IntroDisasm.cs'.

File Explorer Content:

Name	Date modified	Type	Size
BdnDemo.AccurateAllocations-report.csv	11/4/2018 2:29 AM	Microsoft Excel Com...	1 KB
BdnDemo.AccurateAllocations-report.html	11/4/2018 2:29 AM	HTML File	2 KB
BdnDemo.AccurateAllocations-report-github.md	11/4/2018 2:29 AM	MD File	1 KB
BdnDemo.IntroMultimodal-report.csv	10/26/2018 2:29 AM	Microsoft Excel Com...	1 KB
BdnDemo.IntroMultimodal-report.html	10/26/2018 2:29 AM	HTML File	2 KB
BdnDemo.IntroMultimodal-report-github.md	10/26/2018 2:29 AM	MD File	1 KB
BdnDemo.ListBenchmarks-report.csv	10/26/2018 2:29 AM	Microsoft Excel Com...	1 KB
BdnDemo.ListBenchmarks-report.html	10/26/2018 2:29 AM	HTML File	2 KB
BdnDemo.ListBenchmarks-report-github.md	10/26/2018 2:29 AM	MD File	1 KB
BdnDemo.Md5VsSha256_Md5_DefaultJob-asm....	10/24/2018 2:29 AM	Text File	1 KB
BdnDemo.Md5VsSha256_Md5_DefaultJob-asm....	10/24/2018 2:29 AM	Text File	1 KB
BdnDemo.Md5VsSha256_Md5_DefaultJob-asm....	10/24/2018 2:29 AM	Text File	1 KB
BdnDemo.Md5VsSha256-disassembly-report.htm...	10/24/2018 2:29 AM	HTML File	2 KB
BdnDemo.Md5VsSha256-report.csv	10/27/2018 2:29 AM	Microsoft Excel Com...	1 KB
BdnDemo.Md5VsSha256-report.html	10/27/2018 2:29 AM	HTML File	2 KB
BdnDemo.Md5VsSha256-report-github.md	10/27/2018 2:29 AM	MD File	1 KB
BdnDemo.OperationsPerInvokeSample_Increm...	10/26/2018 2:29 AM	Text File	1 KB
BdnDemo.OperationsPerInvokeSample_Increm...	10/26/2018 2:29 AM	Text File	1 KB
BdnDemo.OperationsPerInvokeSample_Increm...	10/26/2018 2:29 AM	Text File	1 KB
BdnDemo.OperationsPerInvokeSample_Increm...	10/26/2018 2:29 AM	Text File	1 KB
BdnDemo.OperationsPerInvokeSample_Increm...	10/26/2018 2:29 AM	Text File	1 KB

Code Editor Content (IntroDisasm.cs):

```
1 `` ini
2
3 BenchmarkDotNet=v0.11.1.817-nightly, OS=Windows 10.0.17134.376 (1803/April2018Update/
4 Intel Core i7-5557U CPU 3.10GHz (Broadwell), 1 CPU, 4 logical and 2 physical cores
5 Frequency=3027346 Hz, Resolution=330.3223 ns, Timer=TSC
6 .NET Core SDK=2.1.403
7 [Host] : .NET Core 2.0.7 (CoreCLR 4.6.26328.01, CoreFX 4.6.26403.03), 64bit Ryu
8 Job-VPAMDV : .NET Framework 4.7.2 (CLR 4.0.30319.42000), 64bit RyuJIT-v4.7.3221.0
9 Job-HUVHDP : .NET Core 2.0.7 (CoreCLR 4.6.26328.01, CoreFX 4.6.26403.03), 64bit Ryu
10 Job-QUSOBD : .NET Core 2.1.5 (CoreCLR 4.6.26919.02, CoreFX 4.6.26919.02), 64bit Ryu
11
12 ...
13
14 | Method | Runtime | Toolchain | Mean | Error | StdDev |
15 | ----- | ----- | ----- | ----- | ----- | ----- |
16 | Md5 | Clr | net46 | 21.56 us | 0.0289 us | 0.0241 us |
17 | Md5 | Core | netcoreapp2.0 | 20.40 us | 0.1329 us | 0.1110 us |
18 | Md5 | Core | netcoreapp2.1 | 20.35 us | 0.0352 us | 0.0329 us |
19
```

# Setup & Cleanup

```
public class SetupAndCleanupExample
{
    [GlobalSetup]
    public void GlobalSetup() { }

    [IterationSetup] // sets 1 iteration = 1 invocation
    public void IterationSetup() { }

    [Benchmark]
    public void Benchmark() { }

    [IterationCleanup]
    public void IterationCleanup() { }

    [GlobalCleanup]
    public void GlobalCleanup() { }
}
```

[More info](#)

# Params

```
public class IntroParams
{
    [Params(100, 200)]
    public int A { get; set; }

    [Params(10, 20)]
    public int B { get; set; }

    [Benchmark]
    public void Benchmark()
        => Thread.Sleep(A + B + 5);
}
```

Method	A	B
Benchmark	100	10
Benchmark	100	20
Benchmark	200	10
Benchmark	200	20

# ParamsSource

```
public class IntroParamsSource
{
    [ParamsSource(nameof(ValuesForA))]
    public int A { get, set, }

    [ParamsSource(nameof(ValuesForB))]
    public int B;

    public IEnumerable<int> ValuesForA
        => new[] { 100, 200 };

    public static IEnumerable<int> ValuesForB()
        => new[] { 10, 20 };

    [Benchmark]
    public void Benchmark()
        => Thread.Sleep(A + B + 5);
}
```

Method	B	A
Benchmark	10	100
Benchmark	10	200
Benchmark	20	100
Benchmark	20	200

# Arguments

```
public class IntroArguments
{
    [Params(true, false)]
    public bool Add5;

    [Benchmark]
    [Arguments(100, 10)]
    [Arguments(100, 20)]
    [Arguments(200, 10)]
    [Arguments(200, 20)]
    public void Benchmark(int a, int b)
    {
        if (Add5)
            Thread.Sleep(a + b + 5);
        else
            Thread.Sleep(a + b);
    }
}
```

Method	Add5	a	b
Benchmark	False	100	10
Benchmark	False	100	20
Benchmark	False	200	10
Benchmark	False	200	20
Benchmark	True	100	10
Benchmark	True	100	20
Benchmark	True	200	10
Benchmark	True	200	20

# ArgumentsSource

```
public class IntroArgumentsSource
{
    [Benchmark]
    [ArgumentsSource(nameof(Numbers))]
    public double Pow(double x, double y)
        => Math.Pow(x, y);

    public IEnumerable<object[]> Numbers()
    {
        yield return new object[] { 1.0, 1.0 };
        yield return new object[] { 2.0, 2.0 };
        yield return new object[] { 4.0, 4.0 };
        yield return new object[] { 10.0, 10.0 };
    }
}
```

Method	x	y
Pow	1	1
Pow	2	2
Pow	4	4
Pow	10	10

# Validators

```
PS D:\projects\BdnDemo> dotnet run -f net7.0 --filter *Algo*
// Validating benchmarks:
// * Assembly BdnDemo which defines benchmarks is non-optimized
Benchmark was built without optimization enabled (most probably a DEBUG configuration). Please, build it in RELEASE.
If you want to debug the benchmarks, please see https://benchmarkdotnet.org/articles/guides/troubleshooting.html#debugging-benchmarks.
```

# Diagnosers

- Plugins that allow to get some extra diagnostic information
- Can attach to the child process on specific events
- Few types: extra run / no overhead / separate logic

