# Prep:

# Get Mnist data and split into train validation and test

```
In [0]: def get_mnist():
    data=np.float64(np.load(datadir+'mnist/MNIST.npy'))
    labels=np.float32(np.load(datadir+'mnist/MNIST_labels.npy'))
    print(data.shape)
    data=np.float32(data)/255.
    train_dat=data[0:50000].reshape((-1,1,28,28))
    train_labels=np.int32(labels[0:50000])
    val_dat=data[50000:60000].reshape((-1,1,28,28))
    val_labels=np.int32(labels[50000:60000])
    test_dat=data[60000:70000].reshape((-1,1,28,28))
    test_labels=np.int32(labels[60000:70000])
    return (train_dat, train_labels), (val_dat, val_labels), (test_dat, test_labels)
```

## Get the data

```
In [0]: def get_data(data_set):
    if (data_set=="mnist"):
        return(get_mnist())
    if (data_set=="cifar"):
        return(get_cifar())
```

## The network

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST_Net, self).__init_
                # 32 output features using 5x5 kernel applied to input image
                self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(32, 64, kernel size=5)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv2_drop = nn.Dropout2d(p)
                # 64 x 4 x 4 = 1024 units total in final spartial layer fully connected to 256 unit
         later
                self.fc1 = nn.Linear(1024, 256)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(256, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                else:
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 2))
                # Apply second conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 2))
                # Reshape 64 x 4 x 4 to 1024 units
                x = x.view(-1, 1024)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fcl(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get acc and loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss, correct
            def run_grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get_acc_and_loss(data,targ)
                # Zero out gradients
                self.optimizer.zero_grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
                return loss, correct
```

# Run one epoch

```
In [0]: def run_epoch(net,epoch,train,batch_size, num=None, ttype="train"):
            # Model is being trained dropout is applied
            net.train()
            if ttype=='train':
                t1=time.time()
                n=train[0].shape[0]
                if (num is not None):
                     n=np.minimum(n,num)
                ii=np.array(np.arange(0,n,1))
                tr=train[0][ii]
                y=train[1][ii]
                train loss=0; train correct=0
                with tqdm(total=len(y)) as progress bar:
                     for j in np.arange(0,len(y),batch_size):
                       # Transfer batch data to device (cpu or gpu)
                        data=torch.from numpy(tr[j:j+batch size]).to(device)
                        targ=torch.from_numpy(y[j:j+batch_size]).type(torch.long).to(device)
                       # Compute gradients, update params and report loss and correct
                        loss, correct = net.run grad(data,targ)
                         train loss += loss.item()
                        train_correct += correct.item()
                        progress_bar.set_postfix(loss=loss.item())
                         progress_bar.update(data.size(0))
                train loss /= len(y)
                print('\nTraining set epoch {}: Avg. loss: \{:.4f\}, Accuracy: \{\}/\{\} (\{:.0f\}%)\n'.form
        at(epoch,
                     train_loss, train_correct, len(y),
                     100. * train correct / len(y)))
                return(train loss)
```

# Run the network on a test set

```
In [0]: def net test(net,val,batch size,ttype='val'):
            # Do not apply dropout or gradients.
            net.eval()
            with torch.no grad():
                         test_loss = 0
                         test_correct = 0
                         vald=val[0]
                         yval=val[1]
                         for j in np.arange(0,len(yval),batch_size):
                             data=torch.torch.from numpy(vald[j:j+batch size]).to(device)
                             targ = torch.torch.from_numpy(yval[j:j+batch_size]).type(torch.long).to(
        device)
                             loss,correct=net.get acc and loss(data,targ)
                             test loss += loss.item()
                             test correct += correct.item()
                         test_loss /= len(yval)
                         SSS='Validation'
                         if (ttype=='test'):
                             SSS='Test'
                         print('\n{} set: Avg. loss: {:.4f}, Accuracy: {}/{} ({:.0f}%)\n'.format(SSS, format(SSS))
                             test loss, test correct, len(yval),
                             100. * test correct / len(yval)))
                         return(test_loss)
```

(a)

## Step 1: Compute the total number of parameters in the original model

```
The total number of parameters in the original model is: 32 \times 5 \times 5 + 32 \times 64 \times 5 \times 5 + (1024 \times 256 + 256) + (256 \times 10 + 10) = 316970
If we also count intercepts at the convolution layers, then it is:
```

 $32 \times 5 \times 5 + 32 + 32 \times 64 \times 5 \times 5 + 64 + (1024 \times 256 + 256) + (256 \times 10 + 10) = 317066$ 

Step 2: Run the model with 10,000 training data and 20 epochs, plot the error rate on training and validation as a function of the epoch number

```
In [8]: import time
        # Some parameters>
        batch size=500
        step_size=.001
        num_epochs=20
        numtrain=50000
        minimizer="Adam"
        data_set="mnist"
        model_name="model"
        dropout_p=0.5
        dim=28
        nchannels=1
        use_gpu=True
        # use GPU when possible
        device = 'cuda:0' if torch.cuda.is available() and use gpu else 'cpu'
        print(device)
        # get data
        train,val,test=get_data(data_set=data_set)
        # Initialize the model
        net = MNIST_Net(p = dropout_p, minimizer=minimizer)
        net.to(device)
        #define optimizer
        # Run epochs
        train err = []
        val_err = []
        for i in range(num epochs):
            train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
            # Test on validation set.
            val_err.append(net_test(net,val,batch_size))
        # Test on test set.
        net_test(net,test,batch_size,ttype='test')
        # Save model
        torch.save(net.state_dict(), datadir+model_name)
```

```
(70000, 784)
              ■ | 50000/50000 [00:02<00:00, 22509.21it/s, loss=0.315]
               0/50000 [00:00<?, ?it/s, loss=0.164]
  0 용 |
Training set epoch 0: Avg. loss: 0.0012, Accuracy: 40801/50000 (82%)
Validation set: Avg. loss: 0.0003, Accuracy: 9613/10000 (96%)
100%| | 50000/50000 [00:02<00:00, 24040.29it/s, loss=0.182]
  2%||
                | 1000/50000 [00:00<00:02, 16973.77it/s, loss=0.147]
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 47563/50000 (95%)
Validation set: Avg. loss: 0.0001, Accuracy: 9762/10000 (98%)
             ■| 50000/50000 [00:02<00:00, 23938.60it/s, loss=0.142]
100% | ■
  1%|
               | 500/50000 [00:00<00:03, 12556.67it/s, loss=0.102]
Training set epoch 2: Avg. loss: 0.0002, Accuracy: 48230/50000 (96%)
Validation set: Avg. loss: 0.0001, Accuracy: 9835/10000 (98%)
             ■| 50000/50000 [00:02<00:00, 23989.90it/s, loss=0.13]
  2%|
                | 1000/50000 [00:00<00:02, 17692.56it/s, loss=0.0989]
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48611/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9875/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 23962.36it/s, loss=0.128]
  1%
                500/50000 [00:00<00:03, 12567.13it/s, loss=0.095]
Training set epoch 4: Avg. loss: 0.0002, Accuracy: 48778/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9878/10000 (99%)
              1 50000/50000 [00:02<00:00, 23834.78it/s, loss=0.0883]
100% | ■
  0위
                 0/50000 [00:00<?, ?it/s, loss=0.0855]
Training set epoch 5: Avg. loss: 0.0001, Accuracy: 48967/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9896/10000 (99%)
             ■| 50000/50000 [00:02<00:00, 23868.01it/s, loss=0.0969]
100%
  1 % |
                500/50000 [00:00<00:04, 11651.75it/s, loss=0.0896]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49036/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9895/10000 (99%)
             ■| 50000/50000 [00:02<00:00, 23776.48it/s, loss=0.0804]
100% | ■■
                500/50000 [00:00<00:03, 12743.92it/s, loss=0.0645]
  1%
```

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```
Validation set: Avg. loss: 0.0001, Accuracy: 9909/10000 (99%)
100% | 50000/50000 [00:02<00:00, 23871.41it/s, loss=0.0644]
               | 1000/50000 [00:00<00:02, 16432.91it/s, loss=0.0816]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49215/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9916/10000 (99%)
              ■ | 50000/50000 [00:02<00:00, 23675.18it/s, loss=0.0611]
100%
               | 1000/50000 [00:00<00:02, 16739.32it/s, loss=0.0665]
  2%||
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49277/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9913/10000 (99%)
100% | 50000/50000 [00:02<00:00, 23835.72it/s, loss=0.0584]
  1 % |
                500/50000 [00:00<00:04, 11905.42it/s, loss=0.0722]
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49276/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9922/10000 (99%)
100% | ■
                50000/50000 [00:02<00:00, 23771.92it/s, loss=0.0648]
  1%
               | 500/50000 [00:00<00:03, 12767.12it/s, loss=0.0417]
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49347/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9917/10000 (99%)
100%
              ■ | 50000/50000 [00:02<00:00, 23921.65it/s, loss=0.0577]
  2용|
               | 1000/50000 [00:00<00:02, 17151.74it/s, loss=0.032]
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49347/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9912/10000 (99%)
100%
             ■ | 50000/50000 [00:02<00:00, 23904.91it/s, loss=0.0479]
               | 1000/50000 [00:00<00:03, 16302.80it/s, loss=0.0413]
  2용||
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49401/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9930/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 23660.93it/s, loss=0.0586]
               | 1000/50000 [00:00<00:02, 16632.12it/s, loss=0.0526]
Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49382/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9931/10000 (99%)
```

Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49126/50000 (98%)

```
100%
                | 50000/50000 [00:02<00:00, 23834.19it/s, loss=0.0386]
                | 1000/50000 [00:00<00:02, 16755.23it/s, loss=0.0317]
  2용||
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49455/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9933/10000 (99%)
100% | ■
              ■ | 50000/50000 [00:02<00:00, 23756.28it/s, loss=0.0345]
  1 % |
                 500/50000 [00:00<00:03, 12664.04it/s, loss=0.0419]
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49470/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9933/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 23742.52it/s, loss=0.0378]
  1% |
                 500/50000 [00:00<00:03, 12550.66it/s, loss=0.0428]
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49475/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9937/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 23785.70it/s, loss=0.0247]
  1%|
                 500/50000 [00:00<00:03, 12558.85it/s, loss=0.0352]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49516/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9928/10000 (99%)
100% | 50000/50000 [00:02<00:00, 23898.68it/s, loss=0.0267]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49539/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9942/10000 (99%)
Test set: Avg. loss: 0.0001, Accuracy: 9920/10000 (99%)
import matplotlib.pyplot as plt
train_plt = plt.plot(range(20),train_err,label='train')
 0.0012
 0.0010
 0.0008
 0.0006
 0.0004
 0.0002
```

In [9]:

0.0

5.0

7.5

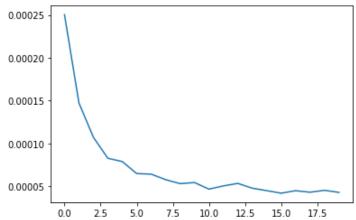
10.0

12.5

15.0

17.5

```
In [10]: val_plt = plt.plot(range(20),val_err,label='val')
```



Both training errors and validation errors decrease with each epoch. The model reaches 99% validation accuracy with very few epochs.

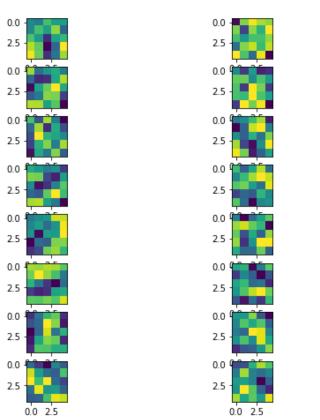
## Step 3: Show an image with the 32 5x5 filters that are estimated in the first layer of the model

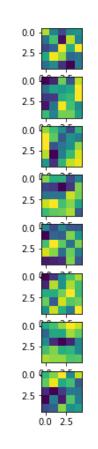
```
In [0]: for p in net.parameters():
    filters = p
    break
```

```
In [12]: filters = filters.reshape([32,5,5])
    plt.figure(figsize=(16,8))
    nrows, ncols = [8,4]

for i in range(nrows):
    for j in range(ncols):
        plt.subplot(nrows,ncols,i*ncols+j+1)
        plt.imshow(filters[i*ncols+j].cpu().data.numpy())
    plt.show
```

Out[12]: <function matplotlib.pyplot.show>







(b)

i.

## Step 1: Half the number of parameters while keeping the same number of layer

For approximately halving the number of parameters, I simply change the number of features in first layer to 16, and the number of features in second layer to 32, and adjust the parameters going into the fully connected layer accordingly.

```
In [13]: print('total number of parameters in the adjusted architecture is:',16*5*5+16*32*5*5+(512*25 6+256)+(256*10+10))
```

total number of parameters in the adjusted architecture is: 147098

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST Net, self). init
                # 16 output features using 5x5 kernel applied to input image
                self.conv1 = nn.Conv2d(1, 16, kernel_size=5)
                # 32 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(16, 32, kernel size=5)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv2_drop = nn.Dropout2d(p)
                \# 32 x 4 x 4 = 512 units total in final spartial layer fully connected to 256 unit 1
        ater
                self.fc1 = nn.Linear(512, 256)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(256, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                else:
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 2))
                # Apply second conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 2))
                # Reshape 64 x 4 x 4 to 512 units
                x = x.view(-1, 512)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fc1(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get acc and loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss, correct
            def run_grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get_acc_and_loss(data,targ)
                # Zero out gradients
                self.optimizer.zero_grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
                return loss, correct
```

```
In [15]: # use GPU when possible
         device = 'cuda:0' if torch.cuda.is_available() and use_gpu else 'cpu'
         print(device)
         # get data
         train,val,test=get_data(data_set=data_set)
         # Initialize the model
         net = MNIST_Net(p = dropout_p, minimizer=minimizer)
         net.to(device)
         # Run epochs
         train_err = []
         val err = []
         for i in range(num epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
             # Test on validation set.
             val_err.append(net_test(net,val,batch_size))
         \# Test on test set.
         net_test(net,test,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

```
0%|
              | 0/50000 [00:00<?, ?it/s]
(70000, 784)
             ■ | 50000/50000 [00:01<00:00, 39267.14it/s, loss=0.342]
100%
                2500/50000 [00:00<00:01, 35810.31it/s, loss=0.211]
Training set epoch 0: Avg. loss: 0.0016, Accuracy: 37890/50000 (76%)
Validation set: Avg. loss: 0.0003, Accuracy: 9486/10000 (95%)
             50000/50000 [00:01<00:00, 42412.29it/s, loss=0.252]
100%
                3000/50000 [00:00<00:01, 37025.23it/s, loss=0.149]
  68
Training set epoch 1: Avg. loss: 0.0004, Accuracy: 46828/50000 (94%)
Validation set: Avg. loss: 0.0002, Accuracy: 9715/10000 (97%)
100%
                50000/50000 [00:01<00:00, 42008.91it/s, loss=0.156]
                3000/50000 [00:00<00:01, 37747.64it/s, loss=0.0745]
  6%
Training set epoch 2: Avg. loss: 0.0003, Accuracy: 47785/50000 (96%)
Validation set: Avg. loss: 0.0001, Accuracy: 9792/10000 (98%)
              50000/50000 [00:01<00:00, 42993.28it/s, loss=0.136]
100% | ■
                3000/50000 [00:00<00:01, 37190.58it/s, loss=0.0774]
  6%
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48188/50000 (96%)
Validation set: Avg. loss: 0.0001, Accuracy: 9834/10000 (98%)
100%
              ■ 50000/50000 [00:01<00:00, 42509.68it/s, loss=0.128]
               2500/50000 [00:00<00:01, 37105.26it/s, loss=0.118]
  5%|
Training set epoch 4: Avg. loss: 0.0002, Accuracy: 48435/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9854/10000 (99%)
100%
                50000/50000 [00:01<00:00, 42860.71it/s, loss=0.113]
                3000/50000 [00:00<00:01, 37243.09it/s, loss=0.0368]
Training set epoch 5: Avg. loss: 0.0002, Accuracy: 48620/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9858/10000 (99%)
100%
              | 50000/50000 [00:01<00:00, 43038.65it/s, loss=0.0951]
                3000/50000 [00:00<00:01, 38467.15it/s, loss=0.0426]
Training set epoch 6: Avg. loss: 0.0002, Accuracy: 48676/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9882/10000 (99%)
```

