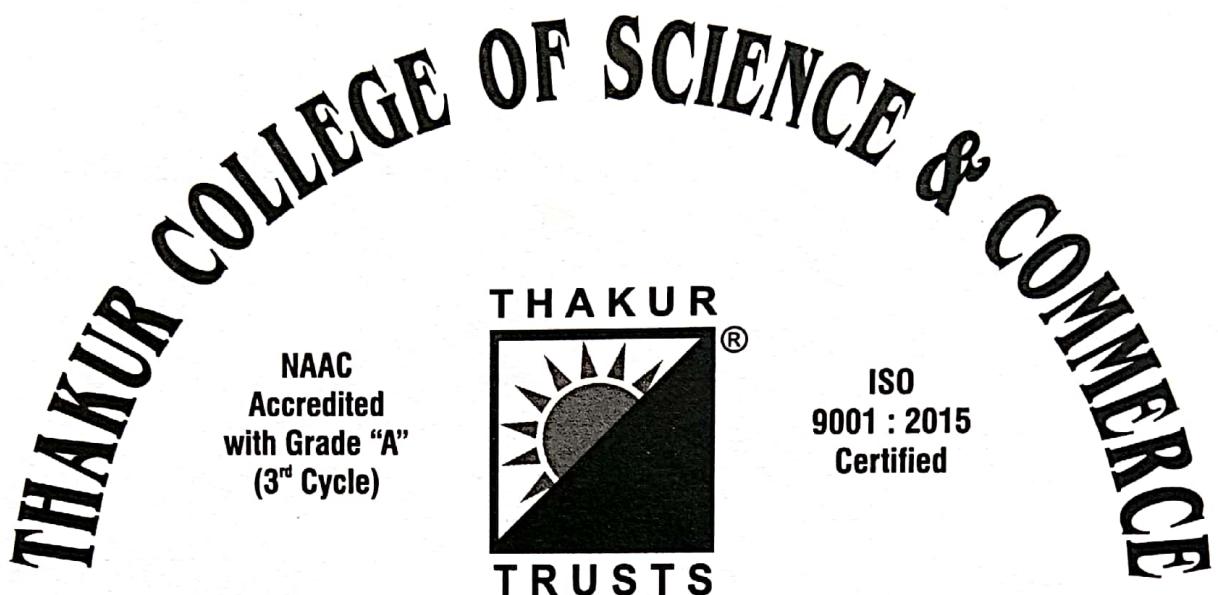


PERFORMANCE

| Term | Remarks | Staff Member's Signature |
|------|----------|--------------------------|
| I | Complete | P.M. |
| II | Complete | Ch. (613) no |

Exam Seat No. _____



Degree College
Computer Journal
CERTIFICATE

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Class F-YBSC Roll No. 1755 Year 2019-20

This is to certify that the work entered in this journal
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who has worked for the year 2019-20 in the Computer
Laboratory.

Teacher In-Charge

Head of Department

Date : 14/03/20

Examiner

★ ★ INDEX ★ ★

PRACTICAL - 01

Aim: Basics of R software.

- 1) R is a software for statistical analysis and data computing.
- 2) It is an effective data handling software and outcome storage is possible.
- 3) It is capable of graphical display.
- 4) It is a free software.

Q.1) Solve the followings:

$$\begin{aligned} & 4+6+8 \div 2-50+9 \\ & > 4+6+8/2-5 \\ & [1] 9 \end{aligned}$$

$$2) 2^2 + 1 - 31 + \sqrt{45}$$

$$\begin{aligned} & > 2^2 + \text{abs}(-3) + \text{sqrt}(45) \\ & [1] 13.7082 \end{aligned}$$

$$3) 5^3 + 7 \times 5 \times 8 + 46/5$$

$$\begin{aligned} & > 5^3 + 7 * 5 * 8 + 46/5 \\ & [1] 414.2 \end{aligned}$$

4) $\sqrt{4^2 + 5 \times 3 + 7/6}$
 $> \text{sqrt}(4^2 + 5 * 3 + 7/6)$
 [1] 5.671567

5) round off $46 \div 7 + 9 \times 8$
 $> \text{round}(46/7 + 9 * 8)$
 [1] 79

Q.2) a) $> c(2, 3, 5, 7) * 2$ b) $> c(2, 3, 5, 7) * c(2, 3)$
 [1] 46 10 14 [1] 49 10 21

c) $> c(2, 3, 5, 7) * c(2, 3, 6, 2)$ d) $> c(1, 6, 2, 3) * c(-2, -3, -4, -1)$
 [1] 4 9 30 14 [1] -2 -18 -8 -3

e) $> c(2, 3, 5, 7)^2$ f) $> c(4, 6, 8, 9, 4, 5)^n c(1, 2, 3)$
 [1] 4 9 25 49 [1] 4 36 812 9 16 125

g) $> c(6, 2, 7, 5) / c(4, 5)$ ✓
 [1] 1.50 0.40 1.75 1.00

Q.3) $> x = 20$ $> y = 30$ $> z = 2$
 $> x^2 + y^3 + z$

[1] 27402

$> \text{sqrt}(x^2 + y)$

[1] 20.73644

$> x^n z + y^n z$

[1] 1300

Q.4) > x<-matrix(nrow=4, ncol=2, data=c(1, 2, 3, 4, 5, 6, 7, 8))

> x
 [1] [1,] 1 5
 [2,] 2 6
 [3,] 3 7
 [4,] 4 8

Q.5) Find $2x+y$ and $2x+3y$ where $x = \begin{bmatrix} 4 & -2 & 6 \\ 7 & 0 & 7 \\ 9 & -5 & 3 \end{bmatrix}$
 $y = \begin{bmatrix} 10 & -5 & 1 \\ 12 & -4 & 9 \\ 15 & -6 & 5 \end{bmatrix}$

> x<-matrix(nrow=3, ncol=3, data=c(4, 7, 9, -2, 0, -5, 6, 7, 3))

> x
 [1] [1,] 4 -2 6
 [2,] 7 0 7
 [3,] 9 -5 3

> y<-matrix(nrow=3, ncol=3, data=c(10, 12, 15, -5, -4, -6,

> y
 [1] [1,] 10 -5 1

[2,] 12 -4 9
 [3,] 15 -6 5

> x+y

| | [1,] | [2,] | [3,] |
|-------|-------|-------|-------|
| [1,] | 19 | -7 | 13 |
| [2,] | 19 | -4 | 16 |
| [3,] | 24 | -11 | 8 |

SA

> 2*x + 3*y

| | [,1] | [,2] | [,3] |
|------|------|------|------|
| [1,] | 38 | -19 | 33 |
| [2,] | 50 | -12 | 41 |
| [3,] | 63 | -28 | 21 |

Q.6) Marks of statistic of CS Batch A

x = c(58, 20, 35, 24, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 52, 36, 29, 35, 39)

> x = c(data)

> breaks = seq(20, 60, 5)

> a = cut(x, breaks, right = FALSE)

> b = table(a)

> c = transform(b)

> c

| | a | Freq |
|---|----------|------|
| 1 | [20, 25) | 3 |
| 2 | [25, 30) | 2 |
| 3 | [30, 35) | 1 |
| 4 | [35, 40) | 4 |
| 5 | [40, 45) | 1 |
| 6 | [45, 50) | 3 |
| 7 | [50, 55) | 2 |
| 8 | [55, 60) | 4 |

Get

PRACTICAL - 02

TOPIC: Probability distribution.