# Memory Diagnoser: sample

```
[MemoryDiagnoser]  
public class AccurateAllocations  
{  
    [Benchmark] public void Nothing() { }  
    [Benchmark] public byte[] EightBytesArray() => new byte[8];  
    [Benchmark] public byte[] SixtyFourBytesArray() => new byte[64];  
  
    [Benchmark] public Task<int> AllocateTask()  
        => Task.FromResult(default(int));  
}
```

# Memory Diagnoser: results

Method	Mean	Error	StdDev	Gen0	Allocated
Nothing	0.0000 ns	0.0000 ns	0.0000 ns	-	-
EightBytesArray	2.4253 ns	0.0854 ns	0.0757 ns	0.0038	32 B
SixtyFourBytesArray	3.4825 ns	0.0891 ns	0.0833 ns	0.0105	88 B
AllocateTask	2.1652 ns	0.0031 ns	0.0025 ns	-	-

```
// * Warnings *
ZeroMeasurement
AccurateAllocations.Nothing: Runtime=NativeAOT 7.0, Toolchain=Latest ILCompiler -> The method duration is indistinguishable from the empty method duration

// * Legends *
Mean      : Arithmetic mean of all measurements
Error     : Half of 99.9% confidence interval
StdDev    : Standard deviation of all measurements
Gen0      : GC Generation 0 collects per 1000 operations
Allocated : Allocated memory per single operation (managed only, inclusive, 1KB = 1024B)
1 ns      : 1 Nanosecond (0.000000001 sec)
```

# Disassembly Diagnoser

- Attaches at the end (no overhead)
- Uses ClrMD to get the ASM
- Works on Windows and Linux
- Supports x64, x86 and arm64
- Command line arguments:
  - -d/--disasm
  - --disasmDepth \$recursiveDepth
  - --disasmFilter \$glob

# Sample HTML report

## BdnDemo.Sum.Field()

```
sub    rsp,28h
xor    eax,eax
xor    edx,edx
mov    rcx,qword ptr [rcx+8]
cmp    dword ptr [rcx+8],0
jle    M00_L01
```

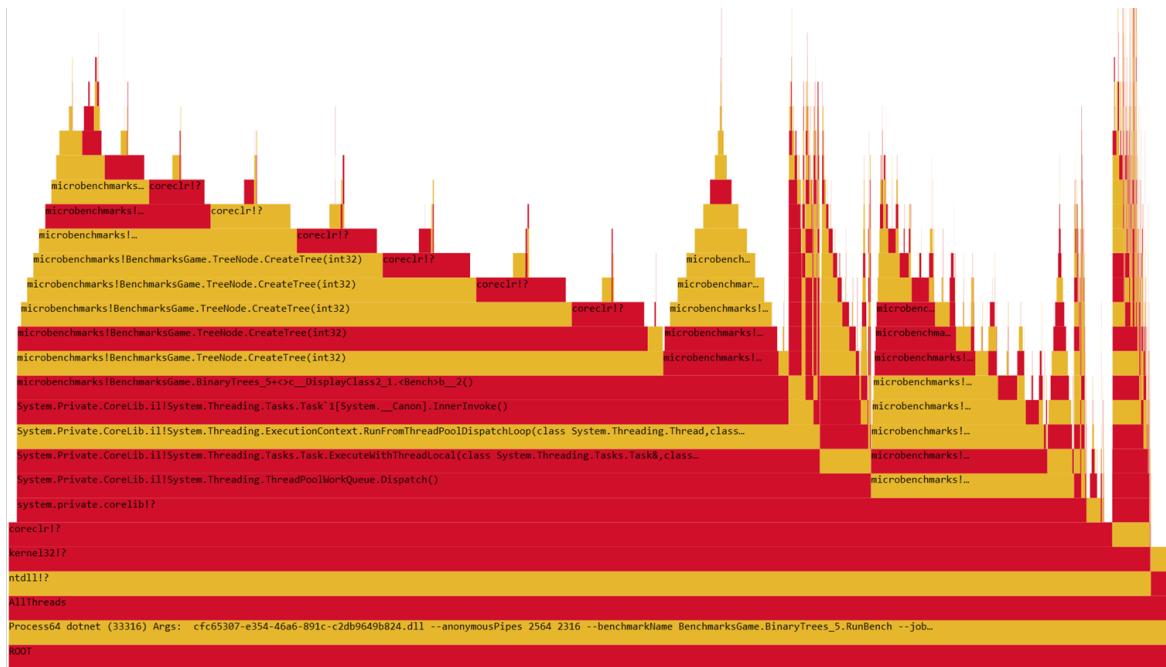
### M00\_L00

```
mov    r8,rcx
cmp    edx,dword ptr [r8+8]
jae    M00_L02
movsx r9,edx
add    eax,dword ptr [r8+r9*4+10h]
inc    edx
cmp    dword ptr [rcx+8],edx
jg     M00_L00
```

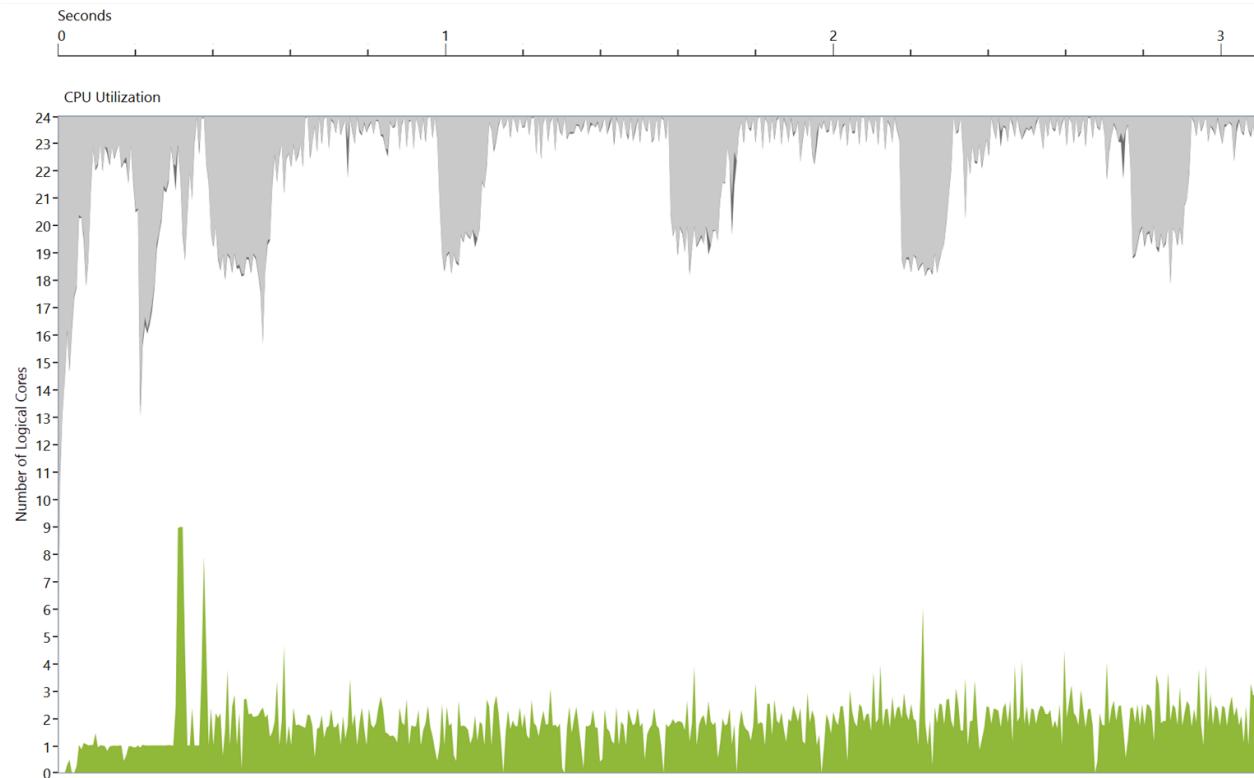
### M00\_L01

```
add    rsp,28h
ret
```