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```
3000/50000 [00:00<00:01, 35739.09it/s, loss=0.0431]
  68
Training set epoch 7: Avg. loss: 0.0002, Accuracy: 48842/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9880/10000 (99%)
             50000/50000 [00:01<00:00, 42858.56it/s, loss=0.101]
100%
  5%
                2500/50000 [00:00<00:01, 37182.75it/s, loss=0.0615]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 48956/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9892/10000 (99%)
100% | ■
                50000/50000 [00:01<00:00, 43459.28it/s, loss=0.104]
  6%
                3000/50000 [00:00<00:01, 37195.20it/s, loss=0.0286]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 48995/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9895/10000 (99%)
100%
                 50000/50000 [00:01<00:00, 42722.39it/s, loss=0.0769]
  6%
                3000/50000 [00:00<00:01, 38239.66it/s, loss=0.0269]
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49046/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9898/10000 (99%)
100%
              ■ | 50000/50000 [00:01<00:00, 42595.50it/s, loss=0.0943]
                3000/50000 [00:00<00:01, 37430.09it/s, loss=0.0226]
  6%|
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49070/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9902/10000 (99%)
100%
                 50000/50000 [00:01<00:00, 42890.32it/s, loss=0.05]
                 2500/50000 [00:00<00:01, 35793.32it/s, loss=0.0511]
  5%|
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49146/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9909/10000 (99%)
100%
                50000/50000 [00:01<00:00, 42535.94it/s, loss=0.0496]
                3000/50000 [00:00<00:01, 36873.54it/s, loss=0.0332]
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49202/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9903/10000 (99%)
100%
              50000/50000 [00:01<00:00, 42313.22it/s, loss=0.0915]
  5%|
                2500/50000 [00:00<00:01, 34852.97it/s, loss=0.048]
```

50000/50000 [00:01<00:00, 42434.45it/s, loss=0.099]

100%

```
Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49222/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9912/10000 (99%)
100%
             50000/50000 [00:01<00:00, 42408.24it/s, loss=0.0862]
                3000/50000 [00:00<00:01, 37647.46it/s, loss=0.0275]
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49229/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9906/10000 (99%)
             ■ | 50000/50000 [00:01<00:00, 41883.56it/s, loss=0.0749]
100% | ■
                3000/50000 [00:00<00:01, 38786.83it/s, loss=0.0184]
  6%
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49266/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9903/10000 (99%)
100%
             50000/50000 [00:01<00:00, 42386.57it/s, loss=0.0511]
                3000/50000 [00:00<00:01, 38700.10it/s, loss=0.0132]
  6%|
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49281/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9913/10000 (99%)
100% | ■■
                50000/50000 [00:01<00:00, 42653.20it/s, loss=0.0591]
  5%|
               2500/50000 [00:00<00:01, 35275.54it/s, loss=0.0567]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49323/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9918/10000 (99%)
100% | 50000/50000 [00:01<00:00, 42779.53it/s, loss=0.0502]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49317/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9924/10000 (99%)
Test set: Avg. loss: 0.0001, Accuracy: 9908/10000 (99%)
```

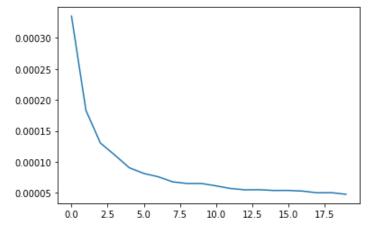
```
In [16]: train_plt = plt.plot(range(20), train_err, label='train')

0.0016
0.0012
0.0010
0.0008
0.0006
0.0004
0.0002
```

```
In [17]: val_plt = plt.plot(range(20), val_err, label='val')
```

17.5

15.0



0.0

2.5

5.0

7.5

10.0

12.5

With half the number of parameters, training and validation loss still decreases to almost 0 as the number of epochs increases, but initially the error rate is higher. Still, the test accuracy is about the same at 99%.

## Step 2: Double the number of parameters while keeping the same number of layer

To double the number of parameters, I simply double the number of features in the first layer to 64, keep the number of features in the second layer constant at 64, and then double the number of parameters in the second layer of the fully connected layer to 512.

```
In [18]: print('total number of parameters in the adjusted architecture is:',64*5*5+64*64*5*5+(1024*5 12+512)+(512*10+10))
```

total number of parameters in the adjusted architecture is: 633930

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST Net, self). init
                # 64 output features using 5x5 kernel applied to input image
                self.conv1 = nn.Conv2d(1, 64, kernel_size=5)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(64, 64, kernel size=5)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv2_drop = nn.Dropout2d(p)
                # 64 x 4 x 4 = 1024 units total in final spartial layer fully connected to 256 unit
         later
                self.fc1 = nn.Linear(1024, 256)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(256, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                else:
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 2))
                # Apply second conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 2))
                # Reshape 64 x 4 x 4 to 1024 units
                x = x.view(-1, 1024)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fcl(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get acc and loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss, correct
            def run_grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get_acc_and_loss(data,targ)
                # Zero out gradients
                self.optimizer.zero_grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
                return loss, correct
```

```
In [20]: # use GPU when possible
         device = 'cuda:0' if torch.cuda.is_available() and use_gpu else 'cpu'
         print(device)
         # get data
         train,val,test=get_data(data_set=data_set)
         # Initialize the model
         net = MNIST_Net(p = dropout_p, minimizer=minimizer)
         net.to(device)
         # Run epochs
         train_err = []
         val err = []
         for i in range(num epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
             # Test on validation set.
             val_err.append(net_test(net,val,batch_size))
         \# Test on test set.
         net_test(net,test,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

