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## Introduction to FEM

A commercial FEM system consists of three basic modules: pre-processor; solver; and post-processor. These modules and their functions are illustrated in Fig. The pre-processor allows the user to create geometry or input CAD geometry, and provides the tools for meshing the geometry. The solver takes the finite element model provided by the pre-processor and computes the required response. The post processor takes the data from solver and presents it in a front that user can understand, which is as shown below.

### pre-processor

1. Read control parameters.
  2. Read/generate nodal co-ordinates and boundary conditions.
  3. Read/generate element connectivity and element loads.
  4. Read materials properties or constitutive matrices.
  5. Read nodal loads and loading conditions.
- ↓

### Solver

1. Compute parameters for memory/file management.
  2. Compute element matrices and vectors.
  3. Form global matrices.
  4. Enforce SPC, MPC, ...
  5. Solution of governing matrix-equations.
- ↓

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## post - processor

1. print / plot deformed mesh over undeformed mesh.
2. print / plot contours of displacement.
3. Compute element strains, stresses, etc.
4. print / plot contours of stresses.
5. Display locations of Max / min. stress.
6. print / plot contours of failure index.

## A general procedure for Finite element analysis

Certain steps in formulating a finite element analysis of a physical are common to all such analysis, whether structural, heat transfer, fluid flow, or some other problem. These steps are embodied in commercial finite element software packages (some are mentioned in the following paragraphs) and are implicitly incorporated in the text, although we do not necessarily refer to the steps explicitly in the following chapters. The steps are described as follows:

### pre processing :-

The pre processing step is, quite generally, described as defining the model and includes:

- \* Define the geometric domain of the problems.
- \* Define the element type(s) to be used.
- \* Define the material properties of the elements.
- \* Define the geometric properties of the elements (length, area and the like).

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- \* Define the element connectivity's (mesh the model).
- \* Define the physical constraints (boundary conditions).
- \* Define the loadings.

### Solution:-

During the Solution phase, finite element software assemble the governing algebraic equations in matrix form and computes the unknown values of the primary field variable(s). The computed values are then used by back substitution to compute addition, derived variables, such as reaction forces, element stresses, & heat flow.

### post processing :-

Analysis & evaluation of the solution results is referred to as post processing. post processor software contains sophisticated routines used for sorting printing & plotting selected result from a finite from a finite element solution. Examples of operations that can be accomplished include,

sort element stresses in order of magnitude.

check equilibrium.

calculate factors of safety.

plot deformed structural shape.

Animate dynamic model behavior.

produce color-coded temperature plots.

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## Introduction to ANSYS

ANSYS is an integrated design analysis tool based on FEM developed by ANSYS, Inc. It has its own tightly integrated pre-and-post-processor. The ANSYS product documentation is excellent & it includes command references; operations guide; modeling and meshing guide; basic analysis procedure guide; advance analysis guide; element reference; theory reference; structural analysis; thermal analysis guide; electromechanical field guide; fluid dynamics guide; and coupled field analysis guide.

Element library in ANSYS lists 189 finite elements. They are broadly grouped into: LINK, PLANE, BEAM, SOLID, CONTAC, COMBIM, PIPE, MASS, SHELL, FLUID, SOURCE, MATRIX, HYPER, VISCO, INFIN, INTER, SURF etc.

## FEM procedure

1. Discretization of given domain into a collection of prescribed finite elements.
  - a. Construct the nodes and elements.
  - b. Number the nodes and elements.
  - c. Generate the geometric properties (eg: coordinate and cross sectional area) needed for the problem.
  
2. Derivation of element equation for all typical element in the mesh.
  - a. construct the variational formulation of the given differential equations over the typical element.

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3. Assembly of element equations to obtain the equations of the whole problem.
  - ④. Identify the inter element continuity conditions among the primary variables by relating the element nodes to global nodes
  - ⑤. Identify the "equilibrium" conditions among the secondary variables.
  - ⑥. Assemble the element equation using step 3a & 3b.
4. Imposition of boundary condition of problem.
5. Solution of the assembled equations.
6. post processing of the results.

Aspects of general purpose finite computer program.

A general purpose finite element program should meet the requirements in general engineering application and should make use of the latest development in numerical techniques.

Main characteristics of finite element programs are:

- Range of application.
- Type of response.
- material types.
- material wall constructions
- loading conditions
- Type of loads

Range of application.

- Structure / solids.
- aerospace structures.

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- Civil engineering structures.
- Nuclear reactions.
- fluid dynamics.
- piping systems.
- Manufacturing processes.

Type of response.

- linear static.
- Non-linear static.
- Thermal analysis.
- Fluid dynamics.
- Heat transfer.
- Electrostatic / electromagnetic etc.

Material wall construction

- Monocyclic.
- Layered.
- sandwich.
- composite material

Types of loads

- point load
- line load
- surface loads.
- volume loads.
- initial stress
- Thermal loadings etc.

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0	1	0	1	2	0	9	1

### Stress analysis

- Small / Large deformation.
- small / large strain.
- elasto-plastic.
- visco-elastic.
- Thermal effects etc.

### Stability analysis

- Buckling instability
- geometric non-linearity.
- material non-linearity.

### Crash analysis

- Impact.
- crash worthiness etc.

### static analysis

- Deflection.
- stresses.
- strains.
- forces
- energies.

### Heat transfer analysis

- Temperature.
- Heat fluxes.
- Thermal gradients.
- Heat flow from convection faces.

### Fluid analysis

- pressure.
- gas temperatures
- convection coefficients
- velocities

### Automotive industry

- static analysis.
- Model analysis.
- transient dynamics.
- Heat transfer.
- mechanisms.
- Fracture mechanics.
- metal forming.
- crashworthiness.

### Architectural

- soil mechanics.
- Rock mechanics.
- Hydraulics.
- Fracture mechanics
- Hydro elasticity.

### Aerospace industry

- static analysis.
- Model analysis.
- aerodynamics.
- transient dynamics
- Heat transfer.
- Fracture Mechanics
- Creep & plasticity analysis.
- composite materials.
- Aero elasticity.
- metal forming.
- crashworthiness.

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## Bar

The simple bar shown in the fig. determine the displacement, stress, and the sections. the clg of the bar is  $500 \text{ mm}^2$ , length is 1000 mm, and the young's modulus is  $E = 2 \times 10^5 \text{ N/mm}^2$ , Take load  $P = 1000 \text{ N}$ .

1. Preferences  $\rightarrow$  structural.
2. preprocessor  $\rightarrow$  Element type  $\rightarrow$  Link  $\rightarrow$  2D-Spiral
3. Real constants  $\rightarrow$  set 1  $\rightarrow$   $500 \text{ mm}^2$
4. Material properties  $\rightarrow$  structural  $\rightarrow$  linear  $\rightarrow$  elastic  
 $\rightarrow$  isotropic  $\rightarrow E = 2 \times 10^5$ ,  $\rho = 0.3$
5. Modelling  $\rightarrow$  Create  $\rightarrow$  key points  $\rightarrow$  active CS  $\rightarrow$  point 1 - 0  $\rightarrow$  point 2 - 1000.
6. Create  $\rightarrow$  line (straight line)  $\rightarrow$  click on required nodes
7. meshing  $\rightarrow$  size control  $\rightarrow$  manual size  $\rightarrow$  all lines  
 $\rightarrow$  No of division  $\rightarrow$  10.

mesh tool  $\rightarrow$  Mesh  $\rightarrow$  pick all.

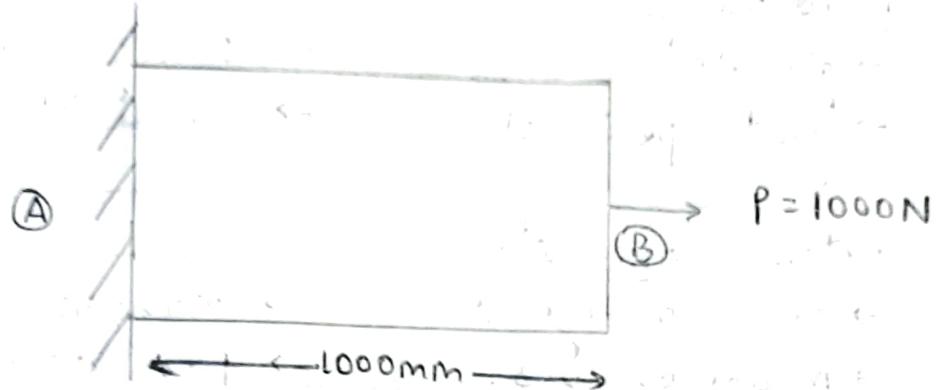
Define loads  $\rightarrow$  Apply  $\rightarrow$  structural  $\rightarrow$  displacement  $\rightarrow$  on  
 nodes 1  $\rightarrow$  All DOF  $\rightarrow$  Force  $\rightarrow$  on node  $\rightarrow$  2 Node  $\rightarrow$  1000  
 solve  $\rightarrow$  current LS

General postprocessing  $\Rightarrow$  Plot results  $\rightarrow$  contour plot  $\rightarrow$   
 Nodal soln  $\rightarrow$  X or Y components.

Element table  $\rightarrow$  Add table  $\rightarrow$  By sequence  $\rightarrow$  LS, 1  
 plot results  $\rightarrow$  contour plot  $\rightarrow$  element table  $\rightarrow$  yes  
 otherwise.

ist results  $\rightarrow$  reaction soln

Q: The comparison is shown b/w theoretical & Ansys  
 software.



