

# IMPLEMENTATION OF PURE PURSUIT AND VECTOR FIELD HISTOGRAM IN MATLAB

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## 1 INTRODUCTION

The purpose of this experiment was to make the robot follow a path predefined by way-points, in an environment filled with obstacles. The robot must follow the path while detecting and avoiding any obstacles in its way and reach the goal point. To make the robot track the predefined path Pure Pursuit algorithm was implemented and to help it navigate through obstacles by avoiding collision with them, Vector field histogram algorithm was implemented.

## 2 PURE PURSUIT

Pure Pursuit is basically a path tracking/following algorithm that works by finding a target point on path "one lookahead distance" away and the curvature needed by robot to reach that point. Pure pursuit takes robot's current position, orientation and waypoints defining the path as input and outputs angular velocity that is needed to go along a curve to reach the target point.

To find the required radius to move along the arc, consider figure-1. Here target point TP is shown in robot's frame. The path or curvature needed for robot to go to TP is defined by the arc between O and TP. This arc is a part of a circle with radius "r" centered at "C" as shown. The chord of this arc is of length "l" the lookahead distance. From the figure-1,

$$x^2 + y^2 = l^2$$

$$x + d = r$$

$$d^2 + y^2 = r^2$$

From the above 3 equations we can simply find :

$$r = \frac{l^2}{2x}$$

To implement this in matlab, following steps were followed:

1. Closest waypoint from the robot's current location was found.

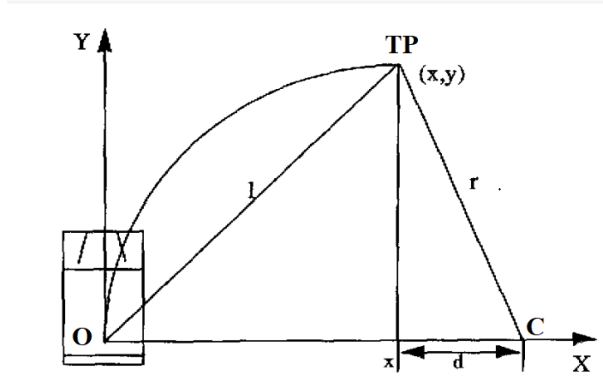


Figure 1: calculation of radius of curvature

2. The waypoint that comes after the closest waypoint along the path *next\_waypoint* was then taken and the line segment between these two was considered.

```

1  wpx=waypoints (:,1);
2  wpy=waypoints (:,2);
3  dist_from_wp=sqrt ((pose(1,1)-wpx).^2 +(pose(2,1)-
   wpy).^2);
4  closest_wp_index=find (dist_from_wp==min(
   dist_from_wp));
5  closest_wp=waypoints (closest_wp_index(1,1),:);
6  s=size (waypoints);
7  next_wp=waypoints (closest_wp_index(1,1),:);
8  if (closest_wp_index(1,1)~=s(1))
9
10     next_wp=waypoints (closest_wp_index(1,1)+1,:);
11  end

```

3. Next, a circle centered at robot's current location with a radius equal to "LOOKAHEAD DISTANCE" was considered and intersection between this circle and the line segment defined in previous step was found.
4. In case of a single intersection point, that was chosen as target point. If there were 2 intersection points then the one closer to the *next\_waypoint* was taken as target point.
5. There can be cases where no valid intersection points exist. In such a case a line segment was considered between the robot's location and it's closest waypoint or the last target point which was lying along the path, whichever is closer. In this case there will always be one intersection point, which will then be taken as target point

```

1 E=transpose(closest_wp);
2 TP=E
3 L=transpose(next_wp);
4 last_TP_on_path=E;
5 C=pose(1:2,1);
6 d=L-E;
7 f=E-C;
8 l=0.35; %lookahead distance
9 a=norm(d)^2;
10 b=2*dot(f,d);
11 c=norm(f)^2-l^2;
12 D=b^2-(4*a*c);
13 if (D<0)
14     flag=1;
15 end
16 if (D>=0)
17     D=sqrt(D);
18     t1=(-b-D)/(2*a);
19     t2=(-b+D)/(2*a);
20     if ( (t1<0 || t1>1) && (t2<0 || t2>1))
21         flag=1;
22     end
23 end
24 D=t2;
25 if (flag==0)
26     if (D==0)
27         TP=E+t1*d;
28     end
29     if (D>0)
30         if ( (t1<0 || t1>1) && (t2>=0 && t2<=1))
31             TP=E+t2*d;
32         end
33         if ((t1>=0 && t1<=1) && (t2<0 || t2>1))
34             TP=E+t1*d;
35         end
36         if ((t1>=0 && t1<=1) && (t2>=0 && t2<=1))
37             TP1=E+t1*d;
38             TP2=E+t2*d;
39             TPs=[transpose(TP1);transpose(TP2)];
40             TPx=TPs(:,1);
41             TPy=TPs(:,2);
42             dist_from_L=sqrt((L(1,1)-TPx).^2 +(L
43                 (2,1)-TPy).^2);
44             closest_TP_index=find(dist_from_L==min(
45                 dist_from_L));
46             TP=transpose(TPs(closest_TP_index