```
(70000, 784)
100% | 50000/50000 [00:03<00:00, 16619.85it/s, loss=0.255]
               | 0/50000 [00:00<?, ?it/s]
Training set epoch 0: Avg. loss: 0.0010, Accuracy: 42294/50000 (85%)
Validation set: Avg. loss: 0.0002, Accuracy: 9658/10000 (97%)
100%
             ■| 50000/50000 [00:03<00:00, 16635.75it/s, loss=0.167]
                0/50000 [00:00<?, ?it/s]
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 47866/50000 (96%)
Validation set: Avg. loss: 0.0001, Accuracy: 9811/10000 (98%)
             ■| 50000/50000 [00:02<00:00, 16704.61it/s, loss=0.139]
100% | ■
  0위
               | 0/50000 [00:00<?, ?it/s]
Training set epoch 2: Avg. loss: 0.0002, Accuracy: 48406/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9847/10000 (98%)
100%
             ■| 50000/50000 [00:02<00:00, 16685.54it/s, loss=0.0886]
  0 % |
               | 0/50000 [00:00<?, ?it/s]
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48745/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9879/10000 (99%)
100%
                 50000/50000 [00:03<00:00, 16647.26it/s, loss=0.104]
  0위
               | 0/50000 [00:00<?, ?it/s]
Training set epoch 4: Avg. loss: 0.0001, Accuracy: 48888/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9892/10000 (99%)
              1 50000/50000 [00:02<00:00, 16863.45it/s, loss=0.0864]
100%
  0위
                0/50000 [00:00<?, ?it/s]
Training set epoch 5: Avg. loss: 0.0001, Accuracy: 49043/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9900/10000 (99%)
             ■| 50000/50000 [00:02<00:00, 16695.75it/s, loss=0.0941]
100%
  0 용 |
                0/50000 [00:00<?, ?it/s]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49139/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9904/10000 (99%)
             ■| 50000/50000 [00:02<00:00, 16745.39it/s, loss=0.0678]
100%
               | 0/50000 [00:00<?, ?it/s]
  0 용 |
```

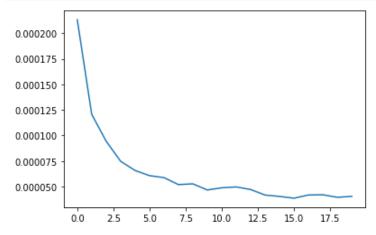
cuda:0

```
Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49247/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9910/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 16672.27it/s, loss=0.0796]
                0/50000 [00:00<?, ?it/s]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49283/50000 (99%)
Validation set: Avg. loss: 0.0001, Accuracy: 9908/10000 (99%)
              50000/50000 [00:02<00:00, 16670.29it/s, loss=0.0388]
100% | ■
  0위
                0/50000 [00:00<?, ?it/s]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49338/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9921/10000 (99%)
100%
             50000/50000 [00:03<00:00, 16635.56it/s, loss=0.0461]
  0위
               0/50000 [00:00<?, ?it/s]
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49343/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9923/10000 (99%)
                50000/50000 [00:02<00:00, 16788.98it/s, loss=0.0412]
100% | ■■
  0위
               | 0/50000 [00:00<?, ?it/s]
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49383/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9921/10000 (99%)
100%
              50000/50000 [00:02<00:00, 16785.34it/s, loss=0.048]
  0 % |
                0/50000 [00:00<?, ?it/s]
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49422/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9922/10000 (99%)
100%
             ■ | 50000/50000 [00:02<00:00, 16688.61it/s, loss=0.033]
                0/50000 [00:00<?, ?it/s]
  0위
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49466/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9929/10000 (99%)
100% | ■■
               | 50000/50000 [00:02<00:00, 16750.92it/s, loss=0.0251]
                0/50000 [00:00<?, ?it/s]
Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49481/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9936/10000 (99%)
```

```
50000/50000 [00:02<00:00, 16668.68it/s, loss=0.0376]
100%
                 0/50000 [00:00<?, ?it/s]
  0 용
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49495/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9939/10000 (99%)
100%
              ■| 50000/50000 [00:02<00:00, 16770.17it/s, loss=0.0376]
  0 %
                 0/50000 [00:00<?, ?it/s]
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49517/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9931/10000 (99%)
                 50000/50000 [00:02<00:00, 16690.59it/s, loss=0.0451]
100% |
  0위
                 0/50000 [00:00<?, ?it/s]
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49523/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9930/10000 (99%)
                 50000/50000 [00:02<00:00, 16682.49it/s, loss=0.0425]
100%
  0 % |
                 0/50000 [00:00<?, ?it/s]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49594/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9942/10000 (99%)
100% | 50000/50000 [00:03<00:00, 16639.28it/s, loss=0.025]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49560/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9943/10000 (99%)
Test set: Avg. loss: 0.0001, Accuracy: 9925/10000 (99%)
train plt = plt.plot(range(20), train err, label='train')
 0.0010
 0.0008
 0.0006
 0.0004
 0.0002
           2.5
                5.0
                     7.5
                          10.0
                              12.5
                                        17.5
       0.0
                                   15.0
```

In [21]:

In [22]: val\_plt = plt.plot(range(20), val\_err, label='val')



The rate of convergence is pretty similar to the original architecture. We see that because of the increased number of parameters, the training error converges even faster than the original architecture. The test accuracy is still at 99%.

# ii. Design a deeper network with more or less the same number of parameters as the original network

I use the following architecture:

- First layer: 32 features with 5x5 kernel and no padding
- · Second layer: 64 features with 5x5 kernel and padding
- Third layer: 70 features with 5x5 kernel and padding
- Fully connected first layer: going from 630 features to 240 features

```
In [23]: print('total number of parameters in the adjusted architecture is:',32*5*5+32*64*5*5+64*70*5 *5+(630*240+240)+(240*10+10))
```

total number of parameters in the adjusted architecture is: 317850

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST_Net, self).__init_
                # 16 output features using 5x5 kernel applied to input image, without padding
                self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(32, 64, kernel size=5,padding=2)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv3 = nn.Conv2d(64,70,kernel_size=5,padding=2)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv3_drop = nn.Dropout2d(p)
                # 70 x 3 x 3 = 630 units total in final spartial layer fully connected to 240 unit 1
        ater
                self.fc1 = nn.Linear(630, 240)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(240, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 2))
                # Apply second conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max_pool2d(self.conv2(x), 2))
                # Apply third conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max_pool2d(self.conv3_drop(self.conv3(x)), 2))
                \# Reshape 64 x 4 x 4 to 630 units
                x = x.view(-1, 630)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fcl(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get_acc_and_loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss,correct
            def run grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get acc and loss(data,targ)
                # Zero out gradients
                self.optimizer.zero grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
```

return loss, correct

```
In [25]: # use GPU when possible
         device = 'cuda:0' if torch.cuda.is_available() and use_gpu else 'cpu'
         print(device)
         # get data
         train,val,test=get_data(data_set=data_set)
         # Initialize the model
         net = MNIST_Net(p = dropout_p, minimizer=minimizer)
         net.to(device)
         # Run epochs
         train_err = []
         val err = []
         for i in range(num epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
             # Test on validation set.
             val_err.append(net_test(net,val,batch_size))
         \# Test on test set.
         net_test(net,test,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

```
(70000, 784)
100% | 100% | 50000/50000 [00:03<00:00, 13720.27it/s, loss=0.198]
Training set epoch 0: Avg. loss: 0.0012, Accuracy: 40498/50000 (81%)
  3%|
               | 1500/50000 [00:00<00:03, 13708.28it/s, loss=0.135]
Validation set: Avg. loss: 0.0002, Accuracy: 9702/10000 (97%)
             ■| 50000/50000 [00:03<00:00, 13758.29it/s, loss=0.152]
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 48018/50000 (96%)
  3%|
               | 1500/50000 [00:00<00:03, 13738.21it/s, loss=0.0674]
Validation set: Avg. loss: 0.0001, Accuracy: 9823/10000 (98%)
100%| 50000/50000 [00:03<00:00, 13735.44it/s, loss=0.0837]
Training set epoch 2: Avg. loss: 0.0002, Accuracy: 48671/50000 (97%)
  3%|
               | 1500/50000 [00:00<00:03, 13655.79it/s, loss=0.0579]
Validation set: Avg. loss: 0.0001, Accuracy: 9870/10000 (99%)
100% | 100% | 50000/50000 [00:03<00:00, 13717.67it/s, loss=0.108]
Training set epoch 3: Avg. loss: 0.0001, Accuracy: 48877/50000 (98%)
  3%|
               | 1500/50000 [00:00<00:03, 13823.18it/s, loss=0.0551]
Validation set: Avg. loss: 0.0001, Accuracy: 9879/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13790.12it/s, loss=0.0573]
Training set epoch 4: Avg. loss: 0.0001, Accuracy: 49144/50000 (98%)
  3%|
               | 1500/50000 [00:00<00:03, 13724.10it/s, loss=0.0421]
Validation set: Avg. loss: 0.0001, Accuracy: 9892/10000 (99%)
             ■ | 50000/50000 [00:03<00:00, 13789.97it/s, loss=0.0608]
Training set epoch 5: Avg. loss: 0.0001, Accuracy: 49235/50000 (98%)
  3%|
               | 1500/50000 [00:00<00:03, 13971.85it/s, loss=0.0472]
Validation set: Avg. loss: 0.0001, Accuracy: 9901/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13876.75it/s, loss=0.0353]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49377/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13605.21it/s, loss=0.035]
```

cuda:0

