IS 607 Final Project

Predicting internet penetration rates

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Introduction:

The internet is the greatest educational tool around today. The fact that I can study at a university that is physically located 6000 miles away from me is astounding. My belief is that internet penetration is strongly correlated to literacy levels. According to a press release by internet.org over 85% of the world is within range of picking up internet signals but only about 35% of the world actually use the internet. I would like to first quantify the correlation between literacy and internet penetration and then study some of the other factors that contribute to a higher internet penetration rate on a country level.

Feature Selection:

In order to find data I have scoured wikipedia and some other sites for country level data which I believe might be relevant towards affecting internet penetration. The features that I have come up with are:

- The literacy rate of a nation
- The GDP per capita (in USD)
- The median age
- The suicide rate
- The unemployment rate
- · The population density
- The ratio of males to females
- The happy planet index, which is an index that says how happy the nation is
- · The percent of English speakers
- · The polution levels
- · The life expectancy

In general these features are variables that I thought might have some effect on internet penetration rates. The reasons chosen may or may not be true. I will quickly try to explain some of the rationale for each of the features. Literacy rate is pretty obvious as internet is a text based world. GDP would be to understand if the costs are a barrier. The median age and life expectancy are because maybe internet is more prevelant amongst young people, or maybe old people, or possibly more developed countries have a higher life expectancy and also a higher adoption rate (merely because they re more developed). Suicide rate, unemployment rate (also related to cost barrier), happy planet index and polution rate all have to do with the populations desire to go on the internet. Ratio of males to females is based on an assumption that internet

adoption is affected by gender. Population density was included under the assumption that a higher population density might mean better infrastructure. Finally percent English speakers is because most of the internet content is in English and unfortunately not the whole world speaks the language.

It is very possible that other reasons exist that could be predictive features, yet this is what I was able to think of to include.

Data Collection and Retrieval:

I started with scraping the data I found on the internet at the following URL's

```
penetration_url <- "http://data.worldbank.org/indicator/IT.NET.USER.P2"
literacy_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_literacy_rate"
gdp_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_past_and_projected_GDP_(PPP)"
median_age_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_median_age"
life_expectancy_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_life_expectancy"
suicide_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_suicide_rate"
unemployment_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_unemployment_rate"
pop_density_url <- "http://simple.wikipedia.org/wiki/List_of_countries_by_population_density"
male_female_ratio_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_sex_ratio"
hpi_url <- "http://en.wikipedia.org/wiki/Happy_Planet_Index"
c02_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_carbon_dioxide_emissions"
eng_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_English-speaking_population"
populations_url <- "http://en.wikipedia.org/wiki/List_of_countries_by_population"</pre>
```

Data Cleansing:

Once reading the URL's into R, I had to massage the data to remove unused metrics from the tables as well as remove things like commas from the number fields and notes from the country field. A lot of regular expression work was used to clean up the data. Eventually from each URL my final data included only the country name and the specific metric as a numeric field. Some of the numeric fields were percentages and were displayed as a number between 0 and 100, I converted those to numbers between 0 and 1. Also in the case of GDP I only had the complete GDP and I had to devide it by population figures.

Once I had each of the tables seperately imported and cleaned, I merged the data together on the country field performing an "Inner Join". Unfortunately since my data did not include all the information for each country, my data set was widdled down to the lowest common denominator for countries included in each data set. If each of the data sets was more complete I would have ended up with 200+ observations for my final analysis, but alas it was not, and I was left with roughly 60 obs. The reason I performed an inner join was because I did not want to perform some sort of bootstrapping method for filling in null values as those methods may be statiscally questionable and might affect the final analysis. Here is the final data set after merging them together.

##	country penet	ration_rate lite	eracy_rate gdp_	per_capita
## 1	Argentina	0.599	0.979	21746
## 2	Australia	0.830	0.960	44413
## 3	Austria	0.806	0.980	44179
## 4	Barbados	0.750	0.997	15660

