

# Macroeconometrics

## Lecture 6   Macroeconometrics research themes

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Forecasting with Bayesian VARs

Assessing policy effects with Structural VARs

Trend and cycle analysis with Unobserved Component models

Forecasting with **Bayesian VARs**

# Forecasting with Bayesian VARs

## Baseline model: Vector Autoregression

$$y_t = A_1 y_{t-1} + \cdots + A_p y_{t-p} + \mu_0 + \epsilon_t$$

$$\epsilon_t | Y_{t-1} \sim iid(\mathbf{0}_N, \Sigma)$$

System modelling – all variables are endogenous

Dynamics – captures system dynamics of the variables

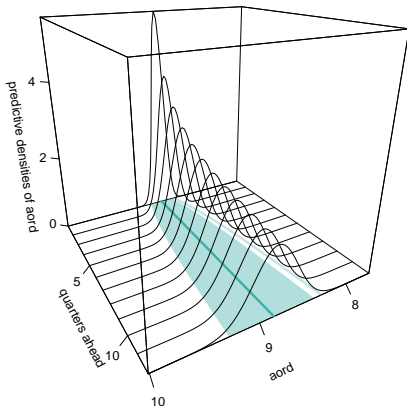
Forecasting – a go to model for predictive applications

Extensions capturing important data features improve forecasting precision

# Forecasting with Bayesian VARs

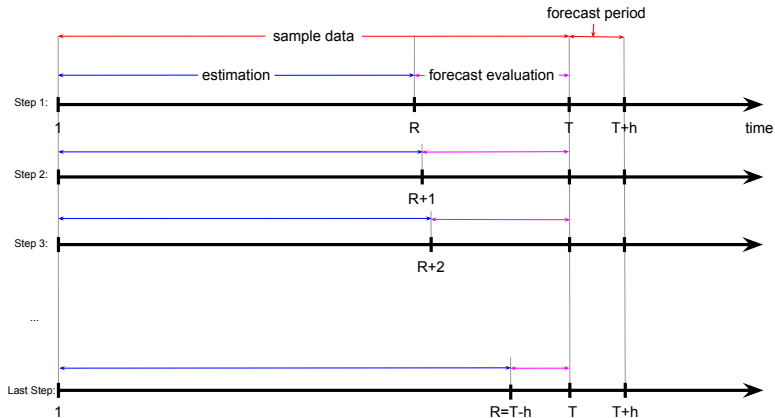
**Objective: Density forecasting performance evaluation**

$$p(y_{T+h} | Y_T)$$



# Forecasting with Bayesian VARs

## Method: Recursive forecasting exercise



# Forecasting with Bayesian VARs

## **Data set examples.**

Fat data of 117 quarterly macro variables for Australia

Bond yield curve modelling using daily/monthly interest rates

Small-open economy forecasting with a foreign sector

# Forecasting with Bayesian VARs

## **Potential model extensions.**

Common heteroskedasticity for all variables

Non-normal error term via gamma-scale mixtures

Estimated prior shrinkage of the Minnesota prior



Assessing policy effects with **Structural VARs**

# Assessing policy effects with Structural VARs

## Structural Vector Autoregressions.

$$y_t = A_1 y_{t-1} + \cdots + A_p y_{t-p} + \mu_0 + \epsilon_t$$

$$B\epsilon_t = u_t$$

$$u_t | Y_{t-1} \sim iid(\mathbf{0}_N, I_N)$$

Structural relationships are explicitly modelled

Economic theory informs identification of structural shocks

Dynamic causal effects can be estimated and interpreted

Policy decision-making is based on evidence provided by SVARs

# Assessing policy effects with Structural VARs

## **Objective: identification of a structural shock and its effects**

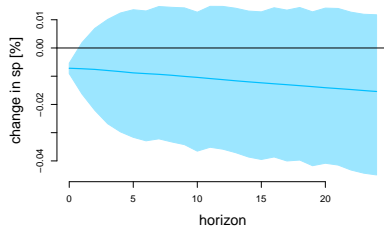
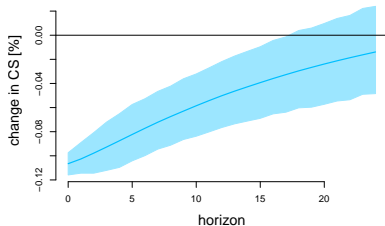
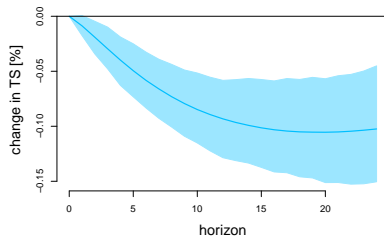
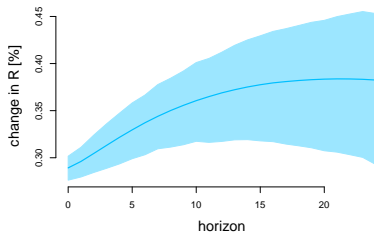
Identification via restrictions leading to fast estimation