```

```

(1,1),:));
45         end
46     end
47     last_TP_on_path=TP
48 end
49 if (flag==1)
50     norm1=norm(pose(1:2,1)-last_TP_on_path)
51     norm2=norm(pose(1:2,1)-E)
52     if (norm1<=norm2)
53         L=last_TP_on_path;
54     end
55     if (norm1>norm2)
56         L=E
57     end
58     E=pose(1:2,1);
59     d=L-E;
60     TP=E+l*(d)/norm(d);
61 end

```

6. After finding target point, which will be in global coordinates, it was carefully converted to robot's body frame, and then using then using pure pursuit the required radius of curvature (r) and hence the angular velocity(w) was calculated as  $w = \frac{v}{r}$ , where 'v' is fixed linear velocity.

```

1 vv=TP-pose(1:2,1);
2 phi=atan2(vv(2,1),vv(1,1));
3 if (phi<0)
4     phi=2*pi+phi;
5 end
6 ang=phi-(sign(pose(3,1))*pose(3,1));
7 if (ang<0)
8     ang=2*pi+ang;
9 end
10 if (ang>pi)
11     TP_bot_x=-l*cos((pi/2)+(ang-2*pi));
12 end
13 if (ang<=pi)
14     TP_bot_x=l*cos((pi/2)-ang);
15 end
16 vRef=0.75
17 R=(l^2)/(2*(TP_bot_x));
18 wRef=(vRef)/(R);

```

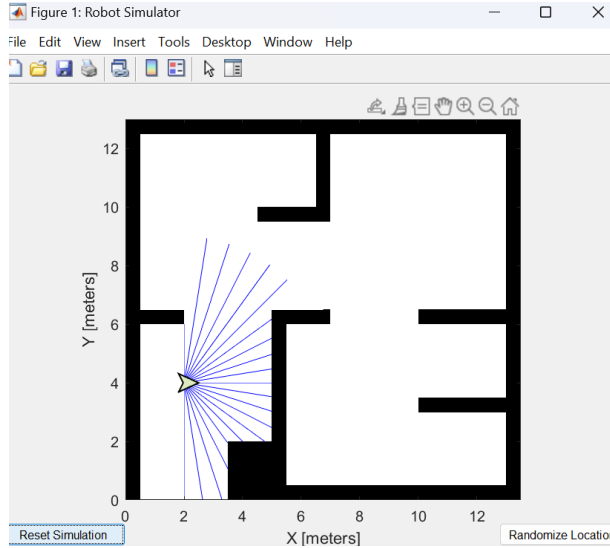


Figure 2: The robot and it's workspace

### 3 VECTOR FIELD HISTOGRAM

Vector field histogram or VHF is an algorithm used for obstacle avoidance in an unknown environment filled with obstacles. VFH tries to steer the robot towards the goal point while steering away from obstacle.

#### 3.1 Certainty Grid

The first step to implement this algorithm is a certainty grid. The robot's workspace is discretized into a 2D array of square grid cells, where each grid cell holds a certainty value CV indicating the presence of an obstacle near that cell.

In our experiment, the workspace is 12.5 x 12.5 units. This was converted into a 126 x 126 grid, where each cell is 0.1x 0.1 units. Each grid cell is initially assigned a probability or CV of 0.5 indicating an equal chance of being occupied by an obstacle or free of obstacle. As the robot moves, the CVs are repeatedly updated by robot's laser scan reading. Hence this certainty grid keeps on updating with the robot's movement through the workspace. Initially at start of simulation, every grid cell has a CV of 0.5.

As shown in figure-2 the robot has 21 laser beams spanning from an angle of  $-\pi/2$  to  $\pi/2$  with 0 degrees along robot's heading. Each of these beam takes a range reading at every time step of simulation. For a given beam, using it's angle and orientation of robot and it's range reading the (x,y) position of that

object is determined, which can be then used to determine which grid cell that point belongs to. Once the grid cell is determined, its confidence value CV is increased since we know there is an obstacle present near that cell. Further, the CV of all the cells lying along that beam up-to the cell that contains the object is decreased since the fact that beam passes through those cells without interruption implies those cells are not occupied by any object.