Solution:

$$A = 500 \text{ mm}^2$$

$$P = 1000 \text{ N}$$

$$E = 2 \times 10^5 \text{ N/mm}^2$$

$$\rightarrow \text{Axial load} \quad \sigma = \frac{F}{A} = \frac{1000}{500} = 2 \text{ N/mm}^2$$

$$\rightarrow \text{Deflection} \quad \Delta L = \frac{PL}{AE} = \frac{2 \times 1000}{2 \times 10^5} = 0.01 \text{ mm}$$

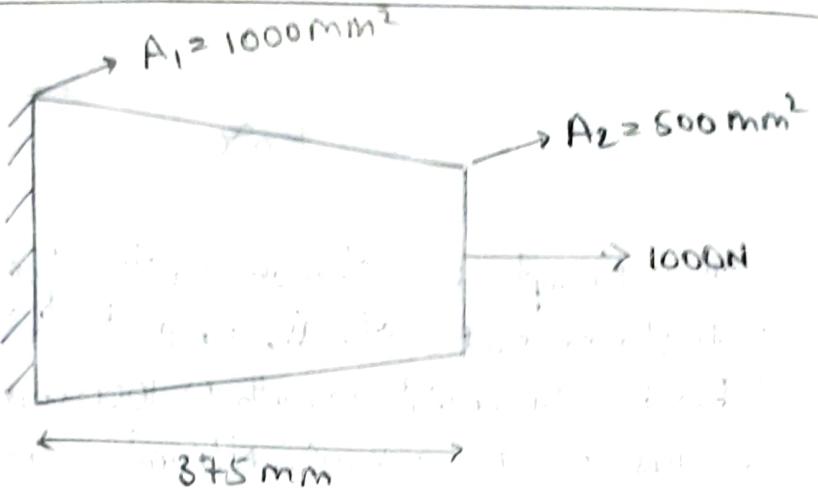
$$\boxed{\Delta L = 10^{-2} = 0.01 \text{ mm}}$$

$$\rightarrow \text{Reaction} = 10^{-3} \text{ N at A.}$$

Comparison.

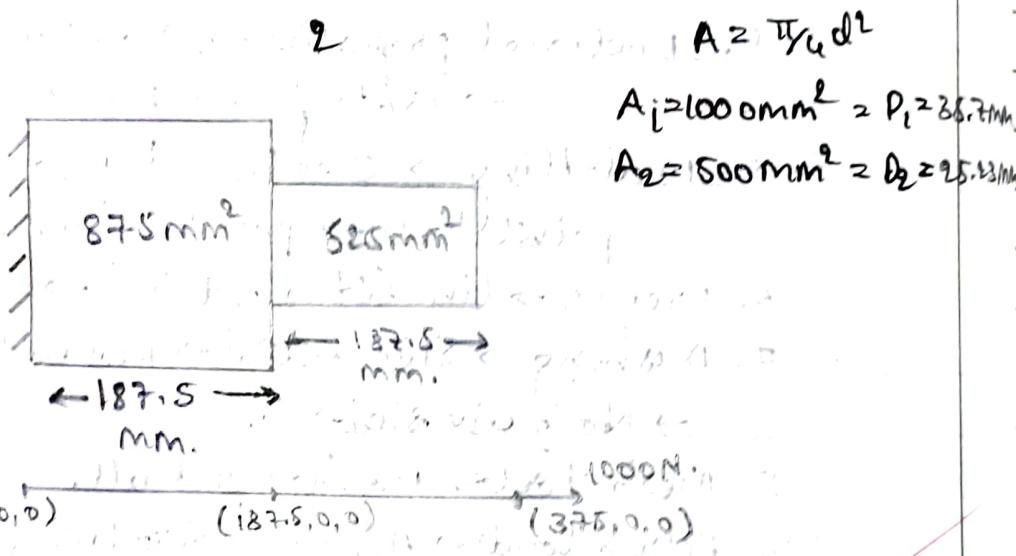
Results	Theoretical	Ans.
$\Delta L$	$10^{-2} \text{ mm}$	$10^{-2} \text{ mm}$
$\sigma$	$2 \text{ N/mm}^2$	$2 \text{ N/mm}^2$
Reaction at A	$-10^{-3} \text{ N}$	$-10^{-3} \text{ N}$
Reaction at B	0 N	0 N

DSCE



$$\text{Stepped bar 1} = \frac{1000 + 750}{2} = 875 \text{ mm}^2$$

$$\text{Stepped bar 2} = \frac{750 + 500}{2} = 625 \text{ mm}^2$$



$$\sigma_1 = \frac{P}{A_1} = \frac{1000}{875} = 1.143 \text{ MPa.}$$

$$\sigma_2 = \frac{P}{A_2} = \frac{1000}{625} = 1.6 \text{ MPa.}$$

$$\text{Displacement} = \Delta L = \frac{4PL}{E\pi d_1 d_2} = \frac{4 * 1000 * 375}{2 * 10^5 * \pi * 38.7 * 25.23}$$

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### Tapered Bar

- Q For the tapered bar shown in the figure determine the displacement, stress and reaction in the bar.

Given:  $A_1 = 1000 \text{ mm}^2$   $E = 2 \times 10^5 \text{ N/mm}^2$

Soln

1. preference → structural.
2. preprocessor → element type → link → 2D spring
3. Real constants → set 1 → 875 → set 2 → 625.
4. Material properties → structural → linear → elastic  
→ isotropic →  $E = 2 \times 10^5$   $\nu = 0.3$
5. Modeling → Create → keypoints → active CS → point 1 → 0 → point 2 → 187.5 → point 3 = 375.
6. Create → line → straight line → click on required nodes.
7. meshing → mesh attributes. → picked line → line 1 → Real constant set 1 → line 2 → Real constant set 2  
Size control → manual size → all line → No. of divisions 10.
8. Mesh tool → mesh → pick all.
9. Define loads → apply → structural → displacement on Nodes → All DOF → force / moment → on nodes  
→ 2nd nodes → magnitude 1000



$$\Delta L = 2.65 \times 10^{-3} \text{ mm}$$

Ansys :

$$\delta M_x = 0.002573 \text{ mm}$$

$$\sigma_{MN} = 1.143 \text{ N/mm}^2$$

$$\delta M_x = 1.6$$

$$\text{Reaction} = -1000$$

Comparison

Theoretical Ansys.

$$\Delta L$$

$$2.65 \times 10^{-3} \text{ mm}$$

$$2.573 \times 10^{-3} \text{ mm}$$

$$\text{Max Stress} (\sigma)$$

$$1.6 \text{ N/mm}^2$$

$$1.6 \text{ N/mm}^2$$

$$\text{Reaction At A}$$

$$-10^3 \text{ N}$$

$$-10^3 \text{ N}$$

$$\text{Reaction at B}$$

$$0$$

$$0$$

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10. Save DB.

11. Solve  $\Rightarrow$  current LS.

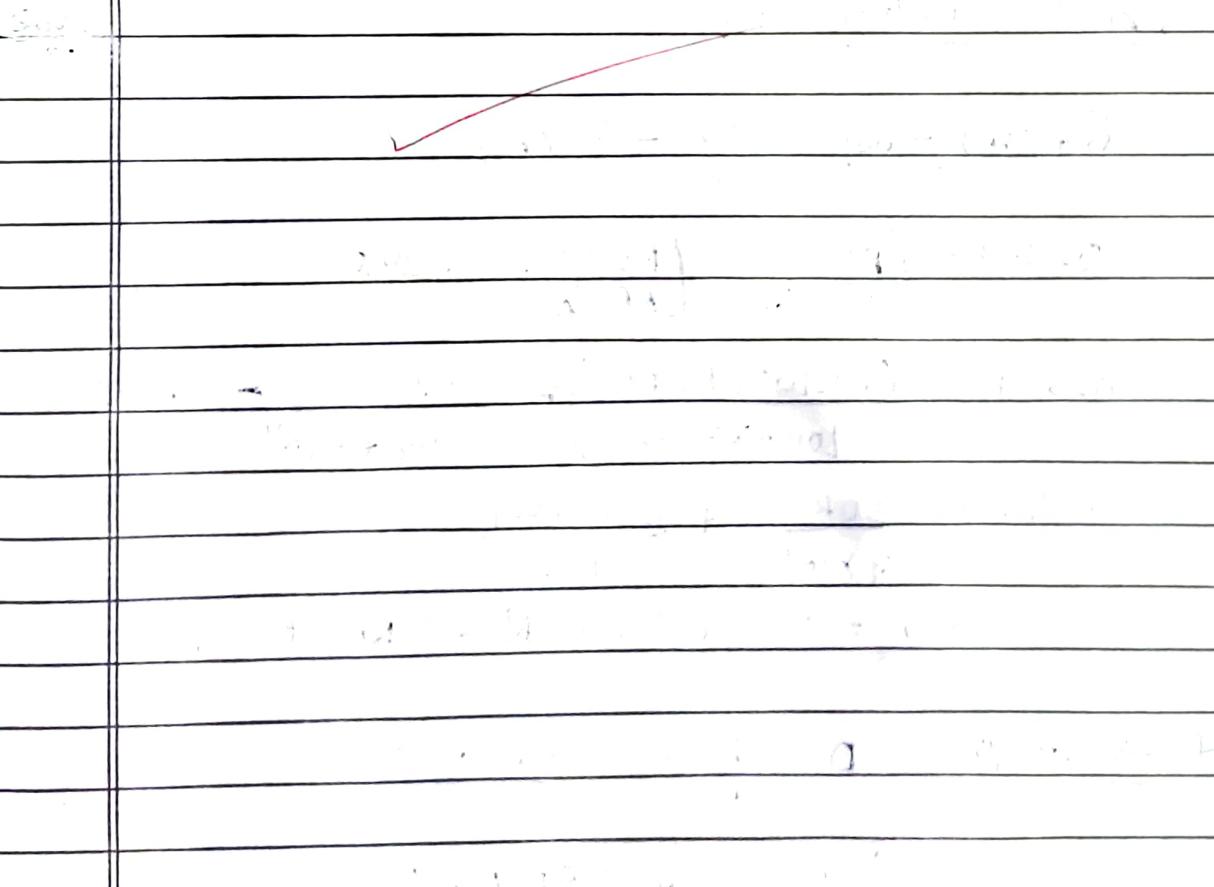
12. General post processing  $\rightarrow$  plot results  $\rightarrow$  contour plot  $\rightarrow$  Nodal solution  $\rightarrow$  X component.