1) Check whether the followings are p.m.f or not,

| x | $p(x)$ |
|-----|--------|
| 0 | 0.1 |
| 1 | 0.2 |
| 2 | -0.5 |
| 3 | 0.4 |
| 4 | 0.3 |
| 5 | 0.5 |

If the given data is p.m.f then

$$\sum p(x) = 1$$

$$\begin{aligned} \therefore p(0) + p(1) + p(2) + p(3) + p(4) + p(5) &= p(x) \\ &= 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ &= 1.6 \end{aligned}$$

$\therefore p(2) = -0.5$, it can't be a probability mass function

$$\therefore p(x) \geq 0 \quad \forall x$$

2)

| x | 1 | 2 | 3 | 4 | 5 |
|--------|-----|-----|-----|-----|-----|
| $p(x)$ | 0.2 | 0.2 | 0.3 | 0.2 | 0.2 |

The condition for pmf is $\sum p(x) = 1$

So,

$$\begin{aligned} \sum p(x) &= p(1) + p(2) + p(3) + p(4) + p(5) \\ &= 0.2 + 0.2 + 0.3 + 0.2 + 0.2 \\ &= 1.1 \end{aligned}$$

\therefore The given data is not a pmf because $p(x) \neq 1$.

| | | | | | | |
|----|--------|-----|-----|------|------|-----|
| 3) | x | 10 | 20 | 30 | 40 | 50 |
| | $P(x)$ | 0.2 | 0.2 | 0.35 | 0.15 | 0.1 |

The condition for p.m.f. is.

- 1) $P(x) \geq 0 \quad \forall x$ satisfy
- 2) $\sum P(x) = 1$

$$\begin{aligned}\sum P(x) &= P(10) + P(20) + P(30) + P(40) + P(50) \\ &= 0.2 + 0.2 + 0.35 + 0.15 + 0.1 \\ &= 1\end{aligned}$$

\therefore The given data is p.m.f.

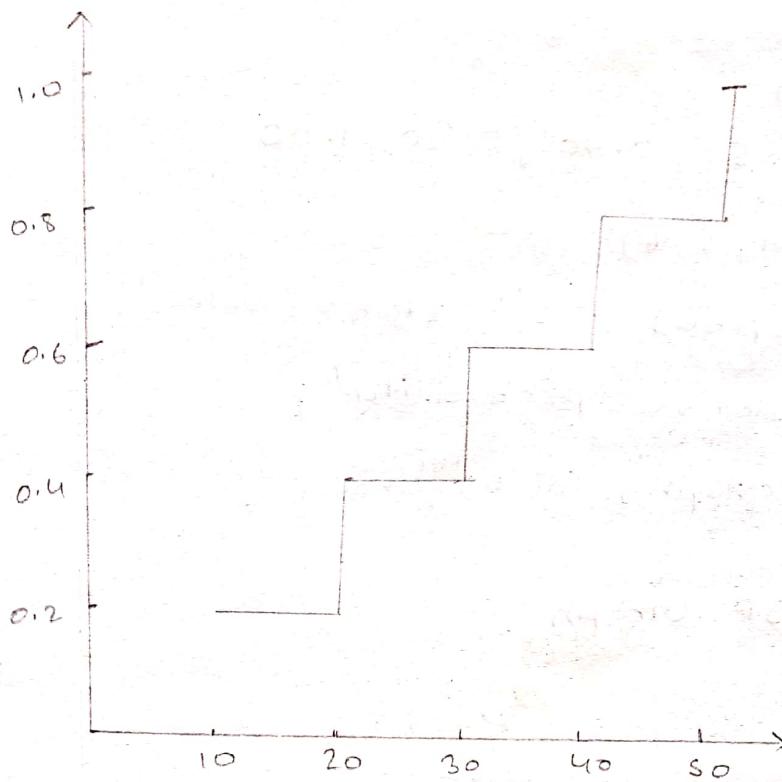
Code:

```
> prob = c(0.2, 0.2, 0.35, 0.15, 0.1)
> sum(prob)
[1] 1
```

Q.2) Find the c.d.f. for the following - p.m.f. and sketch the graph.

| | | | | | |
|--------|-----|-----|------|------|-----|
| x | 10 | 20 | 30 | 40 | 50 |
| $P(x)$ | 0.2 | 0.2 | 0.35 | 0.15 | 0.1 |

$$\begin{aligned}F(x) &= 0 & x < 10 \\ &= 0.2 & 10 \leq x < 20 \\ &= 0.4 & 20 \leq x < 30 \\ &= 0.75 & 30 \leq x < 40 \\ &= 0.90 & 40 \leq x < 50 \\ &= 1.0 & x \geq 50\end{aligned}$$



$\geq x = c(10, 20, 30, 40, 50)$
 $\geq \text{plot}(F(x, \text{cumsum(prob)}), "s")$

Q.3) Find:

| | | | | | | |
|------|------|------|-----|-----|-----|-----|
| x | 1 | 2 | 3 | 4 | 5 | 6 |
| P(x) | 0.15 | 0.25 | 0.1 | 0.2 | 0.2 | 0.1 |

$$\begin{aligned}
 F(x) &= 0 & x < 1 \\
 &= 0.15 & 1 \leq x < 2 \\
 &= 0.40 & 2 \leq x < 3 \\
 &= 0.50 & 3 \leq x < 4 \\
 &= 0.70 & 4 \leq x < 5 \\
 &= 0.90 & 5 \leq x < 6 \\
 &= 1.00 & x \geq 6
 \end{aligned}$$