```
100% | 100% | 50000/50000 [00:03<00:00, 13767.97it/s, loss=0.0624]
Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49447/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13550.44it/s, loss=0.0327]
Validation set: Avg. loss: 0.0000, Accuracy: 9922/10000 (99%)
             ■| 50000/50000 [00:03<00:00, 13760.38it/s, loss=0.0432]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49512/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 14030.46it/s, loss=0.0349]
Validation set: Avg. loss: 0.0000, Accuracy: 9924/10000 (99%)
100%| 50000/50000 [00:03<00:00, 13718.26it/s, loss=0.0345]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49521/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13581.48it/s, loss=0.0339]
Validation set: Avg. loss: 0.0000, Accuracy: 9933/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13739.83it/s, loss=0.0382]
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49593/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13887.57it/s, loss=0.0124]
Validation set: Avg. loss: 0.0000, Accuracy: 9939/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13786.19it/s, loss=0.0156]
Training set epoch 11: Avg. loss: 0.0000, Accuracy: 49594/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13713.03it/s, loss=0.0322]
Validation set: Avg. loss: 0.0000, Accuracy: 9934/10000 (99%)
             ■| 50000/50000 [00:03<00:00, 13782.75it/s, loss=0.0455]
Training set epoch 12: Avg. loss: 0.0000, Accuracy: 49646/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13423.52it/s, loss=0.0151]
Validation set: Avg. loss: 0.0000, Accuracy: 9935/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13684.41it/s, loss=0.0265]
Training set epoch 13: Avg. loss: 0.0000, Accuracy: 49693/50000 (99%)
  3%|
               | 1500/50000 [00:00<00:03, 13721.52it/s, loss=0.0253]
```

Validation set: Avg. loss: 0.0000, Accuracy: 9917/10000 (99%)

```
Validation set: Avg. loss: 0.0000, Accuracy: 9940/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13737.45it/s, loss=0.0213]
Training set epoch 14: Avg. loss: 0.0000, Accuracy: 49697/50000 (99%)
 3용|
               | 1500/50000 [00:00<00:03, 13434.10it/s, loss=0.0174]
Validation set: Avg. loss: 0.0000, Accuracy: 9942/10000 (99%)
             ■ | 50000/50000 [00:03<00:00, 13773.03it/s, loss=0.0116]
Training set epoch 15: Avg. loss: 0.0000, Accuracy: 49720/50000 (99%)
               | 1500/50000 [00:00<00:03, 13846.79it/s, loss=0.00446]
 3%|
Validation set: Avg. loss: 0.0000, Accuracy: 9941/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13734.60it/s, loss=0.00483]
Training set epoch 16: Avg. loss: 0.0000, Accuracy: 49766/50000 (100%)
 3%|
               | 1500/50000 [00:00<00:03, 13785.11it/s, loss=0.00656]
Validation set: Avg. loss: 0.0000, Accuracy: 9932/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13869.65it/s, loss=0.0106]
Training set epoch 17: Avg. loss: 0.0000, Accuracy: 49723/50000 (99%)
 3%|
               | 1500/50000 [00:00<00:03, 13836.89it/s, loss=0.0124]
Validation set: Avg. loss: 0.0000, Accuracy: 9935/10000 (99%)
100% | 50000/50000 [00:03<00:00, 13779.39it/s, loss=0.0233]
Training set epoch 18: Avg. loss: 0.0000, Accuracy: 49769/50000 (100%)
 3%|
               | 1500/50000 [00:00<00:03, 14066.92it/s, loss=0.0179]
Validation set: Avg. loss: 0.0000, Accuracy: 9942/10000 (99%)
             ■ | 50000/50000 [00:03<00:00, 13671.14it/s, loss=0.0405]
Training set epoch 19: Avg. loss: 0.0000, Accuracy: 49769/50000 (100%)
Validation set: Avg. loss: 0.0000, Accuracy: 9938/10000 (99%)
Test set: Avg. loss: 0.0001, Accuracy: 9928/10000 (99%)
```

