

Implementing a polyphase uniform DFT filterbank

Objective:

To study the implementation of a 2 channel DFT filter bank with $h[n] = [1, 1, 1, 1]$ in order to appreciate its computational efficiency over implementing separate filters.

Procedure:

Step 1: Deriving a 2 channel DFT filter bank

We know that $h[n] = [1, 1, 1, 1]$ and since $M = 2$:

$$H_0(z) = E_0(z^2) + z^{-1}E_1(z^2)$$

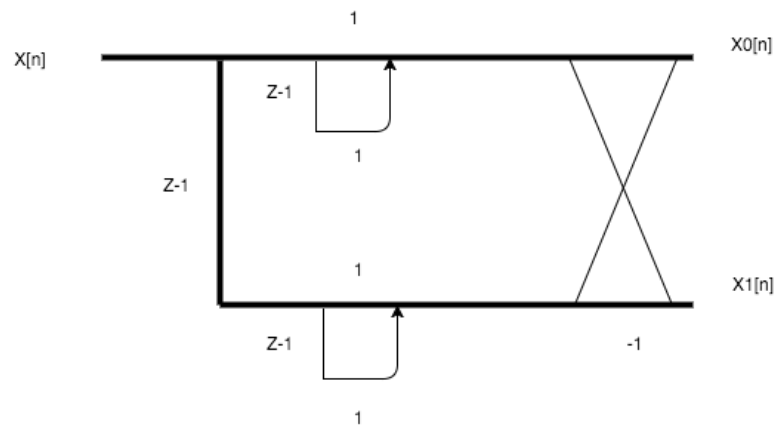
$$e_0[n] = h_0[2n]$$

$$e_1[n] = h_0[2n+1]$$

$$E_0(z^2) = 1 + z^{-2}$$

$$E_1(z^2) = 1 + z^{-2}$$

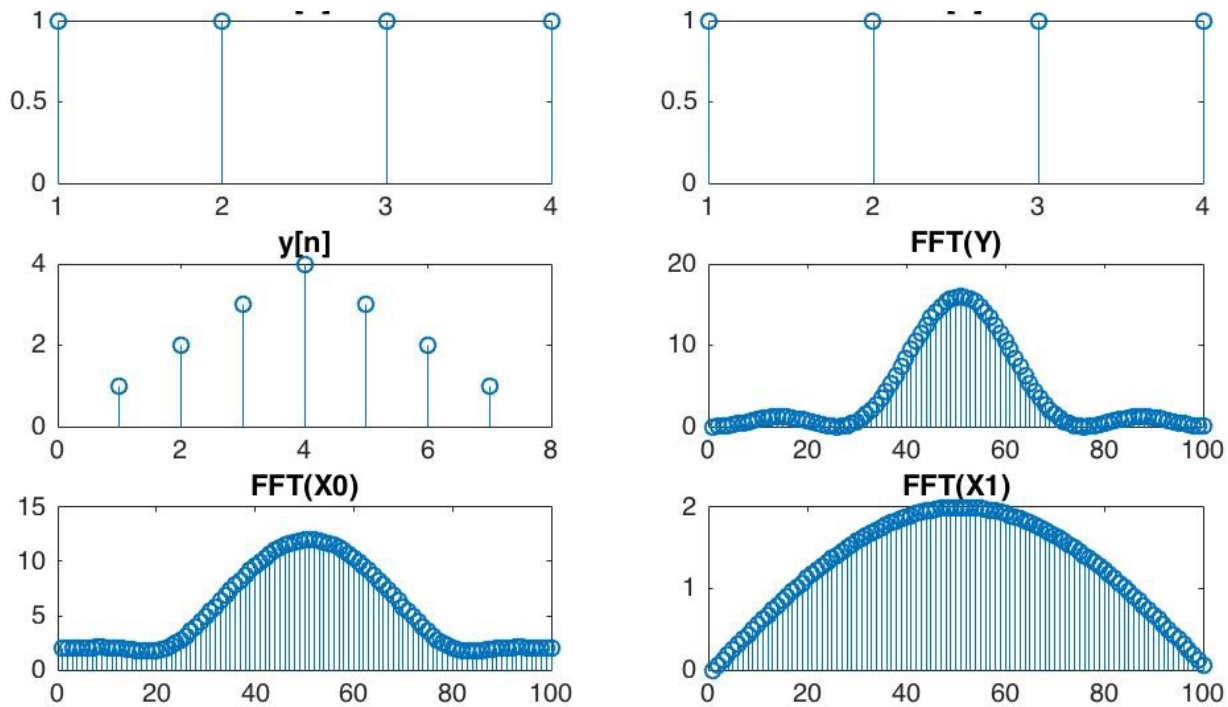
$$H_0(z) = 1 + z^{-2} + z^{-1}(1 + z^{-2})$$



2 channel uniform DFT filterbank implementation

Step 2: Implementing the filter

I first created the signal $h[n]$ in matlab and $x[n] = [1, 1, 1, 1]$ as the test signal and computed the convolution y after which i implemented the filters $E0$ and $E1$. A delay filter z was also created. The outputs at Node 0 and Node 1 were computed (right before the cross in the flow diagram towards $X0$ and $X1$ respectively.) With these values $X0[n]$ and $X1[n]$ were found. The following figure show my results:



As we can see, the result of the convolution between the signal and the filter is a triangular function which is a sinc in the frequency domain. The two outputs $X0$ and $X1$ obtained from the polyphase uniform filter bank are seen here

Conclusions:

The 2 channel polyphase implementation of the DFT filter bank was successful and the output $X0$ and $X1$ was computed efficiently by reusing filter elements through this implementation. The code was later hosted on GitHub: <https://github.com/adarshmammen/Polyphase-DFT-filter-bank---2-Channel>