01 dnn construction

December 3, 2023

1 Deep Neural Network - Construction

In the last assignment, you trained a 2-layer Neural Network with a single hidden layer. In this assignment, you will build a deep neural network with an arbitrary number of hidden layers.

- In this notebook, you'll implement all the functions required to build a deep neural network.
- For the next exercise, you'll use these functions to build a deep neural network for image classification.

By the end of this assignment, you'll be able to:

- Use non-linear units like ReLU to improve your model
- Build a deeper neural network (with more than 1 hidden layer)
- Implement an easy-to-use neural network class

Notation: - Superscript [l] denotes a quantity associated with the l^{th} layer. - Example: $a^{[L]}$ is the L^{th} layer activation. $W^{[L]}$ and $b^{[L]}$ are the L^{th} layer parameters. - Superscript (i) denotes a quantity associated with the i^{th} example. - Example: $x^{(i)}$ is the i^{th} training example. - Lowerscript i denotes the i^{th} entry of a vector. - Example: $a_i^{[l]}$ denotes the i^{th} entry of the l^{th} layer's activations).

1.1 Table of Contents

- 1 Packages
- 2 Outline
- 3 Initialization
 - 3.1 2-layer Neural Network
 - * Exercise 1 initialize parameters
 - 3.2 L-layer Neural Network
 - * Exercise 2 initialize parameters deep
- 4 Forward Propagation Module
 - -4.1 Linear Forward
 - * Exercise 3 linear forward
 - 4.2 Linear-Activation Forward
 - * Exercise 4 linear_activation_forward
 - 4.3 L-Layer Model
 - * Exercise 5 L model forward
- 5 Cost Function
 - Exercise 6 compute cost
- 6 Backward Propagation Module
 - 6.1 Linear Backward

```
* Exercise 7 - linear_backward
```

- 6.2 Linear-Activation Backward
 - * Exercise 8 linear activation backward
- 6.3 L-Model Backward
 - * Exercise 9 L model backward
- 6.4 Update Parameters
 - * Exercise 10 update_parameters

1 - Packages

First, import all the packages you'll need during this assignment.

- numpy is the main package for scientific computing with Python.
- matplotlib is a library to plot graphs in Python.
- dnn_utils provides some necessary functions for this notebook.
- testCases provides some test cases to assess the correctness of your functions
- np.random.seed(1) is used to keep all the random function calls consistent. It helps grade your work. Please don't change the seed.

The autoreload extension is already loaded. To reload it, use: %reload_ext autoreload

```
\#\# 2 - Outline
```

To build the neural network, you'll be implementing several "helper functions." These helper functions will be used in the next assignment to build a two-layer neural network and an L-layer neural network.

Each small helper function will have detailed instructions to walk you through the necessary steps. Here's an outline of the steps in this assignment:

- Initialize the parameters for a two-layer network and for an L-layer neural network
- Implement the forward propagation module (shown in purple in the figure below)
 - Complete the LINEAR part of a layer's forward propagation step (resulting in $\mathbb{Z}^{[l]}$).
 - The ACTIVATION function is provided for you (relu/sigmoid)

- Combine the previous two steps into a new [LINEAR->ACTIVATION] forward function.
- Stack the [LINEAR->RELU] forward function L-1 time (for layers 1 through L-1) and add a [LINEAR->SIGMOID] at the end (for the final layer L). This gives you a new L model forward function.
- Compute the loss
- Implement the backward propagation module (denoted in red in the figure below)
 - Complete the LINEAR part of a layer's backward propagation step
 - The gradient of the ACTIVATION function is provided for you(relu_backward/sigmoid_backward)
 - Combine the previous two steps into a new [LINEAR->ACTIVATION] backward function
 - Stack [LINEAR->RELU] backward L-1 times and add [LINEAR->SIGMOID] backward in a new L model backward function
- Finally, update the parameters

Figure 1

Note:

For every forward function, there is a corresponding backward function. This is why at every step of your forward module you will be storing some values in a cache. These cached values are useful for computing gradients.

In the backpropagation module, you can use the cache to calculate the gradients.

```
\#\# 3 - Initialization
```

Write two helper functions to initialize the parameters for your model. The first function will be used to initialize parameters for a two layer model. The second one generalizes this initialization process to L layers.

```
### 3.1 - 2-layer Neural Network
```

Exercise 1 - initialize_parameters

Create and initialize the parameters of the 2-layer neural network.

Instructions:

- The model's structure is: $LINEAR \rightarrow RELU \rightarrow LINEAR \rightarrow SIGMOID$.
- Use this random initialization for the weight matrices: np.random.randn(d0, d1, ..., dn)
 - * 0.01 with the correct shape. The documentation for np.random.randn
- Use zero initialization for the biases: np.zeros(shape). The documentation for np.zeros

```
[21]: # GRADED FUNCTION: initialize_parameters

def initialize_parameters(n_x, n_h, n_y):
    """

Argument:
    n_x -- size of the input layer
    n_h -- size of the hidden layer
    n_y -- size of the output layer
```

```
Returns:
          parameters -- python dictionary containing your parameters:
                          W1 -- weight matrix of shape (n_h, n_x)
                          b1 -- bias vector of shape (n_h, 1)
                          W2 -- weight matrix of shape (n_y, n_h)
                          b2 -- bias vector of shape (n_y, 1)
          11 11 11
          np.random.seed(1)
          # YOUR CODE STARTS HERE
          W1 = np.random.randn(n_h, n_x) * 0.01
          b1 = np.zeros((n_h, 1))
          W2 = np.random.randn(n_y, n_h) * 0.01
          b2 = np.zeros((n_y, 1))
          # YOUR CODE ENDS HERE
          parameters = {"W1": W1,
                        "b1": b1,
                        "W2": W2,
                        "b2": b2}
          return parameters
[22]: parameters = initialize_parameters(3,2,1)
      print("W1 = " + str(parameters["W1"]))
      print("b1 = " + str(parameters["b1"]))
      print("W2 = " + str(parameters["W2"]))
      print("b2 = " + str(parameters["b2"]))
      initialize_parameters_test_1(initialize_parameters)
     W1 = [[0.01624345 - 0.00611756 - 0.00528172]]
      [-0.01072969 0.00865408 -0.02301539]]
     b1 = [[0.]]
      [0.1]
     W2 = [[0.01744812 -0.00761207]]
     b2 = [[0.]]
      All tests passed.
     Expected output
     W1 = [[ 0.01624345 -0.00611756 -0.00528172]
      [-0.01072969 0.00865408 -0.02301539]]
     b1 = [[0.]]
      [0.]]
```

```
W2 = [[ 0.01744812 -0.00761207]]
b2 = [[0.]]
```

###3.2 - L-layer Neural Network

The initialization for a deeper L-layer neural network is more complicated because there are many more weight matrices and bias vectors. When completing the initialize_parameters_deep function, you should make sure that your dimensions match between each layer. Recall that $n^{[l]}$ is the number of units in layer l. For example, if the size of your input X is (12288, 209) (with m = 209 examples) then:

```
Shape of W
Shape of b
Activation
Shape of Activation
Layer 1
(n^{[1]}, 12288)
(n^{[1]},1)
Z^{[1]} = W^{[1]} X + b^{[1]} 
(n^{[1]}, 209)
Layer 2
(n^{[2]}, n^{[1]})
(n^{[2]}, 1)
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
(n^{[2]}, 209)
:
:
Layer L-1
(n^{[L-1]}, n^{[L-2]})
(n^{[L-1]}, 1)
Z^{[L-1]} = W^{[L-1]}A^{[L-2]} + b^{[L-1]}
(n^{[L-1]}, 209)
Layer L
```

 $(n^{[L]}, n^{[L-1]})$

$$\begin{split} &(n^{[L]},1)\\ &Z^{[L]} = W^{[L]}A^{[L-1]} + b^{[L]}\\ &(n^{[L]},209) \end{split}$$

Remember that when you compute WX + b in python, it carries out broadcasting. For example, if:

$$W = \begin{bmatrix} w_{00} & w_{01} & w_{02} \\ w_{10} & w_{11} & w_{12} \\ w_{20} & w_{21} & w_{22} \end{bmatrix} \quad X = \begin{bmatrix} x_{00} & x_{01} & x_{02} \\ x_{10} & x_{11} & x_{12} \\ x_{20} & x_{21} & x_{22} \end{bmatrix} \quad b = \begin{bmatrix} b_0 \\ b_1 \\ b_2 \end{bmatrix}$$
(2)

Then WX + b will be:

$$WX + b = \begin{bmatrix} (w_{00}x_{00} + w_{01}x_{10} + w_{02}x_{20}) + b_0 & (w_{00}x_{01} + w_{01}x_{11} + w_{02}x_{21}) + b_0 & \cdots \\ (w_{10}x_{00} + w_{11}x_{10} + w_{12}x_{20}) + b_1 & (w_{10}x_{01} + w_{11}x_{11} + w_{12}x_{21}) + b_1 & \cdots \\ (w_{20}x_{00} + w_{21}x_{10} + w_{22}x_{20}) + b_2 & (w_{20}x_{01} + w_{21}x_{11} + w_{22}x_{21}) + b_2 & \cdots \end{bmatrix}$$
(3)

Exercise 2 - initialize_parameters_deep

Implement initialization for an L-layer Neural Network.