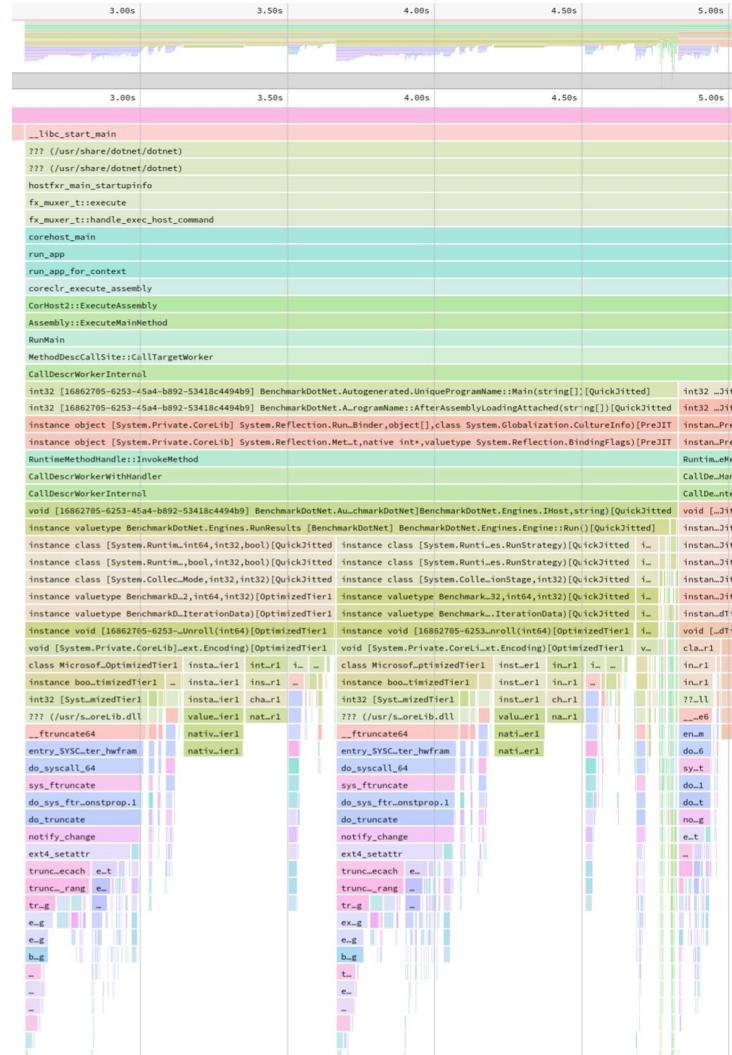
# ETW Profiler (--profiler ETW)



# Concurrency Visualiser (--profiler CV)

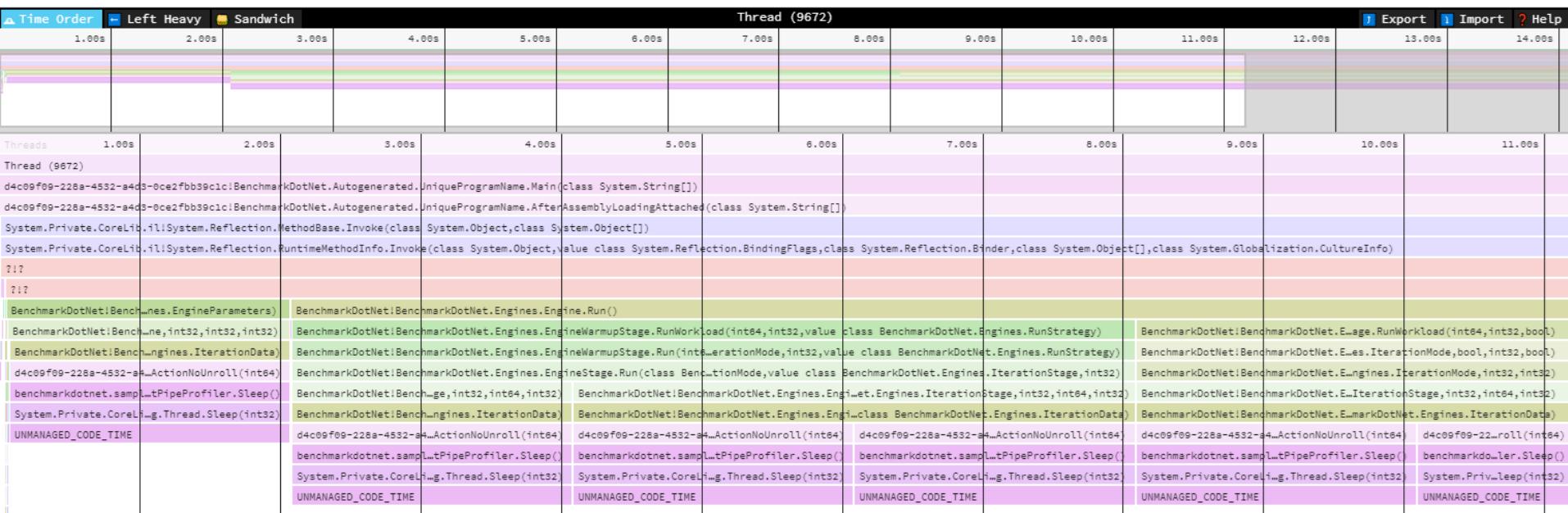


# PerfCollect (--profiler perf)



<https://adamsitnik.com/PerfCollectProfiler/>

# EventPipe (--profiler EP)



<https://wojciechnagorski.com/2020/04/cross-platform-profiling-.net-code-with-benchmarkdotnet/>

# Other Diagnosers

- PmcDiagnoser – Hardware Counters on Windows
- NativeMemoryProfiler - allocated and leaking native memory (Windows)
- InliningDiagnoser uses ETW to get info about inlining
- TailCallDiagnoser uses ETW to get info about Tail Call opt
- ExceptionsDiagnoser - reports the frequency of exceptions
- ThreadingDiagnoser - threading statistics
- Architecture allows for more (like integration with profilers)