The confidence value or certainty value CV of each cell is updated using the procedure described in [1]. To briefly describe the procedure, denote 'm' as a binary random variable for a given grid cell such that it takes value 1 if obstacle present and 0 otherwise. Denote  $x_{1:t}$  as the position of robot from till t time steps and  $z_{1:t}$  as the laser measurements till t time steps. We are interested in the probability that  $m=1$  given  $x_{1:t}$  and  $z_{1:t}$ , i.e how does the probability that  $m=1$  changes after every new measurement at next time step. Following the derivation described in [1] the final update rule is as follows:

$$\logodds(m = 1|z_{1:t}) = \logodds(m = 1|z_t) + \logodds(m = 1|z_{1:t-1})$$

Here,

$$\logodds(x) = \log(P(x)/(1 - P(x)))$$

And  $P(m = 1|z_t)$  is the probability that an obstacle is present given the measurement at time step 't'. If the grid cell lies at the end of laser beam from where the beam reflects off, this term takes an value of 0.8 and if the cell lies along the beam it takes the value of 0.2. The ceratinity value CV for each cell can then be obtained as:

$$P(m = 1|z_{1:t}) = \frac{\exp(\logodds(m=1|z_{1:t}))}{(1+\exp(\logodds(m=1|z_{1:t})))}$$

Figure-3 shows the visualization of occupancy grid obtained during one of the simulations, where robot moves in a predefined path and uses its laser readings to find and repeatedly update the CVs of grid cells using the procedure described above. The grey cells are the ones that robot's laser has not reached hence a CV of 0.5, whereas lighter cells denote very less CV of presence of obstacle and darker cells indicate a strong presence of obstacle nearby. One can compare it with the actual map and see how it has successfully detected the edges of obstacles as well as free space in the map.

### 3.2 Polar Histogram

Here, every grid cell is mapped to a sector around the robot to construct a polar histogram which represents obstacle density in different directions around the robot. Once the certainty grid is created we have the CVs of the grid cells for a given time step. We consider an active window of  $w_s x w_s$  cells centered around robot's center. We consider all the cells that fall in this active window and map them to different sectors around robot. For a cell (i,j), we construct an obstacle vector whose direction and magnitude are given by:

$$\beta_{ij} = \tan^{-1}\left(\frac{y_j - y}{x_i - x}\right)$$

$$m_{ij} = c_{ij}^2(a - bd_{ij})$$

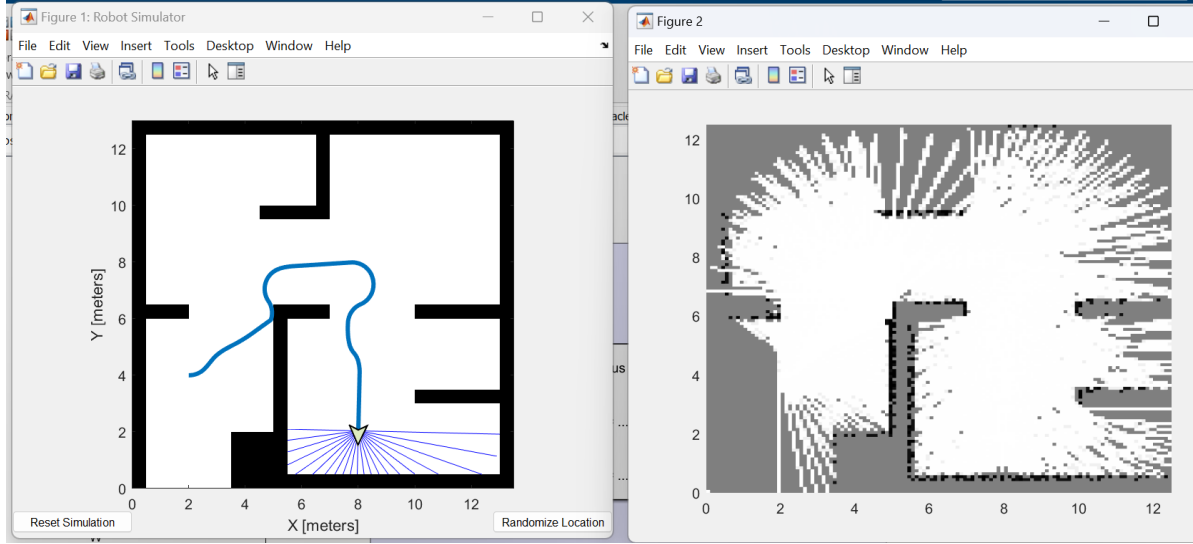


Figure 3: Occupancy map visulaization

where

$x_i, y_j$  = center coordinates of (i,j) cell

$x, y$  = center of robot

$c_{ij}$  = CV of the cell

$d_{ij}$  = distance between robot and cell

$a, b$  = positive constants defined by user

Now we consider an angular resolution  $\alpha$  which gives us  $360/\alpha$  sectors around the robot. Each grid cell is mapped to it's corresponding kth sector using :

$$k = \text{floor}(\beta_{ij}/\alpha) + 1$$

Once every cell in active window is mapped to it's corresponding sector, the next step is to calculate the polar obstacle density  $h_k$  for each sector which is simply given by summation of the magnitude of obstacle vector of all cells in that sector:

$$h_k = \sum m_{ij}$$

A further smoothing is applied as discussed in [2]

$$h_k = \frac{h_{k-l} + 2h_{k-l+1} + \dots + (l+1)h_k + \dots h_{k+l}}{2l+1}$$

It's just a weighted average over a range of sectors determined by 'l'.

