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Neural Networks for sequential data

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General attention idea

Attention

We need a representation of an object.

A "coarse" description of an object is available.

For other objects we have more detailed stored information.

We use attention to extract these information

Single-object key value interpretation

 q_i - query to a database

 k_i - keys in the database

 \boldsymbol{v}_i - values in the database

We calculate attention scores

$$\alpha_i = e(q_i, k_i) = s_i^T k_i$$
 (other distances also possible)

$$\alpha = \operatorname{softmax}(\alpha)$$

Then we extract the information as weighted sum of values

$$\mathbf{a}_{\mathrm{i}} = \sum_{j=1}^{T_{\chi}} \alpha_{j} \mathbf{v}_{j}$$

Matrix key value interpretation

 q_i - query to a database

 $oldsymbol{k}_i$ - keys in the database

 \boldsymbol{v}_i - values in the database

We calculate correspondences

$$A(q, K, V) = \sum_{i} \frac{\exp(\boldsymbol{q}_{i}^{T} \boldsymbol{k}_{j})}{\sum_{l} \exp(\boldsymbol{q}_{i}^{T} \boldsymbol{k}_{l})} \boldsymbol{v}_{j}$$

$$A(Q, K, V) = \operatorname{softmax}(QK^{T})V$$

"Databases" for the attention

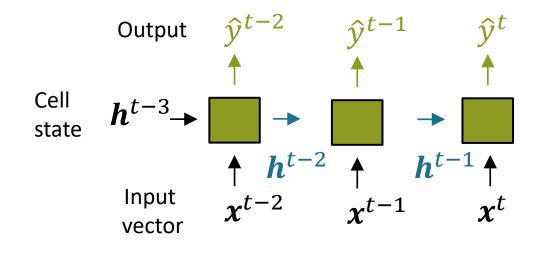
Nodes in a graph

 Tokens in a sequence (we need to specify the position, as the order is important)

Sets of objects

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An example: attention for recurrent neural network



At each step: \hat{y}^t - output / model prediction x^t - input vector / new information h^t - cell / hidden state

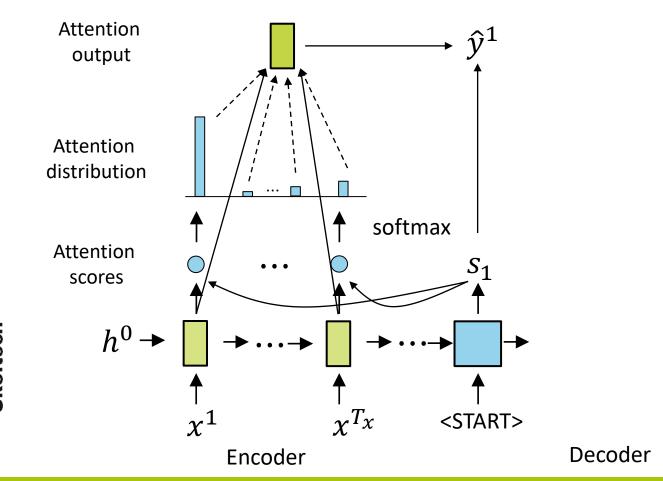
Simple RNN model block

$$h^t = f_h(x^t, h^{t-1})$$
Output \hat{y}^t

$$h^t = \tanh(Vx^t + Wh^{t-1} + b_h)$$
Cell state $h^{t-1} \rightarrow h^t$

$$\hat{y}^t = f_y(h^t)$$
Input x^t
vector \hat{y}^t = softmax $(Uh^t + b_y)$

Sequence 2 sequence with attention



Single-object key value interpretation

 q_i - query to a database Hidden state of the *decoder*

 $oldsymbol{k}_i$ - keys in the database Hidden state of the *encoder*

 v_i - values in the database Hidden state of the *encoder*

We calculate attention scores

 $\alpha_i = e(q_i, k_i) = s_i^T k_i$ (other distances also possible)

 $\alpha = \operatorname{softmax}(\alpha)$

Then we extract the information as weighted sum of values

$$\mathbf{a}_{\mathrm{i}} = \sum_{j=1}^{T_{\chi}} \alpha_{j} \mathbf{v}_{j}$$

Scaled attention values

For large dimension of the space of keys d_k :

- Large variances dot products $q_i^T k_j$
- Softmax only pays attention to some keys
- Gradients are small, hard to learn

Old formula:

$$A(Q, K, V) = \operatorname{softmax}(QK^{T})V$$

New scaled formula:

$$A(Q, K, V) = \operatorname{softmax}(QK^{T}/\sqrt{d_{k}})V$$

Transformers with selfattention

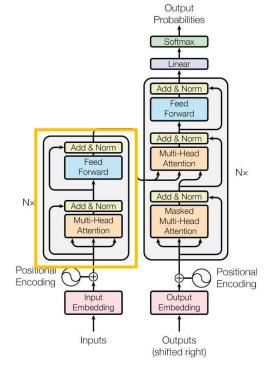
Transformer is based on the same idea

Now we completely drop RNN part

Also we repeat *self-attention* many times

Further we'll consider separate parts:

- Multi-head attention
- Feed Forward



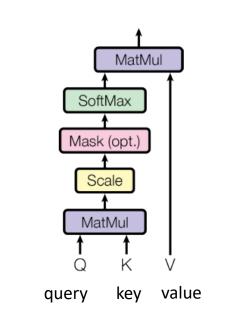
Attention / Self-attention block

Attention
$$(Q, K, V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

 d_k is the dimension of query and key, we scale to take control of large values of dot-product in high dimensions

A possible option is to replace scaled dot-product used here with additive attention: a single-hidden layer neural network.