$\geq \text{prob} = c(0.15, 0.25, 0.1, 0.2, 0.1)$

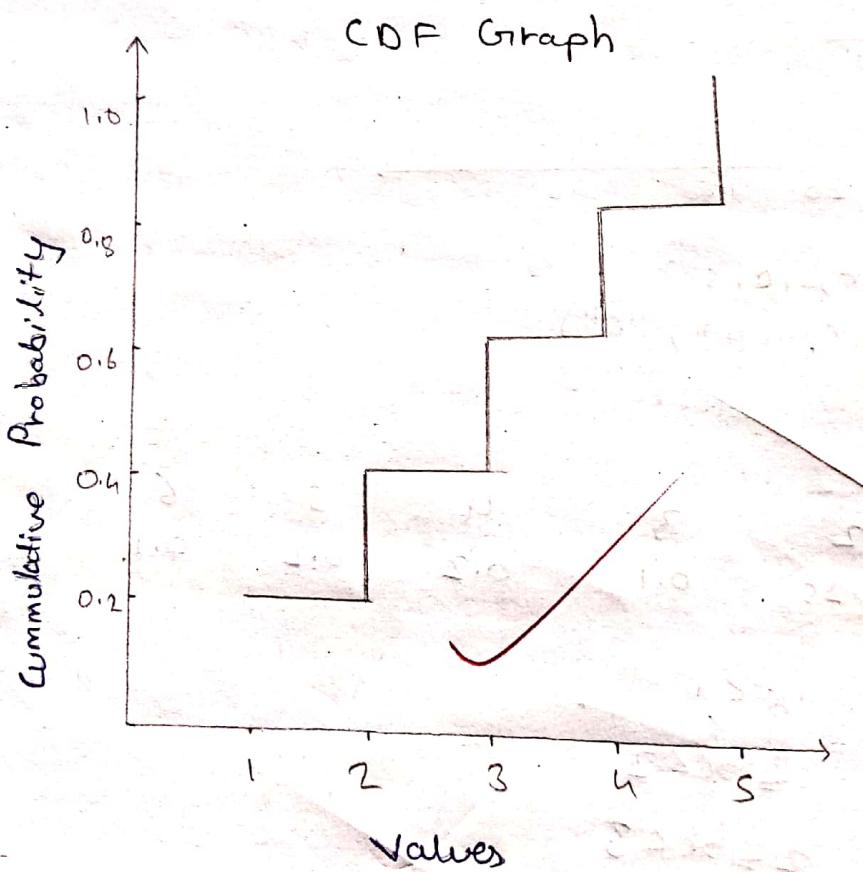
$\geq \text{sum(prob)}$

[1] 1

```

> cumsum (prob)
[1] 0.15, 0.40, 0.50, 0.70, 0.90, 1.00
> x=c(1,2,3,4,5,6)
> plot (x, cumsum (prob), "s", xlab = "value",
       ylab = "cumulative probability",
       main = "CDF graph", col = "brown")

```



Q.4) Check that whether the following is p.d.f. or not.

i) $f(x) = 3 - 2x$; $0 \leq x \leq 1$

ii) $f(x) = 3x^2$; $0 < x < 1$

iii) $f(x) = 3 - 2x$

$$= \int_0^1 f(x) dx$$

$$= \int_0^1 (3 - 2x) dx$$

$$= \Rightarrow \int_0^1 2x^2 dx \left[3x - \frac{2x^2}{2} \right]_0^1$$

$$= 3 - 1$$

$$= 2 \neq 1$$

It is not a pdf.

$$\therefore \int_0^1 f(x) \neq 1$$

ii) $f(x) = 3x^2$

$$\int_0^1 f(x) = 1$$

$$= \int_0^1 3x^2 dx$$

$$= \left[\frac{3x^3}{3} \right]_0^1$$

$$= 1$$

The $\int_0^1 f(x) = 1 \therefore$ It is a pdf.

PRACTICAL - 03

TOPIC : Binomial

$$\# P(X=x) = \text{dbinom}(x, n, p)$$

$$\# P(X \leq x) = \text{pbinom}(x, n, p)$$

$$\# P(X > x) = 1 - \text{pbinom}(x, n, p)$$

If x is unknown

$$P_1 = P(X \leq x) = \text{qbinom}(P_1, n, p)$$

1) Find the probability of exactly 10 success in hundred trials with $p=0.1$.

2) Suppose there are 12 mcq, Each question has 5 options out of which 1 is correct.

- i) Find the probability of having exactly 4 correct answers.
- ii) Atmost 4 correct answers.
- iii) More than 5 correct answers

3) Find the complete distribution when $n=5$ and $p=0.1$.

4) $n=12, p=0.25$, find the following probabilities

- i) $P(X=5)$
- ii) $P(X \leq 5)$
- iii) $P(X > 7)$
- iv) $P(5 < X < 7)$

i) > $x = \text{dbinom}(10, 100, 0.1)$
 > x
 [1] 0.1318653

ii) > $x = \text{dbinom}(4, 12, 0.2)$
 > x
 [1] 0.1328756

iii) > $x = \text{pbinom}(4, 12, 0.2)$
 > x
 [1] 0.9274445

iv) > $1 - \text{pbinom}(5, 12, 0.2)$
 [1] 0.01940528

5) > $x = \text{dbinom}(0:5, 5, 0.1)$
 0 - 0.59049
 1 - 0.32805
 2 - 0.07290
 3 - 0.00816
 4 - 0.00045
 5 - 0.00001

6) i) $\text{dbinom}(5, 12, 0.25)$
 [1] 0.1032414

ii) $\text{pbinom}(5, 12, 0.25)$
 [1] 0.9455918

iii) $1 - \text{pbinom}(7, 12, 0.25)$
 [1] 0.00278151

iv) $\text{dbinom}(6, 12, 0.25)$
 [1] 0.04014945

s> > dbinom(0, 10, 0.15)

[1] 0.1968744

> 1 - pbinom(3, 20, 0.15)

[1] 0.3522748

6> qbinom(0.88, 30, 0.2)

[1] 9

7> > n=10

> p=0.3

> x=0:n

> prob = dbinom(x, n, p)

> compprob = pbinom(x, n, p)

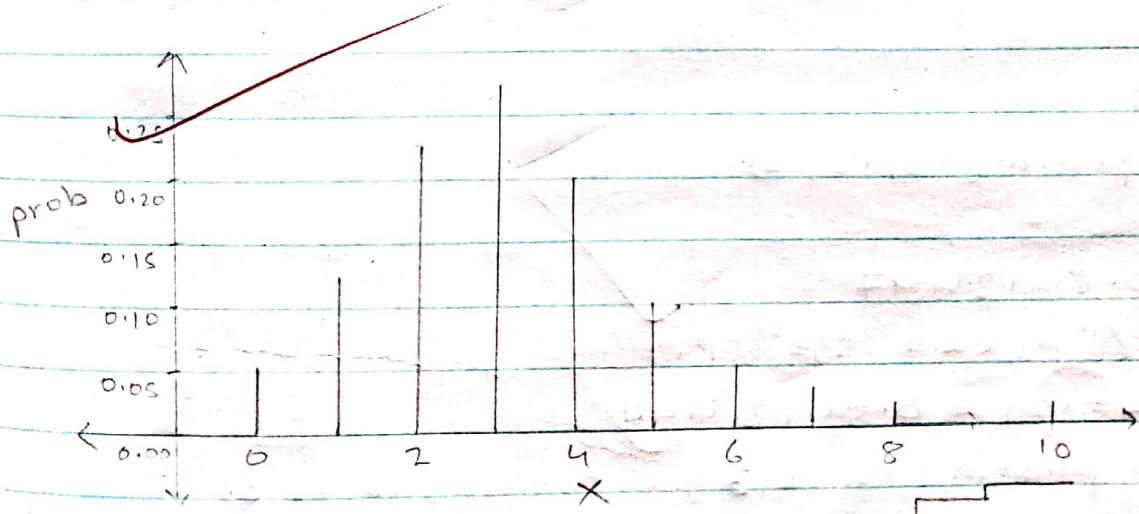
> d = data.frame("x values" = x, "probability" = prob)

> print(d)