##	5	Belgium	0.822	0.990	40529
##	6	Belize	0.317	0.769	8015
##	7	Bhutan	0.299	0.528	7185
##	8	Brazil	0.516	0.913	14798
##	9	Bulgaria	0.531	0.984	16501
##	10	Canada	0.858	0.990	42561
##	12	Chile	0.665	0.986	22202
##	13	Colombia	0.517	0.936	12565
##	14	Croatia	0.667	0.992	20286
##	15	Cyprus	0.655	0.987	29534
##	16	Czech Republic	0.741	0.990	27333
##	17	Denmark	0.946	0.990	42590
##	18	Estonia	0.800	0.998	26138
##	19	Finland	0.915	1.000	39890
##	20	France	0.819	0.990	38356
##	21	Germany	0.840	0.990	43484
##	22	Greece	0.599	0.980	25286
##	23	Grenada	0.350	0.960	11749
##	24	Guyana	0.330	0.918	6668
##	25	Hungary	0.726	0.990	23236
##	26	India	0.151	0.744	5360
##	27	Ireland	0.782	0.990	46275
##	28	Israel	0.708	0.971	31144
##	29	Italy	0.585	0.990	33495
##	30	Jamaica	0.378	0.879	8693
##	31	Jordan	0.442	0.934	11423
##	32	Kazakhstan	0.540	0.995	22756
##	33	Latvia	0.752	0.998	23369
##	34	Lithuania	0.685	0.997	25760
##	35	Luxembourg	0.938	1.000	88252
##	36	Malta	0.689	0.928	30957
##	37	Mauritius	0.390	0.898	17677
##	38	Mexico	0.435	0.934	17199
##	39	Nepal	0.133	0.660	2257
##	40	Netherlands	0.940	0.990	46222
##	41	New Zealand	0.828	0.990	33131
##	42	Pakistan	0.109	0.690	4432
##	43	Philippines	0.370	0.954	6385
##	44	Poland	0.628	0.997	23295
##	45	Portugal	0.621	0.954	25652
##	46	Romania	0.498	0.977	18615
##	47	Singapore	0.730	0.959	77747
##	48	Slovenia	0.727	0.997	28427
##	49	South Africa	0.489	0.931	12270
##	50	Spain	0.716	0.977	32012
##	51	Sri Lanka	0.219	0.981	9841
##	52	Suriname	0.374	0.926	16475

##			Sweden	0.948	0.990	42949
##	54		tzerland	0.867	0.990	52603
##			Thailand	0.289	0.935	14868
##	56	Trinidad an	_	0.638	0.986	30563
##	57		Turkey	0.463	0.953	18828
##	58	United	Kingdom	0.898	0.990	36197
##	59	Unite	d States	0.842	0.990	52519
##	60		Zimbabwe	0.185	0.907	1963
##		median_age	suicide_rate	<pre>unemployment_rate</pre>	population_p	er_sq_km
##	1	30.3	0.0770	0.075		14.0
##	2	37.5	0.1000	0.064		3.2
##	3	42.6	0.1545	0.048		100.0
##	4	36.2	0.0350	0.115		595.0
##	5	42.0	0.1700	0.085		355.0
##	6	20.7	0.0370	0.113		14.0
##	7	24.3	0.1620	0.040		46.0
##	8	30.5	0.0480	0.049		24.0
##	9	41.6	0.1230	0.131		66.0
##	10	40.7	0.1150	0.065		3.4
##	12	31.7	0.1120	0.061		24.0
##	13	27.6	0.0490	0.078		42.0
##	14	41.2	0.1970	0.176		79.0
##	15	34.5	0.0360	0.153		87.0
##	16	40.4	0.1280	0.067		134.0
##	17	40.7	0.1130	0.070		128.0
##	18	40.2	0.1480	0.087		29.0
##	19	41.6	0.1600	0.082		16.0
##	20	39.7	0.1470	0.104		114.0
##	21	43.7	0.1220	0.051		229.0
##	22	42.2	0.0350	0.259		86.0
##	23	28.2	0.0000	0.245		302.0
##	24	23.6	0.2640	0.090		3.5
##	25	41.3	0.2110	0.071		108.0
##	26	25.9	0.1050	0.088		368.0
##	27	35.4	0.1030	0.110		65.0
##	28	29.3	0.0580	0.059		371.0
##	29	44.3	0.0630	0.126		200.0
##	30	23.9	0.0010	0.113		247.0
##	31	21.8	0.0010	0.119		71.0
##	32	29.9	0.2560	0.061		6.2
##	33	40.4	0.2080	0.116		35.0
##	34	39.7	0.3100	0.115		47.0
##	35	39.3	0.0780	0.061		194.0
##	36	39.7	0.0340	0.069		1322.0
##	37	32.3	0.0680	0.079		631.0
##	38	26.7	0.0400	0.049		57.0
##	39	21.2	0.0000	0.460		199.0

