

# Learning from volumetric depth

Geometric Computer Vision

GCV v2021.1, Module 5

Alexey Artemov, Spring 2021

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## Lecture Outline

### §1. Volumetric 3D representations [15 min]

- 1.1. Volumetric 3D shapes
- 1.2. Connections to other 3D modalities
- 1.3. Constructing volumetric 3D shapes from range-images

### §2. Spatial data structures [15 min]

- 2.1. Dense volumetric 3D grids
- 2.2. Sparse data representations
- 2.3. Octrees

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## Lecture Outline

### §3. Constructing neural networks on volumetric data [15 min]

- 3.1. Dense 3D CNNs
- 3.2. Sparse 3D CNNs
- 3.3. Octree-based CNNs

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## §1. Volumetric 3D representations

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# Volumetric 3D shapes

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## 1.1. Volumetric 3D functions

### §1. Volumetric 3D representations

- **Occupancy map:** a binary function  $\text{OCC}(\mathbf{x}) : \Omega \rightarrow \{0,1\}$
- **Signed distance function (SDF):** an array of signed distance values  $\text{SDF}(\mathbf{x}) : \Omega \rightarrow \mathbb{R}$ 
  - Positive values outside the shape (free space), negative inside (occupied space)
- **Truncated SDF (TSDF):**  $\text{TSDF}(\mathbf{x}) : \Omega \rightarrow [-\sigma, \sigma]$ 
  - Set max value to a fixed value  $\text{TSDF}(\mathbf{x}) = \min(\max(\text{SDF}(\mathbf{x}), -\sigma), \sigma)$

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## 1.1. Volumetric 3D data

### §1. Volumetric 3D representations

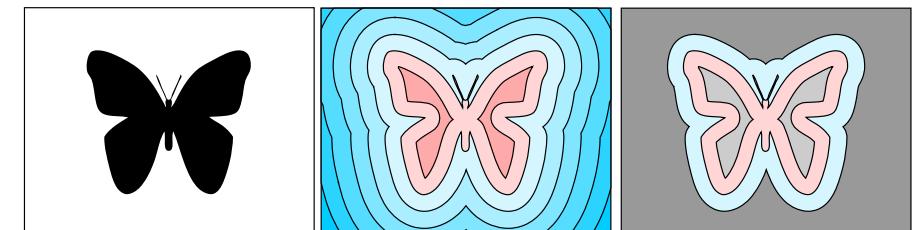
- Dealing with **volumetric representations** of 3D objects and scenes
- **Conceptually simple and most similar** to color 2D images / range-images: defined by sampling a function on a regular grid
- **Fast inside-outside tests** (with distance functions)
- **Fast data modifications** with new information
- **Trivially converted** from different sources of 3D data
  - LIDAR point clouds, RGB-D point clouds, CAD models...
- Acts as a **data source for downstream tasks** (both reconstruction and understanding)
  - Mesh extraction, segmentation / detection / classification, ...

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## 1.1. Volumetric 3D functions

### §1. Volumetric 3D representations



Occupancy map

SDF

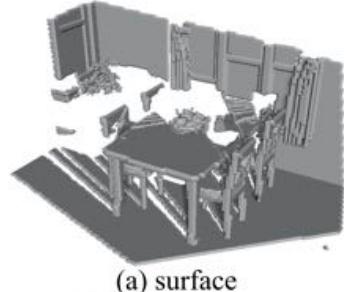
TSDF

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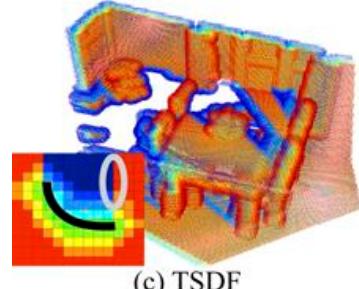
Figure credit: [Representing geometry](#) GCV v2021.1, Module 5

## 1.1. Depth images as TSDFs

### §1. Volumetric 3D representations



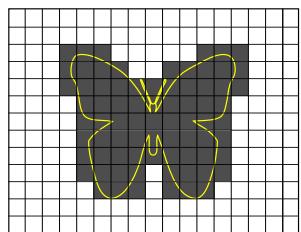
(a) surface



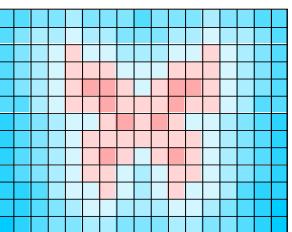
(c) TSDF

## 1.1. Volumetric 3D functions

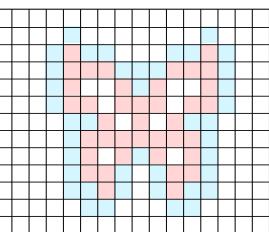
### §1. Volumetric 3D representations



Occupancy map



SDF



TSDF

- Dense volumetric grid: need  $O(N^3)$  voxels where  $N$  is the spatial resolution

## 1.1. Volumetric 3D computational representations

### §1. Volumetric 3D representations

- Sometimes: a **combination of basis functions**  $f(\mathbf{x}) = \sum_i c_i b_i(\mathbf{x})$
- **Dense volumetric grid:** a set  $\Omega = \{0, \dots, n_x\} \times \{0, \dots, n_y\} \times \{0, \dots, n_z\} \subset \mathbb{R}^3$  of **voxels** (Volumetric PIXELs: axis aligned cubes)
- **Hierarchical grid (quadtree / octree):** store function values at progressively finer levels
- **Sparse grid / hash grid:** stores only important cells or blocks of volumetric data

## Connections to other 3D modalities

## 1.2. Connections to other 3D modalities

### §1. Volumetric 3D representations

- Volumetric 3D representations can be...
- Built from:
  - Point sets / meshes / CAD models / you name it: **voxelization** (OCC)
  - Surface modalities: **distance-to-surface queries** (SDF, TSDF)
  - **Fusion** of (registered) range-images into a global surface model (OCC, SDF, TSDF)
- Used for:
  - Implicit surface modeling
  - (Explicit) Mesh extraction

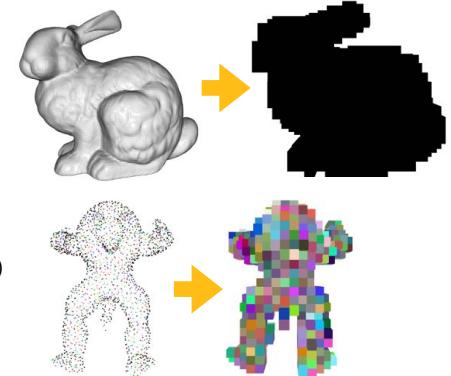
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## 1.2. Voxelization

### §1. Volumetric 3D representations

- Voxelizing **triangle meshes/CAD models**: all voxels that are intersected by a triangle are set to 1, all others are set to 0
- Voxelizing **point clouds**: occupy a voxel if at least one point of the point cloud is within the voxel
- Surface geometry only (no interior occupancy)

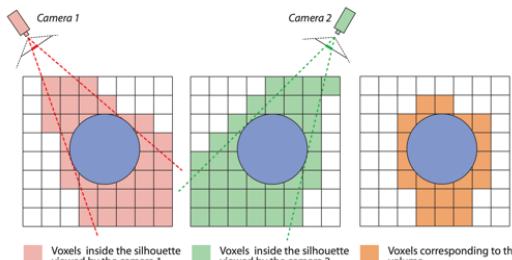


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Figure credit: Open3D GCV v2021.1, Module 5

## 1.2. Voxelization: space carving

### §1. Volumetric 3D representations



- Shape-from-silhouette: discard voxels projecting outside silhouette
- Need multiple views of the same shape

Figure credit: A Real-Time System for Full Body Interaction with Virtual Worlds

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## 1.2. Voxelization: space carving