Instructions: - The model's structure is [LINEAR -> RELU] \$ \times \$ (L-1) -> LINEAR -> SIGMOID. I.e., it has L-1 layers using a ReLU activation function followed by an output layer with a sigmoid activation function. - Use random initialization for the weight matrices. Use np.random.randn(d0, d1, ..., dn) * 0.01. - Use zeros initialization for the biases. Use np.zeros(shape). - You'll store $n^{[l]}$, the number of units in different layers, in a variable layer_dims. For example, the layer_dims for last week's Planar Data classification model would have been [2,4,1]: There were two inputs, one hidden layer with 4 hidden units, and an output layer with 1 output unit. This means W1's shape was (4,2), b1 was (4,1), W2 was (1,4) and b2 was (1,1). In this exercise, you will generalize this to L layers. - Here is the implementation for L=1 (one layer neural network). It should inspire you to implement the general case (L-layer neural network).

```
if L == 1:
    parameters["W" + str(L)] = np.random.randn(layer_dims[1], layer_dims[0]) * 0.01
    parameters["b" + str(L)] = np.zeros((layer_dims[1], 1))
```

```
[23]: # GRADED FUNCTION: initialize_parameters_deep

def initialize_parameters_deep(layer_dims):
    """

    Arguments:
    layer_dims -- python array (list) containing the dimensions of each layer_
    in our network

Returns:
    parameters -- python dictionary containing your parameters "W1", "b1", ..., ...
    → "WL", "bL":
```

```
Wl -- weight matrix of shape (layer_dims[l],_
       \hookrightarrow layer\_dims[l-1])
                           bl -- bias vector of shape (layer_dims[l], 1)
          11 11 11
          np.random.seed(3)
          parameters = {}
          L = len(layer dims) # number of layers in the network
          for 1 in range(1, L):
              # YOUR CODE STARTS HERE
              parameters['W' + str(1)] = np.random.randn(layer_dims[1], layer_dims[1]
       →- 1]) * 0.01
              parameters['b' + str(1)] = np.zeros((layer_dims[1], 1))
              # YOUR CODE ENDS HERE
              assert(parameters['W' + str(l)].shape == (layer_dims[l], layer_dims[l -__
       →1]))
              assert(parameters['b' + str(l)].shape == (layer_dims[l], 1))
          return parameters
[24]: parameters = initialize_parameters_deep([5,4,3])
      print("W1 = " + str(parameters["W1"]))
      print("b1 = " + str(parameters["b1"]))
      print("W2 = " + str(parameters["W2"]))
      print("b2 = " + str(parameters["b2"]))
      initialize_parameters_deep_test_1(initialize_parameters_deep)
     W1 = [[ 0.01788628 \ 0.0043651 ]
                                      0.00096497 -0.01863493 -0.00277388]
      [-0.00354759 -0.00082741 -0.00627001 -0.00043818 -0.00477218]
      [-0.01313865 \quad 0.00884622 \quad 0.00881318 \quad 0.01709573 \quad 0.00050034]
      [-0.00404677 -0.0054536 -0.01546477 0.00982367 -0.01101068]]
     b1 = [[0.]]
      [0.]
      [0.]
      [0.]]
     W2 = [[-0.01185047 -0.0020565 0.01486148 0.00236716]]
      [-0.01023785 -0.00712993 0.00625245 -0.00160513]
      [-0.00768836 -0.00230031 0.00745056 0.01976111]]
     b2 = [[0.]]
```

```
[0.]
[0.]]
All tests passed.
```

Expected output

```
W1 = [[ 0.01788628 \ 0.0043651 ]
                                0.00096497 -0.01863493 -0.00277388]
 [-0.00354759 -0.00082741 -0.00627001 -0.00043818 -0.00477218]
 [-0.01313865 0.00884622 0.00881318 0.01709573 0.00050034]
 [-0.00404677 -0.0054536 -0.01546477 0.00982367 -0.01101068]
b1 = [[0.]]
 [0.]
 [0.]
 [0.]]
W2 = [[-0.01185047 -0.0020565]]
                                0.01486148 0.00236716]
 [-0.01023785 -0.00712993 0.00625245 -0.00160513]
 [-0.00768836 -0.00230031 0.00745056 0.01976111]]
b2 = [[0.]]
 [0.]
 [0.]]
```

4 - Forward Propagation Module

4.1 - Linear Forward

Now that you have initialized your parameters, you can do the forward propagation module. Start by implementing some basic functions that you can use again later when implementing the model. Complete these three functions in this order:

- LINEAR.
- LINEAR -> ACTIVATION where ACTIVATION will be either ReLU or Sigmoid.
- [LINEAR -> RELU] × (L-1) -> LINEAR -> SIGMOID (whole model)

The linear forward module (vectorized over all the examples) computes the following equations:

$$Z^{[l]} = W^{[l]}A^{[l-1]} + b^{[l]} (4)$$

where $A^{[0]} = X$.

Exercise 3 - linear_forward

Build the linear part of forward propagation.

Reminder: The mathematical representation of this unit is $Z^{[l]} = W^{[l]}A^{[l-1]} + b^{[l]}$. You may also find np.dot() useful. If your dimensions don't match, printing W.shape may help.

```
[25]: # GRADED FUNCTION: linear_forward

def linear_forward(A, W, b):
    """
    Implement the linear part of a layer's forward propagation.
```

```
Arguments:
  A -- activations from previous layer (or input data): (size of previous \Box
⇒layer, number of examples)
   W -- weights matrix: numpy array of shape (size of current layer, size of \Box
⇔previous layer)
   b -- bias vector, numpy array of shape (size of the current layer, 1)
  Returns:
  Z -- the input of the activation function, also called pre-activation \Box
\neg parameter
   cache -- a python tuple containing "A", "W" and "b" ; stored for computing _{\sqcup}
→ the backward pass efficiently
  # YOUR CODE STARTS HERE
  Z = np.dot(W, A) + b
  # YOUR CODE ENDS HERE
  cache = (A, W, b)
  return Z, cache
```

```
[26]: t_A, t_W, t_b = linear_forward_test_case()
t_Z, t_linear_cache = linear_forward(t_A, t_W, t_b)
print("Z = " + str(t_Z))

linear_forward_test(linear_forward)
```

```
Z = [[ 3.26295337 -1.23429987]]
All tests passed.
```

Expected output

```
Z = [[ 3.26295337 -1.23429987]]
```

4.2 - Linear-Activation Forward

In this notebook, you will use two activation functions:

• Sigmoid: $\sigma(Z) = \sigma(WA + b) = \frac{1}{1 + e^{-(WA + b)}}$. You've been provided with the sigmoid function which returns **two** items: the activation value "a" and a "cache" that contains "Z" (it's what we will feed in to the corresponding backward function). To use it you could just call:

A, activation_cache = sigmoid(Z)

• **ReLU**: The mathematical formula for ReLu is A = RELU(Z) = max(0, Z). You've been provided with the **relu** function. This function returns **two** items: the activation value "A" and a "cache" that contains "Z" (it's what you'll feed in to the corresponding backward function). To use it you could just call:

A, activation_cache = relu(Z)

For added convenience, you're going to group two functions (Linear and Activation) into one function (LINEAR->ACTIVATION). So, implement a function that does the LINEAR forward step and then, the ACTIVATION forward step.

```
### Exercise 4 - linear_activation_forward
```

Implement the forward propagation of the LINEAR->ACTIVATION layer. Mathematical relation is: $A^{[l]} = g(Z^{[l]}) = g(W^{[l]}A^{[l-1]} + b^{[l]})$ where the activation "g" can be sigmoid() or relu(). Use linear_forward() and the correct activation function.

```
[27]: # GRADED FUNCTION: linear_activation_forward
      def linear_activation_forward(A_prev, W, b, activation):
          Implement the forward propagation for the LINEAR->ACTIVATION layer
          Arguments:
          A_prev -- activations from previous layer (or input data): (size of \Box
       ⇒previous layer, number of examples)
          W -- weights matrix: numpy array of shape (size of current layer, size of \Box
       ⇔previous layer)
          b -- bias vector, numpy array of shape (size of the current layer, 1)
          activation -- the activation to be used in this layer, stored as a text_{\sqcup}
       ⇔string: "sigmoid" or "relu"
          Returns:
          A -- the output of the activation function, also called the post-activation \Box
       \hookrightarrow value
          cache -- a python tuple containing "linear_cache" and "activation_cache";
                    stored for computing the backward pass efficiently
          11 11 11
          if activation == "sigmoid":
              # YOUR CODE STARTS HERE
              Z, linear_cache = linear_forward(A_prev, W, b)
              A, activation_cache = sigmoid(Z)
               # YOUR CODE ENDS HERE
          elif activation == "relu":
               # YOUR CODE STARTS HERE
              Z, linear_cache = linear_forward(A_prev, W, b)
              A, activation_cache = relu(Z)
```

```
# YOUR CODE ENDS HERE
cache = (linear_cache, activation_cache)
return A, cache
```

```
[28]: t_A_prev, t_W, t_b = linear_activation_forward_test_case()

t_A, t_linear_activation_cache = linear_activation_forward(t_A_prev, t_W, t_b, u_activation = "sigmoid")

print("With sigmoid: A = " + str(t_A))

t_A, t_linear_activation_cache = linear_activation_forward(t_A_prev, t_W, t_b, u_activation = "relu")

print("With ReLU: A = " + str(t_A))

linear_activation_forward_test(linear_activation_forward)
```

```
With sigmoid: A = [[0.96890023 0.11013289]]
With ReLU: A = [[3.43896131 0. ]]
All tests passed.
```

Expected output

```
With sigmoid: A = [[0.96890023 \ 0.11013289]]
With ReLU: A = [[3.43896131 \ 0. ]]
```

Note: In deep learning, the "[LINEAR->ACTIVATION]" computation is counted as a single layer in the neural network, not two layers.

```
### 4.3 - L-Layer Model
```

For even *more* convenience when implementing the L-layer Neural Net, you will need a function that replicates the previous one (linear_activation_forward with RELU) L-1 times, then follows that with one linear_activation_forward with SIGMOID.

```
Figure 2 : [LINEAR -> RELU] \times (L-1) -> LINEAR -> SIGMOID model
```

Exercise 5 - L_model_forward

Implement the forward propagation of the above model.

Instructions: In the code below, the variable AL will denote $A^{[L]} = \sigma(Z^{[L]}) = \sigma(W^{[L]}A^{[L-1]} + b^{[L]})$. (This is sometimes also called Yhat, i.e., this is \hat{Y} .)

Hints: - Use the functions you've previously written - Use a for loop to replicate [LINEAR->RELU] (L-1) times - Don't forget to keep track of the caches in the "caches" list. To add a new value c to a list, you can use list.append(c).

```
[29]: # GRADED FUNCTION: L_model_forward

def L_model_forward(X, parameters):
```

```
Implement forward propagation for the [LINEAR->RELU]*(L-1)->LINEAR->SIGMOID_{\sqcup}
\hookrightarrow computation
  Arguments:
  X -- data, numpy array of shape (input size, number of examples)
  parameters -- output of initialize_parameters_deep()
  Returns:
  AL -- activation value from the output (last) layer
   caches -- list of caches containing:
               every cache of linear_activation_forward() (there are L of \Box
\hookrightarrow them, indexed from 0 to L-1)
   11 11 11
  caches = []
  A = X
  L = len(parameters) // 2
                                              # number of layers in the neural
\rightarrownetwork
   # Implement [LINEAR \rightarrow RELU]*(L-1). Add "cache" to the "caches" list.
  # The for loop starts at 1 because layer 0 is the input
  for l in range(1, L):
      A_prev = A
      # YOUR CODE STARTS HERE
       A, cache = linear_activation_forward(A_prev, parameters['W' + str(1)],
→parameters['b' + str(l)], "relu")
       caches.append(cache)
       # YOUR CODE ENDS HERE
  # Implement LINEAR -> SIGMOID. Add "cache" to the "caches" list.
  # YOUR CODE STARTS HERE
  AL, cache = linear_activation_forward(A, parameters['W' + str(L)],_

→parameters['b' + str(L)], "sigmoid")
  caches.append(cache)
  # YOUR CODE ENDS HERE
  return AL, caches
```

```
[30]: t_X, t_parameters = L_model_forward_test_case_2hidden()
    t_AL, t_caches = L_model_forward(t_X, t_parameters)

print("AL = " + str(t_AL))

L_model_forward_test(L_model_forward)
```

 $AL = [[0.03921668 \ 0.70498921 \ 0.19734387 \ 0.04728177]]$ All tests passed.