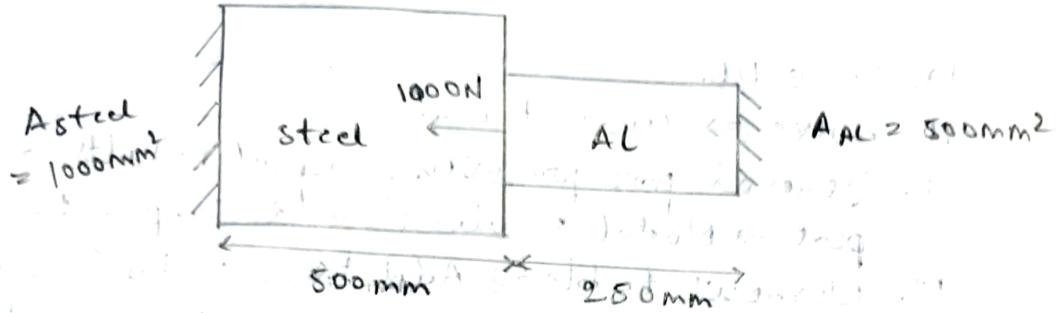
13. Element table  $\rightarrow$  Add table  $\rightarrow$  By Sequence  $\rightarrow$  LS,1 plot results  $\rightarrow$  contour plot  $\rightarrow$  Element table  $\rightarrow$

Yes, average.

List results  $\rightarrow$  Reaction solutions.

Result: The comparison is shown b/w the theoretical and Ansys software.





$$\Delta T = 60^\circ C \quad T_0 = 20^\circ C \quad T_f = 280^\circ C \quad E_{\text{steel}} = 2e5 \quad E_{\text{al}} = 0.7e5$$

$$\alpha_{\text{Steel}} = 11.7 e^{-6}$$

$$\alpha_{\text{al}} = 23 e^{-3}$$

$$\Delta = \alpha_{\text{at La}} + \alpha_{\text{at ls}}$$

$$= 0.345 + 0.381$$

$$\boxed{\Delta = 0.695 \text{ mm}}$$

$$\delta_{T(\text{st})} - \delta_{ST} = \delta_{AL} - \delta_{T(\text{al})}$$

$$0.381 - \left( \frac{PL}{AE} \right)_{\text{st}} = \left( \frac{PL}{AE} \right)_{\text{al}} - 0.345$$

$$0.381 - \left( \frac{(5 \times 10^5 + R) 500}{1000 \times 2 \times 10^5} \right) = \frac{R \times 250}{500 \times 7 \times 10^4} - 0.345$$

$$0.696 = \frac{50R}{4 \times 10^6} + \frac{5 \times 10^5 + R}{4 \times 10^5}$$

$$\Rightarrow R = 57.768 \times 10^3 \text{ N} \rightarrow \text{Reaction.}$$

$$\underline{\text{Stress at Al}} \quad \sigma = \frac{P}{A} = \frac{57.708 \times 10^3}{500}$$

$$\boxed{\sigma = 115.416 \text{ N/mm}^2}$$

D	D	M	M	Y	Y	Y	Y
0	4	0	8	2	0	9	1

### Bar (Stepped bar).

3

Determine the nodal displacement and maximum stress in a 10 stepped bar made of steel and aluminium subjected to point load and thermal load with the boundary conditions as shown.

$$T_0 = 20^\circ\text{C} \quad T_f = 80^\circ\text{C} \quad E_{\text{steel}} = 2e5 \text{ N/mm}^2$$

$$\text{Area of steel } A_{\text{steel}} = 1000 \text{ mm}^2 \quad E_{\text{Al}} = 0.7e5 \text{ N/mm}^2$$

$$\text{Area of aluminium } A_{\text{Al}} = 500 \text{ mm}^2.$$

$$\alpha_{\text{steel}} = 11.7e-6 / ^\circ\text{C}$$

$$\alpha_{\text{alu.}} = 23e-6 / ^\circ\text{C}$$

Soln

1. preference  $\rightarrow$  structural

2. preprocessor  $\rightarrow$  element type  $\rightarrow$  link  $\rightarrow$  2D & pur

3. Real constant  $\rightarrow A_1 = 1000 \text{ mm}^2 \rightarrow A_2 = 500 \text{ mm}^2$

4. material Model 1  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  isotropic

$$E_x = 2e5 \quad \rho_{xy} = 0.3.$$

Second co-efficient for thermal expansion is

$$11.7e-6.$$

5. modelling  $\rightarrow$  repeat for material 2.

6. modelling  $\rightarrow$  Create  $\rightarrow$  key points  $\rightarrow$  active CS  $\rightarrow$  point 1 - 0  $\rightarrow$  point 2 - 500  $\rightarrow$  point 3 - 750.

7. Create  $\rightarrow$  line  $\rightarrow$  straight line  $\rightarrow$  select required nodes.

8. meshing  $\rightarrow$  mesh attribute  $\rightarrow$  picked line  $\rightarrow$  line 1  $\rightarrow$  linear const No = 2

Repeat for line 2  $\Rightarrow$  Real const No = 2.

$$\text{stress at steel} : \frac{5 \times 10^5}{2 \times 10^5} = 57.708 \times 10^3 / 100$$

$$\sigma = 142.292 \text{ N/mm}^2$$

Displacement in steel

$$E = \frac{142.292}{2 \times 10^5}$$

$$E = 7.115 \times 10^{-4}$$

$$\frac{y'_1}{y} = E$$

$$y'_1 = 7.115 \times 10^{-4} \times 800 = 0.3587$$

$$y_{\text{total}} = 0.41 + 0.3587$$

$$= 0.7687 \text{ mm}$$

Displacement in Al

$$E = \frac{y'_1}{y}$$

$$= 1.6488 \times 10^{-3} \times 800$$

$$y'_1 = 0.41$$

$$= 0.341 + 0.41$$

$$= 0.741 \text{ mm.}$$

Result comparison

	Ansye	theoretical.
Deformation	0.753 mm	0.754 mm
Stress	114.90 N/mm <sup>2</sup>	114.92 N/mm <sup>2</sup>

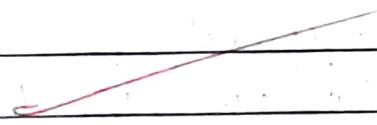
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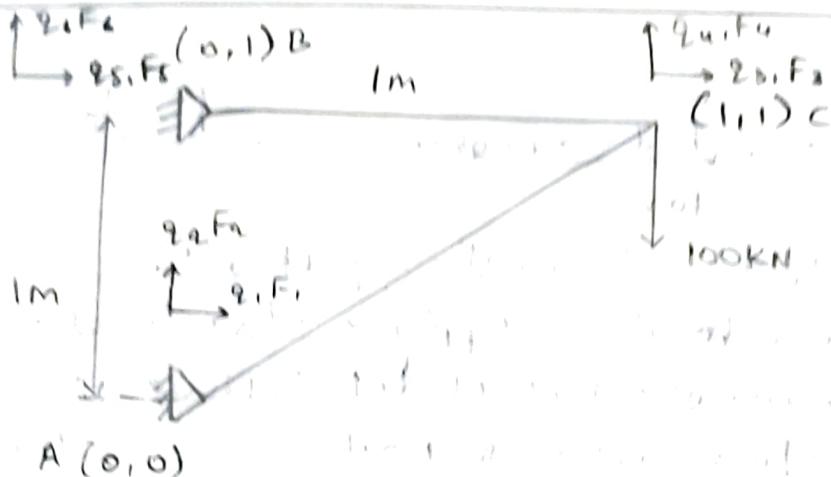
13

Size control → Manual size → all line → No. of divisions  
→ On → 10.

9. Mesh tool → mesh → pick all.
10. Define loads → Apply → Structural → displacement.  
→ On nodes & select Node 1, Node 3 → All DOF
11. Force / moment → on nodes → select Node 3 → -10000  
→ temperature on element → 60
12. Solve → current LS
13. General post processing → plot results → contours  
plate → Nodal solution → Define element table  
→ By sequence → LS 1  
plot result → contours plot → element table →  
yes, org.  
List result → Reaction solution.

Result: The comparison of result is shown.





Solution

$$q_1 = q_2 = q_3 = q_6 = 0 \quad \text{and} \quad F_1 = F_2 = F_4 = F_5 = 0, F_3 = 0$$

$$q_4 = 0.048 \times 10^{-3} \text{ m} \quad F_6 = -100 \text{ KN}$$

$$q_5 = 0.182 \times 10^{-3} \text{ m}$$

$$\sigma = E \cdot E = 210 \times 10^9 \times 0.048 \times 10^{-3}$$

$$\sigma = 10.08 \times 10^8 \text{ N/m}^2$$

using  $K = AE$

$$K = \frac{E}{l} \begin{bmatrix} l^2 & ml & -l^2 & -ml \\ ml & m^2 & -ml & -m^2 \\ -l^2 & -ml & l^2 & ml \\ -ml & -m^2 & ml & m^2 \end{bmatrix}$$

$$\text{or } K_q = F$$

$$\sigma = \frac{E}{l} \begin{bmatrix} -l & m \\ l & m \end{bmatrix}$$

Nodal co-ordinate data

Node No.	x	y
1	0	0
2	1	1
3	0	1

Element connecting data

Element	IN	FN	l <sub>e</sub>	· l	m
1	1	2	1.414	0.707	0.707
2	2	3	1	-1	0

$$k_1 = 10^9 \begin{bmatrix} 0.74 & -0.74 & -0.74 & 0.74 \\ -0.74 & 0.74 & 0.74 & -0.74 \\ -0.74 & 0.74 & 0.74 & -0.74 \\ 0.74 & -0.74 & -0.74 & 0.74 \end{bmatrix}$$

$$k_2 = 10^9 \begin{bmatrix} 2.1 & 0 & -2.1 & 0 \\ 0 & 0 & 0 & 0 \\ -2.1 & 0 & 2.1 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

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### Trusses

1. Two bar truss shown in Fig. Determine nodal displacement & the stress in each member. Take  $E = 210 \text{ GPa}$ .  
 Area = 0.0159 m.

Sdn  
..

1. preference → Element type → link → 2D Sptr.
2. Real constant → link1 → Area → 0.01
3. Material properties → Material models → structural → linear → elastic → isotropic →  $E = 210 \text{ GPa}$  →  $\rho_{xx} = 0.3$
4. Modeling → Create → keypoints → inactive CS.

X Y Z location 0 0 0 A

X Y Z location 0 1 0 B

X Y Z location 1 1 0 C

6. modelling → Create → lines → straight lines → on key points

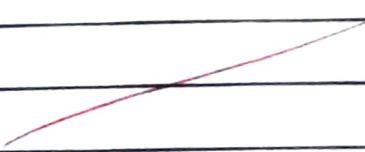
7. meshing → Mesh tool → size controls → manual size → lines → All lines → No. of div → 1

8. meshing → mesh tool → mesh → pick the lines.