### §1. Volumetric 3D representations

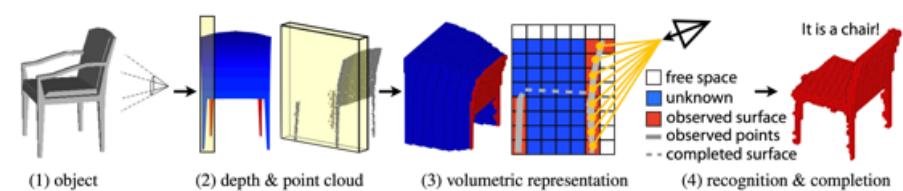


Figure credit: 3DShapeNets

- Useful for sequential tasks (e.g. determining the next-best-view from current reconstructing + a list of previous camera poses)
- Obtain depth maps (raycasting/sensors) → voxelize entire space with several occupancy labels (simplest: free/occupied, but unknown is important, too)

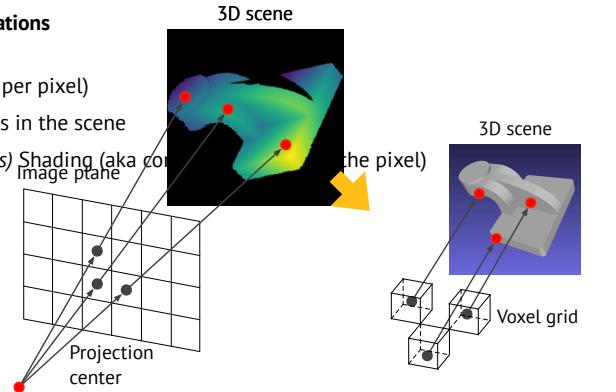
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## 1.2. Distance-to-surface queries: raycasting

### §1. Volumetric 3D representations

1. Generation of rays (one per pixel)
2. Intersection with objects in the scene
3. (For graphics applications) Shading (aka color) the pixel



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## Constructing volumetric 3D shapes from range-images

## 1.3. Constructing volumetric 3D shapes from range-images

### §1. Volumetric 3D representations

- **Input:** a sequence of range-image measurements  $d_1, \dots, d_n$
- **Goal:** to build a single 3D model (preferably a surface)  $D(\mathbf{x})$  (**a fused TSDF volume**)
- **Constraints:**
  - Camera poses can be known (frames registered) or unknown (SLAM variant)
  - Dense 3D modeling
  - Real-time performance (e.g. Kinect / RealSense: depth @30FPS)



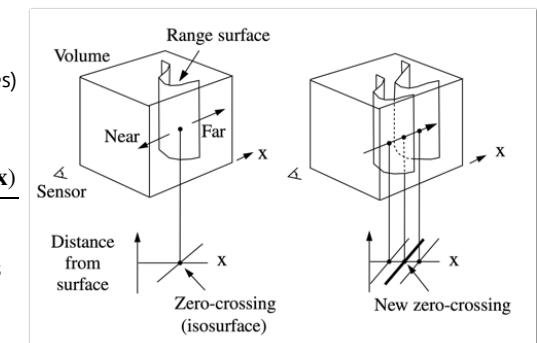
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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations

- Start with range-surfaces (proxy surfaces obtained from range-images)
  - Perform rolling averaging in each spatial location on the grid:
- $$D_{i+1}(\mathbf{x}) = \frac{W_i(\mathbf{x})D_i(\mathbf{x}) + w_{i+1}(\mathbf{x})d_{i+1}(\mathbf{x})}{W_i(\mathbf{x}) + w_{i+1}(\mathbf{x})}$$
- where  $W_i(\mathbf{x}), w_i(\mathbf{x})$  represent cumulative and instantaneous weights
- $$W_{i+1}(\mathbf{x}) = W_i(\mathbf{x}) + w_i(\mathbf{x})$$



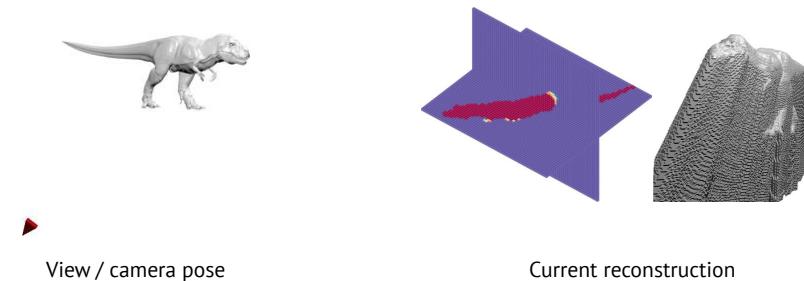
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Figure credit: Curless &amp; Levoy

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations



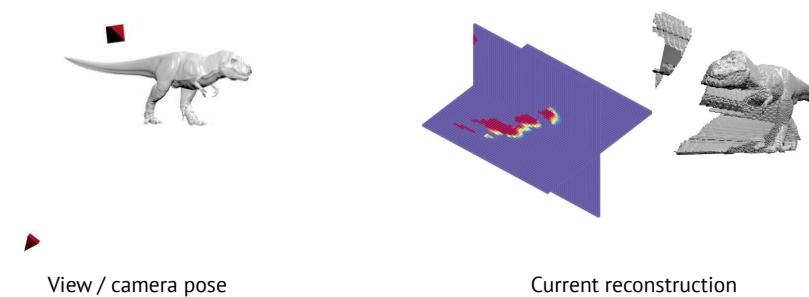
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Slide credit: Riegler et al., OctNet

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations



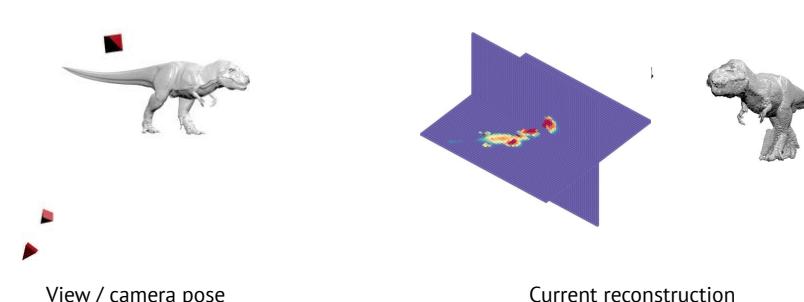
22

Slide credit: Riegler et al., OctNet

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations



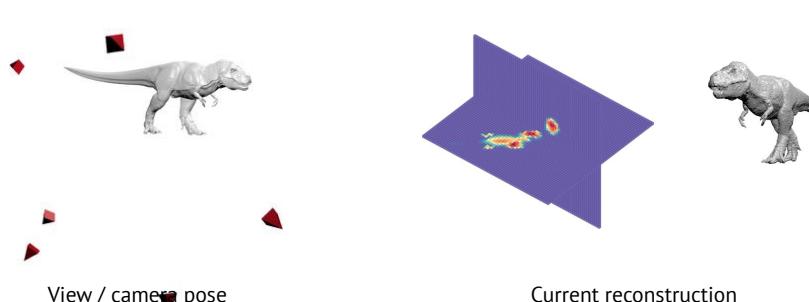
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Slide credit: Riegler et al., OctNet

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations



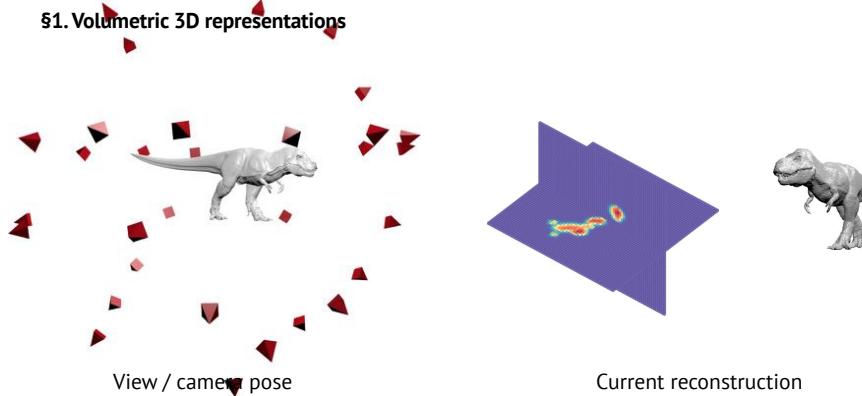
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Slide credit: Riegler et al., OctNet