```
train_plt = plt.plot(range(20),train_err,label='train')
             0.0012
             0.0010
             0.0008
             0.0006
             0.0004
             0.0002
             0.0000
                                             10.0
                                                   12.5
                     0.0
                           2.5
                                 5.0
                                        7.5
                                                          15.0
                                                                17.5
In [27]:
            val plt = plt.plot(range(20), val err, label='val')
             0.00018
             0.00016
             0.00014
             0.00012
             0.00010
             0.00008
             0.00006
             0.00004
                      0.0
                            2.5
                                  5.0
                                         7.5
                                                           15.0
                                                                 17.5
                                              10.0
                                                     12.5
```

Again, the differences are minimal and we still get 99% accuracy for test set.

### iii. Try on full training set and report the result

Having more parameters or a deeper network does not seem to bring significant difference to the error rate which is already very low. Having fewer parameters seem to make the error rate drop slower, while having deeper network makes the training process take longer. We prefer to have fewer parameters to avoid overfitting, so I will just go with the default setting of the original model and train it on the full training set, which is the augmented data set constituting the original training data and validation data.

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST_Net, self).__init_
                # 32 output features using 5x5 kernel applied to input image
                self.conv1 = nn.Conv2d(1, 32, kernel_size=5)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(32, 64, kernel size=5)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv2_drop = nn.Dropout2d(p)
                # 64 x 4 x 4 = 1024 units total in final spartial layer fully connected to 256 unit
         later
                self.fc1 = nn.Linear(1024, 256)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(256, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                else:
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 2))
                # Apply second conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 2))
                # Reshape 64 x 4 x 4 to 1024 units
                x = x.view(-1, 1024)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fcl(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get acc and loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss, correct
            def run_grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get_acc_and_loss(data,targ)
                # Zero out gradients
                self.optimizer.zero_grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
                return loss, correct
```

```
In [29]: import time
         # Some parameters>
         batch size=500
         step_size=.001
         num_epochs=20
         numtrain=50000
         minimizer="Adam"
         data_set="mnist"
         model_name="model"
         dropout_p=0.5
         dim=28
         nchannels=1
         use\_gpu=\textbf{True}
         # use GPU when possible
         device = 'cuda:0' if torch.cuda.is available() and use gpu else 'cpu'
         print(device)
         # get augmented data
         train,val,test=get_data(data_set=data_set)
         train = list(train)
         train[0] = np.concatenate((train[0],val[0]),axis=0)
         train[1] = np.concatenate((train[1],val[1]),axis=0)
         train = tuple(train)
         # Initialize the model
         net = MNIST Net(p = dropout p, minimizer=minimizer)
         net.to(device)
         #define optimizer
         # Run epochs
         train_err = []
         val_err = []
         for i in range(num_epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
         # Test on test set.
         net_test(net,test,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

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```
(70000, 784)
              50000/50000 [00:02<00:00, 23693.13it/s, loss=0.267]
100%
                3000/50000 [00:00<00:01, 24127.10it/s, loss=0.146]
Training set epoch 0: Avg. loss: 0.0011, Accuracy: 41404/50000 (83%)
100% | ■
               50000/50000 [00:02<00:00, 23914.62it/s, loss=0.193]
                3000/50000 [00:00<00:01, 24322.02it/s, loss=0.0668]
  6%||
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 47771/50000 (96%)
             ■ | 50000/50000 [00:02<00:00, 23815.38it/s, loss=0.166]
100%
                3000/50000 [00:00<00:01, 24463.83it/s, loss=0.058]
  6%
Training set epoch 2: Avg. loss: 0.0002, Accuracy: 48344/50000 (97%)
             ■| 50000/50000 [00:02<00:00, 23747.80it/s, loss=0.132]
100%
                3000/50000 [00:00<00:02, 23460.49it/s, loss=0.0552]
  6%||
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48653/50000 (97%)
              50000/50000 [00:02<00:00, 23602.44it/s, loss=0.121]
100%
  6%||
                3000/50000 [00:00<00:02, 23181.97it/s, loss=0.0553]
Training set epoch 4: Avg. loss: 0.0002, Accuracy: 48812/50000 (98%)
100%
              50000/50000 [00:02<00:00, 23491.94it/s, loss=0.103]
                3000/50000 [00:00<00:01, 23967.51it/s, loss=0.0389]
  6%
Training set epoch 5: Avg. loss: 0.0001, Accuracy: 48989/50000 (98%)
100%
             ■ | 50000/50000 [00:02<00:00, 23741.25it/s, loss=0.0879]
  6%
                3000/50000 [00:00<00:02, 23393.18it/s, loss=0.0374]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49081/50000 (98%)
100%
             ■ | 50000/50000 [00:02<00:00, 23842.66it/s, loss=0.0569]
                3000/50000 [00:00<00:01, 24344.73it/s, loss=0.0373]
  6%||
Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49142/50000 (98%)
100% | ■
              ■ | 50000/50000 [00:02<00:00, 23642.72it/s, loss=0.063]
                3000/50000 [00:00<00:01, 24179.79it/s, loss=0.0275]
  6%
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49225/50000 (98%)
100%
                50000/50000 [00:02<00:00, 23807.01it/s, loss=0.0675]
  68||
                3000/50000 [00:00<00:01, 24603.08it/s, loss=0.0179]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49273/50000 (99%)
              ■ 50000/50000 [00:02<00:00, 23757.50it/s, loss=0.0615]
100%
                3000/50000 [00:00<00:01, 23574.79it/s, loss=0.0333]
  6%
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49340/50000 (99%)
```

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```
50000/50000 [00:02<00:00, 23681.60it/s, loss=0.0484]
100%
                3000/50000 [00:00<00:01, 24440.56it/s, loss=0.029]
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49338/50000 (99%)
               | 50000/50000 [00:02<00:00, 23661.67it/s, loss=0.0441]
100% | ■
                3000/50000 [00:00<00:01, 24117.50it/s, loss=0.0172]
  6%
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49427/50000 (99%)
              1 50000/50000 [00:02<00:00, 23631.42it/s, loss=0.0582]
100% | ■
                3000/50000 [00:00<00:01, 23533.63it/s, loss=0.0199]
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49412/50000 (99%)
                50000/50000 [00:02<00:00, 23680.64it/s, loss=0.0415]
100% | ■
                3000/50000 [00:00<00:01, 24303.03it/s, loss=0.0124]
Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49429/50000 (99%)
100%
              1 50000/50000 [00:02<00:00, 23797.10it/s, loss=0.0534]
               3000/50000 [00:00<00:01, 24980.25it/s, loss=0.0258]
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49449/50000 (99%)
                50000/50000 [00:02<00:00, 23679.20it/s, loss=0.0399]
100%
                3000/50000 [00:00<00:01, 24411.55it/s, loss=0.0225]
  6%
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49455/50000 (99%)
                50000/50000 [00:02<00:00, 23630.17it/s, loss=0.0395]
100%
               | 3000/50000 [00:00<00:01, 24521.10it/s, loss=0.017]
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49493/50000 (99%)
                50000/50000 [00:02<00:00, 23942.82it/s, loss=0.0449]
100%
                3000/50000 [00:00<00:01, 24341.73it/s, loss=0.0177]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49521/50000 (99%)
100% | 50000/50000 [00:02<00:00, 23681.26it/s, loss=0.0309]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49540/50000 (99%)
```

Since model using fraction of training set already achieves 99% test accuracy, using the full data set still get 99% accuracy.

(C)

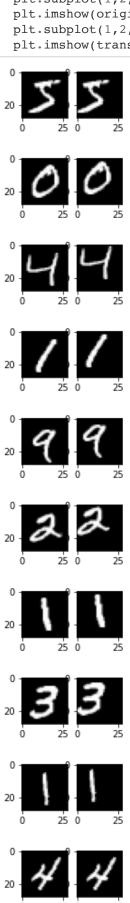
### Step 1: Display few examples of transformed data alongside the original digits

Test set: Avg. loss: 0.0001, Accuracy: 9917/10000 (99%)

```
In [0]: def get mnist transformed():
            data=np.float64(np.load(datadir+'mnist/MNIST_TR.npy'))
            labels=np.float32(np.load(datadir+'mnist/MNIST_labels.npy'))
            print(data.shape)
            data=np.float32(data)/255.
            train_dat=data[0:50000].reshape((-1,1,28,28))
            train labels=np.int32(labels[0:50000])
            val_dat=data[50000:60000].reshape((-1,1,28,28))
            val_labels=np.int32(labels[50000:60000])
            test_dat=data[60000:70000].reshape((-1,1,28,28))
            test_labels=np.int32(labels[60000:70000])
            return (train_dat, train_labels), (val_dat, val_labels), (test_dat, test_labels)
        def get_data(data_set):
            if (data_set=="mnist"):
                return(get_mnist())
            if (data_set=='trans'):
              return(get_mnist_transformed())
```

1

```
In [32]: for i in range(10):
    original = train[0][i,0,:,:]
    trans = train_tr[0][i,0,:,:]
    plt.figure(figsize=(2,4))
    plt.subplot(1,2,1)
    plt.imshow(original,cmap='gray')
    plt.subplot(1,2,2)
    plt.imshow(trans,cmap='gray')
```



Step 2: Using the original architecture to test on this data set	