Scaled Dot-Product Attention



Self-attention block

Attention
$$(Q, K, V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

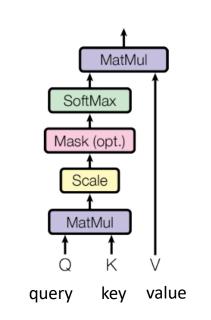
We produce queries, keys, and values using initial word embeddings

$$Q = XW^Q$$
, $dim(W^Q) = d_x \times d_q$,

$$K = XW^K$$
, $dim(W^Q) = d_x \times d_k$,

$$V = XW^V$$
, $dim(W^Q) = d_x \times d_v$,

Scaled Dot-Product Attention

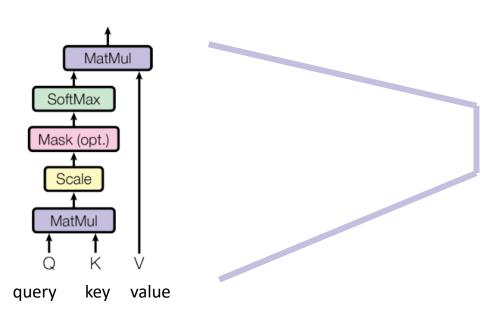


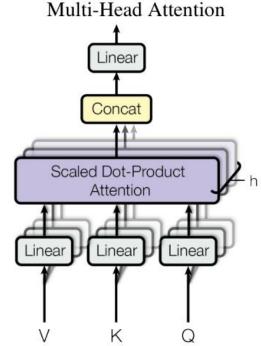
Multi-Head attention

 $MultiHead(Q, K, V) = Concat(head_1, ..., head_h)W^O$ $where head_i = Attention(QW_i^Q, KW_i^K, VW_i^V)$

h heads in total

Scaled Dot-Product Attention





"Attention is all you need" paper

Full block

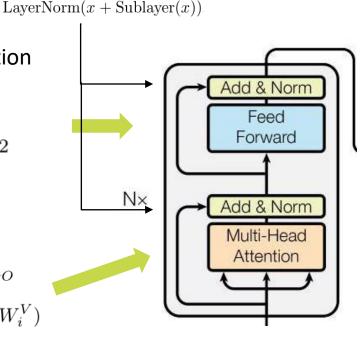
activation

Two linear transformation with ReLU activation in between

$$FFN(x) = \max(0, xW_1 + b_1)W_2 + b_2$$

Multi-head attention

$$\begin{aligned} \text{MultiHead}(Q, K, V) &= \text{Concat}(\text{head}_1, ..., \text{head}_h) W^O \\ \text{where head}_i &= \text{Attention}(QW_i^Q, KW_i^K, VW_i^V) \end{aligned}$$



There are 6 consecutive Full blocks in the paper transformer architecture

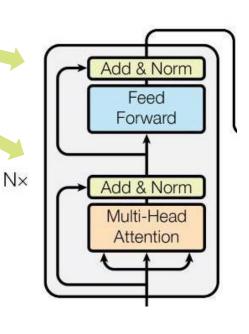
Full block: normalization and residual connection

LayerNorm(x + Sublayer(x))

Why? Speeds up training!

- Similar to Batch Normalization
- But can be used with batch size 1
- Can be used with RNNs and Transformers

$$\mu^{l} = \frac{1}{H} \sum_{i=1}^{H} a_{i}^{l} \qquad \sigma^{l} = \sqrt{\frac{1}{H} \sum_{i=1}^{H} (a_{i}^{l} - \mu^{l})^{2}}$$



Position encoding

In addition to usual embeddings of inputs we use position encoding to capture position

They are not one-hot vectors, as we want to handle various-length sequences

Add & Norn Feed Forward N× Add & Norm Multi-Head Attention Positional Encodina Input Embeddina Inputs

Real example of positional encoding with a toy embedding size of 4

Transformer training

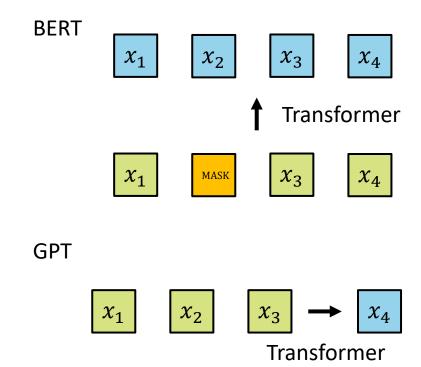
Masked language model:

Replace random tokens with masks, try to reconstruct them using a Neural network

Next token prediction

Predict next token

Self-supervised learning: We don't need labeled examples, we just create them



Efficiency of transformers

Brown, T. B., Mann, B., Ryder, N. et al. (2020). Language models are few-shot learners. *arXiv* preprint arXiv:2005.14165.

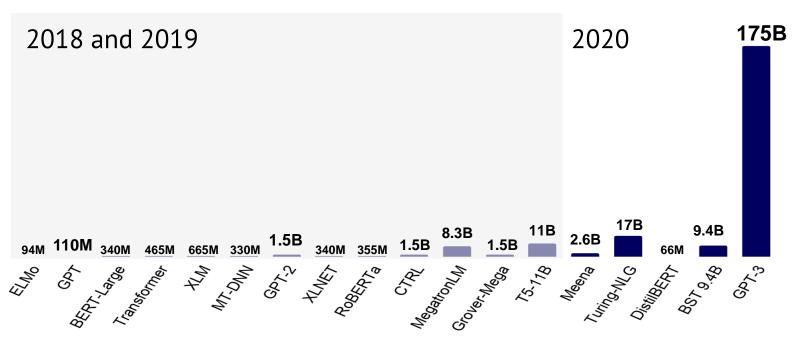
Model Name	n_{params}	n_{layers}	d_{model}	$n_{ m heads}$	$d_{ m head}$	Batch Size	Learning Rate
GPT-3 Small	125M	12	768	12	64	0.5M	6.0×10^{-4}
GPT-3 Medium	350M	24	1024	16	64	0.5M	3.0×10^{-4}
GPT-3 Large	760M	24	1536	16	96	0.5M	2.5×10^{-4}
GPT-3 XL	1.3B	24	2048	24	128	1 M	2.0×10^{-4}
GPT-3 2.7B	2.7B	32	2560	32	80	1M	1.6×10^{-4}
GPT-3 6.7B	6.7B	32	4096	32	128	2M	1.2×10^{-4}
GPT-3 13B	13.0B	40	5140	40	128	2M	1.0×10^{-4}
GPT-3 175B or "GPT-3"	175.0B	96	12288	96	128	3.2M	0.6×10^{-4}

Table 2.1: Sizes, architectures, and learning hyper-parameters (batch size in tokens and learning rate) of the models which we trained. All models were trained for a total of 300 billion tokens.