# Statistics



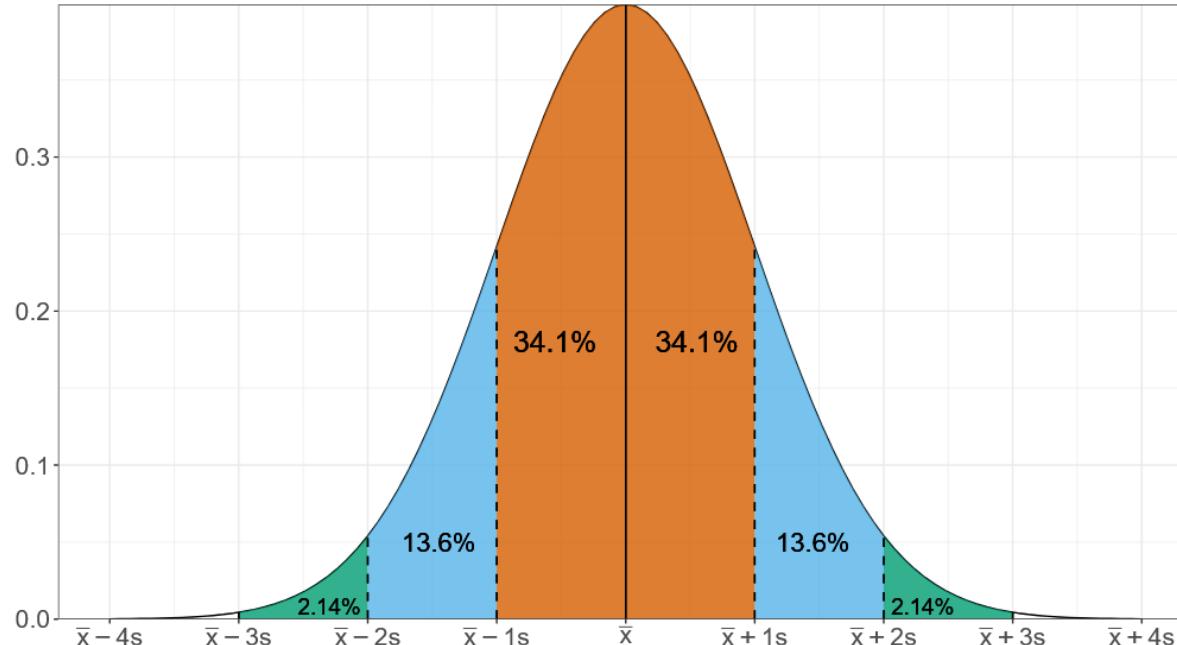
# Statistical challenges

- Summary tables
  - Should be reproducible
  - Should not be misleading
- Benchmark comparison
- Execution strategy

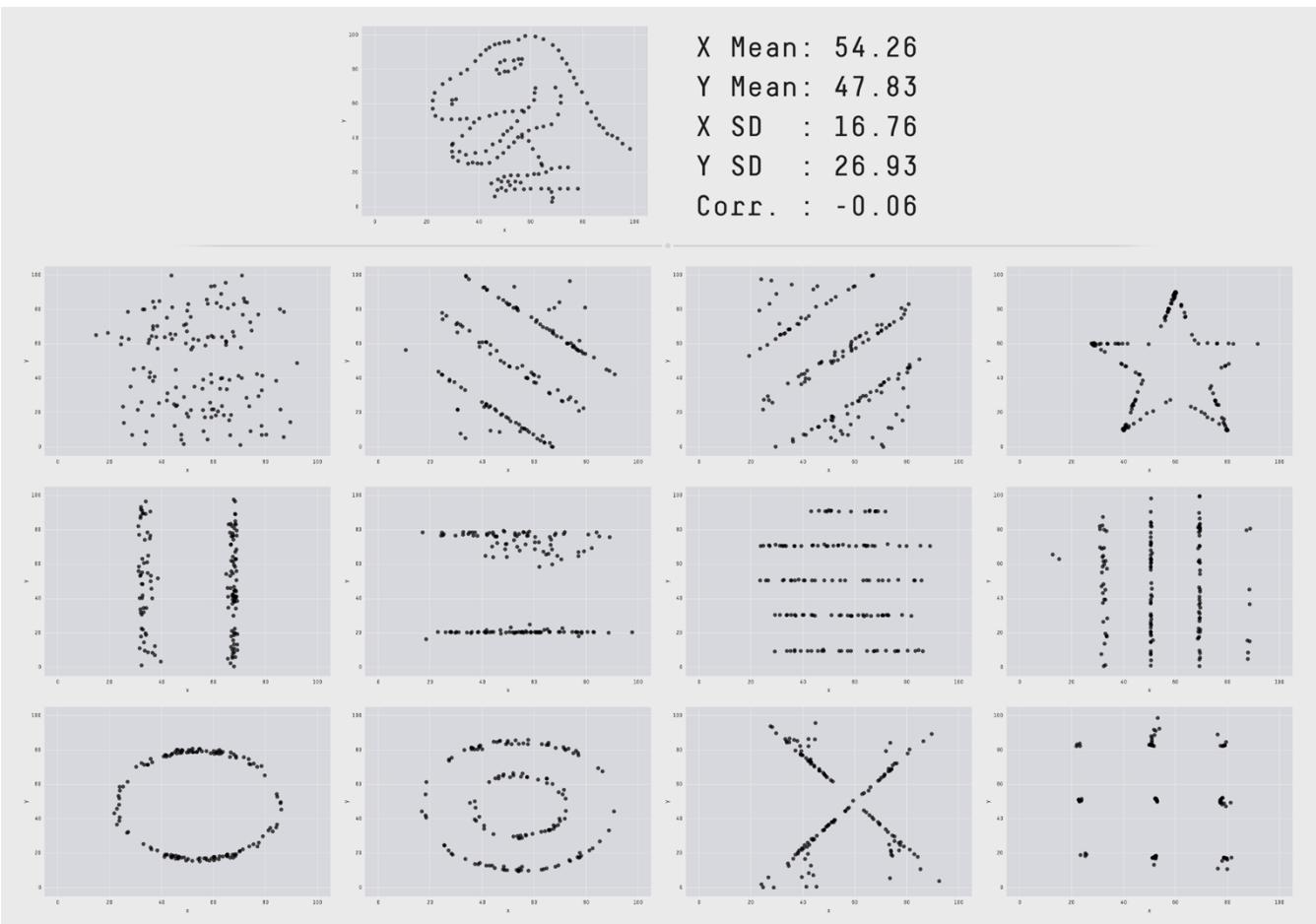
# 2023

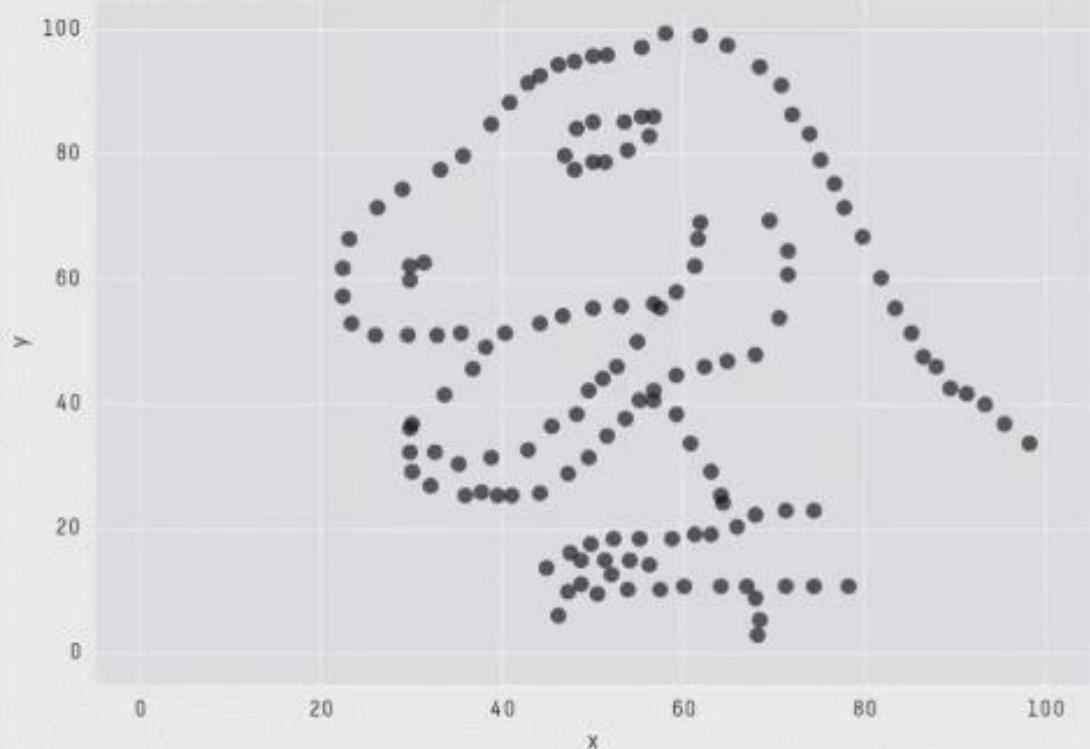
197. Efficiency of the central tendency measures under the uniform distribution (May 16)
196. Unobvious problems of using the R's implementation of the Hodges-Lehmann estimator (May 9)
195. When Python's Mann-Whitney U test returns extremely distorted p-values (May 2)
194. When R's Mann-Whitney U test returns extremely distorted p-values (April 25)
193. Preprint announcement: 'Weighted quantile estimators' (April 18)
192. Rethinking Type I/II error rates with power curves (April 11)
191. Adaptation of continuous scale measures to discrete distributions (April 4)
190. Weighted modification of the Hodges-Lehmann location estimator (March 28)
189. Performance stability of GitHub Actions (March 21)
188. p-value distribution of the Brunner–Munzel test in the finite case (March 14)
187. Comparing statistical power of the Mann-Whitney U test and the Brunner–Munzel test (March 7)
186. p-value distribution of the Mann–Whitney U test in the finite case (February 28)
185. Corner case of the Brunner–Munzel test (February 21)
184. Examples of the Mann–Whitney U test misuse cases (February 14)
183. Types of finite-sample consistency with the standard deviation (February 7)
182. Thoughts about outlier removal and ozone holes (January 31)
181. Nonparametric effect size: Cohen's d vs. Glass's delta (January 24)
180. Trinal statistical thresholds (January 17)
179. Trimmed Hodges-Lehmann location estimator, Part 2: Gaussian efficiency (January 10)
178. Trimmed Hodges-Lehmann location estimator, Part 1: breakdown point (January 3)

