## Module 1: Machine Learning – An overview

Lecture 2- Part 2

Theme: Factors that influence Hypothesis Space Search

Topic-1: Overfitting in the Search Space

#### Training Error:

$$err_{train}(h) = Pr_{x \in D}[h(x) \neq c(x)] = \frac{count\ of\ mismatches}{|D|}$$

$$h_{target} = \underset{h \in H}{\operatorname{argmin}} \{err_{train}(h)\}$$

• True Error:

$$err_{true}(h) = Pr_{x \in S}[h(x) \neq c(x)]$$

• Overfitting:

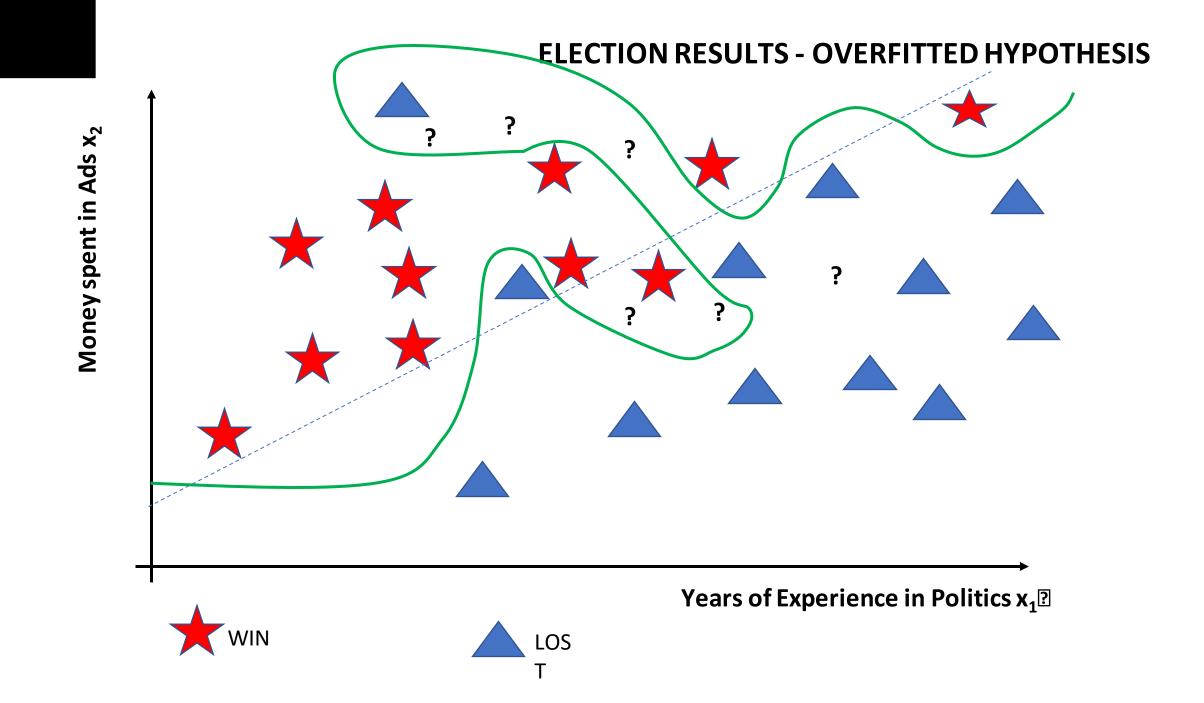
$$err_{true}(h) \gg err_{train}(h)$$

# Overfitting – Case of over-training

 The model performs quite well on training data, but rather poorly on test data

 Overfitting occurs when a model becomes complex due to overtraining.