	Mean accuracy	95% Confidence Interval (low, hi)	t compared to control $(p ext{-value})$	"I don't know" assignments
Control (deliberately bad model)	86%	83%-90%	-	3.6 %
GPT-3 Small	76%	72%-80%	3.9(2e-4)	4.9%
GPT-3 Medium	61%	58%-65%	10.3 (7e-21)	6.0%
GPT-3 Large	68%	64%-72%	7.3 (3e-11)	8.7%
GPT-3 XL	62%	59%-65%	10.7~(1e-19)	7.5%
GPT-3 2.7B	62%	58%-65%	10.4~(5e-19)	7.1%
GPT-3 6.7B	60%	56%-63%	11.2 (3e-21)	6.2%
GPT-3 13B	55%	52%-58%	15.3 (1e-32)	7.1%
GPT-3 175B	52%	49%-54%	16.9 (1e-34)	7.8%

Table 3.11: Human accuracy in identifying whether short (\sim 200 word) news articles are model generated. We find that human accuracy (measured by the ratio of correct assignments to non-neutral assignments) ranges from 86% on the control model to 52% on GPT-3 175B. This table compares mean accuracy between five different models, and shows the results of a two-sample T-Test for the difference in mean accuracy between each model and the control model (an unconditional GPT-3 Small model with increased output randomness).

Transformer models are monstrous



Number of parameters

Training cost estimation: 10-50 MLN US\$ for GPT-3

Self-attention block complexity

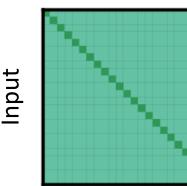
Attention
$$(Q, K, V) = \operatorname{softmax}(\frac{QK^T}{\sqrt{d_k}})V$$

Memory complexity is $O(d_x^2)$ Computational complexity is $O(d_x^2)$

Max sequence size in popular models (e.g. BERT) is only $n=d_{\rm x}=512$ tokens

In modern models tokens are parts of words

Output

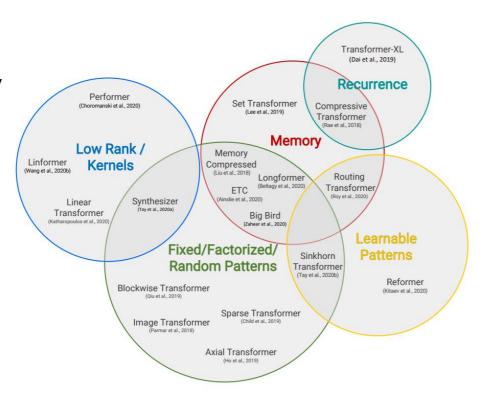


Full n^2 attention

Transformer for long sequences

To work with sequences with significant length we should decrease memory consumption and computation complexity $O(n^2)$





BigBird approach

Memory requirements, n is the sequence length:

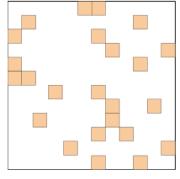
Random attention requires $O(r \cdot n)$

Sliding window requires $O(h \cdot n)$, h is the window size

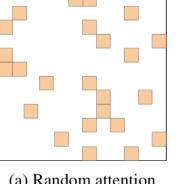
Global requires $O(g \cdot n)$, g is the global tokens number

BigBird combines 3 types of attention mechanism. All of them have linear complexity.

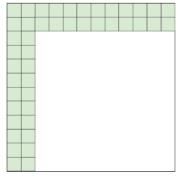
Total: $O((r + h + g) \cdot n)$



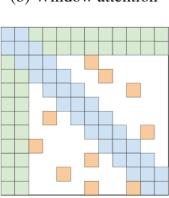
(a) Random attention



(b) Window attention



(c) Global Attention



(d) BIGBIRD

Take-home messages

- Attention mechanism is for "information extraction"
- Transformer architecture is a multi-layer architecture based on the self attention layer

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Common ways for classic ML application for time series data

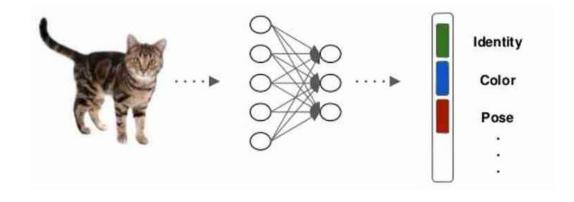
- 1. Take input data including history for the target variable
- Add differences, combinations, rolling means, medians, etc.
- 3. Add one-hot-encoding for important categorical features (day of week, holiday or not)
- Now we have input features for all points
- Let's apply our favorite ML regression algorithm



Deep Learning problems with sequential data: we need representations

Input Output "The quick brown fox jumped over Speech recognition the lazy dog." "There is nothing to like in Sentiment classification this movie." Voulez-vous chanter Machine translation Do you want to sing with me? avec moi? Video activity Running recognition

Semi-structured data processing: why do we need NNs?



Textbook example: next word prediction

The most complicated and difficult part of it was only just beginning.

Textbook example: next word prediction

Idea 1: use previous word(s)

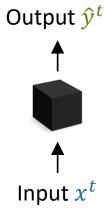
<u>Problem 1:</u> long-term dependencies

"France is where I grew up, but I now live in Boston. I speak fluent ____."

The most complicated and difficult part of it was only just beginning.



Feature representation: [0, 0, 0, 1, 0, 0]



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Textbook example: next word prediction

Idea 1: use previous word(s)

Problem 1: long-term dependencies

Idea 2: use bag of words model

The most complicated and difficult part of it was only just beginning.



Feature representation: [0, 3, 0, 2, 0, 0]

Bag of words: number of occurrences of each word

Textbook example: next word prediction

<u>Idea 1:</u> use previous word(s)

Idea 2: use bag of words model

<u>Problem 1:</u> long-term dependencies

<u>Problem 2:</u> order preservation

The food was good, not bad at all.

VS.

The food was bad, not good at all.

The most complicated and difficult part of it was only just beginning.