##	40	40.8 0.0880	0.073	409.0
##	41	36.8 0.1150	0.056	16.0
##	42	21.2 0.0110	0.066	234.0
##	43	22.7 0.0275	0.070	307.0
	44	38.2 0.1750	0.097	122.0
	45	39.7 0.0960	0.153	115.0
	46			
		38.1 0.1190	0.072	90.0
	47	39.6 0.1030	0.019	7148.0
	48	42.1 0.2180	0.098	106.0
	49	24.7 0.1540	0.255	41.0
##	50	41.5 0.0760	0.256	91.0
##	51	31.3 0.2130	0.042	308.0
##	52	28.3 0.1440	0.090	3.2
##	53	41.7 0.1200	0.081	21.0
##	54	41.3 0.1120	0.031	188.0
##	55	33.7 0.0610	0.009	125.0
##	56	32.6 0.1070	0.037	261.0
##	57	28.1 0.0419	0.088	93.0
##	58	40.5 0.1180	0.060	255.0
##	59	36.9 0.1250	0.058	32.0
##	60	17.8 0.0790	0.700	33.0
##			percent_english_speakers	
##	1	0.97 51.96	0.0652	4.471
##		1.00 34.06	0.9703	16.934
##		0.95 48.77	0.7300	7.974
##		0.94 52.73	0.9857	5.362
##		0.96 44.04	0.5900	
##				9.977
		1.03 51.32	0.8165	1.367
##		1.10 61.08	0.1140	0.665
##		0.98 48.59	0.0790	2.150
##		0.92 31.59	0.2500	6.041
	10	0.98 39.76	0.8563	14.678
##	12	0.98 52.20	0.0953	4.213
##	13	0.98 67.24	0.0422	1.629
##	14	0.93 43.71	0.4900	4.727
##	15	1.04 45.99	0.7300	6.984
##	16	0.95 36.50	0.2700	10.669
##	17	0.98 41.40	0.8600	8.346
##	18	0.84 22.68	0.5000	13.773
##	19	0.96 37.36	0.7000	11.531
##	20	0.96 36.42	0.3900	5.556
##	21	0.97 43.83	0.6400	9.115
##	22	0.96 35.71	0.5100	7.775
	23	1.02 48.96	0.9091	2.487
	24	1.00 56.65	0.9055	2.164
	25	0.91 37.64	0.2000	5.058
	26	1.08 42.46	0.1035	1.666
пπ	20	1.00 42.40	0.1033	1.000

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##	27	0.99	39.	.38	0.9837	8.772
##	28	1.00	39.	. 07	0.8497	9.268
##	29	0.96	40.		0.3400	6.854
##	30	0.98	51.	.01	0.9764	2.660
##	31	1.10	42.	.05	0.4500	3.444
##	32	0.93	36.	.92	0.1540	15.239
##	33	0.86	2/.	. 27	0.4600	3.631
##	34	0.89	29.	. 29	0.3800	4.378
##	35	0.97	45.	.62	0.5600	21.360
##	36	0.99	53.	. 26	0.8900	6.246
##	3/	0.97	49.	.65	0.1597	3.215
##	38	0.96	54.	.39	0.1290	3.764
##	39	0.96	49.	.95	0.4649	0.140
##	40	0.98	46	. 00	0.9000	10.958
##		0.99			0.9782	7.224
##	42	1.09	39.	.40	0.4900	0.932
##	43	1.00	59.	.17	0.5663	0.873
##	44	0.94	39.	. 29	0.3300	8.309
##		0.95				
					0.2700	4.952
##	46	0.95	37.	.72	0.3100	3.889
##	47	0.95	36.	.14	0.8000	2.663
##	48	0.95	44.	.03	0.5900	7.482
##	19	0.99			0.3100	9.041
##	50	0.96	43.	.04	0.2200	5.790
##	51	0.97	60.	.31	0.0990	0.615
##	52	0.99	55.	.03	0.8709	4.540
##	53	0.98	38.	.17	0.8600	5.600
##		0.97			0.6128	4.953
##	55	0.98	55.	. 39	0.2716	4.447
##	56	1.02	51.	.87	0.8774	38.161
##	57	1.02	41.	.40	0.1700	4.131
##	58	0.98	40	. 29	0.9774	7.863
					••••	
##		0.07	20	0.2	0 0420	17 564
	59	0.97				17.564
##		0.97 0.91			0.9420 1 0.4158	17.564 0.721
##	60					
	60	0.91				
##	60 1	0.91 life_expectancy 75.3				
## ## ##	60 1 2	0.91 life_expectancy 75.3 81.4				
## ## ## ##	60 1 2 3	0.91 life_expectancy 75.3 81.4 80.2				
## ## ##	60 1 2 3	0.91 life_expectancy 75.3 81.4				
## ## ## ##	60 1 2 3 4	0.91 life_expectancy 75.3 81.4 80.2				
## ## ## ##	60 1 2 3 4 5	0.91 life_expectancy 75.3 81.4 80.2 76.2				
## ## ## ## ##	60 1 2 3 4 5 6	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3				
## ## ## ## ## ##	60 1 2 3 4 5 6 7	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3 65.7				
## ## ## ## ## ##	60 1 2 3 4 5 6 7 8	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3				
## ## ## ## ## ##	60 1 2 3 4 5 6 7 8	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3 65.7				
## ## ## ## ## ##	60 1 2 3 4 5 6 7 8	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3 65.7 75.5				
## ## ## ## ## ## ##	60 1 2 3 4 5 6 7 8 9 10	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3 65.7 75.5 72.7 80.5				
## ## ## ## ## ##	60 1 2 3 4 5 6 7 8 9 10 12	0.91 life_expectancy 75.3 81.4 80.2 76.2 79.7 75.3 65.7 75.5 72.7				