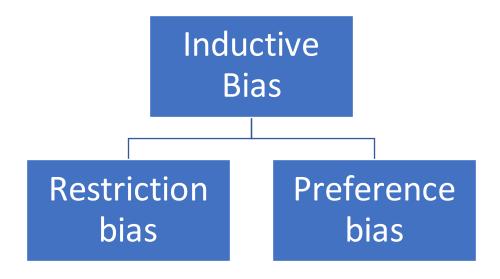
• Overfitting is **the symptom** indicating *Inductive Learning Hypothesis stands falsified* 



### **Optimization Constraints to simplify learning**

- Unbiased learning is futile as It leads to an exhaustive search.
- Inductive bias is a *set of assumptions* on *Target Hypothesis* to achieve generalization
- Additional constraints are imposed to guide search and improve generalization

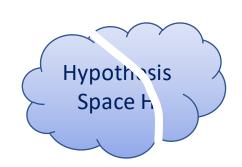
## **Additional Constraints**



# Topic 2: Restriction & Preference Biases

### I. Restriction Bias

- Cuts off portions of the Hypothesis space 
  Incomplete Hypothesis space
- Forces a less expressive learning model to improve generalization
- Takes Less time to search through the hypothesis space



### **Restriction Bias**

➤ If hypothesis is a *Boolean expression*, Allow Only AND terms (conjunctions), *not* AND-OR terms (disjunctions of conjunctions)

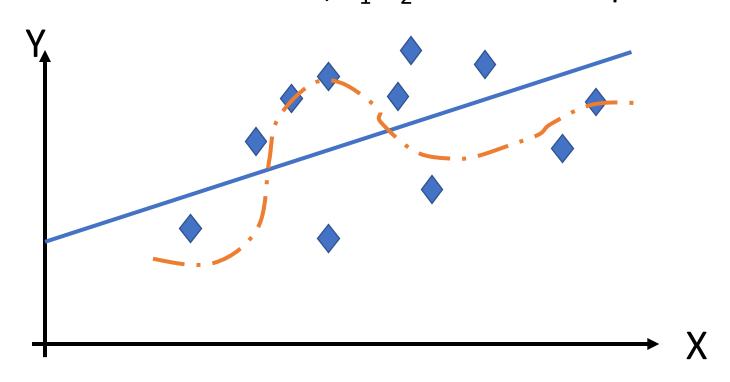
Go to Cinema?

Weekend ?	Pending work?	New Movie?	Friend Available?	See Movie?
Υ	N	Υ	Υ	Υ
N	N	Υ	Υ	Υ
N	Υ	Υ	Υ	N

➤ Not allowed: If Weekend OR New Movie THEN See movie

#### **RESTRICTION BIAS**

If hypothesis is *a curve* that separates or fits data: Allow only first order linear x terms, do not allow higher order terms such as :  $x^2$ ,  $x_{1*}x_{2}$  etc. in the equation of curve:



### II. Preference bias

Principle of OCCAM's Razor\* or Parsimony: *Given two models* that can solve a problem, Prefer the simpler one

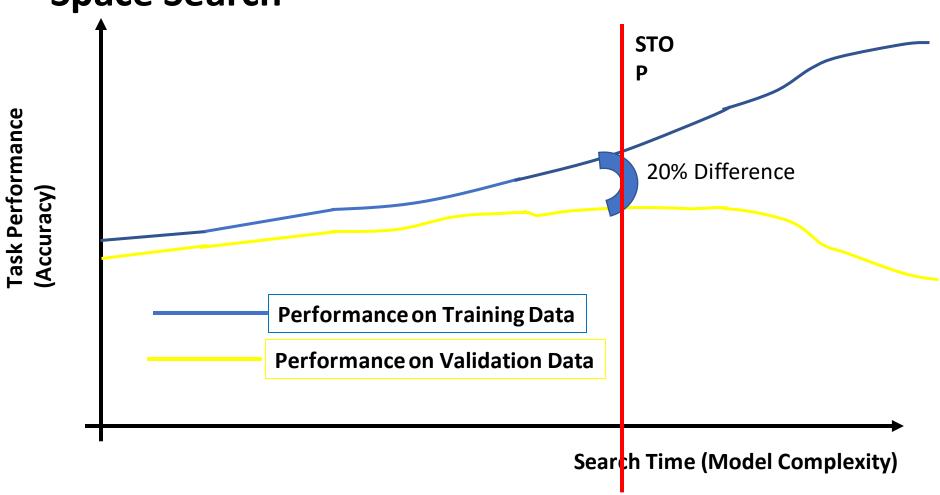
\*Occam is a place, Scottish logician Sir William Hamilton of Occam gave the principle in the 14<sup>th</sup> Century!