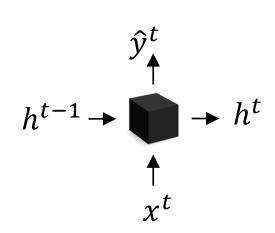
Feature representation: [0, 3, 0, 2, 0, 0]

Bag of words: number of occurrences of each word (see also TF-IDF features)

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Model Design Criteria

- Variable-length sequences processing
- 2. Long-term memory
- 3. Maintain order information
- 4. Natural preprocessing



Recurrent Neural Networks are the solution!

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Sequence processing with classic ML models

- Variable-length sequences processing
- 2. Long-term memory
- 3. Maintain order information
- 4. Natural preprocessing

YES (if one to one)



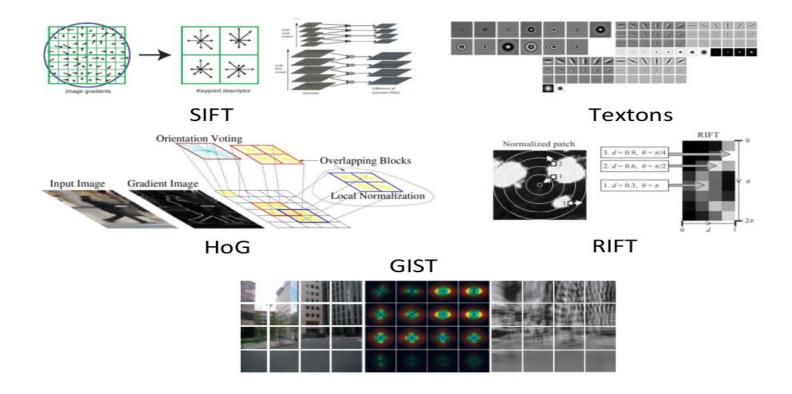


NO

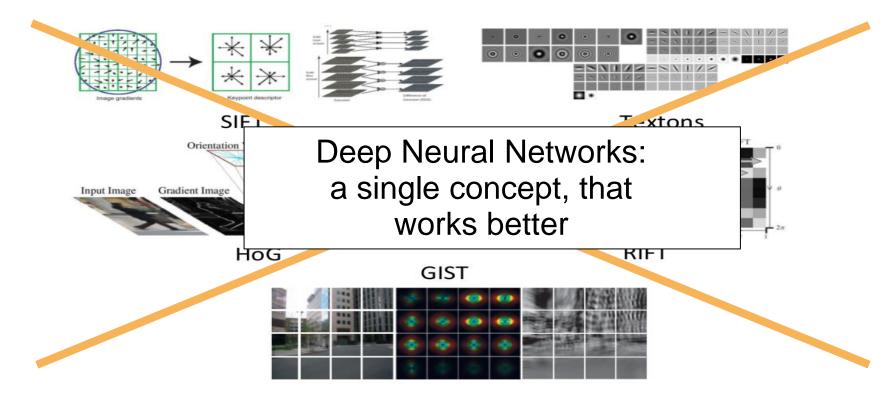


a kind of

An art of feature construction



No art now, just engineering



Why and how Deep learning works

Availability of Graphical processing units (GPU)



Large scale "big" data



Open-source libraries



Complex structured data







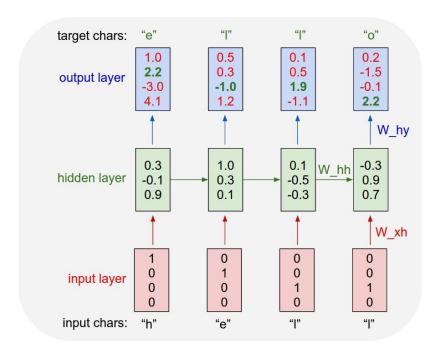


Examples of texts generated by LSTM (Long Short Term Memory NN)

- Shakespeare
- Wiki
- Algebraic geometrics articles
- Linux Source Code
- Dinosaurs names

see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically

For $\bigoplus_{n=1,...,m}$ where $\mathcal{L}_{m_*} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and Lemma 0.1. Assume (3) and (3) by the construction in the description. any sets F on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic Suppose $X = \lim |X|$ (by the formal open covering X and a single map $Proj_{_{Y}}(A) =$ Spec(B) over U compatible with the complex Proof. Proof of (1). It also start we get $Set(A) = \Gamma(X, O_{X,O_X}).$ $S = \operatorname{Spec}(R) = U \times_X U \times_X U$ When in this case of to show that $Q \to C_{Z/X}$ is stable under the following result and the comparicoly in the fibre product covering we have to prove the lemma in the second conditions of (1), and (3). This finishes the proof. By Definition ?? generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points (without element is when the closed subschemes are catenary. If T is surjective we Sch_{Ippf} and $U \rightarrow U$ is the fibre category of S in U in Section, ?? and the fact that may assume that T is connected with residue fields of S. Moreover there exists a any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any closed subspace $Z \subset X$ of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an f is locally of finite type. Since S = Spec(R) and Y = Spec(R). which has a nonzero morphism we may assume that f_i is of finite presentation over Proof. This is form all sheaves of sheaves on X. But given a scheme U and a S. We claim that $\mathcal{O}_{X,x'}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is surjective étale morphism $U \to X$. Let $U \cap U = \coprod_{i=1,...,n} U_i$ be the scheme X over separated. By Algebra, Lemma ?? we can define a map of complexes $GL_{S'}(x'/S'')$ S at the schemes $X_i \rightarrow X$ and $U = \lim_i X_i$. The following lemma surjective restrocomposes of this implies that $F_{x_0} = F_{x_0} =$ To prove study we see that $\mathcal{F}|_{U}$ is a covering of \mathcal{X}' , and \mathcal{T}_{c} is an object of $\mathcal{F}_{X/S}$ for i > 0 and F_p exists and let F_i be a presheaf of O_X -modules on C as a F-module. Lemma 0.2. Let X be a locally Noetherian scheme over S, $E = F_{Y/2}$. Set I =In particular F = U/F we have to show that $\mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq \mathfrak{p}$ is a subset of $\mathcal{J}_{n,0} \circ \overline{A}_2$ works. $\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\operatorname{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$ Lemma 0.3. In Situation ??. Hence we may assume q' = 0. is a unique morphism of algebraic stacks. Note that $Arrows = (Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$ Proof. We will use the property we see that p is the mext functor (??). On the other hand, by Lemma ?? we see that $V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$ is an open subset of X. Thus U is affine. This is a continuous map of X is the where K is an F-algebra where δ_{n+1} is a scheme over S. inverse, the groupoid scheme S. Proof. See discussion of sheaves of sets. The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces, étale}$ which gives an open subspace of X and T equal to S_{Zar} ,