## 14		
## 16	## 14	76.0
## 17	## 15	78.9
## 17	## 16	77.0
## 18		
## 19		
## 20		
## 21		
## 22		
## 23	## 21	79.8
## 24 68.7 ## 25 73.6 ## 26 64.1 ## 27 79.6 ## 28 80.6 ## 29 81.3 ## 30 72.2 ## 31 72.9 ## 32 65.7 ## 33 72.2 ## 34 71.3 ## 35 79.3 ## 36 78.8 ## 37 72.8 ## 38 76.1 ## 39 67.4 ## 40 80.2 ## 41 80.1 ## 42 64.5 ## 43 67.8 ## 44 75.5 ## 45 78.5 ## 44 75.5 ## 45 78.5 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 49 51.2 ## 59 80.7 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 59 77.9	## 22	79.5
## 25	## 23	75.3
## 25	## 24	68.7
## 26		
## 27		
## 28		
## 29		
## 30		
## 31		
## 32 65.7 ## 33 72.2 ## 34 71.3 ## 35 79.3 ## 36 78.8 ## 38 76.1 ## 39 67.4 ## 40 80.2 ## 41 80.1 ## 42 64.5 ## 43 67.8 ## 44 75.5 ## 45 78.5 ## 46 73.1 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 58 79.5 ## 58 79.5 ## 58 79.5 ## 58 79.5 ## 59 77.9	## 30	72.2
## 33	## 31	72.9
## 34	## 32	65.7
## 34	## 33	72.2
## 35		
## 36		
## 37		
## 38		
## 39 67.4 ## 40 80.2 ## 41 80.1 ## 42 64.5 ## 43 67.8 ## 44 75.5 ## 45 78.5 ## 46 73.1 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9		
## 40		
## 41 80.1 ## 42 64.5 ## 43 67.8 ## 44 75.5 ## 45 78.5 ## 46 73.1 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9		
## 42 64.5 ## 43 67.8 ## 44 75.5 ## 45 78.5 ## 46 73.1 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 40	80.2
## 43 67.8 ## 44 75.5 ## 45 78.5 ## 46 73.1 ## 47 80.6 ## 48 78.5 ## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 41	80.1
## 44	## 42	64.5
## 45	## 43	67.8
## 45	## 44	75.5
## 46	## 45	78.5
## 47		
## 48		
## 49 51.2 ## 50 80.7 ## 51 74.2 ## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9		
## 50		
## 51		
## 52 69.6 ## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9		
## 53 80.8 ## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9		
## 54 81.8 ## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 52	69.6
## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 53	80.8
## 55 73.5 ## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 54	81.8
## 56 69.4 ## 57 72.9 ## 58 79.5 ## 59 77.9	## 55	
## 57 72.9 ## 58 79.5 ## 59 77.9		
## 58 79.5 ## 59 77.9		
## 59 77.9		
## 60 46.5		
	## 60	46.5