- ➤ If Hypothesis is a Decision Tree: Search greedily towards immediate rewarding paths
- ➤ If Hypothesis is a Boolean Function: Prefer lesser attributes and lesser number of terms
- ➤ If Hypothesis is a Decision Tree: Prefer shorter trees over long trees

# **Preference Bias - Regularization**

- > If Hypothesis is curve:  $w_0+w_1x_1+w_2x_2=0$ , Prefer lower values of weights especially for unimportant attributes
- ➤ The weight parameters are normally adjusted by optimizing the Objective Function (OF) during the Hypothesis space search process: e.g. Minimize{MSE} / Maximize{Accuracy}
- ➤ Now, OF is augmented with a regularization term to prohibit excessive weights, or even make them vanish!
- > This process is called Regularization

**Detecting and Arresting Overfitting during Hypothesis Space Search** 



# Topic 3- Underfitting & Data Considerations

# Case of Underfitting

- Underfitting happens when the model is too simple
- It gives high training error as it is unable to extract mappings / concepts
- It gives a constant average error over training data called Bias error
- It also gives high true error on test data due to lack of generalization
- It can be tackled by increasing training time, adding more effective features and reducing regularization

#### Factor C: Data considerations for Improving Search Quality

Recall that Training Data D is but a subset of Sample Space S. Training data considerations:

• Is Training Data sufficient?

Else learner may underfit and classify all examples similarly

 Is data noisy (contains measurement, transmission and input errors or has missing values)?

Else may overfit noisy data and misclassify valid new data!

Is data complexity manageable?

Else it may be difficult to arrange for data

### Data considerations

 Does it represent all kinds of variety in original sample population?

Else trained model may not be able to correctly classify new instances which was not represented!

Does it have a balance of all kinds of response (say 'yes' and 'no')

Else trained model may be biased towards one class, and not be able to classify the less represented class!

### Challenges in Preparing Data.....

- Domain understanding Adopt interdisciplinary approach Medical Diagnostics, E-Commerce, Stock analysis
- 2. Data Collection: Can collect only samples from population of real data
- 3. May need to collect from multiple sources **Data integration** 
  - Published databases
  - Collect field data
  - IOT devices
  - Social media
  - Crowd sourcing

## Preparing Data...

- 4. May need to remove noise or errors Data Cleaning
- 5. May need to fill up missing values in table **Data completion**

#### 6. Pre-processing data

- Standardise & Normalize numerical data
- Convert text words to root form
- Find statistical properties of data

#### 7. Feature selection/elimination

### Tackling Bias towards a response class

• Part of the training data is reserved for validation / testing a learner.