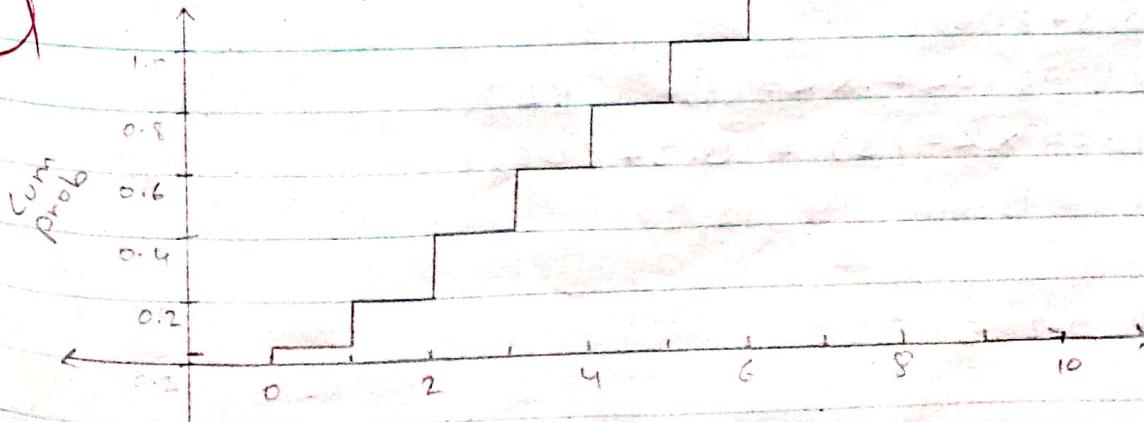
| xvalues | probability |
|---------|-------------|
| 1 | 0.0282 |
| 2 | 0.1210 |
| 3 | 0.2334 |
| 4 | 0.2668 |
| 5 | 0.2001 |
| 6 | 0.1029 |
| 7 | 0.0367 |
| 8 | 0.0090 |
| 9 | 0.0014 |
| 10 | 0.0001 |
| 11 | 0.0000 |

- 5) The probability of a salesman making a sale to customer 0.15. Find the probability of
- No sales out of 10 customers
 - More than 3 sales out of 20 customers.
- 6) A sales man has 20% probability of making a sale to customer. out of 30 customers what minimum number of sales he can make with 88% of probability.
- 7) X follows binomial distribution with $n=10$, $p=0.3$
plot the graph of p.m.f. and c.d.f.

$\rightarrow \text{plot}(x, \text{prob}, "h")$



$\rightarrow \text{plot}(x, \text{cumprob}, "s")$



PRACTICAL-04

Aim: Normal Distribution

- i) $P(x = x) = dnorm(x, \mu, \sigma)$
- ii) $P(X \leq x) = pnorm(x, \mu, \sigma)$
- iii) $P(X > x) = 1 - pnorm(x, \mu, \sigma)$
- iv) To generate random numbers from a normal distribution (n random numbers) the R code is
 $rnorm(n, \mu, \sigma)$

- Q.1) A random variable x follows normal distribution with mean $\mu = 12$ and S.D. $= \sigma = 3$. Find
- i) $P(x \leq 15)$ ii) $P(10 \leq x \leq 13)$ iii) $P(x > 14)$
 - iv) generate 5 observations (random numbers)

Code :

```

> P1 = pnorm(15, 12, 3)
> P1
[1] 0.8413447
> cat ("P(x <= 15) = ", P1)
P(x <= 15) = 0.8413447
> P2 = pnorm(13, 12, 3) - pnorm(10, 12, 3)
> P2
[1] 0.3780661
> cat ("P(10 <= x <= 13) = ", P2)
P(10 <= x <= 13) = 0.3780661
> P3 = 1 - pnorm(14, 12, 3)
> P3
[1] 0.2524925

```

> cat ("P(X>14) = ", p3)

$$P(X>14) = 0.2524925$$

> pu = rnorm (5, 12, 3)

> pu

[1] 15.254723 16.548805 11.280815 6.419944 12.272460

Q.2) X follows normal distribution with $\mu=10$, $\sigma=2$

Find i) $P(X \leq 7)$ ii) $P(5 < X < 12)$ iii) $P(X > 12)$

iv) Generate 10 observations

v) Find k such that $P(X < k) = 0.4$

Code:

> a1 = pnorm (7, 10, 2)

> a1

[1] 0.668072

> a2 = rnorm (5, 10, 2) - rnorm (12, 10, 2)

> a2

[1] 0.8381351

> a3 = 1 - pnorm (12, 10, 2)

> a3

[1] 0.1886553

> a4 = rnorm (10, 10, 2)

> a4

[1] 11.608931 9.920417 12.637741 8.073354

8.721386 9.193726 9.366824 11.707106

9.537584 10.715006

> a5 = qnorm (0.4, 10, 2)

> a5

[1] 9.493306

Q.3) Generate 5 random numbers from a normal distribution $\mu=15$, $\sigma=4$. Find sample mean, median, s.d and print it.

Code:

```
> rnorm(15, 15, 4)
[1] 10.7649 7.793249 9.953444 13.345904
   17.509668

> am = mean(x)
> am
[1] 11.87345

> cat("Sample mean is = ", am)
Sample mean is = 11.87345

> me = median(x)
> me
[1] 10.76499

> cat("Median is = ", me)
Median is = 10.76499.

> n = 5
> v = (n - 1) * var(x) / n
> v
[1] 11.09965

> sd = sqrt(v)
```

✓

```
> sd
[1] 3.33163

> cat("S.D. is = ", sd)
S.D. is = 3.331613
```

Q.4) $X \sim N(30, 100)$, $\sigma = 10$

i) $P(X \leq 40)$

ii) $P(X > 35)$

iii) $P(25 < X < 35)$

iv) Find K such that $P(X < K) = 0.6$

> f1 = pnorm(40, 30, 10)

> f1

[1] 0.8413447

> f2 = 1 - pnorm(35, 30, 10)

> f2

[1] 0.3085375

> f3 = pnorm(25, 30, 10) - pnorm(35, 30, 10)

> f3

[1] -0.3829249

> f4 = qnorm(0.6, 30, 10)