### 3.3 Steering angle

The next step is to find which direction the robot has to steer based on the polar obstacle density around it. For this we identify groups of consecutive sectors around the robot such the each sector in a group has polar obstacle density

below a predefined histogram threshold. Such groups are defined as candidate valleys in [2]. Usually more than one such candidate valley exists around the robot where each of them indicates that obstacle density is less in that direction, where we can identify the direction by the sectors included in that candidate valley.

Pure pursuit algorithm calculates the target point and angle between the robot's heading and target point every time step and this target direction is used as an input to VFH algorithm. Using this target direction we can determine the sector this belongs to by the same logic as we determined every grid cell's sector. Denote this sector as  $k_{targ}$ . For every candidate valley,

1. Find the sector in it closest to  $k_{targ}$  and denote it as  $k_n$ .  $Thisk_n = k_{targ}$  when  $k_{targ}$  is included in the candidate valley. Else, it is either of the two extremes of candidate valley.
2. define  $k_f = k_n + s_{max}$  if valley width is more than  $s_{max}$  else  $k_f =$  other exterme of valley.
3.  $\theta_{steer} = (k_n + k_f)/2$
4. find how far away this  $\theta_{steer}$  is from target direction.

The final steering angle is the one that is closest to the target direction. This ensures that robot steers away from obstacle while trying to be as aligned to target direction as possible. This trade-off often determines the performance of robot when an obstacle lies directly in front of robot and it needs to sharply deviate from path.

### 3.4 Matlab Code

```

1 function [SteerDir,op,op1]= fcn(Ranges,Angles,pose,rmax,
    TargetDir)
2 global log_odds;
3 op1=zeros(1,1);
4 op=zeros(1,1);
5 global theta_steer_prev;
6 res=0.1;
7 w_s=25;
8 coder.varsize('Start');
```



```

9  coder.varsize('End');
10 coder.varsize('Start');
11 coder.varsize('temp4');
12 xx=1;
13 p=0;
14 yy=1;
15 xend=1;
16 yend=1;
17 TargetDir=robotics.internal.wrapToPi(TargetDir);
18 safety=2.0;
19 for k=1:numel(Ranges)
20     dist=Ranges(k);
21     if isnan(Ranges(k))
22         dist=double(rmax);
23     end
24     theta=Angles(k);
25     if (pose(3,1)>=0)
26         if (theta<=0)
27             theta=pose(3,1)-abs(theta);
28         end
29         if (theta>0)
30             theta=pose(3,1)+theta;
31         end
32     end
33     if (pose(3,1)<0)
34         if (theta<=0)
35             theta=pose(3,1)+(theta);
36         end
37         if (theta>0)
38             theta=-abs(pose(3,1))+theta;
39         end
40     end
41     ang=theta;
42     if (theta>=0 && theta<pi/2)
43         xx=pose(1,1):(res/2)*cos(ang):min(pose(1,1)
44             +(dist-2*res)*cos(ang),12.5);
45         yy=pose(2,1):(res/2)*sin(ang):min(pose(2,1)
46             +(dist-2*res)*sin(ang),12.5);
47
48         if (ang==0)
49             yy=ones(1,numel(xx))*pose(2,1);
50         end
51         xx=floor(xx/res)+1.0;
52         yy=floor(yy/res)+1.0;
53         xend=min(pose(1,1)+(dist)*cos(ang),12.5);
54         yend=min(pose(2,1)+(dist)*sin(ang),12.5);