# The Normal distribution



> *Normality is a myth; there never was, and never will be, a normal distribution.*  
>— ["Testing for normality"](#), R.C. Geary, 1947





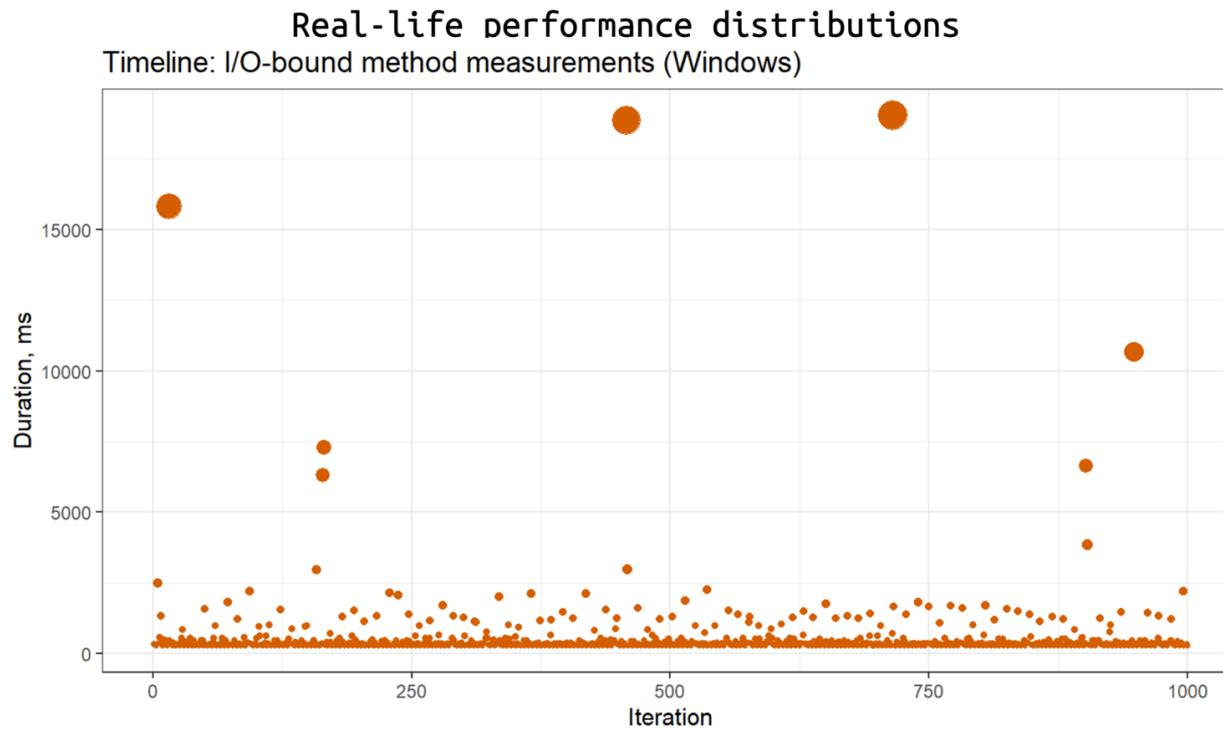
X Mean: 54.2659224  
Y Mean: 47.8313999  
X SD : 16.7649829  
Y SD : 26.9342120  
Corr. : -0.0642526

# IO-Benchmark example

```
int N = 1000; // The number of iterations
var measurements = new long[N];
byte[] data = new byte[64 * 1024 * 1024]; // 64MB

for (int i = 0; i < N; i++)
{
    var stopwatch = Stopwatch.StartNew();
    var fileName = Path.GetTempFileName();
    File.WriteAllBytes(fileName, data);
    File.Delete(fileName);
    stopwatch.Stop();
    measurements[i] = stopwatch.ElapsedMilliseconds;
}
```

# IO-Benchmark example: results



# Distribution features to support

- Huge dispersion
- Extreme outliers
- Multimodality
- Asymmetry
- Discretization

## Central tendency / The mean

$$x = \{x_1, x_2, \dots, x_n\}; \quad \bar{x} = \frac{x_1 + x_2 + \dots + x_n}{n}$$

