

Econometrics-2022-2023
Home assignment 3. Dummy Variables
To be submitted by November 27, 23:55

1. [30 marks] A researcher investigating regional variations in wages uses data on 1,000 individuals in a U.S. survey to fit the following regressions (standard errors in parentheses; *RSS* is residual sum of squares):

$$\hat{EARN} = -5.49 + 1.40S \quad \text{RSS} = 65.50$$

(2.00) (0.15)

$$\hat{EARN} = -5.43 + 1.34S - 0.26NC + 3.28NE + 1.29W \quad \text{RSS} = 64.14$$

(2.03) (0.15) (0.83) (0.97) (1.00)

where *EARN* is hourly earnings in U.S. \$, *S* is the number of years of schooling of the individual, and *NC* (north central), *NE* (north east) and *W* (west) are regional dummy variables for the residence of the individual (south is the reference category).

1.1. [10 marks] ☐ Explain how the dummy variables are defined here.

☐ Explain the meaning and the role of the coefficients.

☐ Represent the second equation graphically.

1.2. [10 marks] ☐ Do the significance tests for the coefficients of the dummy variables.

☐ Do a test of the explanatory power of the dummy variables as a group.

1.3. [10 marks] ☐ Suppose the researcher had taken the western region as the reference category. What differences would this have made to the second regression?

☐ Suppose that the researcher wished to investigate whether the impact of schooling on earnings was different in the four regions. How could this be done?

2. [20 marks] A researcher has observations on *EARN*, earnings measured in \$ per hour, *S*, years of schooling, and *ASVABC*, the score on a test of cognitive ability (here in %), for 2,868 individuals in the United States in 1994. She also defines dummy variables *MALE* and *UNION*. *MALE* is equal to one if the individual is male and 0 if she is female. *UNION* is equal to 1 if the individual belonged to a union in 1994, 0 otherwise. She runs the following regressions, whose results are summarized in the table below:

(1) a regression of the logarithm of earnings on *S*, *ASVABC*, and *MALE*, using the entire sample

(2) the same specification, for those individuals who belonged to a union

(3) the same specification, for those individuals who did not belong to a union

(4) the same specification with the dummy variable *UNION* added, for the entire sample.

The table gives the regression coefficients. Standard errors are given in parentheses, *RSS* is the residual sum of squares, and *n* is the number of observations in the regression. Dependent Var.: Logarithm of Hourly Earnings

	1: whole sample (2868)	2: union only (286)	3: non-union only (2582)	4: whole sample (2868)
<i>S</i>	0.066 (0.004)	0.028 (0.012)	0.070 (0.005)	0.066 (0.004)
<i>ASVABC</i>	0.013 (0.001)	0.011 (0.003)	0.013 (0.001)	0.013 (0.001)
<i>MALE</i>	0.214 (0.017)	0.286 (0.049)	0.199 (0.018)	0.209 (0.017)
<i>UNION</i>	-	-	-	0.189 (0.028)
<i>Constant</i>	0.819 (0.055)	1.545 (0.164)	0.750 (0.058)	0.803 (0.055)
<i>R</i> ² / <i>RSS</i>	0.249 / 588.3	0.195 / 43.7	0.260 / 522.5	0.261 / 579.7

2.1. [10 marks] Give an economic interpretation of the first equation.

2.2. [10 marks] ☐ Determine whether the earnings functions are different for union members and non-members

(i) using a Chow test

(ii) using a *t* test on the coefficient of the union dummy variable.

☐ Explain the relationship between these two approaches to testing for differences in the earnings functions for union and non-union workers. Is it possible that they might lead to different conclusions?

3. [50 marks] For your data set **ha03_data**__ explore whether earnings of respondents are different for different categories defined by several dummy variables - **MALE**, **FEMALE**, **MARRIED** (refer to **ha03_data description.pdf**).

3.1. [10 marks] Generate variable **H=S-12** and run simple regression model **EARNINGS** on **H** and compare it with regression **EARNINGS** on **H** and **MALE**.

☐ Explain why coefficients of **H**, intercepts and other characteristics of these regressions are different. Give a graphical illustration of the equations being investigated.

☐ Is there a discrimination of the workers in earnings on the base of gender?

☐ What would change if instead of regression **EARNINGS** on **H** and **MALE** the regression **EARNINGS** on **H** and **FEMALE** is estimated?

3.2. [10 marks] ☐ Is discrimination in earnings based on gender confirmed by the Chow test? Do Chow test both manually (on the base of subsamples) and automatically (using command).

☐ What is the relation of the test performed in 3.1 to the Chow test in 3.2?

☐ What kind of test is equivalent to the Chow test in the context of this question?

3.3. [10 marks] Repeat Chow test and equivalent test for the group of dummy variables, but now on the basis of multiple regression equation **EARNINGS** on **H**, **ASVABC** and **AGE**.

3.4. [10 marks] Taking as a basis a simple regression of **EARNINGS** on **H**, consider the simultaneous effect of gender (variable **FEMALE**), family status (variable **MARRIED**), and place of residence (variable **URBAN**).

☐ Having calculated the regression with inclusion of three dummy variables, estimate their significance and joint significance, and also offer an explanation of the obtained signs of coefficients.

☐ Having calculated the regression of **EARNINGS** on **H**, **FEMALE**, **MARRIED** and the interaction dummy **FEMALE*MARRIED**, give full interpretation to all its coefficients.

3.5. [10 marks] ☐ Taking the regression of **EARNINGS** on **H**, investigate the presence of discrimination on the basis of ethnicity (**ETHBLACK**, **ETHHISP**, **ETHWHITE** variables).

☐ Explore the impact of the change of reference category on the regression results. What is new in comparison with the similar question in 3.1?