```

```

53         xend=floor(xend/res)+1.0;
54         yend=floor(yend/res)+1.0;
55
56     end
57     if(theta<=pi && theta>=pi/2)
58         ang=pi-theta;
59         xx=pose(1,1):-(res/2)*cos(ang):max(0,pose
60             (1,1)-(dist-2*res)*cos(ang));
61         yy=pose(2,1):(res/2)*sin(ang):min(pose(2,1)
62             +(dist-2*res)*sin(ang),12.5);
63         if(ang==0)
64             yy=ones(1,numel(xx))*pose(2,1);
65         end
66         if(ang==pi/2)
67             xx=ones(1,numel(yy))*pose(1,1);
68         end
69         xx=floor(xx/res)+1.0;
70         yy=floor(yy/res)+1.0;
71         xend=max(pose(1,1)-(dist)*cos(ang),0);
72         yend=min(pose(2,1)+(dist)*sin(ang),12.5);
73         xend=floor(xend/res)+1.0;
74         yend=floor(yend/res)+1.0;
75     end
76     if(theta>=-pi && theta<=-pi/2)
77         ang=pi-abs(theta);
78         xx=pose(1,1):-(res/2)*cos(ang):max(0,pose
79             (1,1)-(dist-2*res)*cos(ang));
80         yy=pose(2,1):-(res/2)*sin(ang):max(0,pose
81             (2,1)-(dist-2*res)*sin(ang));
82         if(ang==0)
83             yy=ones(1,numel(xx))*pose(2,1);
84         end
85         if(ang==pi/2)
86             xx=ones(1,numel(yy))*pose(1,1);
87         end
88         xx=floor(xx/res)+1.0;
89         yy=floor(yy/res)+1.0;
90         xend=max(pose(1,1)-(dist)*cos(ang),0);
91         yend=max(pose(2,1)-(dist)*sin(ang),0);
92         xend=floor(xend/res)+1.0;
93         yend=floor(yend/res)+1.0;
94     end
95     if(theta<0 && theta>-pi/2)
96         ang=abs(theta);
97         xx=pose(1,1):(res/2)*cos(ang):min(pose(1,1)
98             +(dist-2*res)*cos(ang),12.5);

```

```

94         yy=pose(2,1):-(res/2)*sin(ang):max(0,pose
           (2,1)-(dist-2*res)*sin(ang));
95         xx=floor(xx/res)+1.0;
96         yy=floor(yy/res)+1.0;
97         xend=min(pose(1,1)+(dist)*cos(ang),12.5);
98         yend=max(pose(2,1)-(dist)*sin(ang),0);
99         xend=floor(xend/res)+1.0;
100        yend=floor(yend/res)+1.0;
101    end
102
103
104    for i=1:min(numel(xx),numel(yy))
105        ux=xx;
106        uy=yy;
107        if(yy(i)>size(log_odds,1))
108            uy(i)=size(log_odds,1);
109            yy=uy;
110        end
111        if(xx(i)>size(log_odds,1))
112            ux(i)=size(log_odds,1);
113            xx=ux;
114        end
115        log_odds(yy(i),xx(i))=log_odds(yy(i),xx(i))+log
           (0.2/0.8);
116    end
117    if(~isnan(Ranges(k)))
118        if(yend>size(log_odds,1))
119            yend=size(log_odds,1);
120        end
121        if(xend>size(log_odds,1))
122            xend=size(log_odds,1);
123        end
124        log_odds(yend,xend)=log_odds(yend,xend)+log
           (0.8/0.2);
125    end
126 end
127 prob=exp(log_odds)./(1+exp(log_odds));
128 i1_grid=min(floor(pose(2,1)/res)+1+(w_s-1)/2,(12.5/res)
           +1);
129 j1_grid=max(floor(pose(1,1)/res)+1-(w_s-1)/2,1);
130 i2_grid=max(floor(pose(2,1)/res)+1-(w_s-1)/2,1);
131 j2_grid=min(floor(pose(1,1)/res)+1+(w_s-1)/2,(12.5/res)
           +1);
132 i1=i2_grid;
133 i2=i1_grid;
134 j1=j1_grid;

```

```

135 j2=j2_grid;
136 alpha=5*pi/180;
137 b1=5;
138 a1=b1*(2^0.5)*(w_s-1)/2;
139 %C_active_prob=prob(i1:i2,j1:j2);
140 sector_POD=zeros(1,(2*pi/alpha));
141 for i=i1:i2
142     for j=j1:j2
143         xi=(j*res)+res/2;
144         yj=(i*res)+res/2;
145         cell_pos=[xi;yj];
146         beta_ij=atan2(cell_pos(2,1)-pose(2,1),cell_pos
            (1,1)-pose(1,1));
147         if beta_ij<0
148             beta_ij=2*pi+beta_ij;
149         end
150         sector=floor(beta_ij/alpha)+1;
151         d=sqrt((cell_pos(1,1)-pose(1,1))^2 + (cell_pos
            (2,1)-pose(2,1))^2);
152         if (prob(i,j)>=0.5)
153             d=max(sqrt((cell_pos(1,1)-pose(1,1))^2 + (
                cell_pos(2,1)-pose(2,1))^2)-safety,0);
154         end
155         sector_POD(1,sector)=sector_POD(1,sector)+((prob(
            i,j)^2)*(a1-b1*d));
156     end
157 end
158 l=5;
159 smoothened_sector_POD=zeros(1,(2*pi/alpha));
160 temp4=[0];
161 for k=1:(2*pi/alpha)
162     k1=k-1;
163     if (k1<1)
164         k1=(2*pi/alpha)+k1;
165     end
166     k2=k+1;
167     if (k2>(2*pi/alpha))
168         k2=k2-(2*pi/alpha);
169     end
170     temp1=1:l+1;
171     temp2=flipr(temp1);
172     temp3=cat(2,temp1,temp2(1,2:end));
173     disp(k1)
174     disp(k2)
175     if (k1<k2)
176         temp4=sector_POD(1,k1:k2).*temp3;