9. Solutions → Define loads → Apply → structural → ON nodes → All DOF.

10. Define loads → Force/moment → ON nodes at C  
 look N along y direction.

11. Solve the current load setup.



$$K = 10^9 \begin{bmatrix} 0.74 & 0.74 & -0.74 & -0.74 & 0 & 0 \\ 0.74 & 0.74 & -0.74 & -0.74 & 0 & 0 \\ -0.74 & -0.74 & 2.84 & 0.74 & -2.10 & 0 \\ -0.74 & -0.74 & 0.74 & 0.74 & 0 & 0 \\ 0 & 0 & -2.10 & 0 & -2.10 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$K_2 = F$$

$$q_3 = -1.824 \times 10^{-4} \text{ mm.}$$

$$q_8 = 0.477 \times 10^{-4} \text{ mm.}$$

$$\sigma_1 = \frac{E}{l} [ -l \quad -m \quad l \ m ] \begin{bmatrix} q_1 \\ q_2 \\ q_3 \\ q_4 \end{bmatrix}$$

$$\sigma_1 = -1.418 \times 10^7$$

$$\sigma_2 = 1001700 \text{ MPa}$$

### Ansys Solution

$$DMX = 0.188 \times 10^{-3}$$

$$SMN = 0.182 \times 10^{-3}$$

$$SMX = 0.100 \times 10^8$$

### Result

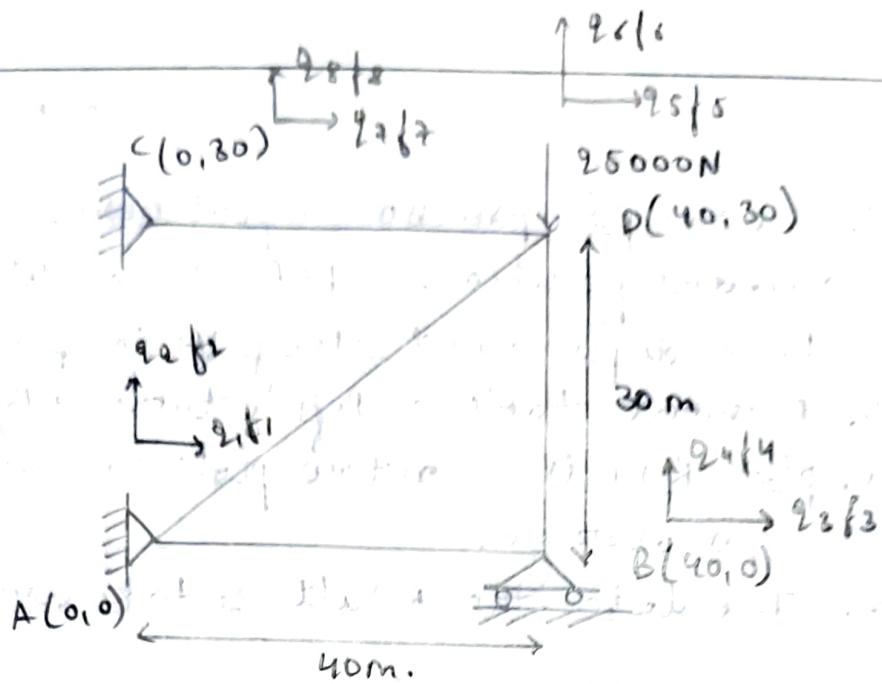
Displacement	Ansyo	theoretical
Strss.	$0.188 \times 10^{-3} \text{ m}$ $10 \times 10^6 \text{ N/m}^2$	$0.182 \times 10^{-3} \text{ m}$ $10.08 \times 10^6 \text{ N/m}^2$

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D	D	M	M	Y	Y	Y	Y
0	4	0	8	2	0	2	1

12. General post processor  $\rightarrow$  plot results  $\rightarrow$  contour plot  
 $\rightarrow$  Nodal solution.  $\rightarrow$  DOF  $\rightarrow$  X E. V components.
13. Find displacement along y-component.
14. Element table  $\rightarrow$  Define table  $\rightarrow$  By sequence  $\rightarrow$  LS.
15. plot .Results  $\rightarrow$  contour plot  $\rightarrow$  Element table  $\rightarrow$  yes average.
16. Tabulate the Result & take down values.

Result: The comparison is shown below.



where

$$q_1 = q_2 = q_4 = q_5 = q_8 = q_9 = 0.$$

$$f_1 = f_2 = f_3 = f_4 = f_7 = f_8 = 0.$$

Using formula

we get.

$$q_3 = \text{Deflection} = -22.25 \times 10^{-3} \text{ m}$$

$$\text{stress} = 4167 \text{ N/mm}^2$$

$$\text{Reaction} = F_x = 4167 \text{ N}$$

$$F_y = 3126 \text{ N}$$

Ans<sup>s</sup> solutim.

$$DMX = 0.092243 \text{ m}$$

$$SMN = -1.0937$$

$$SMX = 4,167 \text{ N/mm}^2$$

Trusses

2 Consider that four bar truss shown in figure. it is given that  $E = 29.5 \times 10^6 \text{ N/m}^2$  and  $A = 1 \text{ m}^2$  for all the elements. Determine the deformation, maximum stress & the reaction forces in the truss system.

1. preference  $\rightarrow$  Element  $\rightarrow$  link  $\rightarrow$  2D & pur.1.

2. Real constants  $\rightarrow$  link1  $\rightarrow$  Area =  $1 \text{ m}^2$

3. Material properties  $\rightarrow$  Material Models  $\rightarrow$  Structural  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  isotropic  $\rightarrow E_x = 2e8 \rightarrow \rho R_{xy} = 0.3$ .

4. modelling  $\rightarrow$  Create  $\rightarrow$  keypoints  $\rightarrow$  In active CS.

xyz location 0 0 0

xyz location 40 0 0

xyz location 0 30 0

xyz location 40 30 0

5. modeling  $\rightarrow$  Create  $\rightarrow$  line  $\rightarrow$  straight line  $\rightarrow$  On key points.

6. Meshing  $\rightarrow$  size controls  $\rightarrow$  manual size  $\rightarrow$  lines  $\rightarrow$  All lines  $\rightarrow$  No of div. 1.

7. Meshing  $\rightarrow$  mesh tool  $\rightarrow$  mesh  $\rightarrow$  pick the lines.

8. Solutions  $\rightarrow$  Define loads  $\rightarrow$  Apply  $\rightarrow$  structural  $\rightarrow$  Displacement  $\rightarrow$  On Nodes  $\rightarrow$  All DOF.

9. Define loads  $\rightarrow$  Force / moment  $\Rightarrow$  ON nodes Fy  $\Rightarrow$  on node 2500 N.

10. Solve  $\rightarrow$  current LS.

## Result

	Ansys	Theoretical
Deformation	0.022952 m	0.0225 m.
stress	4167 N/mm <sup>2</sup>	4167 N/mm <sup>2</sup>
Reaction.	$F_x = 4167 N$ $F_y = 3126 N$	$F_x = 4167 N$ $F_y = 3126 N$

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11. General plot processor  $\rightarrow$  plot results  $\rightarrow$  contour plot  $\rightarrow$  Nodal solution.  $\rightarrow$  All DOF  $\rightarrow$  X or Y component.
12. Element table  $\rightarrow$  Define table  $\rightarrow$  By sequence  $\rightarrow$  LS, 1
13. plot results  $\rightarrow$  contour plot  $\rightarrow$  Element table  $\rightarrow$  yes average.

### Result

The comparison b/w Ansys & theoretical value is shown.



$$E = 200 \text{ GPa} \quad P = 4 \times 10^3 \text{ N} \quad L = 2000 \text{ mm}$$

Solution

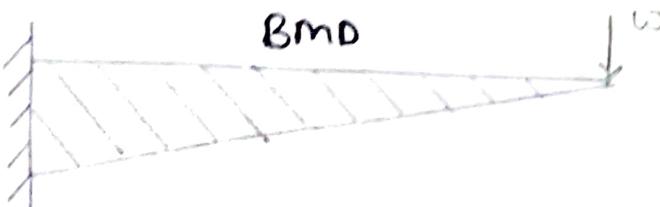
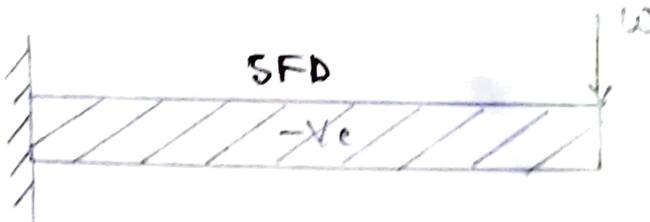
$$\text{Deflection } y = \frac{PL^3}{3EI}$$

$$I = \frac{bh^3}{12} = 3645 \times 10^3 \text{ mm}^4$$

$$A = 60 \times 90 = 5400 \text{ mm}^2$$

$$y = 14.6 \text{ mm}$$

$$\text{stress} = \frac{M}{Z} = \frac{6PL}{BD^2} = 98.765 \text{ N/mm}^2.$$



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### Beam

- 1 A 2m long cantilever with rectangular section (60\*90mm) is subjected to concentrated load of 4KN at the free end of the beam. Determine the deflection, maximum stress due to bending, Bending moment & shear force take.  $E = 200 \text{ GPa}$   $P = 4 \times 10^6 \text{ N}$ .
- Length  $L = 2 \text{ m} = 2000 \text{ mm}$ .