Conclusions

- Classic ML can't handle semistructured data common in sequential data processing
- We can *learn representations* via Neural Networks
- Results are nice even for relatively simple models

Machine translation:application example









War and Peas

Dog Translation Machine

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Machine translation, 50-s

Cold war child: translator from Russian to English IBM 701 Translator

Doctor Dostert predicted that "five, perhaps three years hence, interlingual meaning conversion by electronic process in important functional areas of several languages may well be an accomplished fact." (1954)

Rule-based approach that uses English-Russian dictionary



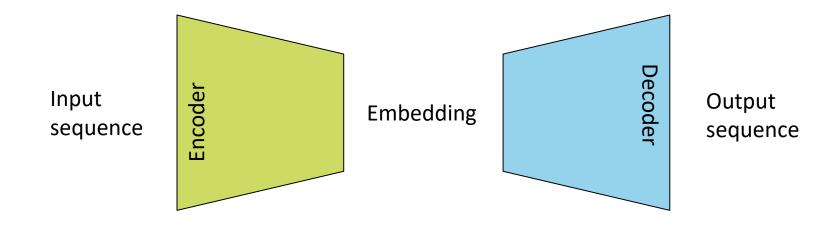
Project shut-down in 5 years: no significant progress

https://www.ibm.com/ibm/history/exhibits/701/701_translator.html https://youtu.be/8ZtdVUB007A

Statistical approach – the leading one before 2014

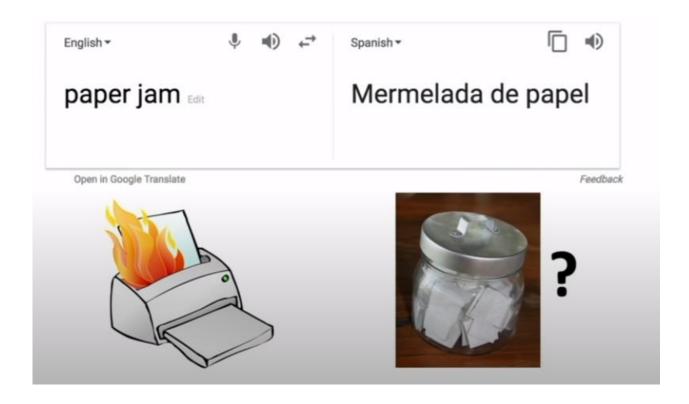
- Complicated and heavy model
- Many separate components
- Complex generation of inputs
- Support of a sophisticated system
- Quality is not great

Neural network for machine translation

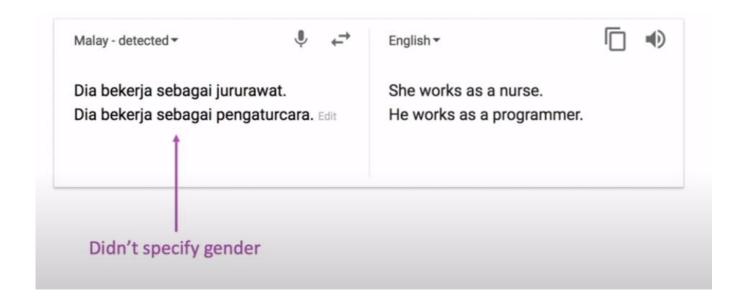


seq2seq (sequence to sequence) architecture

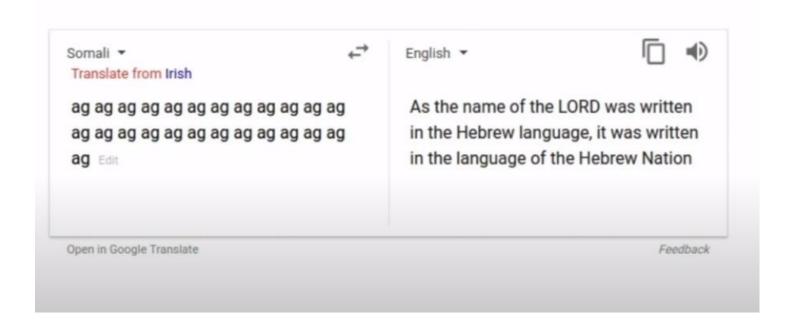
Not a perfect solution with little control over result



Contains biases from learning sample

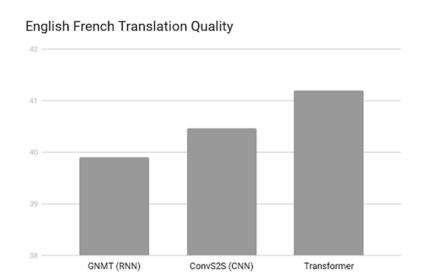


Output strange results



Attention/transformer – new state-of-the art for Machine translation

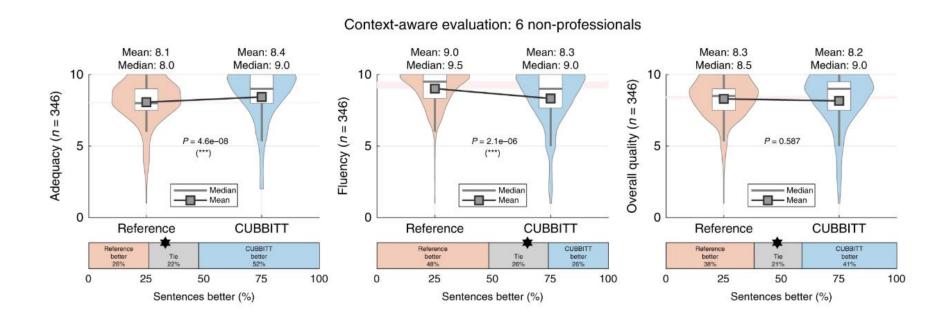
English German Translation quality 28 26 24 29 GNMT (RNN) ConvS2S (CNN) SliceNet (CNN) Transformer