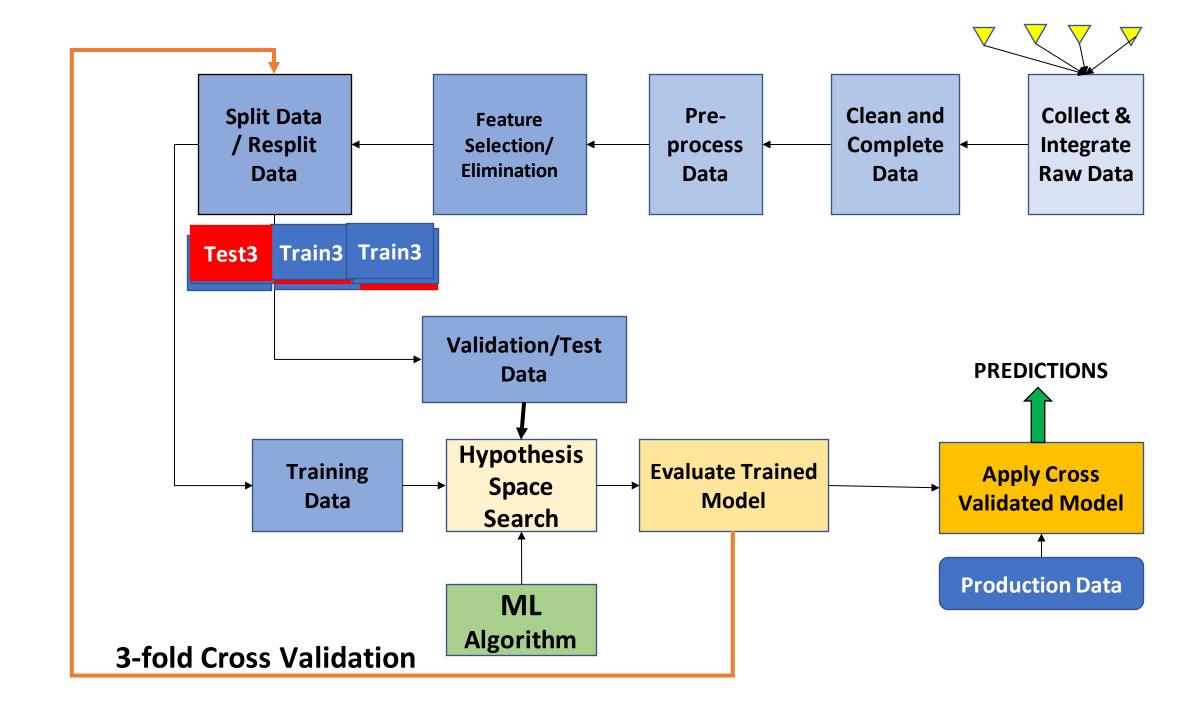
Illustration of biased training / testing:

#### **Training Data For Predicting Recruitment Results**

Highest Qualifica tion	Years of Experience	Level of Coding Skill	Reference	Interview Perf.	Result
UG	5	Good	Excellent	Good	Accept
PG	3	Med	Good	Bad	Reject
UG	6	Poor	Medium	Excellent	Accept
UG	2	Good	Excellent	Good	Accept
•••	•••	•••			•••

#### **Testing**

Highest Qualificat ion	Years of Experie nce	Level of Coding Skill	Reference [	<b>)artte</b> rview Perf	Result
PG	5	Bad	Med	Good	???/Reject
UG	3	Med	Good	Med	???/Reject



# **Learning Points...**

- > Overfitting occurs when a model performs well on training data but poorly on test data (high true error)
- ➤ To avoid overfitting in supervised learning, In addition to assuming an Inductive Bias on the target hypothesis, additional constraints are imposed on learning, that is while searching through Hypothesis Space
  - > Restriction bias limits expressive power of hypothesis space
  - > Preference bias favours simpler models in accordance with Occam's Principle of Parsimony. Preference bias can also prefer searching certain portions of the search space.
  - ➤ Regularization a preference bias, can be achieved in many ways during the Hypothesis Space search process, such as (i) by adding a regularization term in OF (ii) by Stopping the search process early.

## **Learning Points**

- > Underfitting can be detected easily during training and avoided by increasing training time, adding features and reducing regularization.
- > To make search effective, Data must be sufficient, have enough variety to represent all possible cases, remain free of bias and have noisy data purged
- > Data must be pre-processed to improve its quality. This includes data collection, integration, cleaning, filling missing values, and feature selection/elimination
- > Cross-validation ensures that all parts of available data are utilized for training and testing. It removes bias towards a class.

#### **Learning Points**

- > Thus, we conclude that there are three factors that influence Hypothesis Search Space:
- 1. Overfitting
- 2. Underfitting
- 3. Data quality

## See Transcript for Link for self-assessment:

"If there is anything worse than knowing too little, it is knowing too much"

**Enjoy learning!!**