Soh

1. preferences  $\rightarrow$  structural
2. preprocessor  $\rightarrow$  element type  $\rightarrow$  Beam  $\rightarrow$  2D elastic.
3. Real constant  $A = 5400 \text{ mm}^2$   
 $I_{zz} = 3645 \text{ e}3$   
Height = 90
4. material properties  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  isotropic  
 $E_x = 200 \text{ e}3$   $\nu_{xy} = 0.3$
5. preprocessor  $\rightarrow$  modeling  $\rightarrow$  create  $\rightarrow$  Inactive CS  
 $A(0, 0)$   $B(200, 0)$ .
6. modeling  $\rightarrow$  create  $\rightarrow$  lines  $\rightarrow$  straight lines  $\rightarrow$  pick key points.
7. meshing  $\rightarrow$  mesh tool  $\rightarrow$  mesh line.
8. solution  $\rightarrow$  refine loads  $\rightarrow$  apply  $\rightarrow$  structural  $\rightarrow$  displacement  $\rightarrow$  on nodes.
9. solution  $\rightarrow$  solve  $\rightarrow$  current LS
10. general post processor  $\rightarrow$  plot results  $\rightarrow$  contour plot  $\rightarrow$  Nodal solution  $\rightarrow$  DOF solution  $\rightarrow$  Y component
11. general post processor  $\rightarrow$  Element table  $\rightarrow$  Define table  
Element table Data menu  $\rightarrow$  By sequence num  $\rightarrow$  SMISC

### Ansys Solution

Deformation  $y = 14.642 \text{ mm}$

Stress  $\sigma = 98.765 \text{ N/mm}^2$

### Result Comparison

	Ansys	theoretical
Deformation	14.642 mm	14.63 mm.
stress	$98.765 \text{ N/mm}^2$	$98.76 \text{ N/mm}^2$

D	D	M	M	Y	Y	Y	Y
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12. Plot results  $\rightarrow$  Contour plot  $\rightarrow$  Line Element Results

Element table item at node I: MM0M2I

Element table item at node J: MM0M2J.

13. General post processor  $\rightarrow$  Element table  $\rightarrow$  Define table

$\rightarrow$  By Sequence num., 8 MISC (0,8) Apply  $\rightarrow$  OK  $\rightarrow$

close

14. Plot Line Element Results Menu.

Element table item at node I: MF0RYI

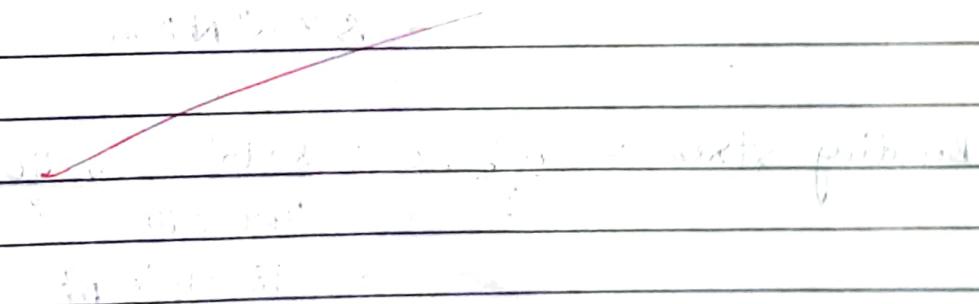
Element table item at node J: MF0RYJ.

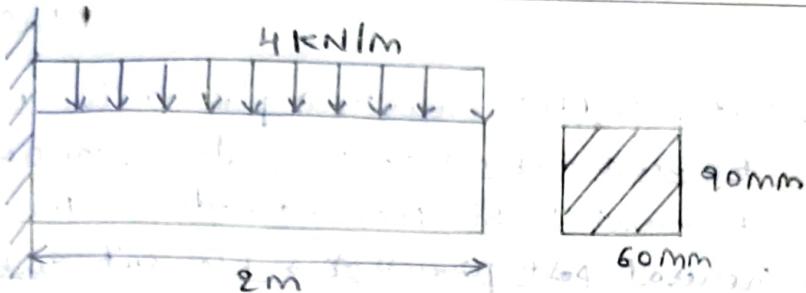
15. List Results  $\rightarrow$  Reaction Solution.

List Reaction Solution Menu.

Select all items  $\rightarrow$  OK.

Result: comparison of result is shown.





$$E = 200 \text{ GPa} \quad P = 4 \text{ kN/m} \quad L = 2000 \text{ mm}$$

$$A = 5400 \text{ mm}^2 \quad I = 3645 \times 10^3 \text{ mm}^4$$

$$H = 90,$$

$$\text{Deflection } \delta = \frac{WL^4}{8EI} = \frac{4 \times 10^3 \times (2000)^4}{8 \times 200 \times 10^3 \times 3645 \times 10^3}$$

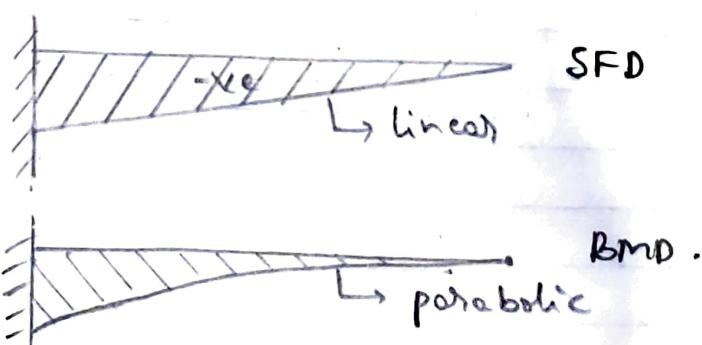
$$\boxed{\delta = 0.0109 \text{ m}}$$

$$\text{Bending Moment } M = \frac{WL^2}{2} = \frac{4 \times 1000 \times (2000)^2}{2}$$

$$= 8 \times 10^6 \text{ Nmm}$$

$$\text{Bending Stress } \sigma = \frac{mb}{I} \cdot c = \frac{8 \times 10^6}{3645 \times 10^3} \times \frac{90}{2}$$

$$= 98.7 \text{ N/mm}^2$$



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## Beam.

- Q A 9m long cantilever with rectangular section (60x90) mm is subjected to uniformly distributed load 4KN/m throughout out its length. Determine maximum bending stress and its deflection take  $E = 200 \text{ GPa}$ .

Soh

1. preference  $\rightarrow$  structural.
  2. preprocessor  $\rightarrow$  element type  $\rightarrow$  beam  $\rightarrow$  2D elastic.
  3. Real constant  $\rightarrow A = 5400 \text{ mm}^2$
- $$I_{zz} = 3645 \text{ e}3$$
- height  $\approx 90$ ,
4. material properties  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  isotropic  
 $E_x = 200 \text{ e}3$  .  $\nu_{xx} = 0.3$
  5. preprocessor  $\rightarrow$  modeling  $\rightarrow$  create  $\rightarrow$  Inactive CS.  
 $A(0,0)$     $B(200,0)$ ,
  6. using Modeling  $\rightarrow$  Create  $\rightarrow$  lines  $\rightarrow$  straight line  $\rightarrow$  pick key points.
  7. modeling  $\rightarrow$  mesh tool  $\rightarrow$  mesh line.
  8. solution  $\rightarrow$  Define loads  $\rightarrow$  Apply  $\rightarrow$  structural  $\rightarrow$  Displacement  $\rightarrow$  on nodes.
  9. solution  $\rightarrow$  solve  $\rightarrow$  current LS.
  10. General preprocessor  $\rightarrow$  plot results  $\rightarrow$  contour plot  $\rightarrow$  Nodal solution  $\rightarrow$  DOF Soln  $\rightarrow$  Y component.
  11. General post processor  $\rightarrow$  Element type table  $\rightarrow$  Defin-e table  $\rightarrow$  By Sequence number  $\rightarrow$  SMISC.

## Result

Ansys

theoretical.

Deflection

10mm

10.84 mm

Stress

98.76 N/mm<sup>2</sup>

98.76 N/mm<sup>2</sup>

D	D	M	M	Y	Y	Y	Y
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12. Plot Results  $\rightarrow$  Contour plot  $\rightarrow$  Line Element Results

Element table item at node I: MMOMZI.

Element table item at node J: MMOMZJ.

13. General post processor  $\rightarrow$  Element table  $\rightarrow$  Definetable  
 $\rightarrow$  By sequence num, SMISC (2,8) Apply  $\rightarrow$  OK  $\rightarrow$  Close.

14. plot Line Element Results menu.

Element table item at node I: MFORYI

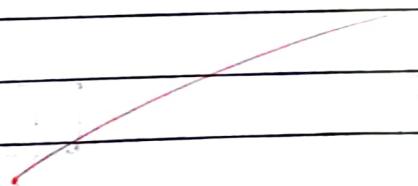
Element table item at node J: MFORYJ.

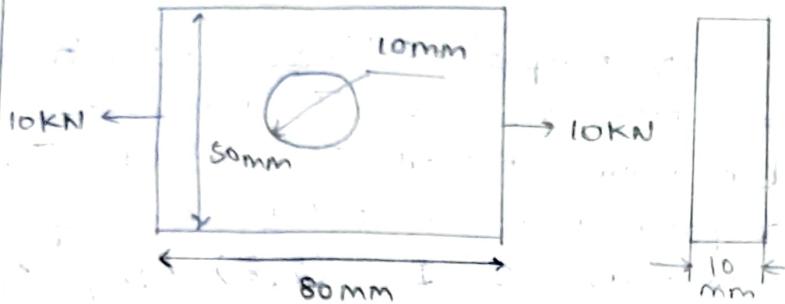
15. List Result  $\rightarrow$  Reaction Sln

List Reaction Sln menu:

Select all items  $\rightarrow$  OK

Result: comparison of result is shown.

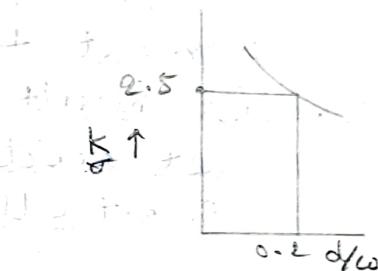




$$F = 10\text{ kN} \quad h = 10\text{ mm} \quad w = 50\text{ mm} \quad d = 10\text{ mm}$$

$$\frac{d}{w} = \frac{10}{50} = 0.2 \quad \therefore k_r = 2.5$$

$$\begin{aligned} \sigma_{avg} &= \frac{F}{A} = \frac{10 \times 10^3}{(b-d)h} \\ &= \frac{10 \times 10^3}{(50-10) \times 10} \\ \boxed{\sigma_{avg} = 28 \text{ N/mm}^2} \end{aligned}$$

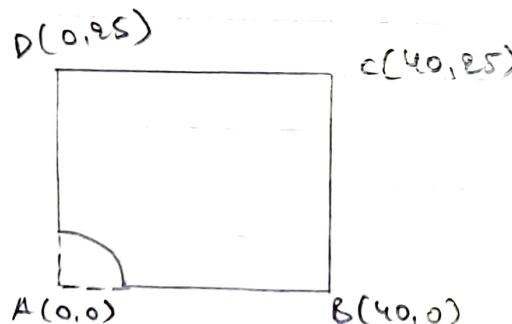


$$\text{pressure} = \frac{F}{A}$$

$$= \frac{10 \times 10^3}{50 \times 10}$$

$$\boxed{P = 20 \text{ N/mm}^2}$$

$$\begin{aligned} \sigma_{max} &= \sigma_{avg} \times k_r \\ &= 28 \times 2.5 \\ \boxed{\sigma_{max} = 62.5 \text{ N/mm}^2} \end{aligned}$$



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## plate with hole

1. Determine the max stress for a rectangular plate of 50 mm  $\times$  80 mm with hole of 10 mm diameter in the centre is loaded in axial tension. Thickness of the plate is 10 mm. Take  $E = 200 \text{ GPa}$ .