- Maximize BLEU translation quality metric
- The best model is **Transformer**

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NLP deep learning models: CUBBITT is comparable to reference human translation for a selected dataset on News translation



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Conclusions

- Machine translation problem was attacked by many problems during a long period of time
- Right now the state-of-the-art is Neural Networks Transformers
- They can even improve over human-translation

Vanilla Recurrent Neural Network



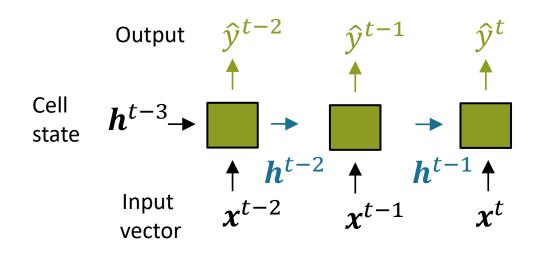
Simple RNN model

At each step:

 \hat{y}^t - output / model prediction

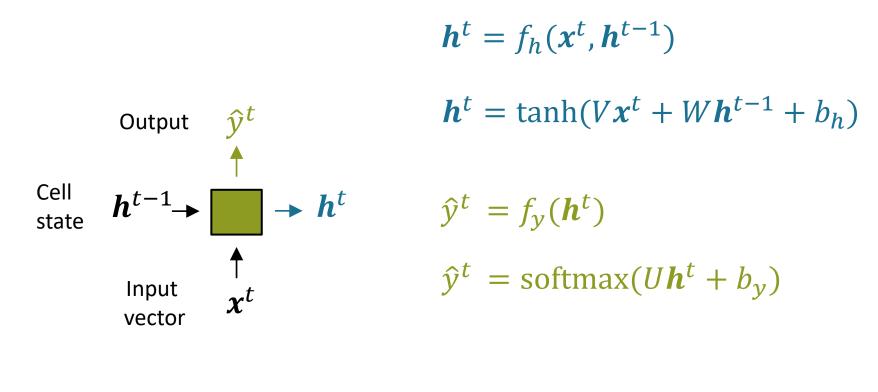
 $oldsymbol{x}^t$ - input vector / new information

 h^t - cell / hidden state



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Simple RNN model block



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Sequence processing with Vanilla RNN

- Long-term memory
- Maintain order information
- Natural preprocessing
- Variable-length sequences processing

NO



YES

a kind of

YES (if one to one)

Another semi-structured data problems

Credit scoring: default prediction

Money Transactions data



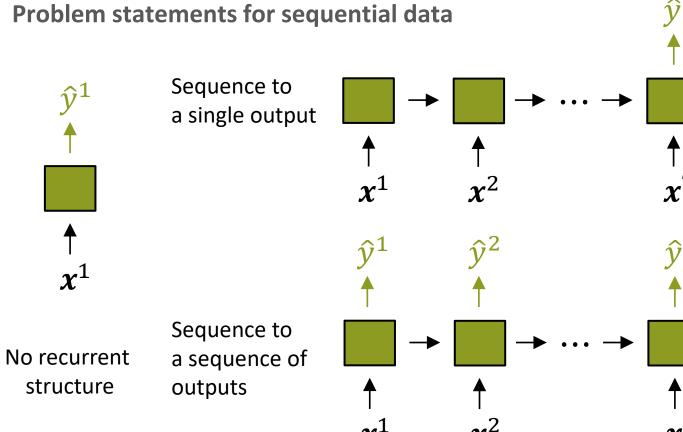
Fraud detection in healthcare insurance

A history of visits

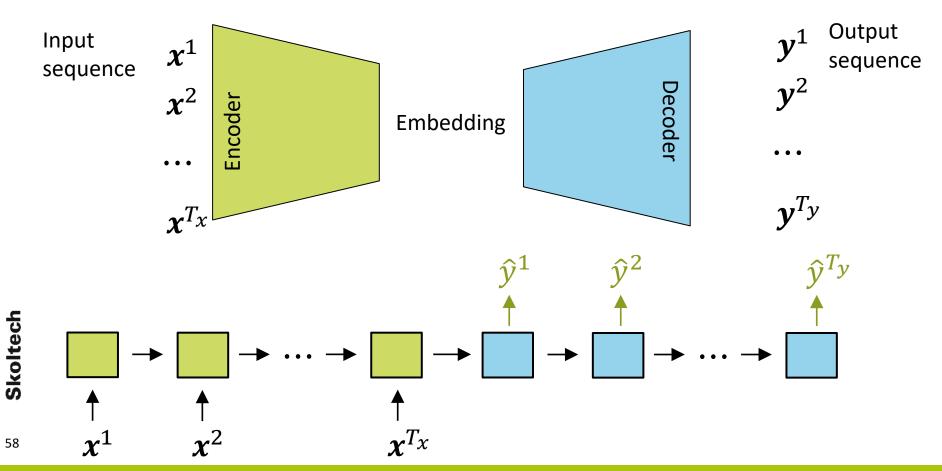
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Is there a fraud?

