

Homework #10

Ben Drucker

6.2

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a)

$$P\left[z_{\alpha_1} \leq (\bar{X} - \mu) \frac{\sigma}{\sqrt{n}} \leq z_{\alpha_2}\right] = 1 - \alpha. \text{ Solving for } \mu : \bar{X} - z_{\alpha_2} \frac{\sigma}{\sqrt{n}} \leq \mu \leq \bar{X} + z_{\alpha_1} \frac{\sigma}{\sqrt{n}}.$$
$$\left(\bar{X} - z_{\alpha_2} \frac{\sigma}{\sqrt{n}}, \bar{X} + z_{\alpha_1} \frac{\sigma}{\sqrt{n}}\right)$$

b)

$z_{\alpha_1} = 2.24; z_{\alpha_2} = 1.78$. So the width is: $(2.24 + 1.78) \frac{\sigma}{\sqrt{n}} = 4.02 \frac{\sigma}{\sqrt{n}}$. This is wider than the $3.96 \frac{\sigma}{\sqrt{n}}$ width of the 7.5 interval.

7.2

12

$$.81 \pm 2.58 \frac{.34}{\sqrt{110}} = (.73, .89)$$

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a)

$$89.1 \pm 1.96 \frac{3.73}{\sqrt{169}} = (88.54, 89.66). \text{ This interval appears very precise.}$$

b)

$$n = \left(\frac{1.96*.16}{.5}\right)^2 = 245.9; n = 246.$$

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$$\bar{x} - z_{1-.9} \frac{s}{\sqrt{n}} = 4.25 - 1.28 \frac{1.3}{\sqrt{75}} = 4.059$$

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$$.15 \pm 2.58 \sqrt{\frac{.15*.85}{4722}} = (.137, .163)$$

7.3

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Via a t table:

a

1.341

b

1.753

c

1.708

d

1.684

e

2.704

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Via a t table:

a

$t_{.025,10} = 2.228$

b

$t_{.025,15} = 2.131$

c

$t_{.005,15} = 2.947$

d

$t_{.005,4} = 4.604$

e

$t_{.01,24} = 2.492$

e

$t_{.005,37} = 2.712$