> f4

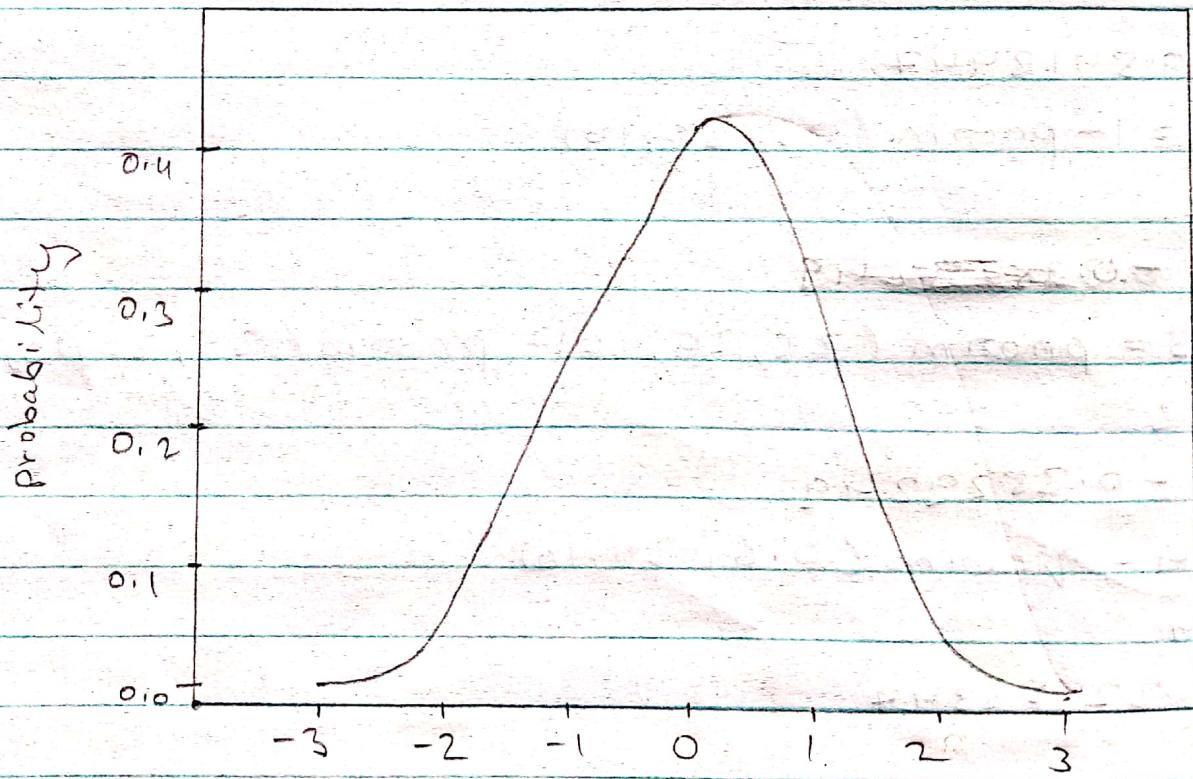
[1] 32.53347

Q.s) Plot the standard normal graph.

```
> xc = seq(-3, 3, by = 0.1)
```

```
> y = dnorm(xc)
```

```
> plot(xc, y, xlab = "x values", ylab = "probability",  
main = "standard normal graph")
```



Q87

PRACTICAL - 05

TOPIC: Normal and t -test.

$$1) H_0: \mu = 15 \quad H_1: \mu \neq 15$$

\nwarrow null \swarrow alternative

Test the hypothesis

Random sample of size 400 is drawn and it is calculated. The sample mean is 14 and S.O. is 3. Test the hypothesis at 5% level of significance.

0.05 > accept the value

0.05 < Less then Reject

> $m_0 = 15$

> $m_x = 14$

> $s_d = 3$

> $n = 400$

> $z_{\text{cal}} = (m_x - m_0) / (s_d / \sqrt{n})$

> z_{cal}

[1] - 6.666667

> cat ("calculated value of z is = ", z_{cal})

Calculated value of z is = -6.666667

> pvalue = 2 * (1 - pnorm(abs(z_{cal})))

> pvalue

[1] 2.616796e-11

\therefore The value is less than 0.05 we will reject the value of $H_0: \mu = 15$.



2) Test the hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$
A random sample size of 400 is drawn with
sample mean = 10.2 and $S.D. = 2.25$,
Test the hypothesis at

```

> m0 = 10
> n = 400
> mx = 10.2
> sd = 2.25
> zcal = (mx - m0) / (sd / (sqrt(n)))
> zcal
[1] 1.77778
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.07544036
∴ The value pvalue is greater than 0.05
∴ The value is accepted.

```

3) Test the hypothesis H_0 : preparation of smokers
is college is 0.2. A sample is collected
and calculated the sample proportional as
0.125. Test the hypothesis at 5% level of
significance (sample size is 400)

```

> p = 0.2
> p = 0.125
> n = 400
> q = 1 - p
> zcal = (p - q) / (sqrt(p * q / n))
> cat ("Calculated value of z is = ", zcal)
[1] Calculated value of z is = -3.75
> pvalue = 2 * (1 - pnorm(abs(zcal)))
> pvalue
[1] 0.0001768346 (Reject)

```

4) Last year farmer's lost 20% of their crops. A random sample of 60 fields are collected. And it is found that a field crops are insect polluted. Test the hypothesis at 1% level of significance.

> p = 0.2

> p = 9 / 60

> n = 60

> zcal = (p - P) / (sqrt(p * q / n))

> zcal

[1] -0.9682458

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.3329216

" The value is 0.01. So value is accepted.

5) Test the hypothesis $H_0: \mu = 12.5$ from the following sample at 5% level of significance.

> x = c(12.25, 11.97, 12.15, 12.08, 12.31, 11.94, 11.89, 12.16,

> n = length(x) ✓ 12.04

> n

[1] 10

> mx = mean(x)

> mx

[1] 12.107

> variance = (n - 1) * var(x) / n

> variance

[1] 0.019521

> sd = sqrt(variance)

> sd

[1] 0.1387176

> mo = 12.5

> t = (mx - mo) / (sd / sqrt(n))

> t

[1] 8.894909

> pvalue = 2 * (1 - pnorm(abs(t)))

> pvalue

[1] 0

∴ The value is less than 0.05 the
value is accepted.

8



PRACTICAL - 06

Aim: Large Sample test

- 1) Let the population mean (the amount spent per customer in a restaurant) is 250. A sample of 100 customers selected the sample mean is calculated as 275 and S.D 30. Test the hypothesis that the population mean is 250 or not on 5% level of significance.

Solⁿ; > $m_0 = 250$

> $m_x = 275$

> $s_d = 30$

> $n = 100$

> $z_{cal} = (m_x - m_0) / (s_d / \sqrt{n})$

> cat("calculated values of z is", "z_{cal}")

[1] Calculated value of z is 8.333333

> pvalue = 2 * (1 - pnorm(abs(z_{cal}))

> pvalue

[1] 0

\because The value is less than 0.05 we will reject the value of the $H_0 = \mu = 250$.

- 2) In a random sample of 1000 students it is found that 750 use blue pen. test the hypothesis that the population proportion is 0.8 at 1% level of significance.

Solⁿ; > $p = 0.8$

> $q = 1 - p$

> $p = 750 / 1000$

> $n = 1000$

> $z_{cal} = (p - p) / (\sqrt{p * q / n})$

> cat("calculated value of z is", "z_{cal}")

> cat("calculated value of z is", "-3.452847")

[1] calculated value of z is -3.452847

28
> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 7.72268e-05

i) The value is less than 0.01. we reject!

3) To. random sample of size 1000 & 2000 are drawn from two population with same s.d 2.5. The sample means are 67.5 and 68. Test the hypothesis. $H_0: \mu_1 = \mu_2$ at 5% level of significance.

> n1 = 1000

> n2 = 2000

> m1 = 67.5

> m2 = 68

> sd1 = 2.5

> sd2 = 2.5

> zcal = (m1 - m2) / sqrt((sd1^2/n1) + (sd2^2/n2))

> zcal

[1] -5.163978

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 2.417564e-07 \therefore (Rejected)

4) A study of noise level in 2 hospital is given below test the claim that 2 hospital have same level of noise at 1% level of significance.

| Hos.A | Hos.B |
|-------|-------|
| 84 | 34 |
| 61.2 | 59.4 |
| 7.9 | 7.5 |

$$>n_1 = 84$$

$$>n_2 = 34$$

$$>\bar{x}_1 = 61.2$$

$$>\bar{x}_2 = 59.4$$

$$>sd_1 = 7.9$$

$$>sd_2 = 7.5$$

$$>z_{\text{cal}} = (\bar{x}_1 - \bar{x}_2) / \sqrt{(\frac{sd_1^2}{n_1} + \frac{sd_2^2}{n_2})}$$

$$>z_{\text{cal}}$$

$$[1] 1.162528$$

>pvalue

$$[1] 0.2456211$$

\therefore The value is greater than 0.01 we accept the value.

- 5) In a sample of 600 students is ~~clg~~ 400 used Blue ink. In another clg from a sample of 900 students 450 use blue ink. Test the hypothesis that the preparation of students using blue ink in two colleges are equal or not at 1% level of significance.