```
In [33]: import time
         # Some parameters>
         batch size=500
         step_size=.001
         num_epochs=20
         numtrain=50000
         minimizer="Adam"
         data_set="mnist"
         model_name="model"
         dropout_p=0.5
         dim=28
         nchannels=1
         use_gpu=True
         # use GPU when possible
         device = 'cuda:0' if torch.cuda.is available() and use gpu else 'cpu'
         print(device)
         # get data
         train,val,test=get_data(data_set="mnist")
         train_tr,val_tr,test_tr=get_data(data_set="trans")
         # Initialize the model
         net = MNIST_Net(p = dropout_p, minimizer=minimizer)
         net.to(device)
         #define optimizer
         # Run epochs
         train_err = []
         val err = []
         for i in range(num epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
             # Test on validation set.
             val_err.append(net_test(net,val,batch_size))
         # Test on test set.
         net_test(net,test_tr,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

```
(70000, 784)
              | 0/50000 [00:00<?, ?it/s, loss=2.31]
(70000, 1, 28, 28)
100% | 322222222 | 50000/50000 [00:02<00:00, 22051.95it/s, loss=0.309]
               | 1000/50000 [00:00<00:02, 17138.92it/s, loss=0.267]
Training set epoch 0: Avg. loss: 0.0012, Accuracy: 40309/50000 (81%)
Validation set: Avg. loss: 0.0003, Accuracy: 9607/10000 (96%)
100%
                50000/50000 [00:02<00:00, 23544.95it/s, loss=0.168]
  1% |
                500/50000 [00:00<00:04, 11237.55it/s, loss=0.156]
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 47564/50000 (95%)
Validation set: Avg. loss: 0.0001, Accuracy: 9803/10000 (98%)
             ■| 50000/50000 [00:02<00:00, 23598.17it/s, loss=0.146]
100% | ■
               | 1000/50000 [00:00<00:02, 16872.99it/s, loss=0.127]
  2%
Training set epoch 2: Avg. loss: 0.0002, Accuracy: 48351/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9836/10000 (98%)
100% | 33901.35it/s, loss=0.122
                500/50000 [00:00<00:04, 11696.59it/s, loss=0.0868]
  1%
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48675/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9880/10000 (99%)
100% | 50000/50000 [00:02<00:00, 23734.87it/s, loss=0.0972]
               | 1000/50000 [00:00<00:02, 16932.73it/s, loss=0.0879]
Training set epoch 4: Avg. loss: 0.0001, Accuracy: 48855/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9898/10000 (99%)
100% | 50000/50000 [00:02<00:00, 23690.19it/s, loss=0.0808]
  2용||
               | 1000/50000 [00:00<00:02, 16455.16it/s, loss=0.0775]
Training set epoch 5: Avg. loss: 0.0001, Accuracy: 48986/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9909/10000 (99%)
100% | ■
             ■ | 50000/50000 [00:02<00:00, 23747.13it/s, loss=0.0715]
  1%|
                500/50000 [00:00<00:04, 12168.69it/s, loss=0.0584]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49058/50000 (98%)
```

Validation set: Avg. loss: 0.0001, Accuracy: 9911/10000 (99%)

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```
| 50000/50000 [00:02<00:00, 23688.29it/s, loss=0.0738]
                | 1000/50000 [00:00<00:02, 16336.27it/s, loss=0.0477]
  2 % ||
Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49172/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9917/10000 (99%)
100% | ■■
       50000/50000 [00:02<00:00, 23630.86it/s, loss=0.0712]
  1 % |
                 500/50000 [00:00<00:04, 11627.33it/s, loss=0.0501]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49217/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9925/10000 (99%)
100% |■
              ■ 50000/50000 [00:02<00:00, 23758.42it/s, loss=0.0534]
  1% |
                 500/50000 [00:00<00:03, 12392.76it/s, loss=0.0484]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49285/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9928/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 23565.94it/s, loss=0.0534]
                500/50000 [00:00<00:04, 12241.85it/s, loss=0.038]
  1%
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49341/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9923/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 23653.27it/s, loss=0.0528]
                500/50000 [00:00<00:03, 13018.59it/s, loss=0.0383]
  1%|
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49332/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9929/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 23667.66it/s, loss=0.0503]
                 500/50000 [00:00<00:03, 12585.00it/s, loss=0.0505]
  1% |
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49383/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9927/10000 (99%)
100%
              ■| 50000/50000 [00:02<00:00, 23412.47it/s, loss=0.0509]
                | 1000/50000 [00:00<00:02, 16529.73it/s, loss=0.0315]
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49428/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9932/10000 (99%)
100%
              50000/50000 [00:02<00:00, 23683.91it/s, loss=0.0449]
  1%
                500/50000 [00:00<00:03, 12588.17it/s, loss=0.0377]
```

100%

```
Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49450/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9941/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 23697.88it/s, loss=0.042]
                 500/50000 [00:00<00:03, 12552.69it/s, loss=0.0489]
  1%
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49480/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9932/10000 (99%)
100% | ■
              ■ | 50000/50000 [00:02<00:00, 23769.52it/s, loss=0.0385]
  1% |
                 500/50000 [00:00<00:03, 12549.15it/s, loss=0.0282]
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49498/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9930/10000 (99%)
             ■ 50000/50000 [00:02<00:00, 23489.17it/s, loss=0.0344]
  2%|
                | 1000/50000 [00:00<00:03, 16113.22it/s, loss=0.0206]
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49536/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9929/10000 (99%)
100% | ■
              ■ | 50000/50000 [00:02<00:00, 23793.25it/s, loss=0.0357]
  2%||
                | 1000/50000 [00:00<00:02, 16464.46it/s, loss=0.0265]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49505/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9931/10000 (99%)
              ■ | 50000/50000 [00:02<00:00, 23743.33it/s, loss=0.0233]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49576/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9935/10000 (99%)
Test set: Avg. loss: 0.0060, Accuracy: 5644/10000 (56%)
```

The test error is now significantly lower, at only 54%.

#### Step 3: Propose changes to the network architecture

From the results we see that the neural network is currently sensitive to local variations. To mitigate this I propose to increase the extent of pooling that occurs at each layer. In particular, I will increase the extent pooling from 2 to 3. To make pooling work, I will also adjust the kernel size to 3 at the second layer. To balance out the drop in parameter due to increase in pooling, I will increase the number of features at each layer.

```
In [0]: class MNIST_Net(nn.Module):
            def __init__(self,p=0.5,minimizer='Adam'):
                super(MNIST Net, self). init
                # 32 output features using 5x5 kernel applied to input image
                self.conv1 = nn.Conv2d(1, 64, kernel_size=5)
                # 64 output features using 5x5 kernel applied to 32 features of previous layer.
                self.conv2 = nn.Conv2d(64, 128, kernel size=3)
                # Dropout - zero out some output features so weights aren't updated.
                self.conv2_drop = nn.Dropout2d(p)
                # 64 x 4 x 4 = 1024 units total in final spartial layer fully connected to 256 unit
         later
                self.fc1 = nn.Linear(512, 256)
                # Last layer has 10 units for 10 classes
                self.fc2 = nn.Linear(256, 10)
                if minimizer == 'Adam':
                    self.optimizer = torch.optim.Adam(self.parameters(), lr = step size)
                else:
                    self.optimizer = torch.optim.SGD(self.parameters(), lr = step size, momentum=0.9
        )
                self.first=True
                # negative log-likelihood loss
                self.criterion=nn.CrossEntropyLoss()
            def forward(self, x):
                # Apply first conv then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv1(x), 3))
                # Apply second conv then drop, then maxpool by factor of 2 then non-linearity relu
                x = F.relu(F.max pool2d(self.conv2 drop(self.conv2(x)), 3))
                # Reshape 64 x 2 x 2 to 256 units
                x = x.view(-1, 512)
                # Apply fully connected layer with non-linearity relu
                x = F.relu(self.fcl(x))
                # Another dropout
                x = F.dropout(x, training=self.training)
                # Final 10 unit logits layer
                x = self.fc2(x)
                return x
            def get acc and loss(self, data, targ):
                # Apply network to batch input
                output = self.forward(data)
                # Comput loss between logit output and targ (correct class labels)
                loss = self.criterion(output, targ)
                # Also compute correct classification rate
                pred = torch.max(output,1)[1]
                correct = torch.eq(pred,targ).sum()
                return loss, correct
            def run_grad(self,data,targ):
                # Compute loss and accuracy
                loss, correct=self.get_acc_and_loss(data,targ)
                # Zero out gradients
                self.optimizer.zero_grad()
                # Compute gradients
                loss.backward()
                # Update parameters based on gradients
                self.optimizer.step()
                return loss, correct
```

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In [35]: import time
         # Some parameters>
         batch size=500
         step_size=.001
         num_epochs=20
         numtrain=50000
         minimizer="Adam"
         data_set="mnist"
         model_name="model"
         dropout_p=0.5
         dim=28
         nchannels=1
         use_gpu=True
         # use GPU when possible
         device = 'cuda:0' if torch.cuda.is available() and use gpu else 'cpu'
         print(device)
         # get data
         train,val,test=get_data(data_set="mnist")
         train_tr,val_tr,test_tr=get_data(data_set="trans")
         # Initialize the model
         net = MNIST_Net(p = dropout_p, minimizer=minimizer)
         net.to(device)
         #define optimizer
         # Run epochs
         train_err = []
         val err = []
         for i in range(num epochs):
             train_err.append(run_epoch(net,i,train,batch_size, num=numtrain, ttype="train"))
             # Test on validation set.
             val_err.append(net_test(net,val,batch_size))
         # Test on test set.
         net_test(net,test_tr,batch_size,ttype='test')
         # Save model
         torch.save(net.state_dict(), datadir+model_name)
```