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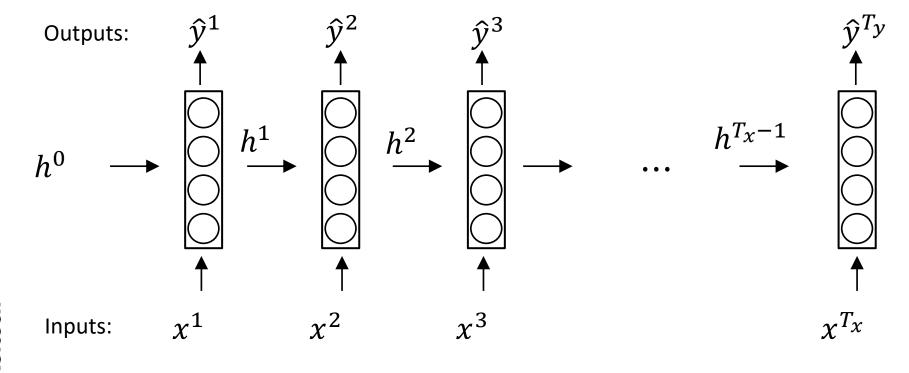
A sequence to sequence problem



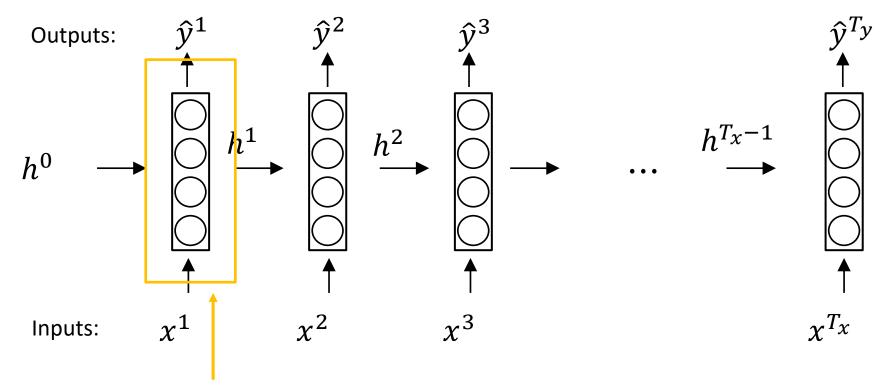
More on Recurrent Neural Networks

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Forward propagation through Recurrent Neural Network

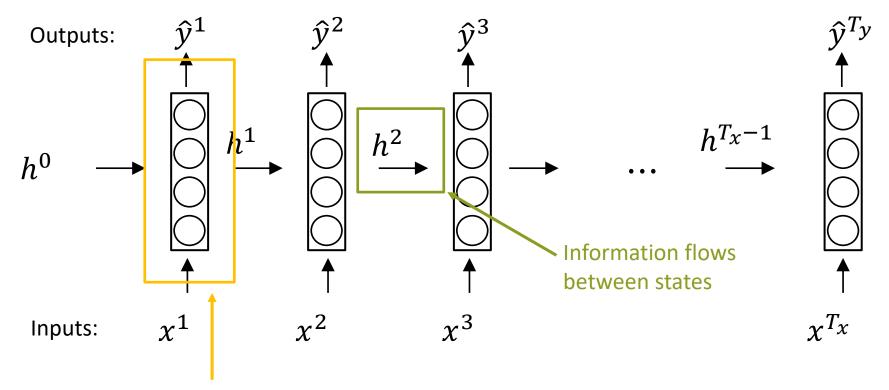


Forward propagation through Recurrent Neural Network



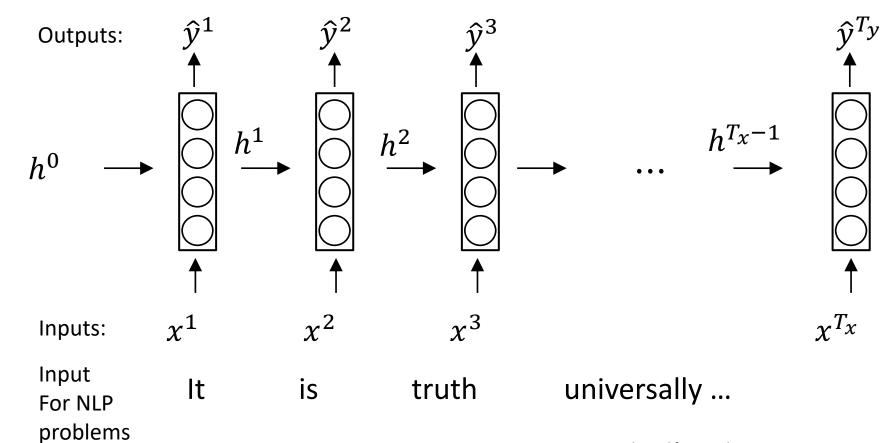
Processing unit is the same for all time moments. Units has parameters we want to learn!

Forward propagation through Recurrent Neural Network



Processing unit is the same for all time moments. Units has parameters we want to learn!

Forward propagation through Recurrent Neural Network



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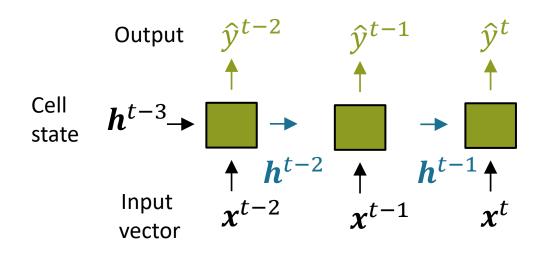
Simple RNN model

At each step:

 \hat{y}^t - output / model prediction

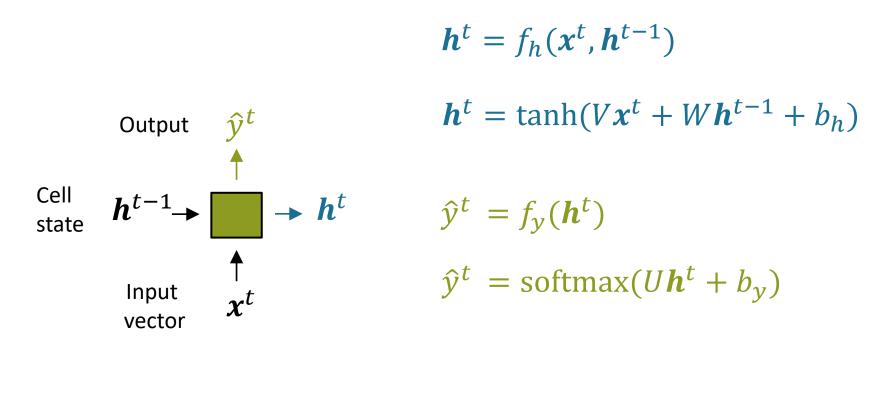
 $oldsymbol{x}^t$ - input vector / new information