$H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$>n_1 = 600$$

$$>n_2 = 400$$

$$>p_1 = 400/600$$

$$>p_2 = 450/900$$

$$>p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$>p$$

$$[1] 0.566067$$

$$> q = 1 - p$$

$$> q$$

[1] 0.4333333

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}}$$

[1] 6.381834

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> pvalue$$

[1] 1.753222e-10

\because Value is less than 0.01 the value is rejected.

6) $H_0: p_1 = p_2$ against $H_1: p_1 \neq p_2$

$$> n_1 = 200$$

$$> n_2 = 200$$

$$> p_1 = 44/200$$

$$> p_2 = 30/200$$

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

[1] 0.185

$$> q = 1 - p$$

$$> q$$

[1] 0.815

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}}$$

[1] 1.802741

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

$$> pvalue$$

[1] 0.0714288

\therefore Accept \because greater than 0.05.

PRACTICAL - 07

TOPIC: Small Sample Test

Q.1) The marks of 10 students are given by
63, 63, 66, 67, 68, 69, 70, 70, 71, 72
Test the hypothesis that the sample comes from a population with average marks 66.

$$\text{Sol}^n: H_0: \mu = 66$$

> $x_c = c(63, 63, 66, 67, 68, 69, 70, 70, 71, 72)$

> t.test(x_c)

one sample t-test

data: x_c

t = 6.8319, df = 9, p-value = 1.558e-13
alternative hypothesis: true mean is not equal to 66 percent confidence interval:

65.65171 70.14829

Sample estimates:

mean of x_c

67.9

Since p-value is less than 0.05

we reject hypothesis at 5%

level of significance

> los = 0.05

> pvalue = 1.558e-13

> if (pvalue > los) { cat("accept H_0") }

else { cat("reject H_0") }

reject H_0 >

Q.2) Two groups of students score the following marks : ~~H0~~ test the hypothesis that there is no significance difference between the two groups.
 group 1 = 18, 22, 21, 17, 20, 17, 23, 20, 22, 21
 group 2 = 16, 20, 14, 21, 20, 18, 13, 15, 17, 21

Soln: H_0 : There is no difference between two groups.
 > $x = c(18, 22, 21, 17, 20, 17, 23, 20, 22, 21)$
 > $y = c(16, 20, 14, 21, 20, 18, 13, 15, 17, 21)$
 > $t.test(x, y)$

Welch Two Sample t-test

data: x and y

$t = 2.2513$, $df = 16.316$, p-value = 0.03798

alternative hypothesis: true difference means it is not equal to 0.

95 percent confidence interval:

0.1628205 5.0371795

Sample estimates:

mean of x mean of y :

20.1 17.5

> pvalue = 0.03798
 > if (pvalue > 0.05) { cat("accept H₀") }
 else { cat("reject H₀") }

reject H₀)

Since p-value is less than 0.05 we

reject hypothesis at 5% level of significance.

Q3)

The sales data of 6 shops before and after a special campaign are given below:

Before : 53, 28, 31, 48, 50, 42

After : 58, 29, 30, 55, 56, 45

Test the hypothesis that the campaign is effective or not.

Soln) H_0 : There is no significant difference of sales before and after the campaign.

> $x = c(53, 28, 31, 48, 50, 42)$

> $y = c(58, 29, 30, 55, 56, 45)$

> $t\text{-test}(x, y, \text{paired} = T, \text{alternative} = \text{"greater"})$

Paired t-test

data : x and y

$t = -2.7815$, $df = 5$, $p\text{-value} = 0.0806$

alternative hypothesis : true difference in mean is greater than 0.

95 percent confidence interval

-6.035547 in

Sample estimates :

mean of the difference

-3.5

> $p\text{value} = 0.0806$

> $\text{if}(p\text{value} > 0.05) \{ \text{cat}(\text{"accept } H_0") \}$

else $\{ \text{cat}(\text{"reject } H_0") \}$

accept H_0

since p-value is greater than 0.05 we accept hypothesis at 5% level of significance.

Q.4) Two medicines are applied to the two groups of patient respectively. 56

group 1: 10, 12, 13, 11, 14

group 2: 8, 9, 12, 14, 15, 10, 9.

Is there any significant difference between two medicines.

Soln: H_0 : There is no significant difference between two medicines of two groups

> x = c(10, 12, 13, 11, 14)

> y = c(8, 9, 12, 14, 15, 10, 9)

> t.test(x, y)

welch two sample t-test

data: x and y

~~t = 0.80384, df = 9.7594, p-value = 0.4406~~

alternative hypothesis: true difference in mean is not equal to 0.

95 percent confidence interval:

-1.781171 3.781171

Sample estimates:

Mean of x and y:

12 11

> pvalue = 0.4406

> if(pvalue > 0.05) { cat("accept H₀") }

else { cat("reject H₀") }

accept H₀ >

Since the p-value is greater than 0.05 we accept the hypothesis at 5% level of significance.

Q.s) The following are ~~the~~ the weight before and after the diet program. Is the diet program effective.

Before : 120, 125, 115, 130, 123, 119

After : 100, 114, 95, 90, 115, 99.

Solⁿ: H_0 : There is no significant difference

$\gt c = c(120, 125, 115, 130, 123, 119)$

$\gt y = c(100, 114, 95, 90, 115, 99)$

$\gt t.test(c, y, paired = T, alternative = "less")$

Paired t-test

data: c and y

$t = 4.3458$, $df = 5$, $p\text{-value} = 0.9963$

alternative hypothesis: true difference in means is less than 0.

95 percent confidence interval:

Inf 29.0295

Sample estimates:

mean of the differences

19.8333

$\gt pvalue = 0.9963$

$\gt \text{if}(pvalue > 0.05) \{ \text{cat}("accept } H_0") \}$

$\gt \text{else} \{ \text{cat}("reject } H_0") \}$

accept H_0

Since the p-value is greater than 0.05 we accept the hypothesis at 5% level of significance.

Q.

Topic : Large and Small Sample tests

Q.1) The arithmetic mean of a sample of 100 items from a large population is 52. If the standard deviation is 7, test the hypothesis that the population mean is 55 against the alternative it is more than 55 at 5% LOS.

$$\text{Soln: } H_0: \mu = 55$$

$$H_1: \mu \neq 55$$

$$> n = 100$$

$$> m_{sc} = 52$$

$$> m_o = 55$$

$$> sd = 7$$

$$> z_{cal} = (m_{sc} - m_o) / (sd / (\sqrt{n}))$$

$$> z_{cal}$$

$$[1] -4.285714$$

> cat "calculated z value is = " z_{cal}
calculated z value is = -4.285714

$$> pvalue = z * (1 - pnorm (abs (z_{cal})))$$

$$> pvalue$$

$$[1] 1.82133e-05$$

Since p value is less than 0.05 we reject the hypothesis at 5% LOS.

Q.2) In a big city 350 out of 700 males are found to be smokers. Does the information supports that exactly half of the males in the city are smokers? Test at 1% LOS.

Solⁿ: $H_0: \mu$

$$> P = 0.5$$

$$> Q = 1 - P$$

$$> P = 350/700$$

$$> n = 700$$

$$> z_{\text{cal}} = (P - P) / (\sqrt{P * Q/n})$$

> (at " calculated z value is = ", z_{cal})

calculated z value is = 0

$$> p_{\text{value}} = 2 * (1 - \text{pnorm}(\text{abs}(z_{\text{cal}})))$$

> p_{value}

[1]

Since p_{value} is greater than 0.05 we accept hypothesis at 1% LOS.