Soln 1. preference  $\rightarrow$  structural  $\rightarrow$  OK.

2. preprocessor  $\rightarrow$  element type  $\rightarrow$  solid  $\rightarrow$  Quad 4  $\rightarrow$  OK.

3. preprocessor  $\rightarrow$  element type  $\rightarrow$  option  $\rightarrow$  K3  $\rightarrow$  plane stress with thickness.

4. Real constant  $\rightarrow$  Add  $\rightarrow$  Select  $\rightarrow$  OK  $\rightarrow$  thickness (10mm)  $\rightarrow$  OK.

5. material properties  $\rightarrow$  model  $\rightarrow$  structural  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  isotropic  $\rightarrow E = 205$   $\rho = 0.3$  value.

6. model  $\rightarrow$  create  $\rightarrow$  Areas  $\rightarrow$  Rectangular  $\rightarrow$  By 2 corners  $\rightarrow$  x, y (0, 0)  $\rightarrow$  width (40) Height (25)

7. model  $\rightarrow$  create  $\rightarrow$  circle  $\rightarrow$  Solid circle  $\rightarrow$  (x, y) (0, 0)  $\rightarrow$  Radius (5).

8. operate  $\rightarrow$  Booleans  $\rightarrow$  subtract  $\rightarrow$  Areas  $\rightarrow$  select (rectangle) OK then (circle) OK

9. meshing  $\rightarrow$  mesh tool  $\rightarrow$  Area (set)  $\rightarrow$  Apply  $\rightarrow$  (0.1)  $\rightarrow$  OK.

10. Rize hidden  $\rightarrow$  mesh  $\rightarrow$  OK.

11. load  $\rightarrow$  Define  $\rightarrow$  Apply  $\rightarrow$  structural  $\rightarrow$  Displacement  $\rightarrow$  symmetric B.C  $\rightarrow$  on lines  $\rightarrow$  select lines  $\rightarrow$  OK.

Ansys Results

Deformation : 0.004329 mm.

Stress : 62.244 N/mm<sup>2</sup>.

Result:

	Ansys	Theoretical
Deformation,	0.004329 mm	—
Stress	62.244 N/mm <sup>2</sup>	62.5 N/mm <sup>2</sup> .

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19. ph

13. So

14. pl

dis

15. pl

perio

16. p

Result

D	D	M	M	Y	Y	Y
1	1	0	8	2	0	2

12. pressure  $\rightarrow$  on lines  $\rightarrow$  (-20) value  $\rightarrow$  OK.
13. Solution  $\rightarrow$  Solve  $\rightarrow$  current L.S  $\rightarrow$  soln done
14. plot results  $\rightarrow$  contour plot  $\rightarrow$  Nodal Soln  $\rightarrow$  displacement  $\rightarrow$  stress  $\rightarrow$  von mises.
15. plot clts  $\rightarrow$  style  $\rightarrow$  symmetric expansion  $\rightarrow$  periodic  $\rightarrow$  V4  $\rightarrow$  OK.
16. plot clts  $\rightarrow$  Animate  $\rightarrow$  stress (von mises)  $\rightarrow$  OK.

Result: The solution is found and tabulated.

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2

C

S

E

Soln

L.F.

2.

3.

4.

5.

6.

7.M.

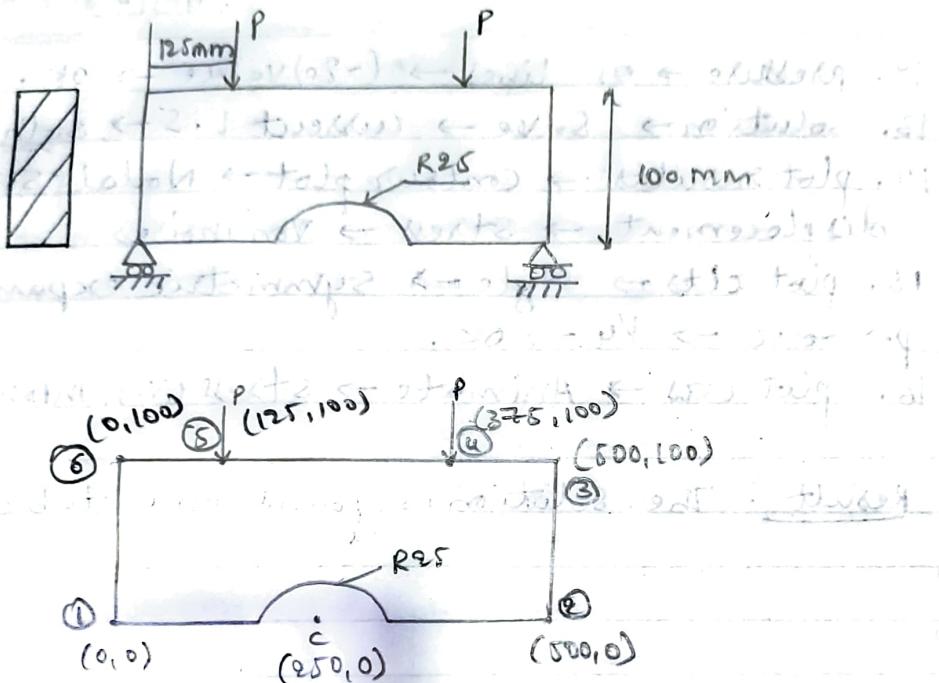
8.

9.

A

10.

e



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## plate problems

- 2 Calculate the stresses and displacement for the plate shown below. Let the load be  $P = 100\text{N}$  applied at equal distance from both ends and  $E = 3e7 \text{ N/mm}^2$ .

Soh 1. preference → structural

2. Element type → Solid → Quad 4 → OK.

3. Element type → Type plane stress with thickness → Element behaviour K3 → plane stress w/ thickness.

4. Real constant → Type PLANE42 → Thickness → 10mm.

5. material properties → material model → structural → linear → elastic → isotropic → Ex: 3e5

6. Modeling → Create → keypoints → In active CS

A location 0, 0, 0

B location 500 0 0

C location 500, 100 0

D location 375 100 0

E location 125 100 0

F location 0 100 0

7. Modeling → Create → Area → Through keypoint

8. modeling → Create → Area → circle → solid circle →

Xaxis: 250 → Yaxis: 0 → Radius: 25

9. Modeling → Create → operate → Boolean → subtract →

Area → pick rectangle first → pick area to be subtract → col (circle) → OK.

10. meshing → Mesh tool → Mesh → Mesh area → Mesh at

element → pick all → Refine Mesh → Level of refinement : 3,

## Ansys Solution

$$\sigma_{MX} = 0.477 \times 10^4 \text{ mm}$$

$$S_{MN} = 0.005404 \text{ mm}$$

$$S_{MX} = 7.879 \text{ N/mm}^2$$

Stress distributions  
are plotted below.  
The maximum stress is  
at the top fiber.  
The minimum stress  
is at the bottom fiber.  
The stress distributions  
are parabolic.

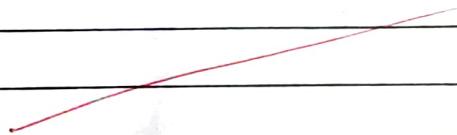
The stress distributions  
are plotted below.

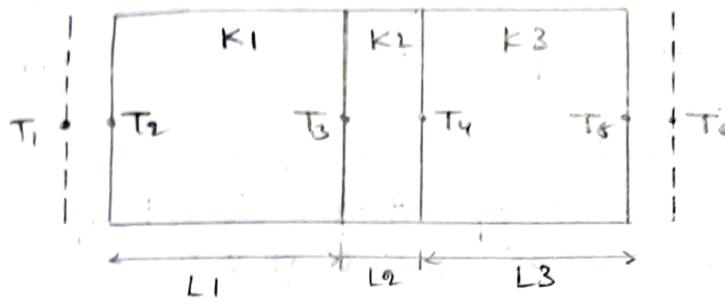
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D	D	M	M	Y	Y	Y	Y
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11. loads → Define loads → structural → Force / moment  
→ on Nodes → pitch node → 1 E, 2 → apply → DOF VY  
→ OK.
12. load → Define loads → apply → structural → Force /  
moment → on Key point → Select Keypoint 4 E, 5 → -100
13. solution → Solve → current LS
14. solution → General soln → plot results → counter  
plot → Nodal soln → Von mises solution.
15. list the Reaction solution.