Identification via sign restrictions that are less controversial

Identification via heteroskedasticity using data properties

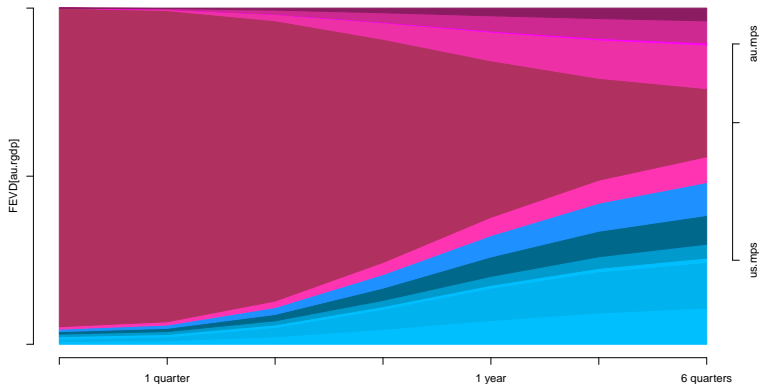
# Assessing policy effects with Structural VARs

## Method: impulse response analysis



# Assessing policy effects with Structural VARs

## Method: forecast error variance decomposition



Trend and cycle analysis with **UC models**

# Trend and cycle analysis with UC models

## Unobserved Component Models.

$$y_t = \tau_t + \epsilon_t$$

$$\tau_t = \mu + \tau_{t-1} + \eta_t$$

$$\epsilon_t = \alpha_1 \epsilon_{t-1} + \dots + \alpha_p \epsilon_{t-p} + e_t$$

$$\eta_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_\eta^2)$$

$$e_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_e^2)$$

Trend and cycle decomposition of a variable

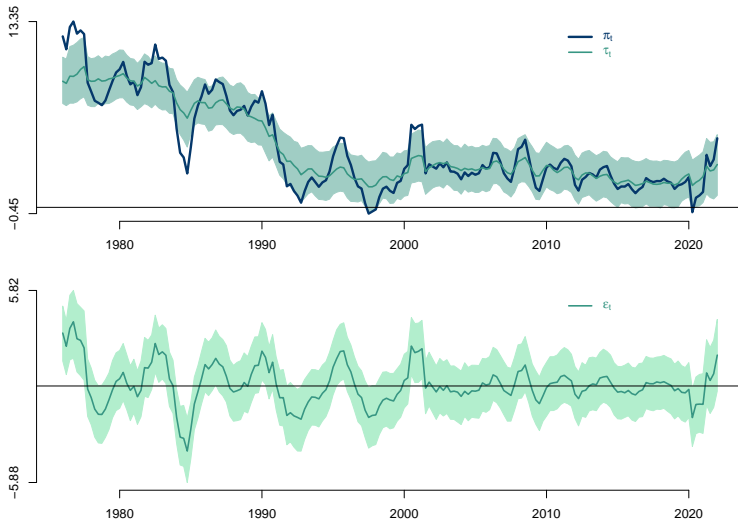
Long-run trend is highly-persistent

Oscillating cycle captures short-term dynamics

Inflation trend analysis and output gap estimation are the main applications

# Trend and cycle analysis with UC models

**Objective: inflation trend and cycle analysis.**





# Trend and cycle analysis with UC models

## Heteroskedastic Model.

$$y_t = \tau_t + \epsilon_t$$

$$\tau_t = \mu + \tau_{t-1} + \eta_t$$

$$\epsilon_t = \alpha_1 \epsilon_{t-1} + \cdots + \alpha_p \epsilon_{t-p} + e_t$$

$$\eta_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_{\eta.t}^2)$$

$$e_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_{e.t}^2)$$

# Trend and cycle analysis with UC models

## Time-varying trend.

$$y_t = \tau_t + \epsilon_t$$

$$\tau_t = \mu_t + \tau_{t-1} + \eta_t$$

$$\mu_t = \mu_{t-1} + m_t$$

$$\epsilon_t = \alpha_1 \epsilon_{t-1} + \cdots + \alpha_p \epsilon_{t-p} + e_t$$

$$\eta_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_\eta^2)$$

$$e_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_e^2)$$

$$m_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_m^2)$$

# Trend and cycle analysis with UC models

## Common factor.

$$y_{n,t} = \tau_t + \epsilon_{n,t}$$

$$n = 1, \dots, N$$

$$\tau_t = \mu + \tau_{t-1} + \eta_t$$

$$\epsilon_t = \alpha_1 \epsilon_{t-1} + \dots + \alpha_p \epsilon_{t-p} + e_t$$

$$\eta_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_\eta^2)$$

$$e_t | Y_{t-1} \sim iid \mathcal{N}(0, \sigma_e^2)$$

**The choice is yours!**