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations



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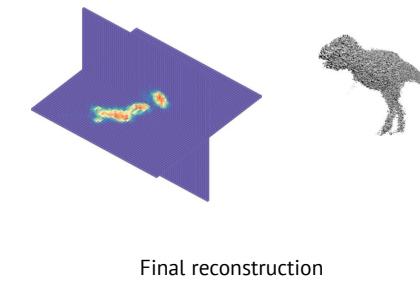
Slide credit: Riegler et al., OctNet

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## 1.3. Depth fusion: Curless & Levoy fusion

### §1. Volumetric 3D representations

- Pros
  - Simple
  - Fast
  - Easy implementation
- Cons
  - Many views required
  - Can not handle outliers
  - No surface completion



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Slide credit: Riegler et al., OctNet

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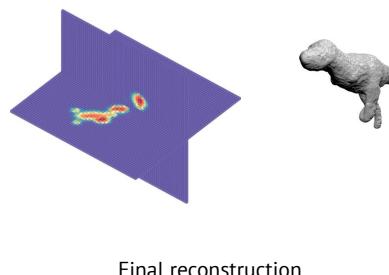
## 1.3. Depth fusion: TV-L1

### §1. Volumetric 3D representations

- Obtained by minimizing a surface-shrinking functional during updates

$$\min_u \int_{\Omega} |\nabla u| + \lambda \sum_{i \in \mathcal{I}(x)} |u - f_i| dx$$

- Pros
  - Prior on surface area
  - Noise reduction
- Cons
  - Simplistic local prior, shrinkage bias
  - Can not complete missing surfaces



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Slide credit: Riegler et al., OctNet

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## 1.3. Volumetric 3D data: summary

### §1. Volumetric 3D representations

- Generic **regular representation** for 3D data
- **Distance-to-shape function** (or its variants) encoded on a volumetric grid
- Naive implementation **scales cubically** with the required resolution:  $O(N^3)$
- Can be constructed with simple procedures from other types of 3D data (e.g., voxelization, space carving, ray-casting, or more complex depth fusion)

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## §2. Spatial data structures

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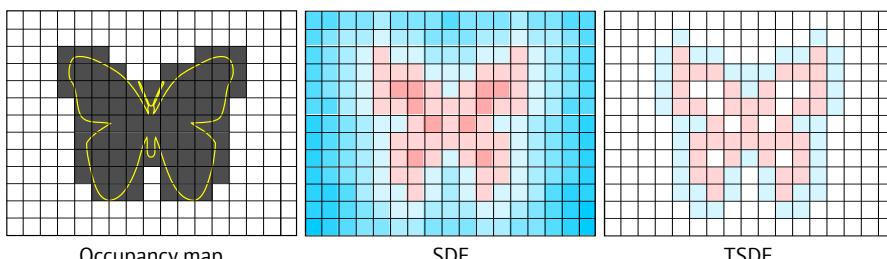
## Dense volumetric 3D grids

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### 2.1. Dense volumetric 3D grids

#### §1. Volumetric 3D representations



- Dense volumetric grid: need  $O(N^3)$  voxels where  $N$  is the spatial resolution

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Figure credit: [Representing geometry](#) GCV v2021.1, Module 5

### 2.1. Dense volumetric 3D grids

#### §1. Volumetric 3D representations

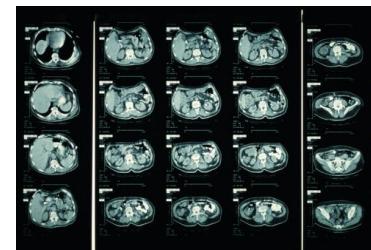


Figure credit: [NBC News](#)

- “Truly dense” volumetric data is rare (e.g., CT/MRI scans)

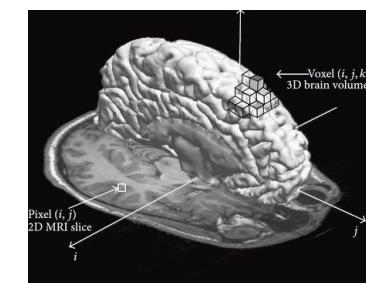
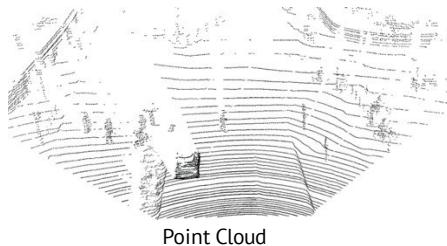


Figure credit: Despotovic et al., 2010

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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Point Cloud



Mesh

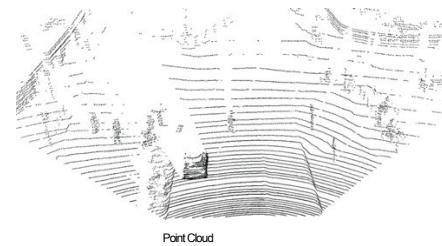
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Slide credit: Riegler et al., OctNet

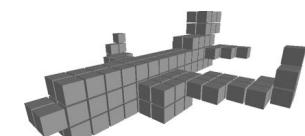
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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Point Cloud



Voxelized  $16^3$  Occupancy  
4.19%

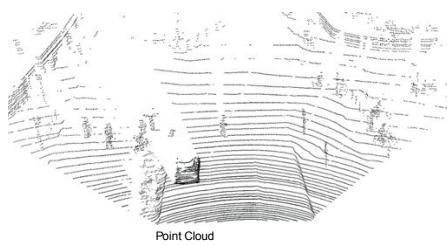
34

Slide credit: Riegler et al., OctNet

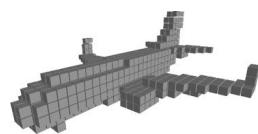
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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Point Cloud



Voxelized  $32^3$  Occupancy  
2.11%

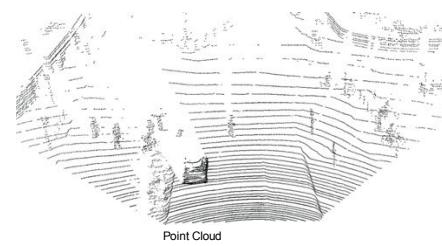
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Slide credit: Riegler et al., OctNet

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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Point Cloud



Voxelized  $64^3$  Occupancy  
1.06%

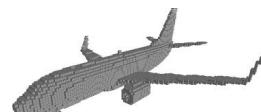
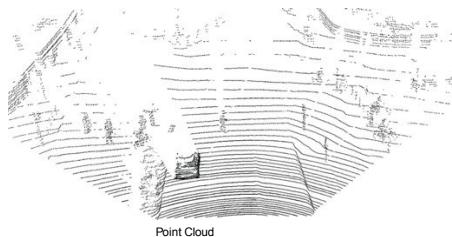
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Slide credit: Riegler et al., OctNet

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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Voxelized  $128^3$  Occupancy  
0.56%

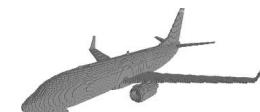
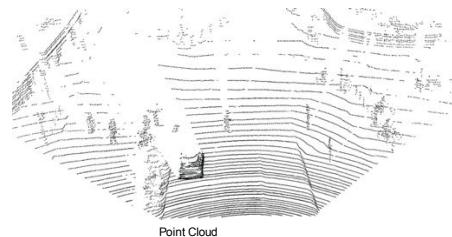
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Slide credit: Riegler et al., OctNet

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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Voxelized  $256^3$  Occupancy  
0.31%

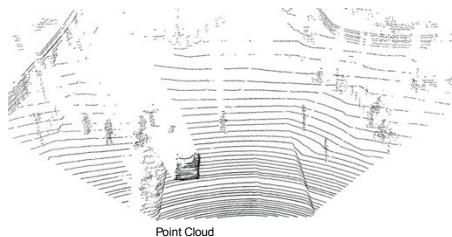
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Slide credit: Riegler et al., OctNet

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## 2.1. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Voxelized  $512^3$  Occupancy  
0.16%

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Slide credit: Riegler et al., OctNet

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# Sparse data representations

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## 2.2. Sparse data representations

### §2. Spatial data structures

- Storage requirements for volumetric data:  $O(N^3)$  where  $N$  is the spatial resolution
- Need  $O(N^3)$  for truly volumetric 3D data (e.g., MRI scans)
- Encoding surfaces:  $O(N^2)$
- Point clouds: inherently sparse  $O(N_{\text{points}})$
- Store data only in occupied locations (active values)
  - Sparse tensor representation**
  - Which format to choose?