Expected output

```
AL = [[0.03921668 \ 0.70498921 \ 0.19734387 \ 0.04728177]]
```

Great! - You've completed a full forward propagation implementation that takes the input X and outputs a row vector $A^{[L]}$ containing your predictions. It also records all intermediate values in "caches". Using $A^{[L]}$, you can compute the cost of your predictions.

5 - Cost Function

Now you can implement forward and backward propagation. Compute the cost in order to check whether your model is actually learning.

Exercise 6 - compute cost Compute the cross-entropy cost J, using the following formula:

$$-\frac{1}{m}\sum_{i=1}^{m} (y^{(i)}\log\left(a^{[L](i)}\right) + (1 - y^{(i)})\log\left(1 - a^{[L](i)}\right)) \tag{7}$$

```
[31]: # GRADED FUNCTION: compute_cost

def compute_cost(AL, Y):
    """
    Implement the cost function defined by equation (7).

Arguments:
    AL -- probability vector corresponding to your label predictions, shape (1, □ → number of examples)
    Y -- true "label" vector (for example: containing 0 if non-cat, 1 if cat), □ → shape (1, number of examples)

Returns:
    cost -- cross-entropy cost
    """

m = Y.shape[1]

# Compute loss from aL and y.

# YOUR CODE STARTS HERE
```

```
cost = - (1/m) * np.sum(Y * np.log(AL) + (1 - Y) * np.log(1 - AL))

# YOUR CODE ENDS HERE

cost = np.squeeze(cost) # To make sure your cost's shape is what we
→expect (e.g. this turns [[17]] into 17).

return cost
```

```
[32]: t_Y, t_AL = compute_cost_test_case()
t_cost = compute_cost(t_AL, t_Y)

print("Cost: " + str(t_cost))

compute_cost_test(compute_cost)
```

Cost: 0.2797765635793422 All tests passed.

Expected Output:

cost

0.2797765635793422

6 - Backward Propagation Module

Just as you did for the forward propagation, you'll implement helper functions for backpropagation. Remember that backpropagation is used to calculate the gradient of the loss function with respect to the parameters.

Reminder:

Figure 3: Forward and Backward propagation for LINEAR->RELU->LINEAR->SIGMOID The purple blocks represent the forward propagation, and the red blocks represent the backward propagation.

Now, similarly to forward propagation, you're going to build the backward propagation in three steps: 1. LINEAR backward 2. LINEAR -> ACTIVATION backward where ACTIVATION computes the derivative of either the ReLU or sigmoid activation 3. [LINEAR -> RELU] \times (L-1) -> LINEAR -> SIGMOID backward (whole model)

For the next exercise, recall that:

- b is a matrix(np.ndarray) with 1 column and n rows, i.e: b = [[1.0], [2.0]] (remember that b is a constant)
- np.sum performs a sum over the elements of an ndarray
- axis=1 or axis=0 specify if the sum is carried out by rows or by columns, respectively
- keepdims specifies if the original dimensions of the matrix must be kept.
- Look at the following example to clarify:

```
[33]: A = np.array([[1, 2], [3, 4]])

print('axis=1 and keepdims=True')
print(np.sum(A, axis=1, keepdims=True))
print('axis=1 and keepdims=False')
print(np.sum(A, axis=1, keepdims=False))
print('axis=0 and keepdims=True')
print(np.sum(A, axis=0, keepdims=True))
print('axis=0 and keepdims=False')
print(np.sum(A, axis=0, keepdims=False))
```

axis=1 and keepdims=True
[[3]
[7]]
axis=1 and keepdims=False
[3 7]
axis=0 and keepdims=True
[[4 6]]
axis=0 and keepdims=False
[4 6]

6.1 - Linear Backward

For layer l, the linear part is: $Z^{[l]} = W^{[l]}A^{[l-1]} + b^{[l]}$ (followed by an activation).

Suppose you have already calculated the derivative $dZ^{[l]} = \frac{\partial \mathcal{L}}{\partial Z^{[l]}}$. You want to get $(dW^{[l]}, db^{[l]}, dA^{[l-1]})$.

Figure 4

The three outputs $(dW^{[l]}, db^{[l]}, dA^{[l-1]})$ are computed using the input $dZ^{[l]}$.

Here are the formulas you need:

$$dW^{[l]} = \frac{\partial \mathcal{J}}{\partial W^{[l]}} = \frac{1}{m} dZ^{[l]} A^{[l-1]T}$$
(8)

$$db^{[l]} = \frac{\partial \mathcal{J}}{\partial b^{[l]}} = \frac{1}{m} \sum_{i=1}^{m} dZ^{[l](i)}$$

$$\tag{9}$$

$$dA^{[l-1]} = \frac{\partial \mathcal{L}}{\partial A^{[l-1]}} = W^{[l]T} dZ^{[l]}$$

$$\tag{10}$$

 $A^{[l-1]T}$ is the transpose of $A^{[l-1]}$.