$$x = \{1, 2, 3, 4, 5, 6, 7\}; \quad \bar{x} = 4$$

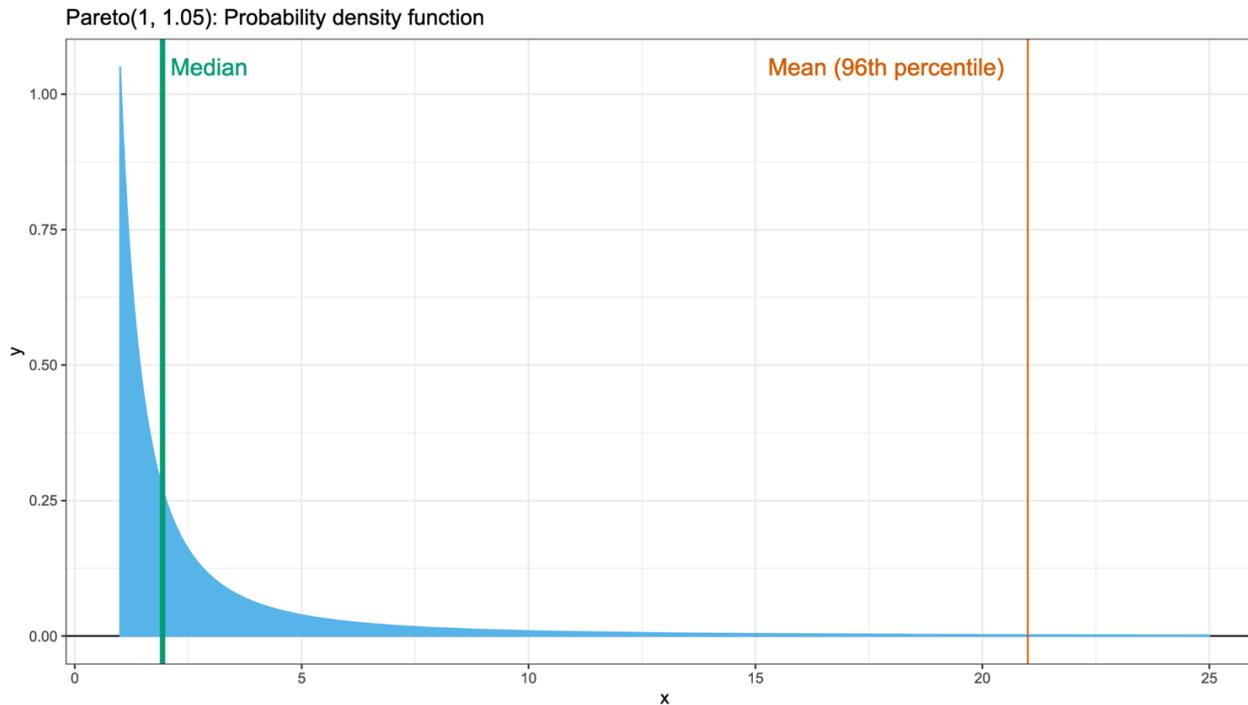
$$x = \{1, 2, 3, 4, 5, 6, 273\}; \quad \bar{x} = 42$$

## Central tendency / The median

$$x = \{1, 2, 3, 4, 5, 6, 7\}; \quad \tilde{x} = 4$$

$$x = \{1, 2, 3, 4, 5, 6, 273\}; \quad \tilde{x} = 4$$

# Central tendency



# Central tendency

	Mean	Median
Gaussian efficiency	100%	≈64%

# Central tendency

	Mean	Median
Gaussian efficiency	100%	≈64%
Cost	100€	<b>157€</b>

# Central tendency / Hodges-Lehmann

$$\text{HL} = \underset{i \leq j}{\text{median}} \left( \frac{x_i + x_j}{2} \right)$$

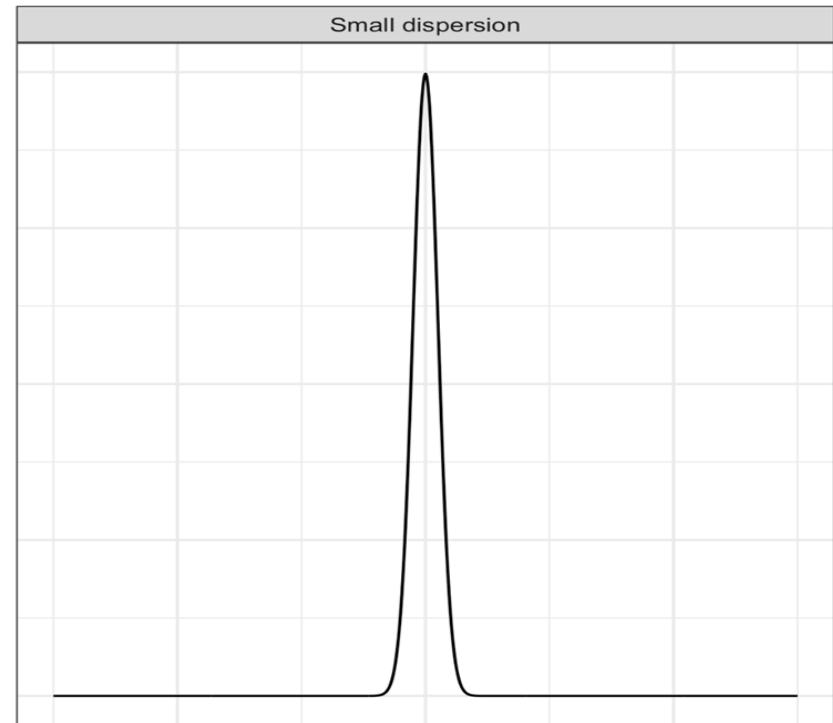
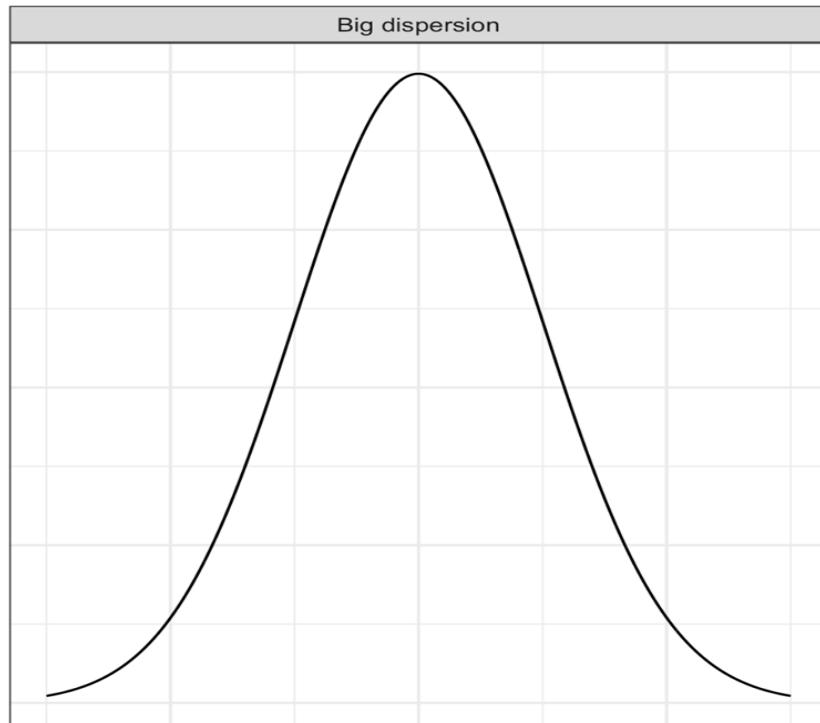
# Central tendency

	Mean	Median	HL
Gaussian efficiency	100%	≈64%	≈96%
Cost	100€	157€	104€

# Central tendency / Other estimators

- Trimmed mean
- Winsorized mean
- Mode
- Geometric mean
- Harmonic mean
- Interquartile mean
- Midrange
- Midhinge
- Trimean
- Huber M-estimator
- Andrews M-estimator
- Hampel M-estimator
- Biweight M-estimator
- ...

# Dispersion



## Dispersion / Standard deviation

$$s = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2}$$

## Dispersion / Median absolute deviation

$$\text{MAD} = C_n \cdot \text{median}\left(|x_i - \text{median}(x)|\right)$$

# Dispersion / Other estimators

## **Shamos estimator**

$$\text{Shamos} = C_n \cdot \text{median}(|x_i - x_j|_{i < j}); \quad C_\infty \approx 1.048358$$

## **Rousseeuw-Croux estimator**

$$S_n = C_n \cdot \text{median}_i \left( \text{median}_j (|x_i - x_j|) \right); \quad C_\infty \approx 1.1926$$

$$Q_n = C_n \cdot Q(|x_i - x_j|_{i < j}, 0.25); \quad C_\infty \approx 2.2191$$

# Dispersion / Quantile absolute deviation

## Quantile absolute deviation

Andrey Akinshin

### Abstract

The median absolute deviation (MAD) is a popular robust measure of statistical dispersion. However, when it is applied to non-parametric distributions (especially multimodal, discrete, or heavy-tailed), lots of statistical inference issues arise. Even when it is applied to distributions with slight deviations from normality and these issues are not actual, the Gaussian efficiency of the MAD is only 37% which is not always enough.