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(70000, 784)
              | 500/50000 [00:00<00:04, 11529.85it/s, loss=2.3]
(70000, 1, 28, 28)
100% | 32347.77it/s, loss=0.265]
              0/50000 [00:00<?, ?it/s, loss=0.179]
Training set epoch 0: Avg. loss: 0.0015, Accuracy: 38404/50000 (77%)
Validation set: Avg. loss: 0.0002, Accuracy: 9678/10000 (97%)
100%
                50000/50000 [00:02<00:00, 22250.95it/s, loss=0.167]
  0위
               | 0/50000 [00:00<?, ?it/s, loss=0.139]
Training set epoch 1: Avg. loss: 0.0003, Accuracy: 47427/50000 (95%)
Validation set: Avg. loss: 0.0001, Accuracy: 9780/10000 (98%)
             50000/50000 [00:02<00:00, 22276.67it/s, loss=0.154]
100%
                0/50000 [00:00<?, ?it/s, loss=0.103]
  0 %
Training set epoch 2: Avg. loss: 0.0003, Accuracy: 48114/50000 (96%)
Validation set: Avg. loss: 0.0001, Accuracy: 9828/10000 (98%)
100% | 50000/50000 [00:02<00:00, 22268.95it/s, loss=0.101]
  0위
               0/50000 [00:00<?, ?it/s, loss=0.0945]
Training set epoch 3: Avg. loss: 0.0002, Accuracy: 48471/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9857/10000 (99%)
             50000/50000 [00:02<00:00, 22268.65it/s, loss=0.0861]
100%
              0/50000 [00:00<?, ?it/s, loss=0.0982]
Training set epoch 4: Avg. loss: 0.0002, Accuracy: 48682/50000 (97%)
Validation set: Avg. loss: 0.0001, Accuracy: 9870/10000 (99%)
100% | 50000/50000 [00:02<00:00, 22159.24it/s, loss=0.0808]
  0위
               0/50000 [00:00<?, ?it/s, loss=0.0843]
Training set epoch 5: Avg. loss: 0.0002, Accuracy: 48847/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9896/10000 (99%)
100% | ■
             ■| 50000/50000 [00:02<00:00, 22181.93it/s, loss=0.117]
  0위
                0/50000 [00:00<?, ?it/s, loss=0.0641]
Training set epoch 6: Avg. loss: 0.0001, Accuracy: 49021/50000 (98%)
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Validation set: Avg. loss: 0.0001, Accuracy: 9900/10000 (99%)

cuda:0

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50000/50000 [00:02<00:00, 22335.27it/s, loss=0.109]
100%
                0/50000 [00:00<?, ?it/s, loss=0.075]
  0 용
Training set epoch 7: Avg. loss: 0.0001, Accuracy: 49033/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9893/10000 (99%)
100% | 50000/50000 [00:02<00:00, 22227.13it/s, loss=0.0666]
  0 용 |
                 0/50000 [00:00<?, ?it/s, loss=0.0536]
Training set epoch 8: Avg. loss: 0.0001, Accuracy: 49111/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9907/10000 (99%)
100% | ■
              ■ 50000/50000 [00:02<00:00, 22462.27it/s, loss=0.065]
  0위
                 0/50000 [00:00<?, ?it/s, loss=0.0599]
Training set epoch 9: Avg. loss: 0.0001, Accuracy: 49213/50000 (98%)
Validation set: Avg. loss: 0.0001, Accuracy: 9919/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 22268.10it/s, loss=0.0516]
  0위
                0/50000 [00:00<?, ?it/s, loss=0.0509]
Training set epoch 10: Avg. loss: 0.0001, Accuracy: 49249/50000 (98%)
Validation set: Avg. loss: 0.0000, Accuracy: 9924/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 22378.33it/s, loss=0.0723]
               | 0/50000 [00:00<?, ?it/s, loss=0.047]
  0 % |
Training set epoch 11: Avg. loss: 0.0001, Accuracy: 49265/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9925/10000 (99%)
100%
                 50000/50000 [00:02<00:00, 22435.82it/s, loss=0.04]
                0/50000 [00:00<?, ?it/s, loss=0.0426]
  0위
Training set epoch 12: Avg. loss: 0.0001, Accuracy: 49311/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9930/10000 (99%)
100%
              ■ | 50000/50000 [00:02<00:00, 22141.57it/s, loss=0.0569]
                0/50000 [00:00<?, ?it/s, loss=0.0465]
Training set epoch 13: Avg. loss: 0.0001, Accuracy: 49346/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9932/10000 (99%)
100%
              | 50000/50000 [00:02<00:00, 22117.10it/s, loss=0.0669]
  0위
                0/50000 [00:00<?, ?it/s, loss=0.0597]
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Training set epoch 14: Avg. loss: 0.0001, Accuracy: 49381/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9933/10000 (99%)
100%
             ■| 50000/50000 [00:02<00:00, 22428.85it/s, loss=0.0576]
                0/50000 [00:00<?, ?it/s, loss=0.041]
Training set epoch 15: Avg. loss: 0.0001, Accuracy: 49392/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9932/10000 (99%)
              ■ | 50000/50000 [00:02<00:00, 22252.91it/s, loss=0.0669]
100% | ■
                0/50000 [00:00<?, ?it/s, loss=0.0432]
 0위
Training set epoch 16: Avg. loss: 0.0001, Accuracy: 49421/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9937/10000 (99%)
100%
             50000/50000 [00:02<00:00, 22040.54it/s, loss=0.0448]
               0/50000 [00:00<?, ?it/s, loss=0.0346]
 0위
Training set epoch 17: Avg. loss: 0.0001, Accuracy: 49490/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9937/10000 (99%)
                50000/50000 [00:02<00:00, 22317.42it/s, loss=0.0496]
100% | ■■
 0 % |
               0/50000 [00:00<?, ?it/s, loss=0.0351]
Training set epoch 18: Avg. loss: 0.0001, Accuracy: 49443/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9940/10000 (99%)
             ■ | 50000/50000 [00:02<00:00, 22269.29it/s, loss=0.0437]
Training set epoch 19: Avg. loss: 0.0001, Accuracy: 49501/50000 (99%)
Validation set: Avg. loss: 0.0000, Accuracy: 9943/10000 (99%)
Test set: Avg. loss: 0.0028, Accuracy: 7229/10000 (72%)
```

We see that with pooling, now the test error has improved from 54% to 70%. A deeper neural network with more fine tuned number of features could improve this error rate further.