Exercise 7 - linear_backward

Use the 3 formulas above to implement linear_backward().

Hint:

• In numpy you can get the transpose of an ndarray A using A.T or A.transpose()

```
[34]: # GRADED FUNCTION: linear_backward
      def linear_backward(dZ, cache):
           Implement the linear portion of backward propagation for a single layer ...
        \hookrightarrow (layer 1)
          Arguments:
           dZ -- Gradient of the cost with respect to the linear output (of current<sub>\subset</sub>
        \hookrightarrow layer l)
           cache -- tuple of values (A_prev, W, b) coming from the forward propagation_{\sqcup}
        in the current layer
          Returns:
          dA\_prev -- Gradient of the cost with respect to the activation (of the \sqcup
        \hookrightarrowprevious layer l-1), same shape as A_prev
           dW -- Gradient of the cost with respect to W (current layer 1), same shape_{\sqcup}
           db -- Gradient of the cost with respect to b (current layer l), same shape_{\sqcup}
       \hookrightarrow as b
           11 11 11
          A_{prev}, W, b = cache
          m = A_prev.shape[1]
          # YOUR CODE STARTS HERE
          dW = (1/m) * np.dot(dZ, A_prev.T)
          db = (1/m) * np.sum(dZ, axis=1, keepdims=True)
          dA_prev = np.dot(W.T, dZ)
          # YOUR CODE ENDS HERE
          return dA_prev, dW, db
[35]: t_dZ, t_linear_cache = linear_backward_test_case()
      t_dA_prev, t_dW, t_db = linear_backward(t_dZ, t_linear_cache)
      print("dA_prev: " + str(t_dA_prev))
      print("dW: " + str(t_dW))
      print("db: " + str(t_db))
      linear_backward_test(linear_backward)
     dA_prev: [[-1.15171336 0.06718465 -0.3204696
                                                          2.09812712]
       [ 0.60345879 -3.72508701 5.81700741 -3.84326836]
       [-0.4319552 -1.30987417 1.72354705 0.05070578]
       [-0.38981415 0.60811244 -1.25938424 1.47191593]
```

```
[-2.52214926 2.67882552 -0.67947465 1.48119548]]
dW: [[ 0.07313866 -0.0976715 -0.87585828 0.73763362 0.00785716]
  [ 0.85508818 0.37530413 -0.59912655 0.71278189 -0.58931808]
  [ 0.97913304 -0.24376494 -0.08839671 0.55151192 -0.10290907]]
db: [[-0.14713786]
  [-0.11313155]
  [-0.13209101]]
All tests passed.
```

Expected Output:

```
dA_prev: [[-1.15171336  0.06718465 -0.3204696  2.09812712]
  [ 0.60345879 -3.72508701  5.81700741 -3.84326836]
  [-0.4319552  -1.30987417  1.72354705  0.05070578]
  [-0.38981415  0.60811244 -1.25938424  1.47191593]
  [-2.52214926  2.67882552 -0.67947465  1.48119548]]
dW: [[ 0.07313866 -0.0976715  -0.87585828  0.73763362  0.00785716]
  [ 0.85508818  0.37530413 -0.59912655  0.71278189 -0.58931808]
  [ 0.97913304 -0.24376494 -0.08839671  0.55151192 -0.10290907]]
db: [[-0.14713786]
  [-0.11313155]
  [-0.13209101]]
```

6.2 - Linear-Activation Backward

Next, you will create a function that merges the two helper functions: linear_backward and the backward step for the activation linear_activation_backward.

To help you implement linear_activation_backward, two backward functions have been provided: - sigmoid_backward: Implements the backward propagation for SIGMOID unit. You can call it as follows:

dZ = sigmoid_backward(dA, activation_cache)

• relu_backward: Implements the backward propagation for RELU unit. You can call it as follows:

dZ = relu_backward(dA, activation_cache)

If g(.) is the activation function, sigmoid_backward and relu_backward compute

$$dZ^{[l]} = dA^{[l]} * g'(Z^{[l]}). (11)$$

Exercise 8 - linear_activation_backward

Implement the backpropagation for the LINEAR->ACTIVATION layer.

```
[36]: # GRADED FUNCTION: linear_activation_backward

def linear_activation_backward(dA, cache, activation):
    """

Implement the backward propagation for the LINEAR->ACTIVATION layer.
```

```
Arguments:
          dA -- post-activation gradient for current layer l
          cache -- tuple of values (linear_cache, activation_cache) we store for_
       ⇔computing backward propagation efficiently
          activation -- the activation to be used in this layer, stored as a text_{\sqcup}
       ⇔string: "sigmoid" or "relu"
          Returns:
          dA\_prev -- Gradient of the cost with respect to the activation (of the \sqcup
       \negprevious layer l-1), same shape as A_prev
          dW -- Gradient of the cost with respect to W (current layer 1), same shape_{\sqcup}
          db -- Gradient of the cost with respect to b (current layer l), same shape_{\sqcup}
       \hookrightarrow as b
          linear_cache, activation_cache = cache
          if activation == "relu":
              # YOUR CODE STARTS HERE
              dZ = relu_backward(dA, activation_cache)
              dA_prev, dW, db = linear_backward(dZ, linear_cache)
              # YOUR CODE ENDS HERE
          elif activation == "sigmoid":
              # YOUR CODE STARTS HERE
              dZ = sigmoid_backward(dA, activation_cache)
              dA_prev, dW, db = linear_backward(dZ, linear_cache)
              # YOUR CODE ENDS HERE
          return dA_prev, dW, db
[37]: t_dAL, t_linear_activation_cache = linear_activation_backward_test_case()
      t_dA_prev, t_dW, t_db = linear_activation_backward(t_dAL,__
       ot_linear_activation_cache, activation = "sigmoid")
      print("With sigmoid: dA_prev = " + str(t_dA_prev))
      print("With sigmoid: dW = " + str(t dW))
      print("With sigmoid: db = " + str(t_db))
      t_dA_prev, t_dW, t_db = linear_activation_backward(t_dAL,__
       →t_linear_activation_cache, activation = "relu")
```

```
print("With relu: dA_prev = " + str(t_dA_prev))
print("With relu: dW = " + str(t_dW))
print("With relu: db = " + str(t_db))

linear_activation_backward_test(linear_activation_backward)
```