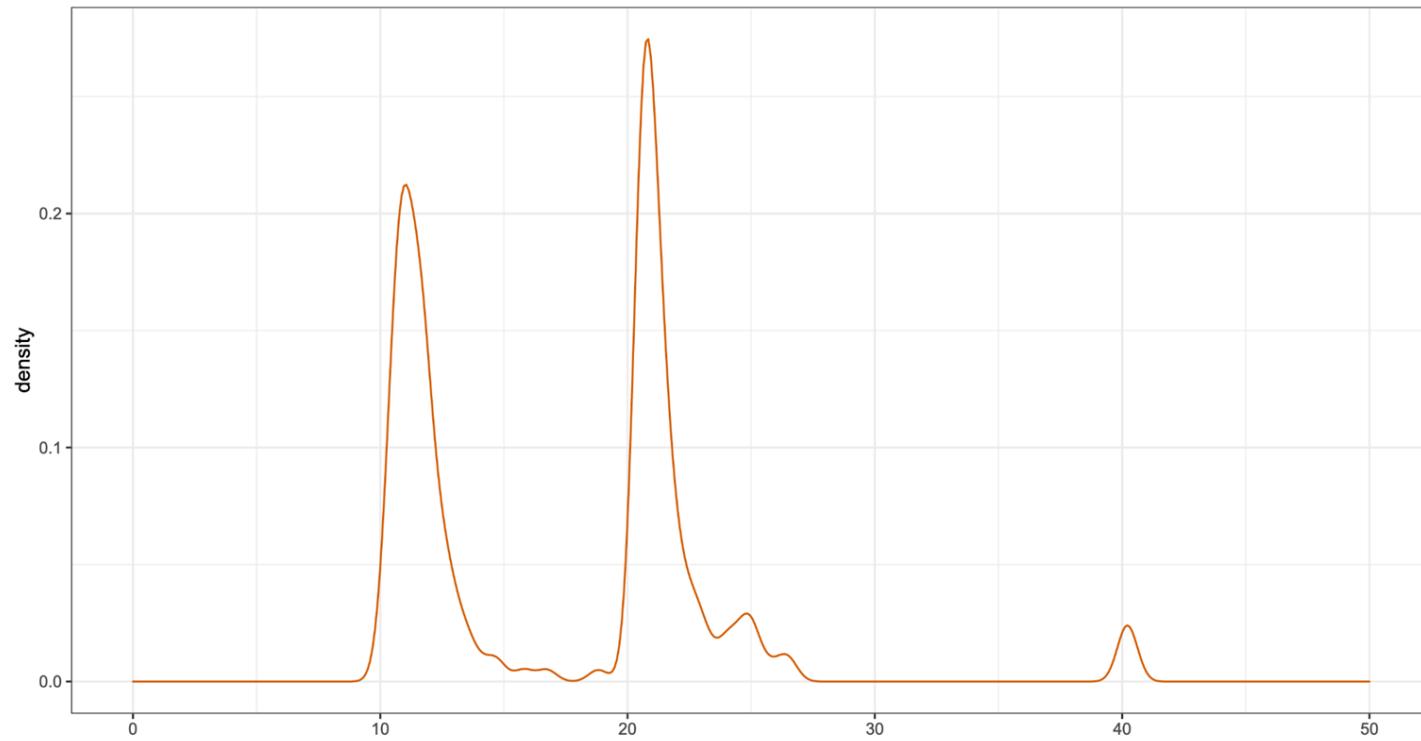
In this paper, we introduce the *quantile absolute deviation* (QAD) as a generalization of the MAD. This measure of dispersion provides a flexible approach to analyzing properties of non-parametric distributions. It also allows controlling the trade-off between robustness and statistical efficiency. We use the trimmed Harrell-Davis median estimator based on the highest density interval of the given width as a complimentary median estimator that gives increased finite-sample Gaussian efficiency compared to the sample median and a breakdown point matched to the QAD.

As a rule of thumb, we suggest using two new measures of dispersion called the *standard QAD* and the *optimal QAD*. They give 54% and 65% of Gaussian efficiency having breakdown points of 32% and 14% respectively.

**Keywords:** statistical dispersion, median absolute deviation, robustness, statistical efficiency.

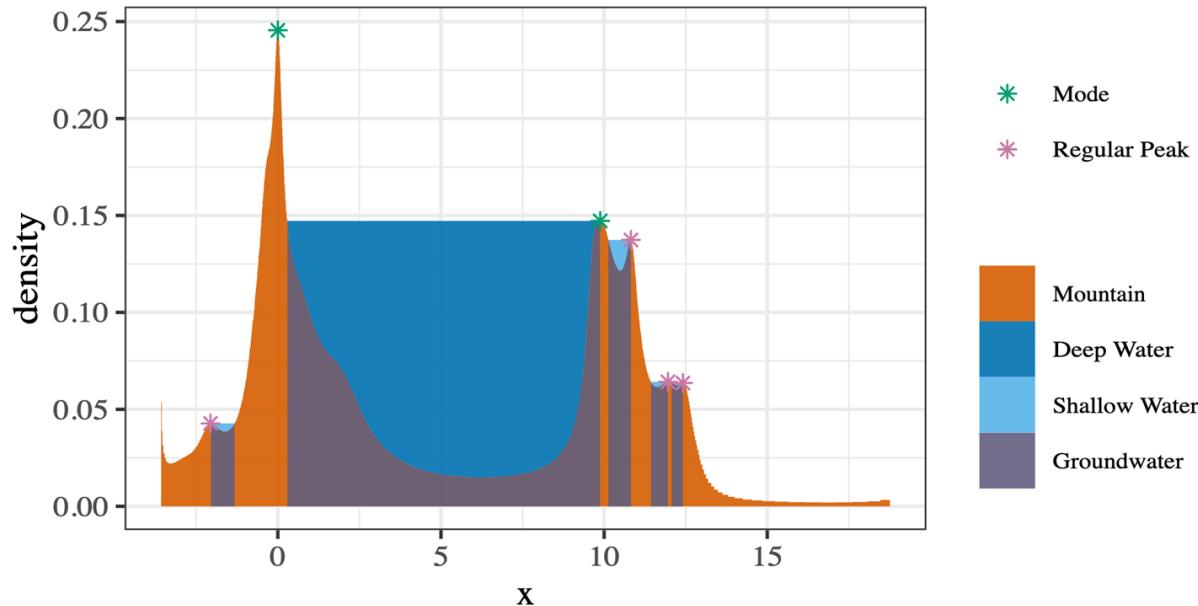
# Real-life distributions

Multimodal distribution



# Multimodality

Modality: 2



# Quantile estimations / “Traditional”

Type	$h$	Equation
1	$Np + 1/2$	$x_{\lceil h - 1/2 \rceil}$
2	$Np + 1/2$	$(x_{\lceil h - 1/2 \rceil} + x_{\lceil h + 1/2 \rceil})/2$
3	$Np$	$x_{\lfloor h \rfloor}$
4	$Np$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$
6	$(N + 1)p$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$
5	$Np + 1/2$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$
7	$(N - 1)p + 1$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$
8	$(N + 1/3)p + 1/3$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$
9	$(N + 1/4)p + 3/8$	$x_{\lfloor h \rfloor} + (h - \lfloor h \rfloor)(x_{\lceil h \rceil} - x_{\lfloor h \rfloor})$