```

```

177         end
178         if (k1>k2)
179
180             temp4=cat (2,sector_POD (1,k1:end) ,sector_POD (1,1:
                k2)) .* temp3;
181
182         end
183         disp (temp4)
184         smoothened_sector_POD (1,k)=sum (temp4)/(2*l+1);
185     end
186
187     Start =[0];
188     End =[0];
189     flag =1;
190
191     opp=[min (smoothened_sector_POD) ;max (smoothened_sector_POD
        ) ];
192     h_t=1; %Histogram Threshold
193     for i=1:size (smoothened_sector_POD ,2)
194         if (smoothened_sector_POD (i)<h_t && flag==1)
195             Start=cat (2,Start ,[ i ] );
196             flag=0;
197         end
198         if (smoothened_sector_POD (i)>=h_t && i>1 && flag==0)
199             End=cat (2,End ,[ i -1 ] );
200             flag=1;
201         end
202         if (i==size (smoothened_sector_POD ,2) &&
            smoothened_sector_POD (i)<h_t)
203             if (size (Start ,2)==2 && size (End ,2)==1)
204                 End=cat (2,End ,[ i ] );
205                 continue;
206             end
207             if (smoothened_sector_POD (1)<h_t)
208                 Start (1)=Start (end);
209                 Start (end) =[];
210             end
211             if (smoothened_sector_POD (1)>=h_t)
212
213                 End=cat (2,End ,[ i ] );
214             end
215         end
216     end
217     Start=Start (1,2:end);
218     End=End (1,2:end);
219     op1=size (Start ,2);

```

```

220 op=size(End,2);
221 theta_targ=pose(3,1)+TargetDir;
222 if(theta_targ<0)
223     theta_targ=2*pi+theta_targ;
224 end
225 k_targ=floor(theta_targ/alpha)+1;
226 Cost=inf;
227 kn=1;
228 kf=1;
229 smax=15;
230 a=3;
231 b=0.02;
232 c=0;
233 theta_steer_opt=TargetDir;
234 for m=1:size(Start,2)
235     v_start=0;
236     v_end=0;
237     if(Start(m)<End(m))
238         if(k_targ>=Start(m) && k_targ<=End(m))
239             kn=k_targ;
240             kf=kn+smax
241             if(kf>2*pi/alpha)
242                 kf=mod(kf,2*pi/alpha);
243             end
244             end
245         if(~(k_targ>=Start(m) && k_targ<=End(m)))
246             if(Start(m)-k_targ<0)
247                 v_start=2*pi/alpha;
248             end
249             if(k_targ-End(m)<0)
250                 v_end=2*pi/alpha;
251             end
252             if(abs(Start(m)-k_targ+v_start)<=abs(k_targ-
253                 End(m)+v_end))
254                 kn=Start(m);
255                 kf=kn+smax
256                 if(kf>2*pi/alpha)
257                     kf=mod(kf,2*pi/alpha);
258                 end
259                 if(abs(Start(m)-k_targ+v_start)>abs(k_targ-
260                     End(m)+v_end))
261                     kn=End(m);
262                     kf=kn-smax
263                     if(kf<0)
264                         kf=mod(kf,2*pi/alpha);

```

```

264         end
265         %kf=mod(kn-smax,2*pi/alpha); %mod(-12,72)
           =60 as per this function!! so works
266     end
267
268     end
269 end
270 if (Start(m)==End(m))
271     kn=Start(m);
272     kf=kn+smax
273     if (kf>2*pi/alpha)
274         kf=mod(kf,2*pi/alpha);
275     end
276     %kf=mod(kn+smax,2*pi/alpha);
277 end
278 if (Start(m)>End(m))
279     if ((k_targ>=Start(m) && k_targ<=2*pi/alpha) || (
           k_targ>=1 && k_targ<=End(m)))
280         kn=k_targ;
281         kf=kn+smax
282         if (kf>2*pi/alpha)
283             kf=mod(kf,2*pi/alpha);
284         end
285         %kf=mod(kn+smax,2*pi/alpha);
286     end
287     if (~((k_targ>=Start(m) && k_targ<=2*pi/alpha) ||
           (k_targ>=1 && k_targ<=End(m))))
288         if (abs(Start(m)-k_targ)<=abs(k_targ-End(m)))
289             kn=Start(m);
290             kf=kn+smax
291             if (kf>2*pi/alpha)
292                 kf=mod(kf,2*pi/alpha);
293             end
294             %kf=mod(kn+smax,2*pi/alpha);
295
296         end
297         if (abs(Start(m)-k_targ)>abs(k_targ-End(m)))
298             kn=End(m);
299             kf=kn-smax
300             if (kf<0)
301                 kf=mod(kf,2*pi/alpha);
302             end
303             %kf=mod(kn-smax,2*pi/alpha); %mod(-12,72)
           =60 as per this function!! so works
304
305     end

