

Experimental Analysis of Mastery Learning Criteria

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Mastery Learning

- common personalization approach in educational systems
- “practice until mastery, then move to a subsequent topic”

Example

item	answer	time	correct?
$\frac{2}{3} + \frac{4}{5}$	$\frac{13}{15}$	12s	correct
$\frac{3}{4} + \frac{1}{6}$	$\frac{10}{12}$	7s	incorrect
$\frac{2}{7} + \frac{3}{14}$	$\frac{1}{2}$	9s	correct
$\frac{1}{4} + \frac{2}{3}$	$\frac{11}{12}$	7s	correct
$\frac{2}{5} + \frac{3}{7}$	$\frac{29}{35}$	13s	correct

Should the learner continue or move to another topic?

Mastery Criteria

important, interesting, understudied research direction

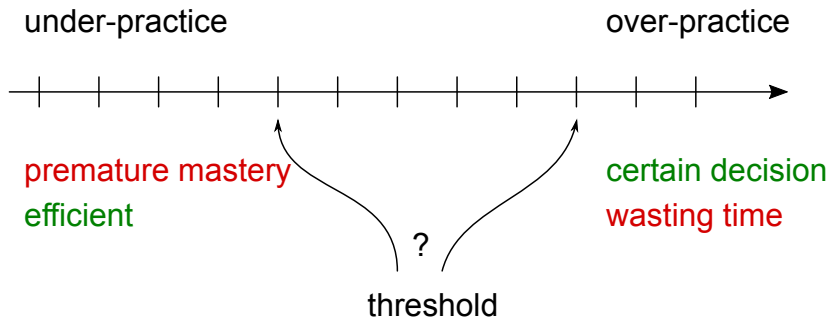
- hard to decide what to use
- easy to change in real systems
- significant impact on users

Mastery Criteria

- N consecutive correct (NCC)
- moving average
 - moving window
 - exponential moving average (EMA)
- based on learner model – threshold rule
 - Bayesian knowledge tracing (BKT)
 - logistic models

Evaluation, Thresholds

evaluation difficult, no clear “correct decisions”



Questions

- Which criterion to use?
- Does the use of learner modeling bring advantage?
- How to evaluate mastery criteria?
- How to choose thresholds?

Evaluation: Data

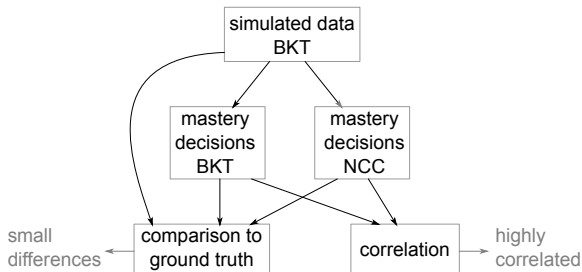
- simulated data
 - simplified
 - ground truth available
- real data
 - realistic
 - difficult evaluation

Results

- learner models are not fundamental
- the choice of thresholds and input data is more important
- exponential moving average is a convenient approach

Importance of Learner Models: BKT vs NCC

Bayesian knowledge tracing (BKT) vs N consecutive correct (NCC)



Even under optimistic setting, the learner model does not provide fundamental advantage over a very simple mastery criterion.

Importance of Learner Models: Input Data

real data (adaptive practice of mathematics)

	logistic learner model	exponential moving average	
correctness	M1	M2	less correlated
correctness + response time	M3	M4	

highly
correlated

Exponential Moving Average

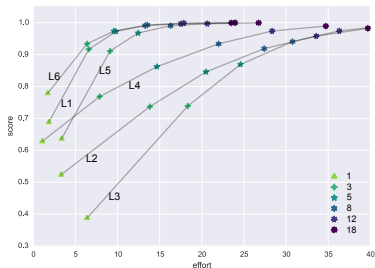
flexible, sufficiently powerful:

- two parameters: decay, threshold
- by tuning these parameters it can fit many circumstances

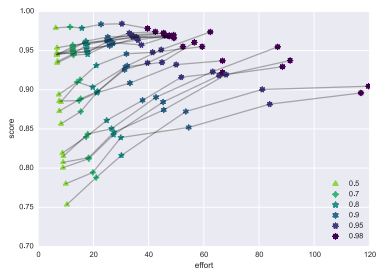
Effort-score graphs

Visualizing the trade-off

NCC for simulated data



EMA for real data



Summary and Future Work

Use simple criteria, focus on input data and thresholds, not on models.

limitations and future work:

- multiple knowledge components
- wheel-spinning students
- forgetting
- partial credit