Data Exploration:

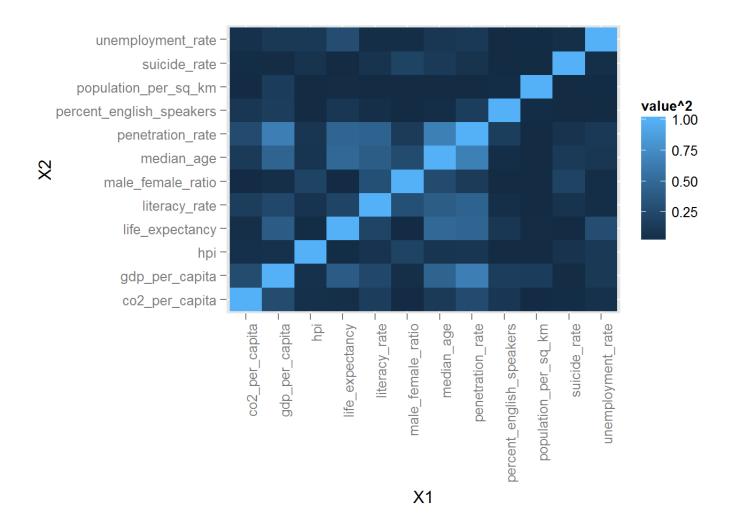
Lets begin by taking a quick look at the summary statistics of the data.

```
##
      country
                        penetration_rate literacy_rate
                                                           gdp_per_capita
    Length:59
                        Min.
                                :0.109
                                          Min.
                                                  :0.528
                                                           Min.
                                                                   : 1963
##
    Class :character
                                          1st Qu.:0.934
                        1st Qu.:0.438
                                                           1st Qu.:14833
##
                                          Median :0.981
##
    Mode :character
                        Median :0.655
                                                           Median:23369
##
                        Mean
                                :0.608
                                          Mean
                                                  :0.945
                                                           Mean
                                                                   :26687
##
                        3rd Qu.:0.803
                                          3rd Qu.:0.990
                                                           3rd Qu.:37277
                        Max.
                                :0.948
                                          Max.
                                                  :1.000
                                                           Max.
                                                                   :88252
##
##
      median age
                     suicide rate
                                      unemployment rate population per sq km
    Min.
           :17.8
                   Min.
                           :0.0000
                                      Min.
                                             :0.009
                                                         Min.
##
    1st Qu.:28.2
                    1st Qu.:0.0535
                                      1st Qu.:0.061
##
                                                         1st Qu.:
    Median :36.9
                   Median :0.1070
                                      Median :0.079
##
                                                         Median :
##
    Mean
           :34.4
                    Mean
                           :0.1080
                                      Mean
                                             :0.109
                                                         Mean
                                                                : 278
    3rd Qu.:40.7
                    3rd Qu.:0.1475
                                      3rd Qu.:0.114
                                                         3rd Qu.: 232
##
                                                                 :7148
           :44.3
                           :0.3100
                                             :0.700
##
    Max.
                    Max.
                                                         Max.
                                      Max.
##
    male_female_ratio
                            hpi
                                       percent_english_speakers co2_per_capita
    Min.
           :0.840
                       Min.
                              :16.6
                                       Min.
                                               :0.0422
                                                                 Min.
                                                                         : 0.14
##
    1st Qu.:0.950
                       1st Qu.:37.5
                                       1st Qu.:0.2700
                                                                 1st Qu.: 3.33
##
                       Median :43.0
    Median :0.970
                                       Median :0.5000
                                                                 Median: 5.36
##
##
    Mean
           :0.974
                       Mean
                              :43.5
                                       Mean
                                              :0.5332
                                                                 Mean
                                                                         : 6.86
##
    3rd Qu.:0.990
                       3rd Qu.:50.5
                                       3rd Qu.:0.8582
                                                                  3rd Qu.: 8.56
    Max.
           :1.100
                              :67.2
                                              :0.9857
                                                                  Max.
                                                                         :38.16
##
                       Max.
                                       Max.
    life_expectancy
##
##
    Min.
           :46.5
    1st Qu.:72.8
##
    Median:76.0
##
##
    Mean
           :74.7
    3rd Qu.:79.5
##
##
   Max.
           :81.8
```

My original assumption was that literacy levels were highly correlated to internet penetration. In order to check if that is true we can calculate the Pearson Coefficient between those two variables.

```
## [1] "The Correlation Coefficient between Literacy rate and Internet Penetration is : 0.67"
```

Now that we know that there is a strong correlation, it would be interesting to look at the cross correlations between all the variable. Below is a heatmap of the R-squared for each pair of variables. The lighter the color the more correlated the variables are. Notice that the diaganol is completely light blue as each variable's correlation with itself is 1.