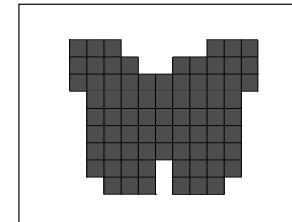


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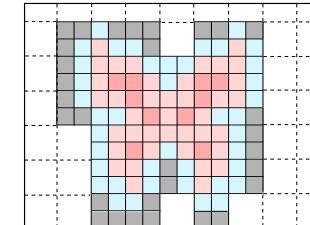
## 2.3. Disadvantages of dense volumetric 3D grid

### §2. Spatial data structures



Occupancy map

- Sparse volumetric grid: need  $O(K)$  voxels where  $K$  is the number of nonempty voxels



TSDF

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Figure credit: Representing geometry GCV v2021.1, Module 5

## 2.2. Sparse data representations

### §2. Spatial data structures

- Dense array storage

10	20	0	0	0	0
0	30	0	40	0	0
0	0	50	60	70	0
0	0	0	0	0	80

Matrix 6 × 4



```
[ 10, 20, 0, 0, 0, 0,
  0, 30, 0, 40, 0, 0,
  0, 0, 50, 60, 70, 0,
  0, 0, 0, 0, 0, 80 ]
```

Memory array 24-floats

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Example credit: boristhebrave GCV v2021.1, Module 5

## 2.2. Sparse data representations

### §2. Spatial data structures

- Coordinate list storage (COO)

10	20	0	0	0	0
0	30	0	40	0	0
0	0	50	60	70	0
0	0	0	0	0	80

Matrix 6 × 4



Row	Column	Value
0	0	10
0	1	20
1	1	30
1	3	40
2	2	50
2	3	60
2	4	70
3	5	80

COO

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Example credit: boristhebrave GCV v2021.1, Module 5

## 2.2. Sparse data representations

## §2. Spatial data structures

- Compressed sparse row (CSR) and compressed sparse column (CSC)

10	20	0	0	0	0
0	30	0	40	0	0
0	0	50	60	70	0
0	0	0	0	0	80

## Matrix $6 \times 4$



```
values      = [ 10, 20, 30, 40, 50, 60, 70, 80 ]
col_indices = [ 0, 1, 1, 3, 2, 3, 4, 5 ]
row_indptr = [ 0, 2, 4, 7, 8 ]
```

CSR

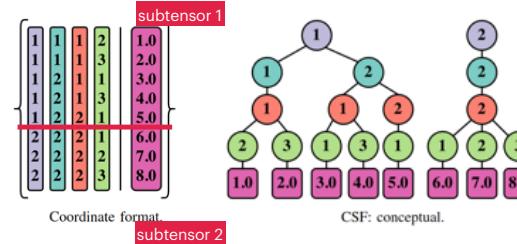
```
row_idx = 2
col_start = row_inptr[row_idx] # 4
col_end = row_inptr[row_idx] # 7
col_idxs = col_indices[col_start:col_end]
vals = values[col_start:col_end]
```

## Reading from a CSR

## 2.2. Sparse data representations

## §2. Spatial data structures

- Compressed sparse fiber (CSF)



## Coordinate forms

CSF: concep

fptr[0]	{0, 2, 3}	fids[0]	{1, 2}
fptr[1]	{0, 1, 3, 4}	fids[1]	{1, 2, 2}
fptr[2]	{0, 2, 4, 5, 8}	fids[2]	{1, 1, 2, 2}
		fids[3]	{2, 3, 1, 3, 1, 1, 2, 3}
vals	{1.0, 2.0, 3.0, 4.0, 5.0, 6.0, 7.0, 8.0}		

CSE: implementation

## Octrees

## 2.3. Octrees

## §2. Spatial data structures

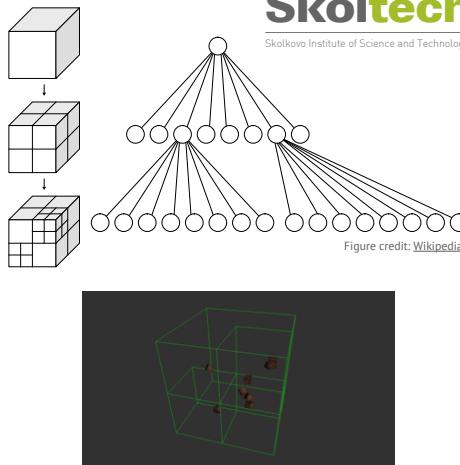
- Memory-efficient data structure for spatial indexing
  - Many applications:
    - Efficient 3D spatial indexing at high resolutions
    - Visualization (e.g. level of detail, frustum culling, raycasting)
    - Nearest neighbour search (e.g. needed by ICP)
    - Discrete geometry processing (e.g. meshing)

Figure credit: [gifer.com](#)

## 2.3. Octrees

### §2. Spatial data structures

- A search tree with exactly 8 children in each node
- Recursively subdivide space into 8 octants at each spatial scale
- Point-region and matrix-based
- Insertion:  $O(\log N)$
- Nearest-neighbour search:  $O(\log N)$

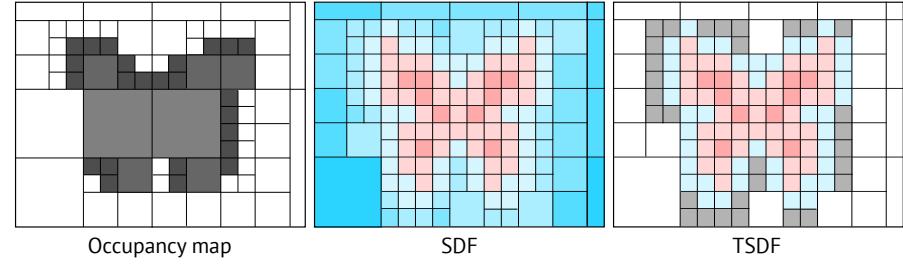


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## 2.3. Octrees

### §2. Spatial data structures



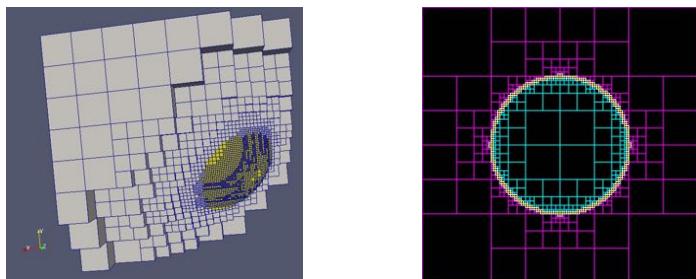
- Quadtree/octree voxel grid: adaptively subdivide space to accommodate active sites

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Figure credit: Representing geometry GCV v2021.1, Module 5

## 2.3. Octrees

### §2. Spatial data structures



- Quadtree/octree voxel grid: resolution changes/dynamics

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Figure credit: Representing geometry GCV v2021.1, Module 5

## 2.3. Spatial data structures: summary

### §2. Spatial data structures

- **Dense volumetric grid:** a set  $\Omega = \{0, \dots, n_x\} \times \{0, \dots, n_y\} \times \{0, \dots, n_z\} \subset \mathbb{R}^3$  of voxels
  - Simplest, off-the-shelf, easy to use
  - Memory and computationally inefficient
- **Hierarchical grid (quadtree / octree):** store function values at progressively finer levels
  - Fast insertion and search:  $O(\log N)$
  - Maintain a separate data structure, still pointwise-constant approximation
- **Sparse grid / hash grid:** stores only important cells or blocks of volumetric data
  - Removes redundancy by not storing / computing values in empty voxels
  - Separate sparse data-structures (e.g. COO-formatted sparse tensors)