Q.3) Thousand articles from a factory A are found to have 2% defectives, 1500 articles from a 2nd factory B are found to have 1% defective. Test at 5% LOS that the two factories are similar or not.

Solⁿ: $H_0: P_1 = P_2$ as $H_1: P_1 \neq P_2$

$$> n_1 = 1000$$

$$> n_2 = 1500$$

$$> p_1 = 0.02$$

$$> p_2 = 0.01$$

22

$$> p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$> p$$

$$[1] 0.014$$

$$> q = 1 - p$$

$$> q$$

$$[1] 0.986$$

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> p$$

$$[1] 0.014$$

$$> q = 1 - p$$

$$> q$$

$$[1] 0.986$$

$$> z_{\text{cal}} = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$> z_{\text{cal}}$$

$$[1] 2.084842$$

~~> cat("Calculated z value is ", zcal)~~

~~Calculated z value is = 2.084842~~

$$> pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$> pvalue$$

$$[1] 0.03708364$$

Since pvalue is less than 0.05 we
reject the hypothesis at 5%
level of significance.

Q.4) A sample of size 400 was drawn at a sample mean is 99. Test at 5% LOS that the sample comes from a population with mean 100 and variance 64.

Soln:

$$H_0: \mu = 100$$

$$> msc = 99$$

$$> mo = 100$$

$$> sd = 8$$

$$> n = 400$$

$$> zcal = (msc - mo) / (sd * (\text{sqrt}(n)))$$

$$> zcal$$

$$[1] -2.5$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(zcal)))$$

$$> pvalue$$

$$[1] 0.01241933$$

Since pvalue is less than 0.05 we reject the hypothesis at 5% LOS.

Q.5)

The flower stems are selected and the heights are found to be (cm) 63, 63, 68, 69, 71, 72 test the hypothesis that the mean height is 66 or not at 1% LOS.

Sol:

$$H_0: \mu = 66$$

$$> x = (63, 63, 68, 69, 71, 72)$$

$$> t.test(x)$$

one sample t-test

data: x

$t = 47.94$, df = 6, p-value = 5.522×10^{-9}
 alternative hypothesis: true mean is
 not equal to 0.

as percent confidence interval:

64.66479

71.62092

Sample estimates:

mean of \bar{x}

68.14286

Since pvalue is less than 0.05 we
 reject hypothesis at 1% level of
 significance.

Q.6} Two ~~random samples~~ were drawn from
 2 normal populations and their values are
 A - 66, 67, 75, 76, 82, 84, 88, 90, 92
 B - 64, 74, 78, 82, 85, 87, 92, 93, 95, 97
 Test whether the population have the
 same variance of 5% .

Solⁿ: $H_0: \sigma^2_1 = \sigma^2_2$

>> $x = c(66, 67, 75, 76, 82, 84, 88, 90, 92)$
 > $y = c(64, 74, 78, 82, 85, 87, 92, 93, 95, 97)$

> var.test(>x, y)

F test to compare two variance
 data: \bar{x} and y

$F = 0.70686$, num df = 8, denom df = 10,
 p value = 0.6359

60

alternative hypothesis : true ratio of variances is not equal to 1.

as percent confidence interval ;

0.1833662

3.0360393

Sample of variance

0.7068567

$\Rightarrow p\text{value} = 0.6359$

$\Rightarrow \text{if } (\text{pvalue} > 0.05) \{ \text{cat}(\text{"accept } H_0") \}$
 $\quad \quad \quad \text{else } \{ \text{cat}(\text{"reject } H_0") \}$

accept H_0 \Rightarrow

Since p-value is greater than 0.05

we accept hypothesis at 5% LOS.

Q.77 A company producing light bulbs finds that mean life span of the population of bulbs is 1200 hours with s.d. 125.

A sample of 100 bulbs have mean 1150 hours.

Test whether the difference between population and sample mean is significantly different?

Soln: $H_0: \mu = 1200$

$\Rightarrow m_0 = 1200$

$\Rightarrow m_{sc} = 1150$

$\Rightarrow n = 100$

$\Rightarrow s_d = 125$

$\Rightarrow z_{\text{cal}} (m_{sc} - m_0) / (s_d / (\sqrt{n}))$

$\Rightarrow \text{cat}(\text{"Calculated z value is = "}, z_{\text{cal}})$

Calculated z value is = -4.

Q.8

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(z(\text{cal}))))$
[1] 6.334248e-05

Since pvalue is less than 0.05 we
reject hypothesis.

Q.8) From each of two consignments of apples, a sample of size 200 is drawn and number of bad apples are counted. Test whether the proportion of rotten apples in two assignments are significantly different at 1% LOS?

| | Sample Size | No. of bad apples |
|---------------|-------------|-------------------|
| Consignment 1 | 200 | 64 |
| Consignment 2 | 300 | 56 |

Soln: $H_0: \mu = P_1 \neq P_2$

> n1 = 200

> n2 = 300

> p1 = 64/200

> p2 = 56/300

> p = $(n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$

> p

[1] 0.2

> q = 1 - p

> zcal = $(p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$

> zcal

[1] 0.9128709

```
> cat("Calculated z value is ", zcal)
Calculated z value is = 0.9128709
> pvalue = 2 * (1 - pnorm (abs (z(cal))))
> pvalue
[1] 0.3613104
```

Since pvalue is greater than 0.05 we accept the hypothesis.

Practical - 09

TOPIC: Chi-square Test & Anova

Q.1) Use the following data to test whether the condition of the home and condition of child are independent or not.

| | clean | dirty |
|--------------|-------|-------|
| clean | 70 | 50 |
| fairly clean | 80 | 20 |
| dirty | 35 | 45 |

Soln: H_0 : Condition of home and child are independent.

> $x = c(70, 80, 35, 50, 20, 45)$

> $m = 3$

> $n = 2$

> $y = \text{matrix}(x, nrow = m, ncol = n)$

> y

| | [1] | [2] |
|-----|-----|-----|
| [1] | 70 | 50 |
| [2] | 80 | 20 |
| [3] | 35 | 45 |

> $p = \text{chisq.test}(y)$

> p

Pearson's Chi-square test.

62

data: y

$$\chi^2 = 25.646, df = 2, p\text{-value} = 2.698e-$$

pvalue is less than 0.05 we reject the hypothesis at 5% level of significance.

Q.2) Test the hypothesis that ~~the~~ the vaccination and the disease are independent or not.

| | Aff. | Not aff. |
|---------|------|----------|
| Disease | | |
| Aff. | 70 | 46 |
| N.A. | 35 | 37 |

Soln: H_0 : Disease and vaccination are independent.

$$> x = c(70, 35, 46, 37)$$

$$> m = 2$$

$$> n = 2$$

$$> y = \text{matrix}(x, \text{row}=m, \text{ncol}=n)$$

$$\begin{bmatrix} [1,1] & [1,2] \\ [2,1] & [2,2] \end{bmatrix}$$

$$[1,1] 70 46$$

$$[2,1] 35 37$$

$$> pv = \text{chisq.test}(y)$$

$$> pv$$

28

data: y

χ^2 -squared = 2.0275, df = 1, p-value = 0.1545

∴ Pvalue is more than 0.05 we accept the hypothesis at 5% level of significance.

Q.3) Perform a ANOVA for the following data.