Result: The Ansys solution is found and shown.





$$T_1 = 820^\circ\text{C} \quad T_6 = 110^\circ\text{C}$$

$$R_C = \frac{L_2}{A_2 k_2} = \frac{1}{k_2 A_2}$$

$$k_2 = 1 \text{ W/mK}$$

$$k_1 = 1.5 \text{ W/mK}$$

$$k_2 = 1 \text{ W/mK}$$

$$k_3 = 4.9 \text{ W/mK}$$

$$h_1 = h_2 = 38 \text{ W/m}^2\text{K}$$

$$L_1 = L_3 = 100 \text{ mm}$$

$$L_2 = L_4 = L_5 = 1 \text{ mm}$$

$$A = 1 \text{ m}^2$$



$$R = \frac{L}{K_A}$$

$$R_C = 0.001 \text{ m}^2\text{K/W}$$

$$R_1 = \frac{1}{h_1} = 0.029 = R_8$$

$$R_2 = \frac{L_1}{A_1 k_1} = 0.067 \text{ m}^2\text{K/W}$$

$$R_8 = \frac{1}{h_2} = 10^{-3} \text{ m}^2\text{K/W}$$

$$R_4 = \frac{L_3}{A_3 k_3} = 0.02 \text{ m}^2\text{K/W}$$

$$R_{eq} = R_1 + R_2 + R_8 + R_C + R_4 + R_5$$

$$R_{eq} = 0.148 \text{ m}^2\text{K/W}$$

$$Q = \frac{T_1 - T_6}{R_{eq}} = \frac{820 - 110}{0.148} = 4797.3 = Q$$

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## Heat transfer

A furnace wall is made of inside Silica brick ( $K=1.5 \text{ W/mK}$ ) and outside of magnesia brick ( $K=4.9 \text{ W/mK}$ ), each  $10\text{cm}$  thick. The inner and outer surfaces are exposed to fluids at temperature at  $820^\circ\text{C}$  and  $110^\circ\text{C}$  respectively. The contact resistance is  $0.001 \text{ m}^2\text{K/W}$ . The heat transfer coefficient for the inner and outer surface is  $35 \text{ W/m}^2\text{K}$ . Find the heat flow through the wall per unit area per unit time and temperature distribution across the wall.

Soh

1. preference  $\rightarrow$  Thermal  $\rightarrow$  OK.
2. preprocess  $\rightarrow$  Element type  $\rightarrow$  Link  $\rightarrow$  conduction (Link33)  
Apply  $\rightarrow$  convection (Link34)  $\rightarrow$  OK.
3. Real constant  $\rightarrow$  Add  $\rightarrow$  Link33 (Area 1)  $\rightarrow$  OK  
Link34 (Area 1)  $\rightarrow$  OK.
4. Material properties  $\rightarrow$  Material Models  $\rightarrow$  Thermal  $\rightarrow$  conduction  $\rightarrow$  isotropic ( $K_1 = 1.5$ )  
Material  $\rightarrow$  New Model  $\rightarrow$  Isotropic  $\rightarrow$  ( $K_2 = 1$ )  
Material  $\rightarrow$  New Model  $\rightarrow$  Isotropic  $\rightarrow$  ( $K_3 = 4.9$ )  
Material  $\rightarrow$  New Model  $\rightarrow$  Convection  $\rightarrow$  (HF = 35).  
Material  $\rightarrow$  exit.
5. Modeling  $\rightarrow$  Create  $\rightarrow$  Nodes  $\rightarrow$  In active CS  $\rightarrow$  Apply (0,0)  
(0.001m) Apply ; (0.101m) Apply , (0.102m) Apply , (0.202m)  
Apply , (0.203m) Apply .
6. Element  $\rightarrow$  Element Attributes  $\rightarrow$  Values of convection (1-2)  
34.  $\rightarrow$  Auto Numbered  $\rightarrow$  Thru nodes  $\rightarrow$  Select Nodes.

$$4797.3 = \frac{T_1 - T_2}{0.029}$$

$$T_2 = 670.878^\circ\text{C}$$

$$4797.3 = \frac{T_2 - T_3}{0.067}$$

$$T_3 = 349.46^\circ\text{C}$$

$$4797.3 = \frac{T_3 - T_4}{10^{-3}}$$

$$T_4 = 344.66^\circ\text{C}$$

$$4797.3 = \frac{T_4 - T_5}{0.02}$$

$$T_5 = 248.7^\circ\text{C}$$

Result:

Quantity	Ans	Theory
$T_2$	680.81°C	680.31°C
$T_3$	384.36°C	384.36°C
$T_4$	349.47°C	349.47°C
$T_5$	249.69°C	249.69°C
Heat flow	4889.2 W/m²	4797.3 W/m²

D	D	M	M	Y	Y	Y	Y
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node 2-3 → link 33 → set 1 → material 1

node 3-4 → link 33 → set 1 → material 2.

node 4-5 → link 32 → set 2 → material 3.

node 5-6 → link 34 → set 2 → material 4.

7. Solution → Ansys tool → New Analysis → Steady State → OK

8. Define loads → Apply → Thermal → Temperature → on Node

Node (1) Select (Apply) → Temp (820°).

Node (6) Select (Apply) → Temp (110°)

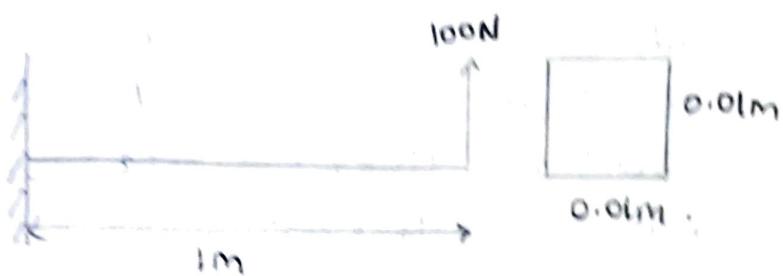
9. Solve → current LS

10. General post process → plot results → contour plot  
→ DOF Soln → Nodal soln :

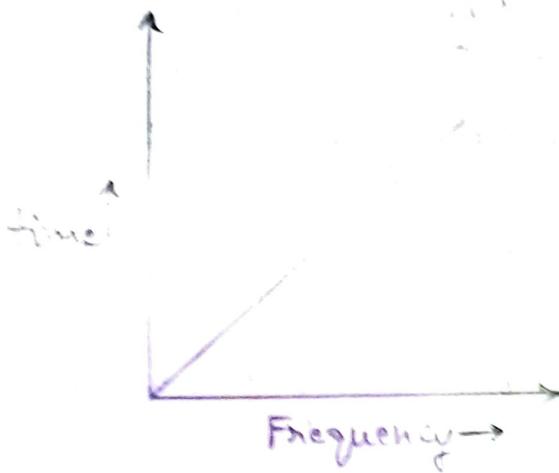
11. List Results → For listing table → Reaction Soln  
→ Heat flow.

12. Define table → Add → By sequence num → SMISCI

Result: The comparison is shown between ansys &  
theory.



### Nature of graph:



Scale

x-axis

1cm = 10 units

y-axis

1cm = 10 units



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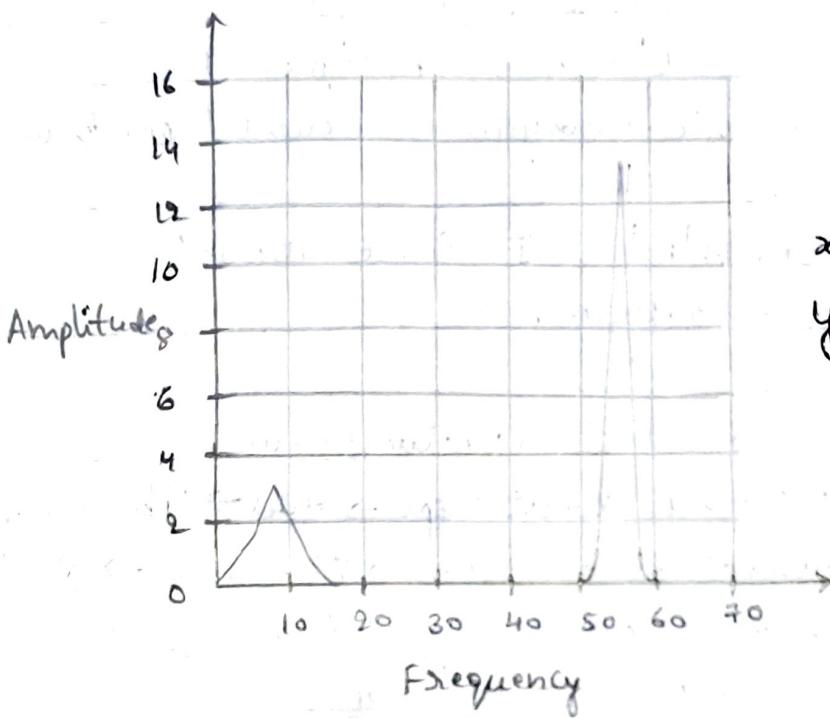
## Dynamic Analysis (Harmonic Analysis)

- Simple harmonic analysis of a cantilever beam as shown below.

$$E = 206800 \text{e} 6 \text{ N/m}^2 \quad I = 8.33 \text{e} - 10 \text{ mm}^4$$

$$P = 7830 \text{ kg/m}^3$$

- Soln
- preference → Select structural → OK.
  - preference → Element type → Add → Library of element types menu → Select Beam → 2D statics → OK
  - Real constants → Add → Type 1 BEAMS → OK.  
 $c/8 \text{ Area} = 0.01 \times 0.01$   
 $I = 8.33 \text{e} - 10$   
 $\text{Height} = 0.01 \rightarrow \text{OK}$ .
  - preprocessor → Material properties → Material Model → structural → linear → elastic → isotropic →  $E = 206800$   
 $e6 \cdot \sqrt{2} = 0.3$ ,  
Density → DENS → 7830 → OK
  - preprocessor → Modeling → Create → Key points → Inactive CS → Kp1(0,0) Kp2(1,0).
  - preprocessor → Modeling Create → linear → straight line → pick lines → OK.
  - preprocessor → Meshing → Mesh tool → Global size = 100 → OK.
  - Solution → Analysis type → New analysis → Analysis option → on → Harmonic load step optim → Time / frequency → frequency & sub steps. 0, 100, 100  
 stepped.



Scale

x axis 1cm = 10 units

y axis 1cm = 10 units

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9. Solution → Define loads → Apply → structural → Displacement

→ on keys → pick left end key points → All DOF → OK

10. Solution → Define loads → Apply → structural → force /  
moment → on keys.

→ pick right end point → FX → value of force → -100.