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## §3. Constructing neural networks on volumetric data

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## Dense 3D CNNs

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### 3.1. Dense 3D CNNs

#### §3. Constructing neural networks on volumetric data

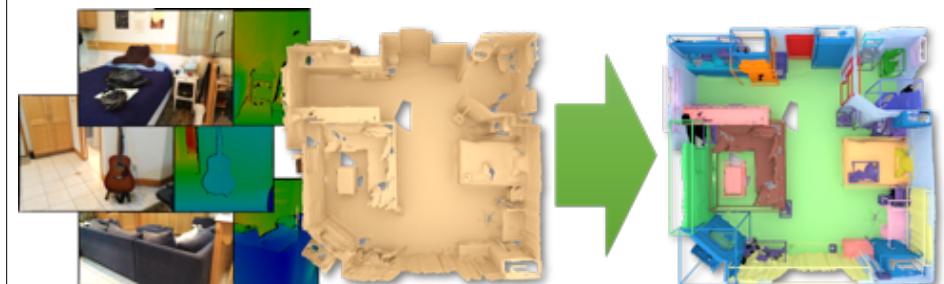
- 2D convolutions: mainstream tool for processing signals
  - Images, video, RGBD, ...
- Dense 3D volumetric data: directly extend 2D convolutions to 3rd dimension
  - No-brainer (add another loop into the code for convolution computation)

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### 3.1. Dense 3D CNNs: understanding 3D scans

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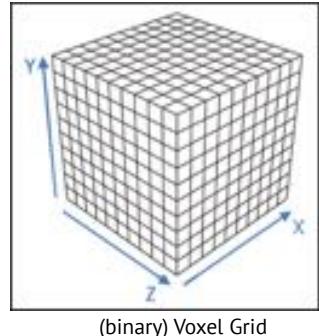


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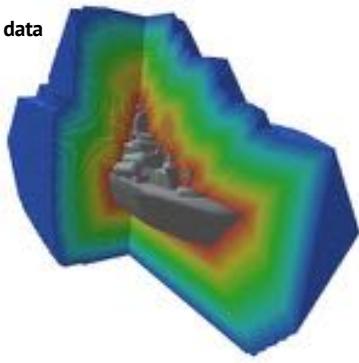
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## 3.1. Dense 3D CNNs: Deep Learning in 3D

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(binary) Voxel Grid



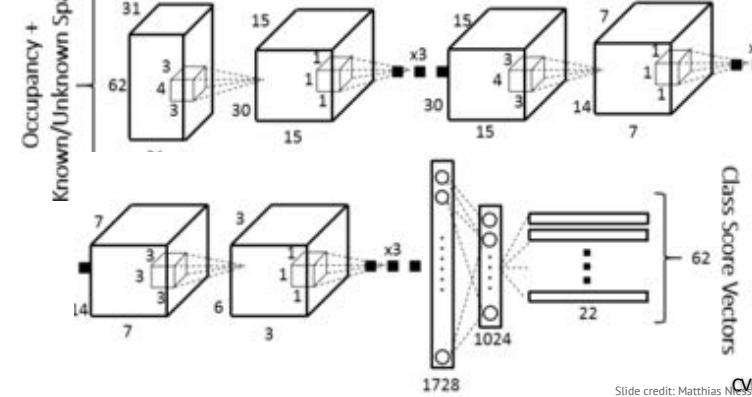
Implicit Function

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## 3.1. Dense 3D CNNs: 3D Semantic Segmentation

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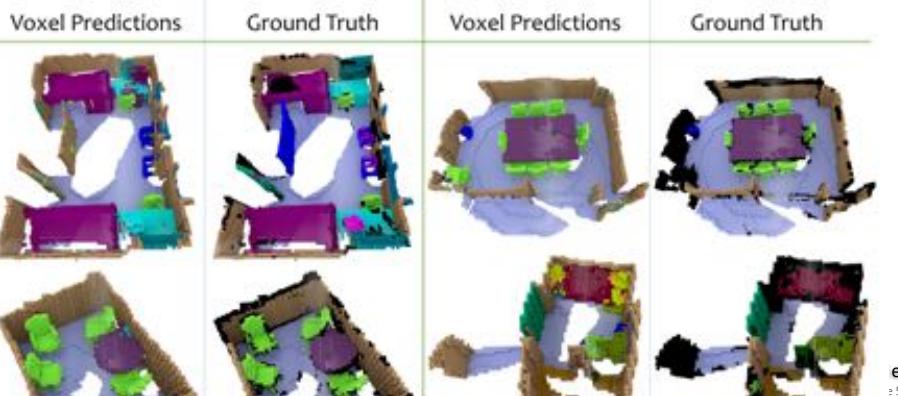


CVPR'17 (spotlight) [Dai et al.]

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## 3.1. Dense 3D CNNs: 3D Semantic Segmentation

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## 3.1. Dense 3D CNNs: 3D Reconstructions



TOG'17 [Dai et al.]; Bu

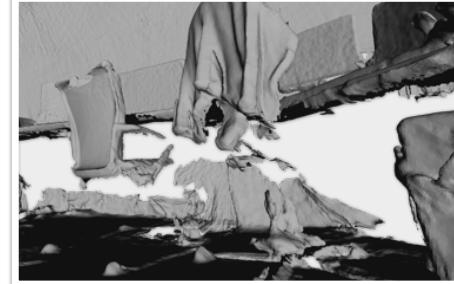
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### 3.1. Dense 3D CNNs: Incomplete Scan Geometry

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TOG'17 [Dai et al.]: Bu

### 3.1. Dense 3D CNNs: Completing 3D Shapes

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### 3.1. Dense 3D CNNs: Data-driven Shape Completion

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CVPR'17 (spotlight) [Dai et al.]