Expected output:

Now you will implement the backward function for the whole network!

Recall that when you implemented the $L_model_forward$ function, at each iteration, you stored a cache which contains (X,W,b, and z). In the back propagation module, you'll use those variables to compute the gradients. Therefore, in the $L_model_backward$ function, you'll iterate through all the hidden layers backward, starting from layer L. On each step, you will use the cached values for layer l to backpropagate through layer l. Figure 5 below shows the backward pass.

Figure 5: Backward pass

Initializing backpropagation:

6.3 - L-Model Backward

To backpropagate through this network, you know that the output is: $A^{[L]} = \sigma(Z^{[L]})$. Your code thus needs to compute $\mathtt{dAL} = \frac{\partial \mathcal{L}}{\partial A^{[L]}}$. To do so, use this formula (derived using calculus which, again, you don't need in-depth knowledge of!):

```
dAL = - (np.divide(Y, AL) - np.divide(1 - Y, 1 - AL)) # derivative of cost with respect to AL
```

You can then use this post-activation gradient dAL to keep going backward. As seen in Figure 5, you can now feed in dAL into the LINEAR->SIGMOID backward function you implemented (which

will use the cached values stored by the L_model_forward function).

After that, you will have to use a for loop to iterate through all the other layers using the LINEAR->RELU backward function. You should store each dA, dW, and db in the grads dictionary. To do so, use this formula:

$$grads["dW" + str(l)] = dW^{[l]}$$
(15)

For example, for l = 3 this would store $dW^{[l]}$ in grads["dW3"].

Exercise 9 - L $_{model}$ backward

Implement backpropagation for the $[LINEAR->RELU] \times (L-1) -> LINEAR -> SIGMOID$ model.

```
[38]: # GRADED FUNCTION: L model backward
      def L_model_backward(AL, Y, caches):
          Implement the backward propagation for the [LINEAR->RELU] * (L-1) -> LINEAR_{
m L}
       →-> SIGMOID group
          Arguments:
          AL -- probability vector, output of the forward propagation_
       \hookrightarrow (L_model_forward())
          Y -- true "label" vector (containing 0 if non-cat, 1 if cat)
          caches -- list of caches containing:
                       every cache of linear_activation_forward() with "relu" (it's_
       \neg caches[l], for l in range(L-1) i.e l = 0...L-2)
                       the cache of linear_activation_forward() with "sigmoid" (it's_
       \hookrightarrow caches [L-1])
          Returns:
          grads -- A dictionary with the gradients
                    grads["dA" + str(l)] = \dots
                    grads["dW" + str(l)] = \dots
                    grads["db" + str(l)] = \dots
           .....
          grads = {}
          L = len(caches) # the number of layers
          m = AL.shape[1]
          Y = Y.reshape(AL.shape) # after this line, Y is the same shape as AL
          # Initializing the backpropagation
          # YOUR CODE STARTS HERE
          dAL = - (np.divide(Y, AL) - np.divide(1 - Y, 1 - AL))
```

```
# YOUR CODE ENDS HERE
          # Lth layer (SIGMOID -> LINEAR) gradients. Inputs: "dAL, current_cache". __
       →Outputs: "grads["dAL-1"], grads["dWL"], grads["dbL"]
         # YOUR CODE STARTS HERE
         current_cache = caches[L - 1]
         grads["dA" + str(L-1)], grads["dW" + str(L)], grads["db" + str(L)] = _L
       Glinear_activation_backward(dAL, current_cache, activation = "sigmoid")
         # YOUR CODE ENDS HERE
         # Loop from l=L-2 to l=0
         for l in reversed(range(L-1)):
             # lth layer: (RELU -> LINEAR) gradients.
             # Inputs: "grads["dA" + str(l + 1)], current_cache". Outputs:
       \rightarrow "grads["dA" + str(l)] , grads["dW" + str(l + 1)] , grads["db" + str(l + 1)]
             # YOUR CODE STARTS HERE
             current cache = caches[1]
             dA_prev_temp, dW_temp, db_temp = linear_activation_backward(grads["dA"__
       grads["dA" + str(1)] = dA_prev_temp
             grads["dW" + str(1 + 1)] = dW_temp
             grads["db" + str(1 + 1)] = db_temp
             # YOUR CODE ENDS HERE
         return grads
[39]: t_AL, t_Y_assess, t_caches = L_model_backward_test_case()
     grads = L_model_backward(t_AL, t_Y_assess, t_caches)
     print("dA0 = " + str(grads['dA0']))
     print("dA1 = " + str(grads['dA1']))
     print("dW1 = " + str(grads['dW1']))
     print("dW2 = " + str(grads['dW2']))
     print("db1 = " + str(grads['db1']))
     print("db2 = " + str(grads['db2']))
     L_model_backward_test(L_model_backward)
     dAO = [[ 0.
                         0.522579017
      [ 0.
                  -0.3269206 ]
```

```
[ 0.
              -0.32070404]
 [ 0.
              -0.74079187]]
dA1 = [[ 0.12913162 -0.44014127]
 [-0.14175655 0.48317296]
 [ 0.01663708 -0.05670698]]
dW1 = [[0.41010002 \ 0.07807203 \ 0.13798444 \ 0.10502167]
                         0.
 [0.05283652 0.01005865 0.01777766 0.0135308 ]]
dW2 = [[-0.39202432 -0.13325855 -0.04601089]]
db1 = [[-0.22007063]]
 [ 0.
 [-0.02835349]]
db2 = [[0.15187861]]
All tests passed.
```