11. Solution → Solve → current LS → Solution → done → OK

12. Time list post processor → A window opens → click on  
element shown in window

[UV2 | 2 | Y-comdis]

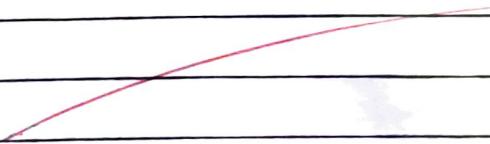
→ DOF Solv

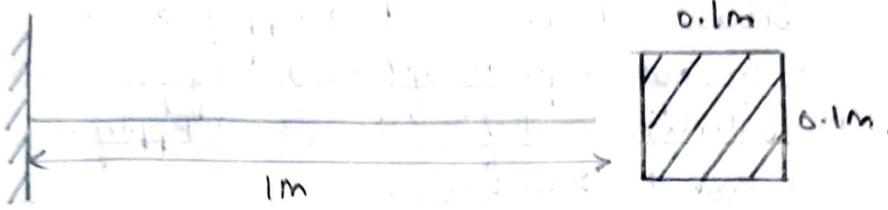
→ Y-Component.

→ select a point where load / time is acted (Rightend  
KP).

→ graph appears.

Result: The graph of frequency v/s values is plotted.





$$g = 9.81 \quad (B_1 I)^2 = 3.52 \quad (B_2 I)^2 = 22 \quad B_3 I^2 = 61.7$$

$$\omega_1 = \frac{(BI)^2}{\sqrt{EI/\rho I^4}} \quad I = 8.33E-06 \quad \rho = 7,830 \text{ kg/m}^3$$

$$\text{Natural frequency} = \frac{\omega}{2\pi}$$

$$\omega_1 = 1.608E3$$

$$f_1 = 2985.89$$

$$\omega_2 = 1.005E4$$

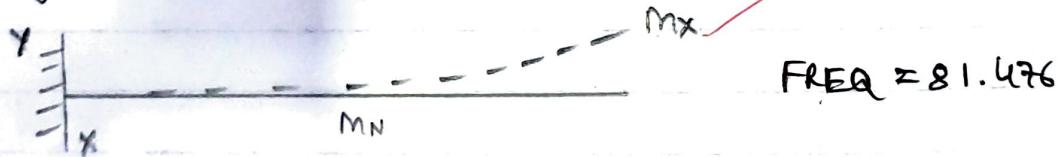
$$f_2 = 6599.35$$

$$\omega_3 = 2.819E4$$

$$f_3 = 4488.47$$

Soln

### Ansys results



DD MM YY  
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## Dynamic Analysis (Model Analysis)

- 2 Simple modal analysis of a cantilever beam as shown below. objective is to get the frequency and different modes of vibration.

$$E = 211 \text{ N/mm}^2$$

$$I = 8.33 \times 10^{-6} \text{ m}^4$$

$$\text{Area } A = 0.01 \text{ m}^2$$

$$\text{Density} = 7830 \text{ kg/m}^3.$$

Soln

1. preference  $\rightarrow$  structural  $\rightarrow$  OK.

2. preprocessor  $\rightarrow$  Elemental type  $\rightarrow$  Adel  $\rightarrow$  Select Beam  $\rightarrow$  2D elastic  $\rightarrow$  OK.

3. Real constant  $\rightarrow$  Adel  $\rightarrow$  Type1  $\rightarrow$  Beam B  $\rightarrow$  OK

$$(1) \text{ Area} = 0.1 \times 0.1$$

$$I = 8.33 \times 10^{-6}$$

$$t = 0.1$$

4. preprocessor  $\rightarrow$  material property  $\rightarrow$  Material models  $\rightarrow$  Structural  $\rightarrow$  linear  $\rightarrow$  elastic  $\rightarrow$  Isotropic.

$$E_x = 211$$

$$\nu = 0.5$$

Density  $\rightarrow$  PENS  $\rightarrow$  7830  $\rightarrow$  OK.

5. preprocessor  $\rightarrow$  Modeling  $\rightarrow$  Create  $\rightarrow$  Key points  $\rightarrow$  In active CS  $\rightarrow$  KP1(0,0) KP2(4,0).

6. preprocessor  $\rightarrow$  Modeling  $\rightarrow$  Create  $\rightarrow$  Line  $\rightarrow$  straight line pick end key points of line  $\rightarrow$  OK.

7. preprocessor  $\rightarrow$  Meshing  $\rightarrow$  mesh tool  $\rightarrow$  Global size  $\rightarrow$  no. of divisions - 100  $\rightarrow$  click on mesh  $\rightarrow$  OK.

Result:

Mode	Ansys (Hz) Frequency	theory (Hz) Frequency
1	81.476	81.7
2	506.37	510.63
3	1278	1432.1

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8. Solution → Analysis → New analysis →  model → Analy -bis option.

No of mods to extract [10]

No of mods to expand [10]

9. Solution → Define loads → Apply → structural → Displace -ment → on keypoints → pick left and key points → All DOF → ok.

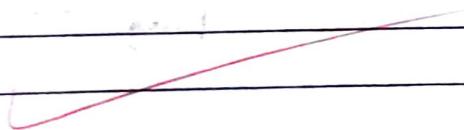
10. Solution → Solve → wait until s → Solutions is done → ok

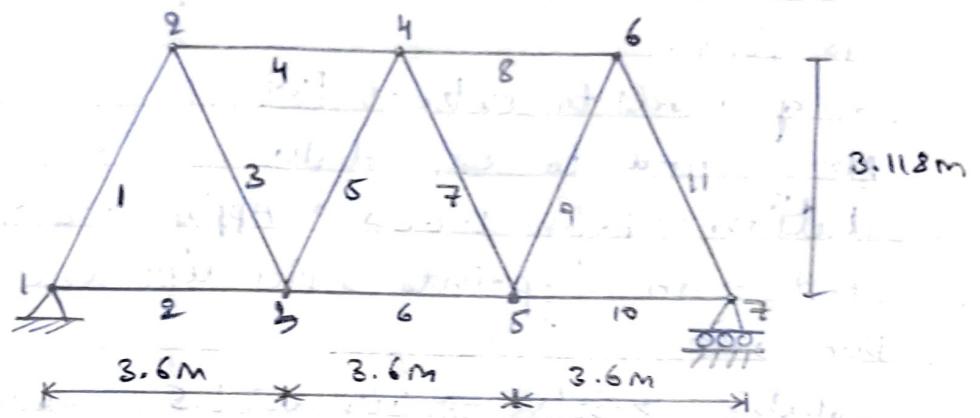
11. General post processor → result symmetry → Read result → first set.  
next set.

→ plot result → contour plot → Nodal Soln → Note down

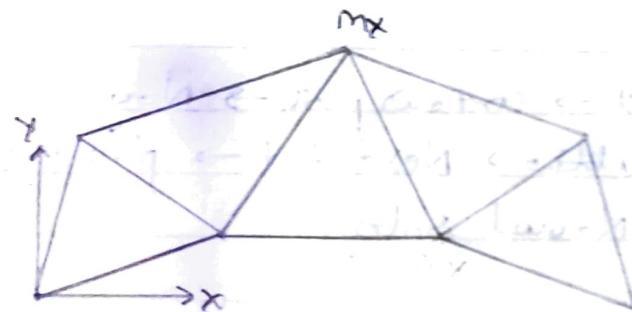
→ Read results → Next Set → plot results → counter  
plot → Nodal soln.

Result: The comparison is shown in table.



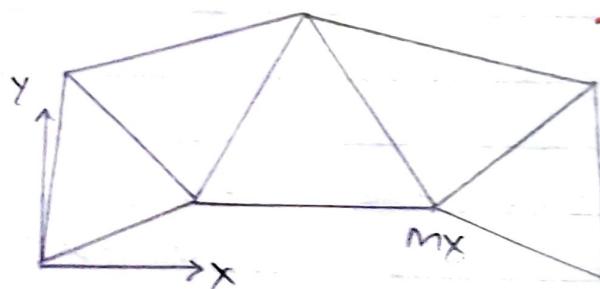


Set 1:



$$\text{Freq} = 48.394 \text{ Hz}$$

Set 2:



$$\text{Freq} = 79.86 \text{ Hz}$$

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## Dynamic analysis

- 3 Determine the modal deflections for the truss system shown below ( $E = 200 \text{ GPa}$ ,  $A = 3250 \text{ mm}^2$ ).

Soln

1. preference → Select structural → ok.
2. preprocessor → Element type → Add → library of element → link 2D Spur → ok.
3. Real constant → Link1 → Area =  $3250 \times 10^6$
4. preprocessor → Material property → Material Model → Structural → linear → elastic → Isotropic → Ex = 2e5 → PRxy = 0.3

5. Modeling → Create → keypoints → inactive cs,

XYZ location [0] [0]

XYZ location [18] [3.118]

XYZ location [3.6] [0]

XYZ location [8.4] [3.118]

XYZ location [7.2] [0]

XYZ location [9] [3.118]

XYZ location [10.8] [0]

6. Modeling → Create → line → straight line → on key points.

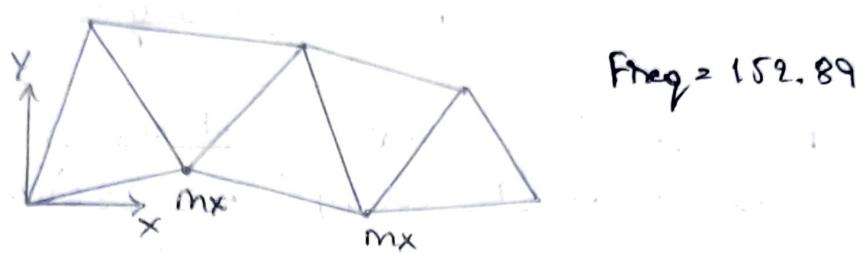
7. preprocessor → Meshing → Mesh tool → Global size → No. of division - 1 → click on mesh → ok.

8. solution → Analysis type → New Analysis →  model  
→ Analysis option.

No. of modes to extract [10]

No. of modes to expand [10]

Set 3:



Result:

Set	Time/Freq
1	48.384
2	72.864
3	152.89
4	195.24
5	246.76

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9. Solution → Define Loads → Apply → structural → Displacement → on keypoints → pick left end and right end  
 Key point (1, 8, 7) DOF → UY → OK

10. Solution → Solve → current L.S → Solution → OK.

11. General postprocessor → Result summary → Read result  
 → first set.  
 → Next set.  
 → plot results → contour plot → Nodal soln → Note down  
 → Read results → Next set → plot results → contour plots  
 → Nodal soln.

Result: The result are tabulated.

~~(a)~~  
 11/8/21