```

```

306         end
307     end
308     theta_steer=(kn+kf)*alpha/2;
309     if (abs(kn-kf)>smax)
310         theta_steer=((kn+kf)/2)+(pi/alpha)*alpha;
311     end
312
313     %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
314     p=pose(3,1);
315     if (pose(3,1)<0)
316         p=2*pi+pose(3,1);
317     end
318     theta1=abs(robotics.internal.wrapToPi(theta_steer-p))
319         ;
320     theta2=abs(robotics.internal.wrapToPi(theta_targ-
321         theta_steer));
322     theta3=abs(robotics.internal.wrapToPi(
323         theta_steer_prev-theta_steer));
324
325     if ((a*theta2 +b*theta1 +c*theta3)<=Cost)
326         Cost=(a*theta2 +b*theta1 +c*theta3);
327         theta_steer_opt=robotics.internal.wrapToPi(
328             theta_steer-p);
329     end
330     SteerDir=theta_steer_opt;
331     theta_steer_prev=theta_steer_opt;
332     if (size(Start,2)==1 && size(End,2)==1)
333         if (Start(1,1)==1 && End(1,1)==2*pi/alpha)
334             SteerDir=TargetDir;
335             theta_steer_prev=SteerDir;
336         end
337     end

```

## 4 SIMULATION AND RESULTS

A Simulink model was used to simulate the results. The model was connected to a ROS network. ROS allowed exchange of information about robot's different components such as its current pose, laser scan readings which are essential inputs for pure pursuit and VFH. The calculated angular velocity was published to velocity topic of ROS which enabled the robot to move.

Figure-4 shows simulation results when the path is defined by [(2,4); (2,10);(10,4)].