### 3.1. Dense 3D CNNs: Data-driven Shape Completion

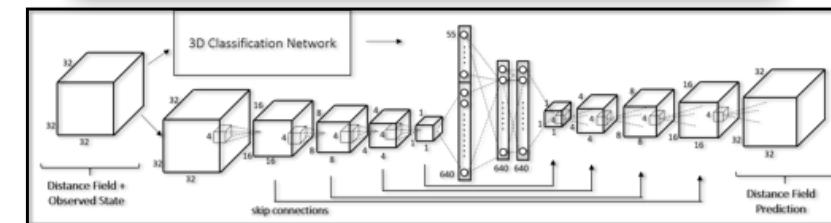
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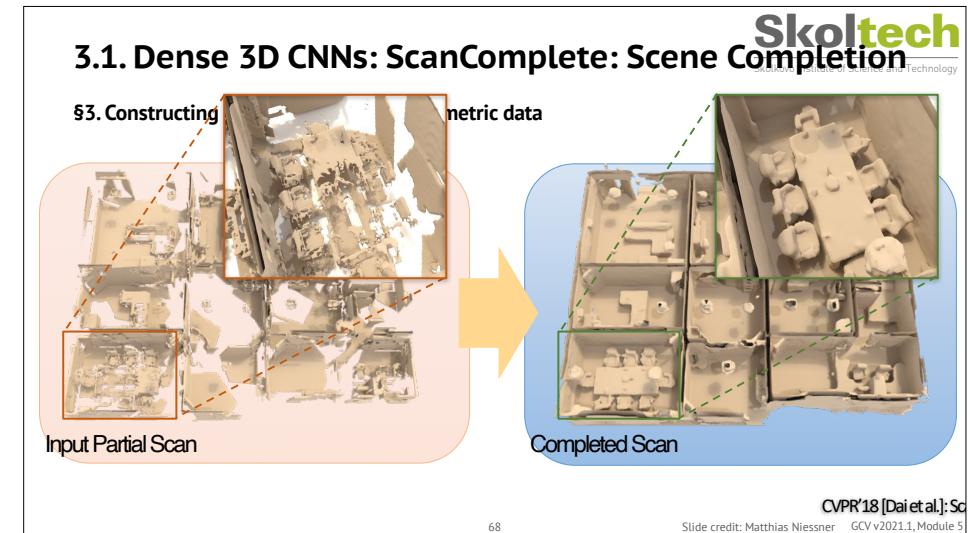
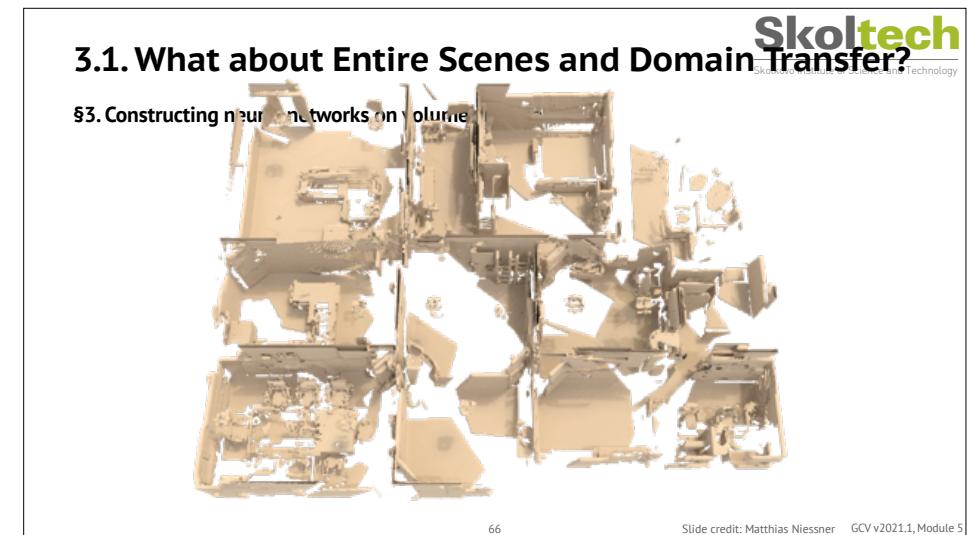
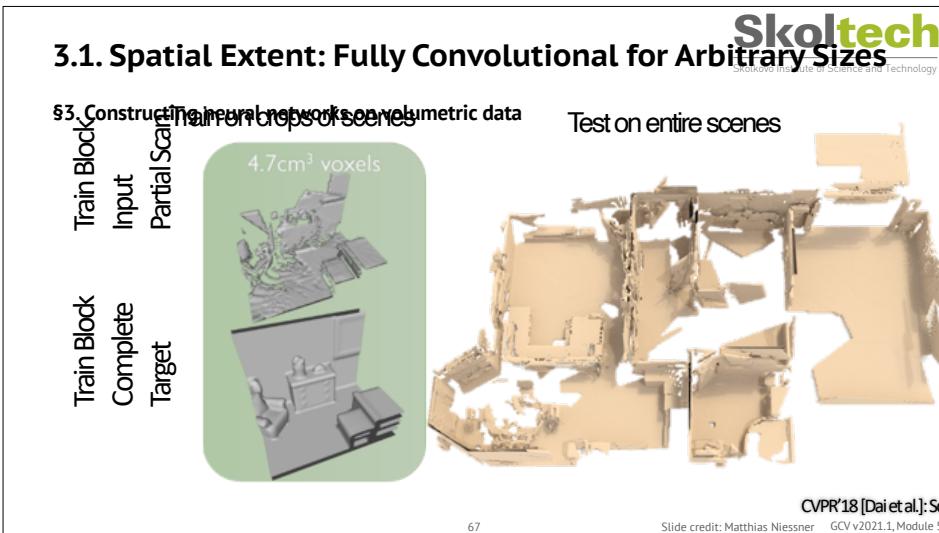
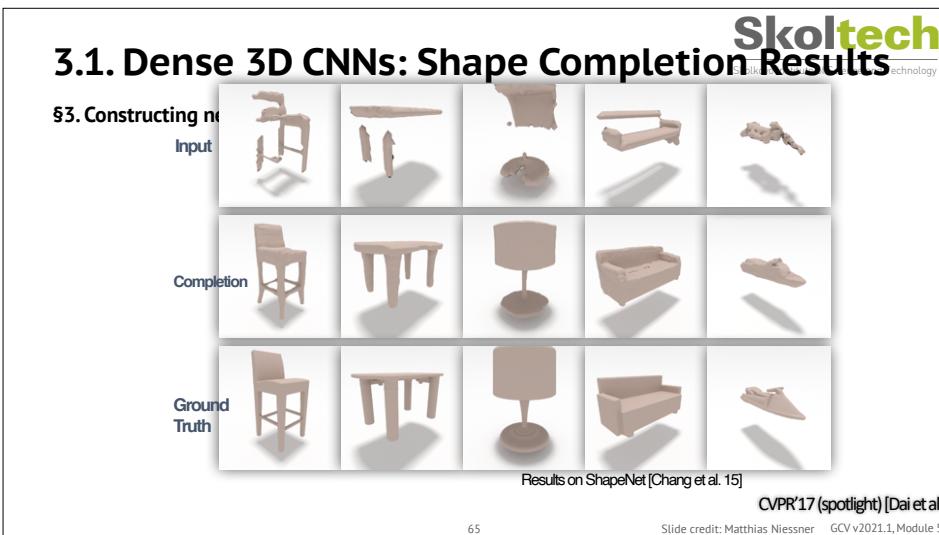


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CVPR'17 (spotlight) [Dai et al.]





### 3.1. Dense 3D CNNs: ScanComplete

§3.



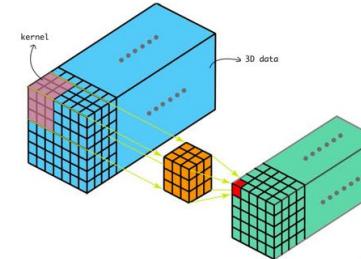
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### 3.1. Dense 3D CNNs: memory requirements

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- Network evaluation with batch size 32 (Voxelized ModelNet10 meshes)



Riegler et al., OctNet - 5  
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### 3.1. Naive 3D CNNs: summary

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- Dense 3D CNNs: directly extend 2D convolutions to 3rd dimension
- **Computationally inefficient** (scale cubically with spatial resolution)
  - Process low-resolution shapes only (e.g.,  $32^3$  or  $64^3$ ) or use shallower NNs
  - Many applications can leverage low-resolution volumes (e.g. semantic segmentation, scene completion...)
- **Sample inefficient** (perform worse compared to 2D CNNs)

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## Octree-based CNNs

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### 3.3. Octree-based CNNs

#### §3. Constructing neural networks on volumetric data

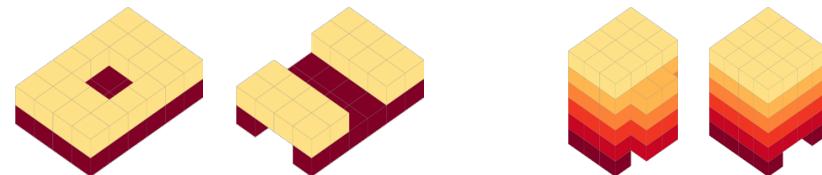
- Goal: train deep architectures at high spatial resolutions
  - Deeper models → higher learning efficiency
  - Higher resolution → more detail in input 3D shapes/scenes

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### 3.3. Octree-based CNNs: effect of resolution

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Voxelized 8<sup>3</sup>

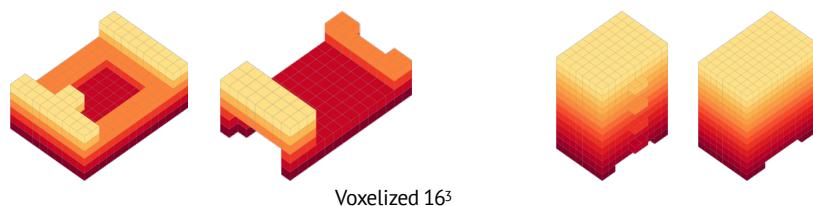
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### 3.3. Octree-based CNNs: effect of resolution