# Quantile estimations / Harrell-Davis

$$Q_{HD}(p) = \sum_{i=1}^n W_i \cdot x_{(i)}$$

$$W_i = I_{i/n}(a, b) - I_{(i-1)/n}(a, b)$$

$$a = p(n + 1), \quad b = (1 - p)(n + 1)$$

# Quantile estimations / Sfakianakis-Verginis

$$\text{SV1}_p = \frac{B_0}{2} (X_{(1)} + X_{(2)} - X_{(3)}) +$$

$$\sum_{i=1}^n \frac{B_i + B_{i-1}}{2} X_{(i)} +$$

$$\frac{B_n}{2} (-X_{(n-2)} + X_{(n-1)} - X_{(n)}),$$

$$\text{SV2}_p = \sum_{i=1}^n B_{i-1} X_{(i)} + B_n \cdot (2X_{(n)} - X_{(n-1)}),$$

$$\text{SV3}_p = \sum_{i=1}^n B_i X_{(i)} + B_0 \cdot (2X_{(1)} - X_{(2)}).$$

# Quantile estimations / Navruz-Özdemir

$$\begin{aligned} \text{NO}_p = & \left( (3p - 1)X_{(1)} + (2 - 3p)X_{(2)} - (1 - p)X_{(3)} \right) B_0 + \\ & + \sum_{i=1}^n \left( (1 - p)B_{i-1} + pB_i \right) X_{(i)} + \\ & + \left( -pX_{(n-2)} + (3p - 1)X_{(n-1)} + (2 - 3p)X_{(n)} \right) B_n \end{aligned}$$

# Quantile estimations / Trimmed Harrell-Davis

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Trimmed Harrell-Davis quantile estimator based on the highest density interval of the given width

Andrey Akinshin  
JetBrains, [andrey.akinshin@gmail.com](mailto:andrey.akinshin@gmail.com)

## Abstract

Traditional quantile estimators that are based on one or two order statistics are a common way to estimate distribution quantiles based on the given samples. These estimators are robust, but their statistical efficiency is not always good enough. A more efficient alternative is the Harrell-Davis quantile estimator which uses a weighted sum of all order statistics. Whereas this approach provides more accurate estimations for the light-tailed distributions, it's not robust. To be able to customize the trade-off between statistical efficiency and robustness, we could consider *a trimmed modification of the Harrell-Davis quantile estimator*. In this approach, we discard order statistics with low weights according to the highest density interval of the beta distribution.

**Keywords:** quantile estimation, robust statistics, Harrell-Davis quantile estimator.

# Mann-Whitney U-test

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## ≡ Mann-Whitney *U* test

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In statistics, the **Mann-Whitney *U* test** (also called the **Mann-Whitney-Wilcoxon (MWW/MWU)**, **Wilcoxon rank-sum test**, or **Wilcoxon-Mann-Whitney test**) is a **nonparametric test** of the **null hypothesis** that, for randomly selected values  $X$  and  $Y$  from two populations, the probability of  $X$  being greater than  $Y$  is equal to the probability of  $Y$  being greater than  $X$ .

Nonparametric tests used on two *dependent* samples are the **sign test** and the **Wilcoxon signed-rank test**.

# Mann-Whitney U-test

```
> x <- 101:150
> y <- 1:50
>
> # The default approximation
> wilcox.test(x, y, alternative = "greater")$p.value
[1] 0.0000000000000003533036
>
> # The true correct value
> wilcox.test(x, y, alternative = "greater", exact = TRUE)$p.value
[1] 0.000000000000000000000000009911653
```

**Difference: 356'452'748'856 times!!!**

# Mann-Whitney U-test

## **Different Outcomes of the Wilcoxon–Mann–Whitney Test From Different Statistics Packages**

Reinhard BERGMANN, John LUDBROOK, and Will P. J. M. SPOOREN

# Mann-Whitney U-test

## 2.2 The Edgeworth Approximation

For the Edgeworth approximation  $A_E(x)$  with two terms we use (see Froda and van Eeden, 2001, Corollary 3.1)

$$A_E(x) = \Phi(x) - \phi(x) \frac{1}{N} \frac{c_{20}}{4!} H_3(x),$$

where  $\Phi$  and  $\phi$  are, respectively, the distribution function and the density of an  $\mathcal{N}(0, 1)$  random variable,  $H_3(x) = x^3 - 3x$  (*i.e.*  $H_3(x)$  is a Hermite polynomial) and (see Froda and van Eeden, 2001, Lemma 2.3)

$$c_{20} = -\frac{6(1-p^5 - (1-p)^5)}{25(p(1-p))^2},$$

where  $p = m/N \in (0, 1)$ .

Assuming that  $m$  and  $n$  converge to infinity such that  $m/N$  stays fixed, the rate of convergence of the error term is given by (see again Froda and van Eeden, 2001, Corollary 3.1)

$$A_E(x) - F(x) = O(N^{-3/2}).$$

The error term thus converges to 0 faster than the one for the normal approximation. But a disadvantage is that  $A_E(x)$  is not a proper distribution function and can take values outside the interval  $[0, 1]$  when  $x$  is far in the tails.

## 2.3 The Saddlepoint Approximation

We use the saddlepoint with two terms of Froda and van Eeden (2001), and we approximate  $1 - F(x)$  for  $x > 0$ . Let  $Q_F$  be the moment generating function of  $T$  given by Froda and van Eeden (2001, p. 139)

$$Q_F(u) = \exp\left(\frac{-umn}{\sigma}\right) \prod_{j=1}^m \frac{j}{n+j} \frac{1 - \exp(u(n+j)/\sigma)}{1 - \exp(uj\sigma)},$$

where  $\sigma^2$  is the variance of  $W$ . Further, let  $a(u) = d(\log Q_F(u))/du$  and  $b(u) = d^2(\log Q_F(u))/du^2$  and let  $u$  solve  $a(u) = x$ . Then (see Froda and van Eeden, 2001, formula (31)) the saddle-point approximation to  $1 - F(x)$  is given by

$$1 - A_S(x) = Q_F(u) \exp(-ux + u^2 b(u)/2) \{1 - \Phi(u(b(u))^{1/2})\} \\ \times \left\{1 + \frac{3}{N} \frac{c_{20}}{4!} \frac{u}{(b(u))^{3/2}} W_3(u(b(u))^{1/2})\right\},$$

where  $W_3(v)$  is defined by

$$W_3(v) = \frac{(v^2 - 1)\phi(v)}{1 - \Phi(v)} - v^3.$$

Further, for  $x$  bounded and again assuming that  $m/N \in (0, 1)$  is fixed, note that (see Froda and van Eeden, 2001; formula (25))

$$1 - F(x) = 1 - A_S(x) + O(N^{-3/2}).$$



# Pro .NET Benchmarking

The Art of Performance Measurement

—  
Andrey Akinshin

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# Roadmap to BenchmarkDotNet 1.0.0

1. New statistical engine
2. Fix some bugs
3. Improve API

# Conclusion



# BenchmarkDotNet: Summary

- Accurate, Repeatable and Stable Results
- **Powerful** Statistics
- Rich support:
  - C#, F#, VB
  - .NET 4.6+, .NET Core 2.0+, Mono, NativeAOT, WASM
  - Windows, Linux, macOS
  - x64, x86, arm64, arm, S390x, LoongArch64, armv6, ppc64le
- Easy benchmark design (no boilerplate code and nice API)
- Great User Experience
- Strong community
- Very good test coverage

Do you still want to write your own harness using Stopwatch?

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@BenchmarkDotNet



<https://aakinshin.net>

andrey.akinshin@gmail.com

@andrey\_akinshin



<https://adamsitnik.com>

adam.sitnik@gmail.com

@SitnikAdam