Predictive Model Building

In order to build a predictive model, I will devide my dataset into a training set and a test set. I will use 70% of the observations to train on and the other 30% to validate the model. R-squared is a good indication, but physically plotting the actual versus the expected is something I always find to be great way to visualize the results.

Once I seperate out the test set from the training set I will run a simple linear regression as a naive model just to see how well each of the variables are at helping to predict the penetration rate in each country. As you can see from the regression result, some of the variables below are not significant.

```
##
## Call:
  lm(formula = penetration_rate ~ literacy_rate + gdp_per_capita +
##
       median age + suicide rate + unemployment rate + population per sq km +
##
       male_female_ratio + hpi + percent_english_speakers + co2_per_capita +
##
       life_expectancy, data = training_set)
##
##
##
  Residuals:
        Min
                  1Q
                       Median
                                    3Q
                                            Max
##
   -0.18458 -0.03599 0.00514 0.05499 0.15314
##
## Coefficients:
                             Estimate Std. Error t value Pr(>|t|)
##
                                                    -0.48
## (Intercept)
                            -3.26e-01
                                         6.79e-01
                                                            0.6348
## literacy rate
                             1.93e-01
                                        2.23e-01
                                                     0.87
                                                            0.3933
## gdp_per_capita
                             5.03e-06
                                        1.63e-06
                                                     3.08
                                                            0.0044 **
## median_age
                                        5.74e-03
                                                            0.1064
                             9.56e-03
                                                     1.66
                                                            0.9137
## suicide rate
                             3.37e-02
                                        3.09e-01
                                                     0.11
## unemployment rate
                            -1.37e-01
                                        2.06e-01
                                                    -0.66
                                                            0.5116
                                                    -0.49
                                                            0.6270
## population_per_sq_km
                            -4.18e-05
                                        8.52e-05
## male female ratio
                                        5.08e-01
                                                    -0.30
                                                            0.7658
                            -1.53e-01
## hpi
                            -3.95e-03
                                        2.51e-03
                                                    -1.58
                                                            0.1256
## percent_english_speakers 1.16e-01
                                         5.68e-02
                                                     2.05
                                                            0.0491 *
## co2_per_capita
                             1.28e-03
                                         3.20e-03
                                                     0.40
                                                            0.6923
## life_expectancy
                             7.58e-03
                                         5.98e-03
                                                            0.2145
                                                     1.27
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0951 on 30 degrees of freedom
## Multiple R-squared: 0.891, Adjusted R-squared:
## F-statistic: 22.2 on 11 and 30 DF, p-value: 1.83e-11
```

Becuase of this, I will now run a stepwise regression (bi-directional) in order to remove some of the variables which dont provide enough predictive power to the model. Here are the final results of the stepwise model.

```
## Start: AIC=-187.8
##
   penetration_rate ~ literacy_rate + gdp_per_capita + median_age +
       suicide rate + unemployment rate + population per sq km +
##
##
       male_female_ratio + hpi + percent_english_speakers + co2_per_capita +
##
       life_expectancy
##
                              Df Sum of Sq
                                              RSS AIC
##
## - suicide_rate
                               1
                                    0.0001 0.271 -190
## - male_female_ratio
                               1
                                    0.0008 0.272 -190
## - co2_per_capita
                               1
                                    0.0014 0.273 -190
## - population_per_sq_km
                               1
                                    0.0022 0.273 -190
## - unemployment rate
                               1
                                    0.0040 0.275 -189
```