#### §3. Constructing neural networks on volumetric data



Voxelized 16<sup>3</sup>

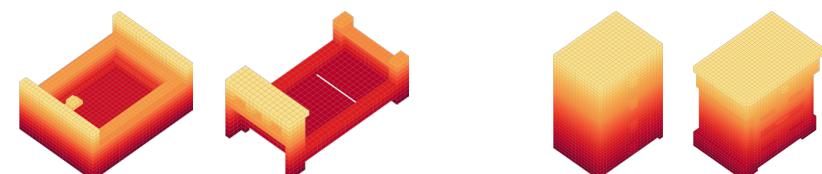
75

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### 3.3. Octree-based CNNs: effect of resolution

#### §3. Constructing neural networks on volumetric data



Voxelized 32<sup>3</sup>

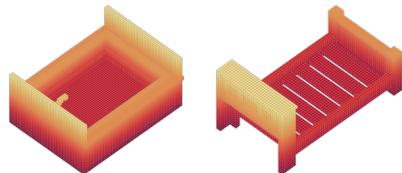
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### 3.3. Octree-based CNNs: effect of resolution

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Voxelized 64<sup>3</sup>

77

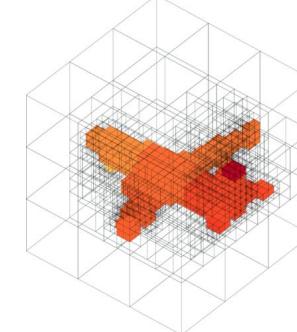
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### 3.3. Octree-based CNNs: grid of octrees

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### 3.3. Octree-based CNNs: grid of octrees

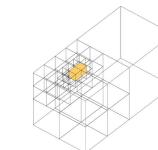
§3. Constructing neural networks on volumetric data



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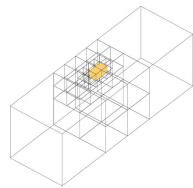
Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: grid of octrees

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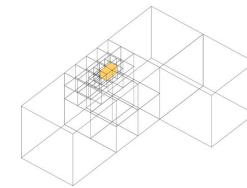
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### 3.3. Octree-based CNNs: grid of octrees

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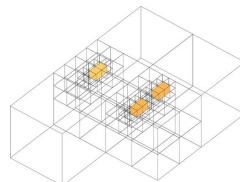
Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: grid of octrees

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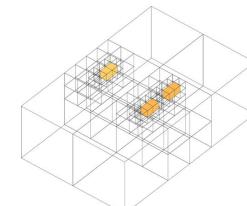


A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

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A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

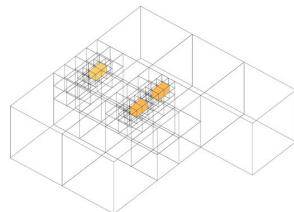
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### 3.3. Octree-based CNNs: grid of octrees

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A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

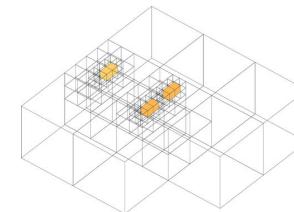
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### 3.3. Octree-based CNNs: grid of octrees

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A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

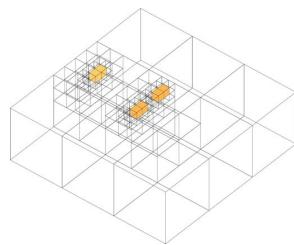
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### 3.3. Octree-based CNNs: grid of octrees

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A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

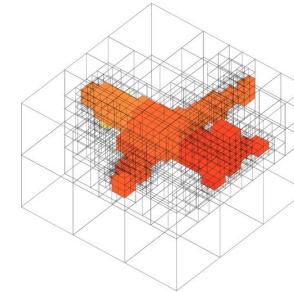
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### 3.3. Octree-based CNNs: grid of octrees

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A. Miller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

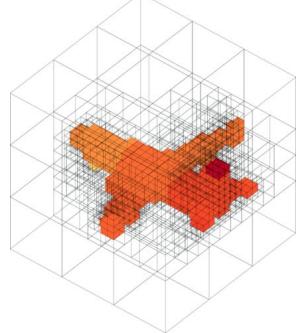
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### 3.3. Octree-based CNNs: grid of octrees

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A. Müller et al. "Real-time rendering and dynamic updating of 3-d volumetric data". In: GPGPU. 2011.

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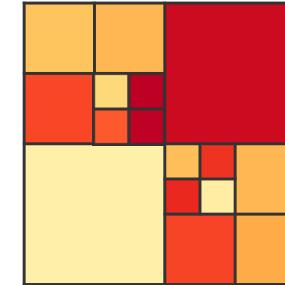
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### 3.3. Octree-based CNNs: convolution

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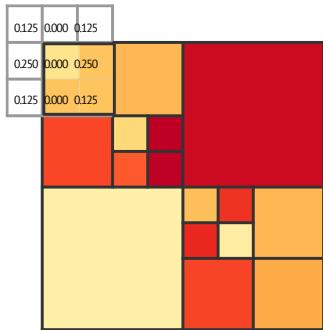
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### 3.3. Octree-based CNNs: convolution

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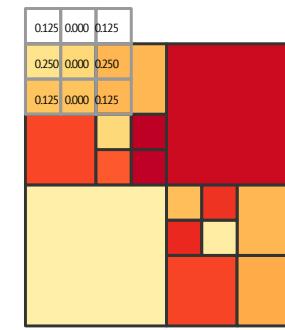
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### 3.3. Octree-based CNNs: convolution

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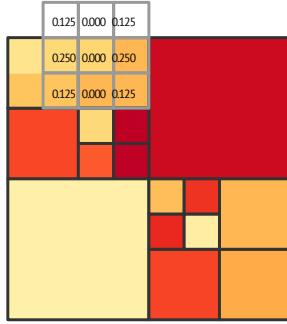
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



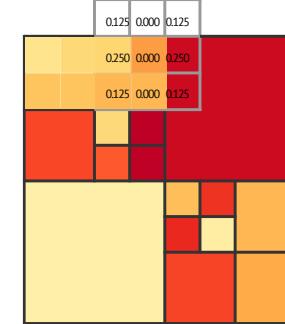
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data

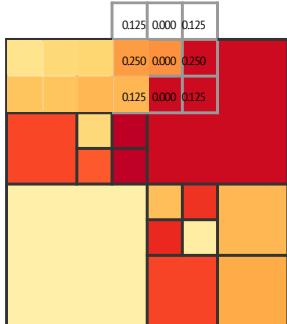


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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



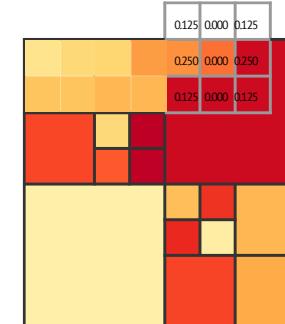
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



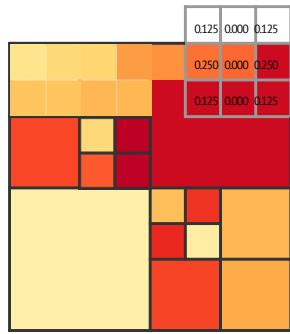
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



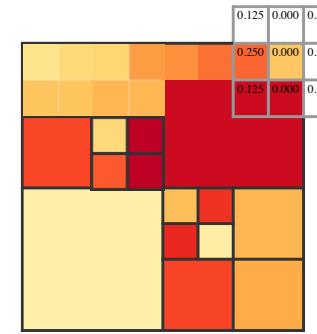
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



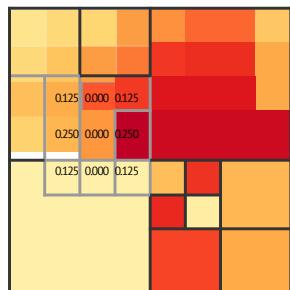
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