Type observation

A 50, 52

B 53, 55, 53

C 60, 58, 57, 56

D 52, 54, 54, 55

Solⁿ: H₀: The mean's are equal for A, B, C, D

> x1 = c(50, 52)

> x2 = c(53, 55, 53)

> x3 = c(60, 58, 57, 56)

> x4 = c(52, 54, 54, 55)

> d = stack(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4))

> names(d)

[1] "values" "ind"

> oneway.test(values ~ ind, data = d,

var.equal = T)

One-way ANOVA

One-way analysis of means

data: values and ind

$F = 11.735$, numdf = 3, denom df = 9,

pvalue = 0.00183

```
> anova = aov(values ~ ind, data = cl)
```

```
> summary(anova)
```

| | DF | Sum Sq | Mean Sq | F value | Pr(>F) |
|-----------|----|--------|---------|---------|------------|
| ind | 3 | 71.06 | 23.688 | 11.73 | 0.00183 ** |
| Residuals | 9 | 18.17 | 2.019 | | |

Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ''

Since p value is less than 0.05 we

reject the hypothesis at 5% level of significance.

Q4) The following data gives the life of tyres of four brands.

| Type | life |
|------|----------------------------|
| A | 20, 23, 18, 17, 18, 22, 24 |
| B | 19, 15, 17, 20, 16, 17 |
| C | 21, 19, 22, 17, 26 |
| D | 18, 14, 16, 18, 14, 16 |

Q8
Solⁿ: H₀: The average life of tyre is equal for (A, B, C, D)

```
> x1 = c(20, 23, 18, 17, 18, 22, 24)
> x2 = c(19, 15, 17, 20, 16, 17)
> x3 = c(21, 19, 22, 17, 20)
> x4 = c(15, 14, 16, 18, 14, 16)
> d = stack(list(b1 = x1, b2 = x2,
+ b3 = x3, b4 = x4))
> names(d)
[1] "values" "ind"
> oneway.test(values ~ ind, data=d,
+ var.equal= T)
```

One-way analysis of means

data: values and ind
 $F = 6.8445$, num df = 3, denom df = 20,
p-value = 0.002349.

Since p value is less than 0.05 we reject the ~~importance~~ hypothesis at 5% level of significance.

R> Import excel file in R software

```
soln: >xl=read.csv("C:/users/admin/Desktop/marks.csv")
> print(xl)
```

| | stats | Maths |
|----|-------|-------|
| 1 | 40 | 60 |
| 2 | 45 | 48 |
| 3 | 42 | 47 |
| 4 | 15 | 20 |
| 5 | 37 | 25 |
| 6 | 36 | 27 |
| 7 | 49 | 57 |
| 8 | 59 | 58 |
| 9 | 20 | 25 |
| 10 | 27 | 27 |

> am = mean(x\$stats)

> am

[1] 37

> me = median(x\$stats)

> me

[1] 38.5

> n = length(x\$stats)

> sd = sqrt((n-1) * var(x\$stats)/n)

> sd

[1] 12.64911

> am = mean(x\$maths)

> am

* [1] 39.4

> me = median(x\$maths)

> me

[1] 37

> n = length(x\$maths)

> sd = sqrt((n-1) * var(x\$maths)/n)

> sd

[1] 15.2

> cor(x\$stats, x\$maths)

[1] 0.830618

6

TOPIC: Non - Parametric Test

Q.1) Following are the amount of sulphur oxide emitted by a industry in 20 days. Apply sign test, to test the hypothesis that the population median is 21.5 at 5% level of significance.

17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26.

Sol: H_0 : Population median is 21.5

$\gg c = \{17, 15, 20, 29, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26\}$

$\gg me = 21.5$

$\gg sp = \text{length}(\{c[c > me]\})$

$\gg sn = \text{length}(\{c[c < me]\})$

$\gg n = sp + sn$

$\gg n$

[1] 20

$\gg pv = \text{pbinom}(sp, n, 0.5)$

$\gg pv$

[1] 0.4119015

Since pvalue is more than 0.05 we accept the hypothesis at 5% level of significance.

If the alternative (H_1) not equal to ($H_1 \neq$ ve)
 $(<)$ then $pv = \text{pbinom}(sp, n, 0.5)$ and if
 $H_1 > me$ then $pv = \text{binom}(sn, n, 0.5)$.

Q.2) Following is data obtained observations apply sign test to the hypothesis that the population median is ~~620~~ 625 against the alternative it is more than 625.

612, 619, 631, 628, 643, 640, 655, 649, 670, 663.

Solⁿ: H_0 : population median is 625.

$$> x = \{612, 619, 631, 628, 643\}$$

$$> m_e = 625$$

$$> s_p = \text{length}(\{x | x > m_e\})$$

$$> s_n = \text{length}(\{x | x < m_e\})$$

$$> n = s_p + s_n$$

$$> n$$

$$[1] 10$$

$$> p_v = \text{binom}(s_n, n, 0.5)$$

$$> p_v$$

$$[1] 0.0546875$$

Since pvalue is greater than 0.05 we accept the hypothesis at 5% level of significance.

Q.3) Following are values of a sample test the hypothesis that the population median is 60 against the alternative it is more than 60. at 5% level of significance using wilcoxon signed Rank Test.

63, 65, 60, 89, 61, 71, 58, 51, 69, 62,
63, 39, 72, 69, 48, 66, 72, 63, 87, 69.

Solⁿ: H_0 : population median = 60

H_1 : population median > 60

$\gg c = \text{c}(63, 65, 60, 89, 61, 71, 58, 51, 69,$
 $62, 63, 39, 72, 69, 48, 66, 72,$
 $63, 87, 69)$

~~$\gg \text{wilcox.test}(c, \text{alter} = "greater", \text{mu} = 60)$~~

wilcoxon signed Rank Test

with continuity correction

data: c

V = 145, p-value = 0.02298

alternative hypothesis: true location
is greater than 60.

Note: If the alternative is less than ($\text{alter} = "less"$) and if alternative is not equal then ($\text{alter} = "two.sided"$).

Since pvalue is less than 0.05 we reject the hypothesis at 5% level of significance.

Q.4) Using WSR test
population median is 12 or less than 12.
15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26

Soln: H_0 : population median is 12.

H_1 : population median < 12

$\gt c = c(15, 17, 24, 25, 20, 21, 32, 28, 12, 25, 24, 26)$

$\gt wilcox.test(c, alter = "less", mu = 12)$

wilcoxon signed Rank Test

with continuity correction

data: c

v = 66, p-value = 0.9986

alternative hypothesis: true location
is less than 12.

Since p-value is greater than 0.05
we accept the hypothesis at 5% level
of significance.

Q.5) The weights of students before and
after they stop smoking are given
below. Using WSR test that there is
no significant change.

| Before | After |
|-----------------|-----------------|
| 65, 75, 75, 62, | 72, 74, 72, 66, |
| 72 | 73 |

Solⁿ: H_0 : Before and after there is no significant change

H_1 : There is a change.

$>x = (65, 75, 75, 62, 72)$

$>y = (72, 74, 72, 66, 73)$

$>d = x - y$

$>\text{wilcox.test}(x, \text{after} = \text{"two.sided"}, \text{mu} = 0)$

wilcoxon signed Rank Test with continuity correction

data: x

V = 15, p-value = 0.05791

alternative hypothesis: true location is not equal to 0.

since pvalue is greater than 0.05 we accept the hypothesis at 5% level of significance.

Q9