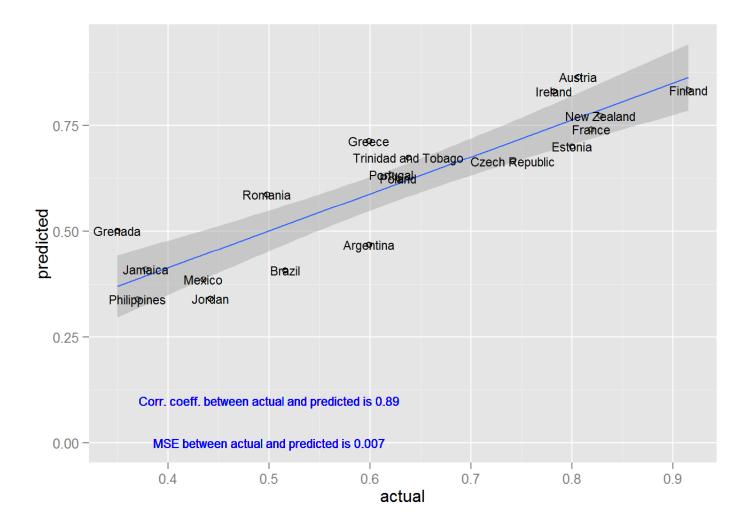
```
## - literacy_rate
                               1
                                    0.0068 0.278 -189
## <none>
                                           0.271 -188
## - life_expectancy
                               1
                                    0.0145 0.286 -188
## - hpi
                               1
                                    0.0224 0.294 -186
## - median age
                               1
                                    0.0250 0.296 -186
## - percent_english_speakers 1
                                    0.0380 0.309 -184
## - gdp per capita
                                    0.0858 0.357 -178
                               1
##
## Step: AIC=-189.8
##
   penetration rate ~ literacy rate + gdp per capita + median age +
##
       unemployment rate + population per sq km + male female ratio +
       hpi + percent_english_speakers + co2_per_capita + life_expectancy
##
##
                              Df Sum of Sq
                                             RSS AIC
##
## - male_female_ratio
                                    0.0010 0.272 -192
## - co2_per_capita
                                    0.0013 0.273 -192
                               1
## - population_per_sq_km
                                    0.0036 0.275 -191
                               1
## - unemployment_rate
                               1
                                    0.0053 0.277 -191
## - literacy_rate
                               1
                                    0.0068 0.278 -191
## <none>
                                           0.271 -190
## - life expectancy
                                    0.0186 0.290 -189
                               1
## - hpi
                                    0.0232 0.294 -188
                               1
## + suicide rate
                               1
                                    0.0001 0.271 -188
## - median age
                                    0.0343 0.305 -187
                               1
## - percent english speakers 1
                                    0.0401 0.311 -186
## - gdp per capita
                               1
                                    0.0860 0.357 -180
##
## Step: AIC=-191.6
   penetration_rate ~ literacy_rate + gdp_per_capita + median_age +
       unemployment_rate + population_per_sq_km + hpi + percent_english_speakers +
##
##
       co2_per_capita + life_expectancy
##
##
                              Df Sum of Sq
                                             RSS AIC
## - co2_per_capita
                               1
                                    0.0012 0.273 -194
## - population_per_sq_km
                               1
                                    0.0040 0.276 -193
## - unemployment rate
                                    0.0045 0.277 -193
                               1
## - literacy_rate
                                    0.0116 0.284 -192
                               1
                                           0.272 -192
## <none>
## - life expectancy
                                    0.0177 0.290 -191
                               1
## - hpi
                               1
                                    0.0238 0.296 -190
## + male female ratio
                               1
                                    0.0010 0.271 -190
## + suicide rate
                               1
                                    0.0003 0.272 -190
## - percent_english_speakers 1
                                    0.0393 0.311 -188
## - median_age
                                    0.0578 0.330 -186
                               1
## - gdp_per_capita
                               1
                                    0.0855 0.358 -182
##
## Step: AIC=-193.5
```

```
penetration_rate ~ literacy_rate + gdp_per_capita + median_age +
##
       unemployment_rate + population_per_sq_km + hpi + percent_english_speakers +
##
       life_expectancy
##
##
                              Df Sum of Sq
                                              RSS AIC
                                    0.0043 0.278 -195
##
  population_per_sq_km
                               1
## - unemployment rate
                                     0.0063 0.280 -194
                               1
                                            0.273 -194
## <none>
## - literacy rate
                                     0.0135 0.287 -193
                               1
## - life expectancy
                                     0.0171 0.290 -193
                               1
## - hpi
                               1
                                     0.0231 0.296 -192
## + co2_per_capita
                               1
                                     0.0012 0.272 -192
## + male female ratio
                               1
                                     0.0008 0.273 -192
## + suicide_rate
                                    0.0001 0.273 -192
                               1
## - percent_english_speakers 1
                                    0.0454 0.319 -189
## - median_age
                               1
                                    0.0599 0.333 -187
## - gdp_per_capita
                               1
                                    0.1303 0.404 -179
##
## Step: AIC=-194.8
##
   penetration_rate ~ literacy_rate + gdp_per_capita + median_age +