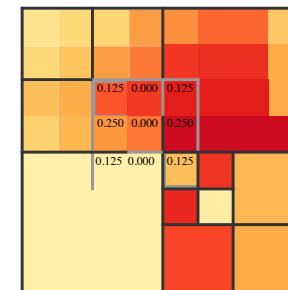
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### 3.3. Octree-based CNNs: convolution

#### §3. Constructing neural networks on volumetric data



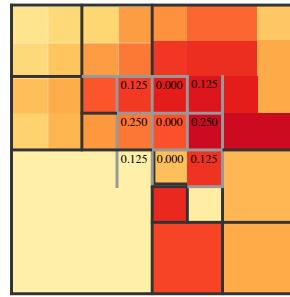
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: convolution

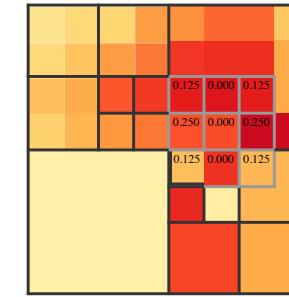
§3. Constructing neural networks on volumetric data



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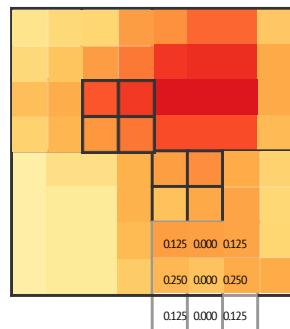
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: convolution

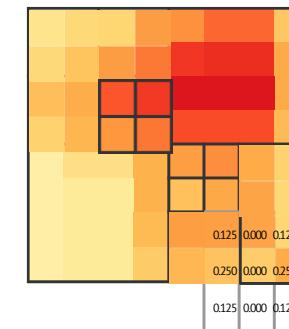
§3. Constructing neural networks on volumetric data



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Slide credit: Riegler et al., OctNet

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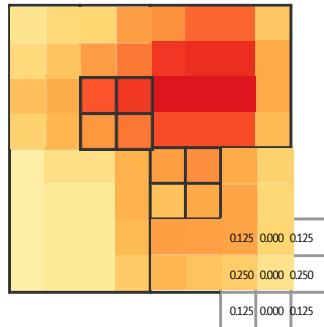
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: convolution

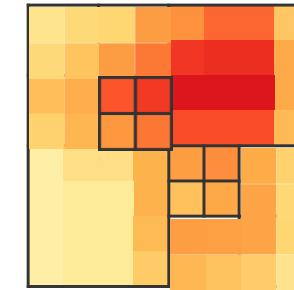
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Slide credit: Riegler et al., OctNet

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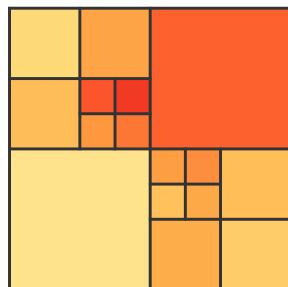
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: convolution

§3. Constructing neural networks on volumetric data



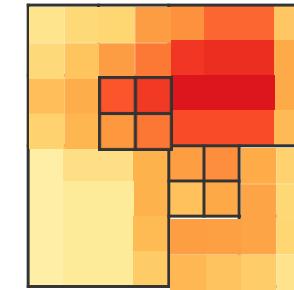
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Slide credit: Riegler et al., OctNet

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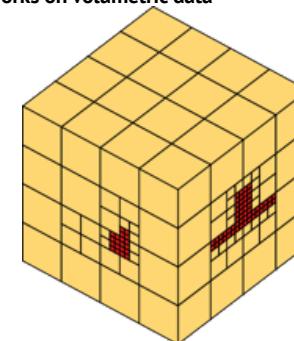
### 3.3. Octree-based CNNs: convolution

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### 3.3. Octree-based CNNs: pooling

§3. Constructing neural networks on volumetric data



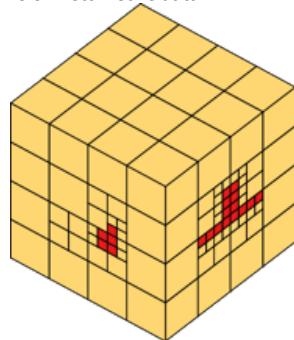
108

Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: pooling

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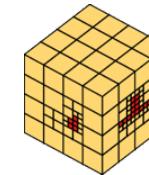
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: pooling

§3. Constructing neural networks on volumetric data



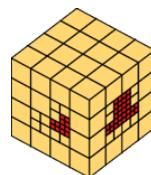
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Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: pooling

§3. Constructing neural networks on volumetric data



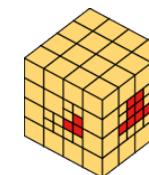
111

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### 3.3. Octree-based CNNs: pooling

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GCV v2021.1, Module 5

### 3.3. Octree-based CNNs: pooling

#### §3. Constructing neural networks on volumetric data



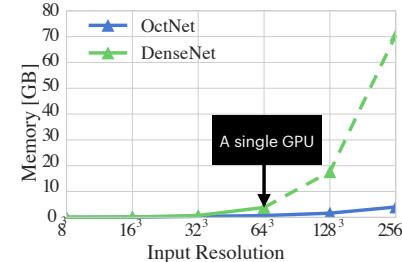
113

Slide credit: Riegler et al., OctNet

GCV v2021.1, Module 5

### 3.3. Octree-based CNNs: experiments

#### §3. Constructing neural networks on volumetric data



Network evaluation with batch size 32  
Voxelized ModelNet10 meshes

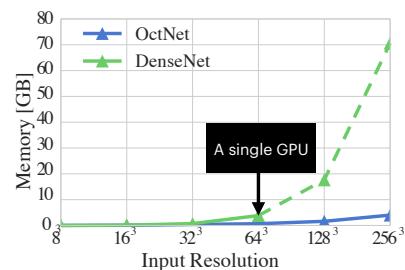
114

Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: experiments

#### §3. Constructing neural networks on volumetric data



Network evaluation with batch size 32  
Voxelized ModelNet10 meshes

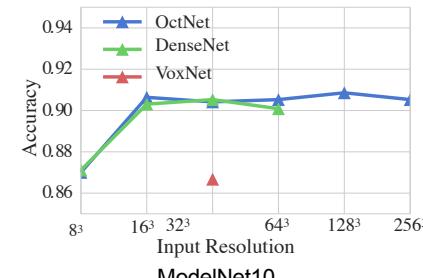
115

Slide credit: Riegler et al., OctNet

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### 3.3. Octree-based CNNs: experiments

#### §3. Constructing neural networks on volumetric data



D.Maturana and S.Scherer. "VoxNet: A 3D Convolutional Neural Network for real-time object recognition". In: IROS. 2015.

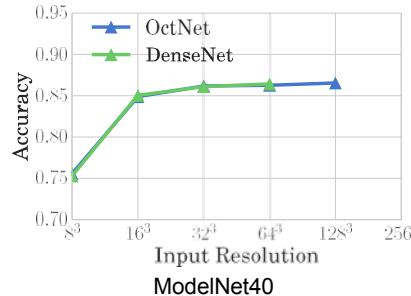
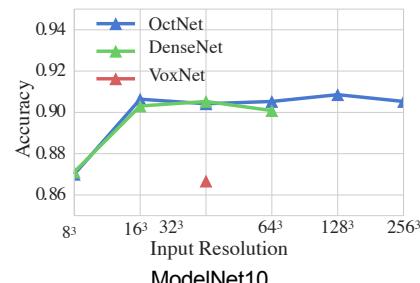
116

Slide credit: Riegler et al., OctNet

GCV v2021.1, Module 5

### 3.3. Octree-based CNNs: experiments

#### §3. Constructing neural networks on volumetric data



D. Maturana and S. Scherer. "VoxNet: A 3D Convolutional Neural Network for real-time object recognition". In: IROS. 2015.

### 3.3. Octree-based CNNs: summary

#### §3. Constructing neural networks on volumetric data

- Define a convolutional / pooling operators on top of octree data structure
- Capability to train deeper architectures at higher spatial resolutions