Expected output:

```
dAO = [[ 0.
                      0.52257901]
 [ 0.
              -0.3269206 ]
 [ 0.
              -0.32070404]
 ΓО.
              -0.74079187]]
dA1 = [[ 0.12913162 -0.44014127]
 [-0.14175655 0.48317296]
 [ 0.01663708 -0.05670698]]
dW1 = [[0.41010002 \ 0.07807203 \ 0.13798444 \ 0.10502167]
 ГО.
             0.
                         0.
                                     0.
 [0.05283652 0.01005865 0.01777766 0.0135308 ]]
dW2 = [[-0.39202432 -0.13325855 -0.04601089]]
db1 = [[-0.22007063]]
 [ 0.
 [-0.02835349]]
db2 = [[0.15187861]]
```

In this section, you'll update the parameters of the model, using gradient descent:

 $W^{[l]} = W^{[l]} - \alpha \ dW^{[l]} \tag{16}$

$$b^{[l]} = b^{[l]} - \alpha \ db^{[l]} \tag{17}$$

where α is the learning rate.

6.4 - Update Parameters

After computing the updated parameters, store them in the parameters dictionary.

Exercise 10 - update_parameters

Implement update_parameters() to update your parameters using gradient descent.

Instructions: Update parameters using gradient descent on every $W^{[l]}$ and $b^{[l]}$ for l = 1, 2, ..., L.

```
[40]: # GRADED FUNCTION: update_parameters
      def update_parameters(params, grads, learning_rate):
          Update parameters using gradient descent
          Arguments:
          params -- python dictionary containing your parameters
          grads -- python dictionary containing your gradients, output of __
       \hookrightarrow L model backward
          Returns:
          parameters -- python dictionary containing your updated parameters
                        parameters["W" + str(l)] = ...
                        parameters["b" + str(l)] = ...
          11 11 11
          parameters = params.copy()
          L = len(parameters) // 2 # number of layers in the neural network
          # Update rule for each parameter. Use a for loop.
          for l in range(L):
              # YOUR CODE STARTS HERE
              parameters["W" + str(1+1)] = parameters["W" + str(1+1)] - learning_rate_

→* grads["dW" + str(l+1)]

              parameters["b" + str(1+1)] = parameters["b" + str(1+1)] - learning_rate_u

→* grads["db" + str(l+1)]

              # YOUR CODE ENDS HERE
          return parameters
[41]: t_parameters, grads = update_parameters_test_case()
      t_parameters = update_parameters(t_parameters, grads, 0.1)
      print ("W1 = "+ str(t_parameters["W1"]))
      print ("b1 = "+ str(t parameters["b1"]))
      print ("W2 = "+ str(t_parameters["W2"]))
      print ("b2 = "+ str(t_parameters["b2"]))
      update_parameters_test(update_parameters)
     W1 = [[-0.59562069 -0.09991781 -2.14584584 1.82662008]
      [-1.76569676 -0.80627147 0.51115557 -1.18258802]
      [-1.0535704 -0.86128581 0.68284052 2.20374577]]
     b1 = [[-0.04659241]]
      [-1.28888275]
```

```
W2 = [[-0.55569196 0.0354055 1.32964895]]
b2 = [[-0.84610769]]
All tests passed.

Expected output:
W1 = [[-0.59562069 -0.09991781 -2.14584584 1.82662008]
[-1.76569676 -0.80627147 0.51115557 -1.18258802]
[-1.0535704 -0.86128581 0.68284052 2.20374577]]
b1 = [[-0.04659241]
[-1.28888275]
[ 0.53405496]]
W2 = [[-0.55569196 0.0354055 1.32964895]]
b2 = [[-0.84610769]]
```

1.1.1 Congratulations!

[0.53405496]]

You've just implemented all the functions required for building a deep neural network, including:

- Using non-linear units to improve your model
- Building a deeper neural network (with more than 1 hidden layer)
- Implementing an easy-to-use neural network class

This was a challenging assignment, but the next part of the assignment is easier...

In the next exercise, you'll put all these functions together to build two models:

- A two-layer neural network
- An L-layer neural network

You will in fact use these models to classify cat vs non-cat images...