       unemployment_rate + hpi + percent_english_speakers + life_expectancy
##
##
##
                              Df Sum of Sq
                                              RSS AIC
                                     0.0085 0.286 -196
## - unemployment rate
                               1
                                            0.278 -195
## <none>
## - literacy rate
                               1
                                     0.0144 0.292 -195
## - life expectancy
                               1
                                     0.0204 0.298 -194
## + population_per_sq_km
                               1
                                     0.0043 0.273 -194
## + suicide_rate
                                    0.0017 0.276 -193
## + co2_per_capita
                                     0.0015 0.276 -193
                               1
## + male_female_ratio
                                     0.0012 0.276 -193
                               1
## - hpi
                               1
                                    0.0394 0.317 -191
## - percent_english_speakers
                                    0.0412 0.319 -191
                               1
## - median_age
                                    0.0562 0.334 -189
                               1
## - gdp_per_capita
                               1
                                    0.1360 0.414 -180
##
## Step: AIC=-195.5
   penetration_rate ~ literacy_rate + gdp_per_capita + median_age +
       hpi + percent english speakers + life expectancy
##
##
                              Df Sum of Sq
##
                                              RSS AIC
## <none>
                                            0.286 -196
## - literacy_rate
                                     0.0158 0.302 -195
                               1
## + unemployment_rate
                                    0.0085 0.278 -195
                               1
## + population_per_sq_km
                               1
                                    0.0065 0.280 -194
## + suicide_rate
                               1
                                    0.0049 0.281 -194
## + co2_per_capita
                                    0.0040 0.282 -194
                               1
```

```
## - life_expectancy
                                     0.0282 0.314 -194
                                1
## + male_female_ratio
                                1
                                     0.0000 0.286 -194
## - hpi
                                1
                                     0.0310 0.317 -193
## - percent_english_speakers
                                1
                                     0.0365 0.323 -192
## - median age
                                1
                                     0.0656 0.352 -189
## - gdp_per_capita
                                     0.1378 0.424 -181
                                1
```

```
##
## Call:
  lm(formula = penetration_rate ~ literacy_rate + gdp_per_capita +
      median_age + hpi + percent_english_speakers + life_expectancy,
##
      data = training_set)
##
##
## Residuals:
       Min
                  1Q
                      Median
                                    3Q
##
                                           Max
  -0.17757 -0.05220 -0.00476 0.05962 0.17201
##
##
## Coefficients:
##
                            Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                                  -2.47 0.01869 *
                            -5.78e-01
                                       2.34e-01
## literacy rate
                            2.58e-01
                                       1.86e-01
                                                   1.39 0.17349
## gdp_per_capita
                            5.36e-06
                                       1.31e-06
                                                   4.11 0.00023 ***
## median_age
                            1.05e-02
                                       3.71e-03
                                                   2.83 0.00761 **
                                                  -1.95 0.05962 .
## hpi
                            -3.66e-03
                                       1.88e-03
## percent_english_speakers 1.01e-01
                                                   2.11 0.04169 *
                                       4.80e-02
## life_expectancy
                            7.41e-03
                                       3.99e-03
                                                    1.86 0.07149 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.0904 on 35 degrees of freedom
## Multiple R-squared: 0.885, Adjusted R-squared: 0.865
## F-statistic: 44.8 on 6 and 35 DF, p-value: 5.48e-15
```

Using the final model, I will now apply the model estimates to the test set in order to see how accurate I predicted Internet Penetration. Here I have plotted the actual internet penetration rates versus the predicted rates by the model. As you can see, the model predicts internet pentration extremely well and most observations fall within the confidence interval.



Conclusion

We now see that we can use predictive features to understand internet penetration rates in various countries. Now it is still unsure as to whether the features are a cause to internet penetration or vice versa, but indeed a relationship exists. And understanding the relationship is the first step to making the world more open and connected.