1. Heuristic Function:

The idea is to simplify the problem a bit (or relax) and then try calculating the heuristic value of every state.

I simplify the problem by assuming that the problem only consists of only six intersection tiles [(0,0), (180,180), (90,0), (90, 180), (90, 90), (90, 270)].

Later, the approach is to calculate the avg of the sum of shortest distance (in terms of no of rotation) of only these six tiles and take actions accordingly.

The idea of using the shortest number of rotation instead of straight forward Manhattan distance [(x2-x1) - (y2-y1)] of the degree of movement of the tiles is because the final cost is in terms of the number of rotation to reach the goal instead of degree of movement.

Hence, when adding g(n) which is the count of rotations till now to h(n), h(n) should again be in terms of rotation and not degree.

Admissible (Why will this heuristic be optimal and always get a value lesser than the actual cost?)

- a. Shortest Distance: The idea of using the shortest distance average as a heuristic is to create a lower bound to the actual cost.
- b. The shortest distance will always ensure that the cost count is minimal and will always be lesser or equal (in a hypothetical case of all 6 mentioned tiles take the right position by avg rotation calculated as the heuristic value).
- c. Whenever the action is taken with this heuristic, the expanded node is in its optimal path because of the shortest distance consideration.

Since the search space is a tree, the need to show consistency is not applicable.

A possible shortcoming of this heuristic:

The initial idea of minimizing the number of tiles to six was to relax the constraints on the

problem so as to avoid overestimating the heuristic value. I'm not sure if this logic actually helps to improve the heuristic or can be a cause of high underestimation, which may make the heuristic optimal but very slow to reach the goal state.

2. Code submitted as Assign2.zip and document as Assign2.pdf.

3.

The code runs with optimal results for all PathN-n.md files.

Puzzle files:

Detail Running Parameters (For puzzle 0):

Puzzle File: Puzzle-0.md

Time	BFS	A-Star	RBFS
100 seconds	States Explored: 322456	States Explored: 280261	States Explored: 39998
	Maximum Frontier Length: 1362224 Current Path	Maximum frontier length: 1132001	Current Path Length: 7
	Length: 8	Current Path Length:9	
200 seconds	States Explored: 456618	States Explored: 455037	States Explored: 93412
	Maximum Frontier Length: 1956675 Current Path	Maximum frontier length: 1556872	Current Path Length: 8
	Length: 8	Current Path Length:10	
300 seconds	States Explored: 571467	States Explored: 547935	States Explored: 135436 Current Path
	Maximum Frontier	Maximum frontier	Length: 8

	Length: 2452883	length: 1908038	
	Current Path Length: 9	Current Path Length:9	
400 seconds	States Explored: 656091	States Explored: 567062	States Explored: 181215
	Maximum Frontier Length: 2811114	Maximum frontier length: 2300019	Current Path Length: 7
	Current Path Length: 9	Current Path Length: 8	
500 seconds	States Explored: 756981	States Explored: 647203	States Explored: 236132
	Maximum Frontier Length: 3190874	Maximum frontier length: 2509127	Current Path Length: 7
	Current Path Length: 9	Current Path Length: 8	
600 seconds	States Explored: 785496	States Explored: 680670	States Explored: 267133
	Maximum Frontier Length: 3367748	Maximum frontier length: 2798090	Current Path Length: 9
	Current Path Length: 9	Current Path Length: 8	
700 seconds	States Explored: 941986	States Explored: 695182	States Explored: 301232
	Maximum frontier length: 4033704	Maximum frontier length: 3004563	Current Path Length: 9
	Current Path Length: 9	Current Path Length: 9	
800 seconds	States Explored: 942740	States Explored: 765369	States Explored: 323412
	Maximum frontier length: 4037586	Maximum frontier length: 3216576	Current Path Length: 9

	Current Path Length: 9	Current Path Length: 9	
900 seconds	States Explored: 1011249	States Explored: 765369	States Explored: 356989
	Maximum frontier length: 4329546	Maximum frontier length: 3499891	Current Path Length: 8
	Current Path Length: 9	Current Path Length:9	

Brief Report: For algorithms run over Puzzle 0,8, and 11 for 15 mins each.

Puzzle	BFS	A-Star	RBFS
Puzzle-0	Max Explored States: 1011249 Max Frontier Size:	Max Explored States: 795925 Max Frontier Size:	Max States Explored: 465817
	4329546	2981204	
Puzzle-8	Max Explored States: 1121980	Max Explored States: 809165	Max States Explored: 489132
	Max Frontier Size: 4532192	Max Frontier Size: 3032418	
Puzzle-11	Max Explored States: 1090231	Max Explored States: 778093	Max States Explored: 455392
	Max Frontier Size: 4423217	Max Frontier Size: 2899801	
Average Puzzle	Average States Explored: 1074486	Average States Explored: 794394	Average States Explored: 470113
	Average Frontier Size: 4428318	Average Frontier Size: 2971141	

Inferences:

- Breadth-First Search is a good algorithm when the solution is not very deep in the search space. The algorithm begins saturating as the levels begin to increase.
- 2. A*, when compared to BFS, needs to visits far fewer nodes in the search space due to the guiding heuristics and hence achieves much faster results.
- 3. RBFS is a good optimization for saving space. The problem can be recursion. From my observation doing the assignment (in python) and exploring the results, the algorithms do save space but explore fewer states than A* in the same amount of time.

The best algorithm for this problem: A*

BFS is not a suitable algorithm because of its uninformed nature and the algorithm saturates after traversing few levels (in a tree space search).

A* is better than RBFS when the tradeoff between time and space is considered under the resources available under which assignment has been done and the language of choice.

Python (the language of implementation) is not suited for recursive algorithms and does not have a good reputation with recursion.

It is also evident with the observations from the detailed report. The number of explored states for RBFS is far less than states explored by A* in a given amount of time.

Hence, with space being a cheap resource and time being of more importance A* is a better algorithm for this problem.