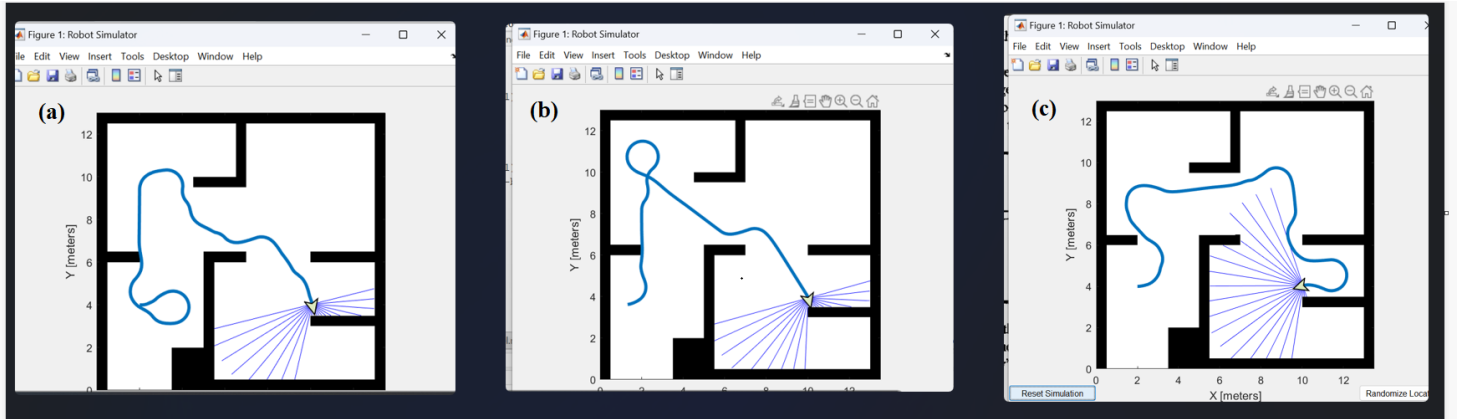


Figure 4: (a) and (b) small lookahead,  $l=0.35$ ; (c)  $l=1.85$

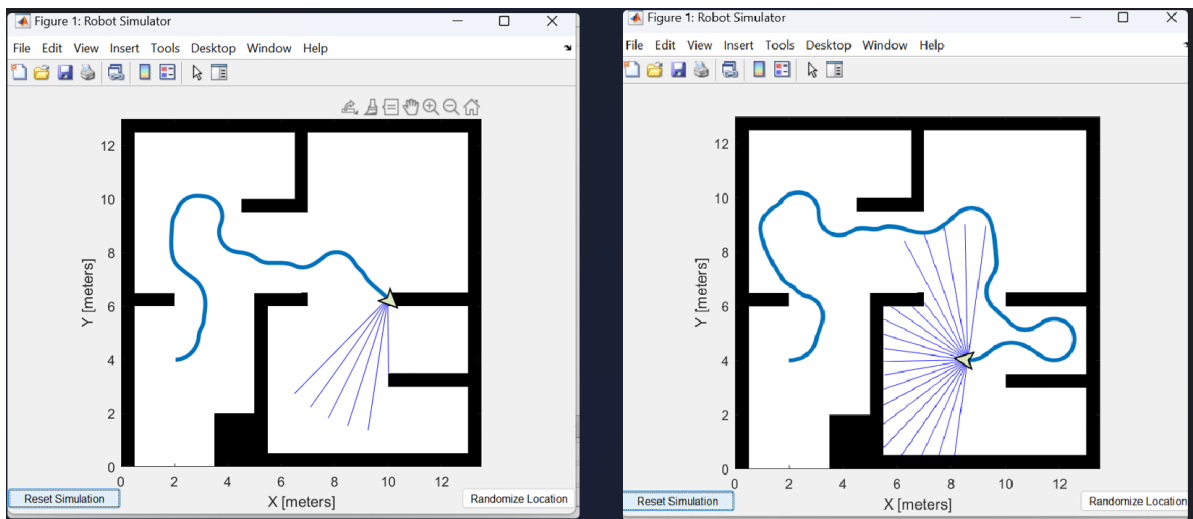


Figure 5: waypoints:  $[(2,4); (2,10); (10,4)]$

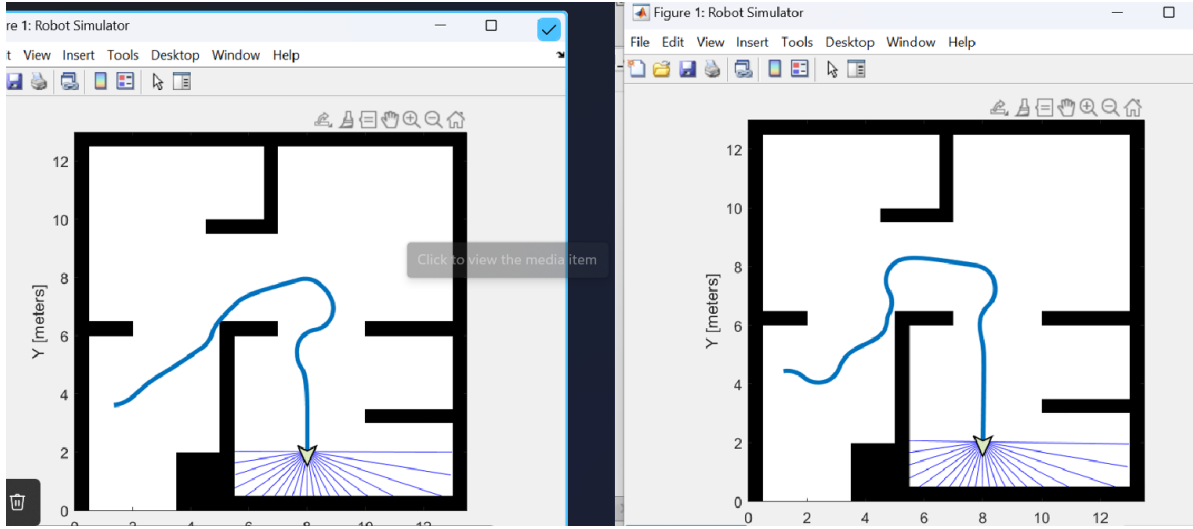


Figure 6: waypoints:[(2,4); (8,8);(8,2)]

It can be seen that when lookahead distance is small like in case of (a),(b) the robot follows the path more closely as compared to the (c) where lookahead is large.

Figure 4 and 5 shows some more simulations obtained by varying active window size,  $s_{max}$ , and histogram threshold. It was observed that when robot is very closely surrounded by obstacles it shows unpredictable behaviour and more often than not it collides with obstacle. Further active window size also plays a significant role in robot's performance. For example, a small window will make the robot closely follow the path until it comes very close to the obstacle, in which case it does not have enough space to steer away from obstacle. A large window leads to the robot trying to avoid obstacles even when it is not that near to one, which leads to oscillatory behaviour and also sometimes robot wanders away from path. In most cases VFH is a tradeoff between not deviating much from target direction and steering clear of obstacles. If one puts more bias towards the former, then robot may collide with an obstacle whereas putting more bias towards the later leads the robot wandering off from the path. In both cases performance is undesirable, hence one should properly tune various parameters to balance this tradeoff.

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