 h^t - cell / hidden state

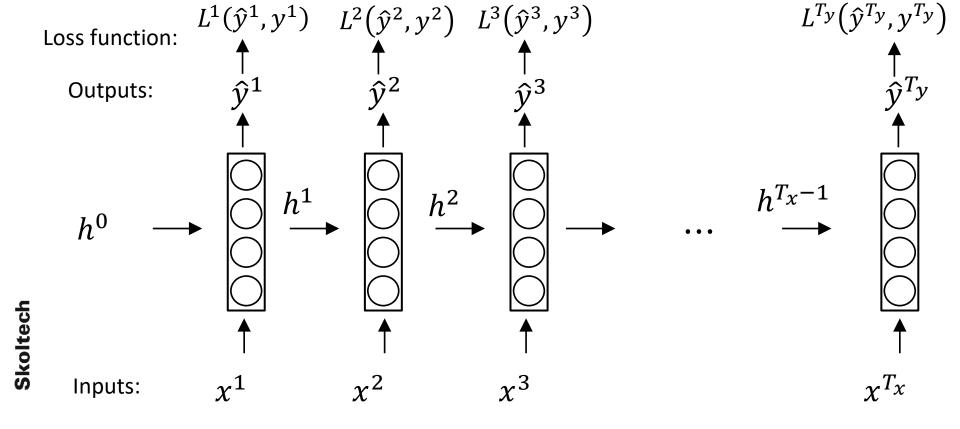


tech

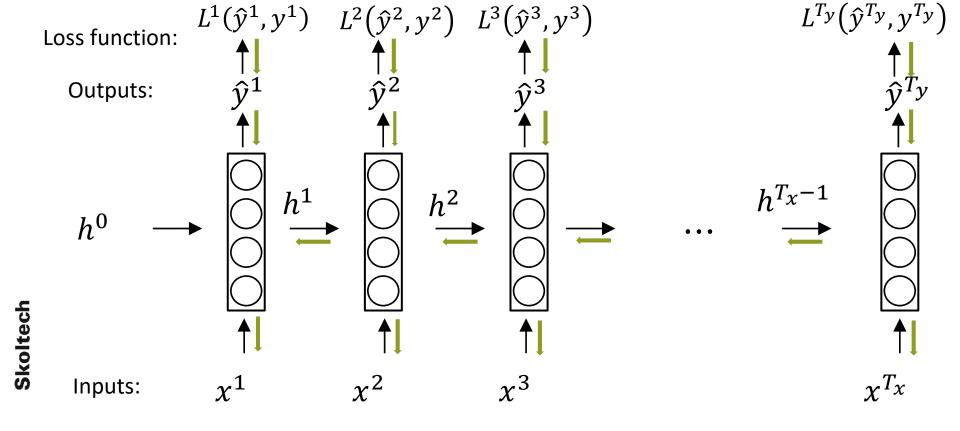
Simple RNN model block



Backward propagation through Recurrent Neural Network



Backward propagation through Recurrent Neural Network

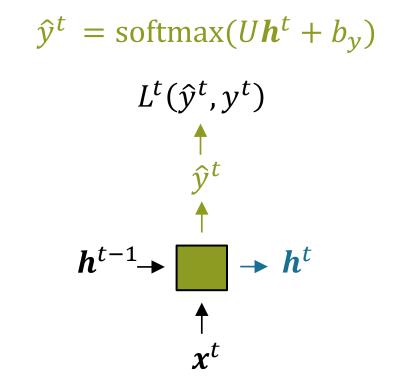


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Backpropagation w.r.t. U

$$L = \sum_{i=1}^{T_y} L^i(\hat{y}^i, y^i)$$

$$\frac{\partial L}{\partial U} = \sum_{i=1}^{T_y} \frac{\partial L_i}{\partial U} = \sum_{i=1}^{T_y} \frac{\partial L_i}{\partial \hat{y}^i} \frac{\partial \hat{y}^i}{\partial U}$$



Backpropagation w.r.t. W

$$L = \sum_{i=1}^{T_{y}} L^{i}(\hat{y}^{i}, y^{i})$$

$$\frac{\partial L}{\partial W} = \sum_{i=1}^{T_{y}} \frac{\partial L_{i}}{\partial W} = \sum_{t=1}^{T_{y}} \frac{\partial L_{i}}{\partial \hat{y}^{t}} \frac{\partial \hat{y}^{t}}{\partial W}$$

$$\boldsymbol{h}^{t} = \tanh(V\boldsymbol{x}^{t} + W\boldsymbol{h}^{t-1} + b_{h})$$

$$\frac{\partial L_{i}}{\partial \hat{y}^{i}} \frac{\partial \hat{y}^{i}}{\partial W} = \frac{\partial L_{i}}{\partial \hat{y}^{i}} \frac{\partial \hat{y}^{i}}{\partial h_{t}} (\frac{\partial h_{t}}{\partial W} + \frac{\partial h_{t}}{\partial h_{t-1}} \frac{\partial h_{t-1}}{\partial W} +)$$

$$\frac{\partial L_{i}}{\partial \hat{y}^{i}} \frac{\partial \hat{y}^{i}}{\partial W} = \frac{\partial L_{i}}{\partial \hat{y}^{i}} \frac{\partial \hat{y}^{i}}{\partial h_{t}} \sum_{i=0}^{T_{y}} (\prod_{j=i+1}^{T_{y}} \frac{\partial h_{j}}{\partial h_{i-1}}) \frac{\partial h_{i}}{\partial W}$$

$$\hat{y}^{t} = \operatorname{softmax}(Uh^{t} + b_{y})$$

$$L^{t}(\hat{y}^{t}, y^{t})$$

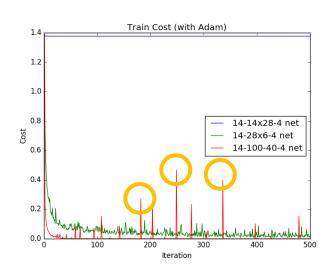
$$\hat{y}^{t}$$

$$\uparrow$$

$$h^{t-1} \rightarrow \qquad \uparrow$$

$$x^{t}$$

Problems of classic RNN



Solution:

Gradient clipping to scale big gradients

1.
$$g = \frac{\partial L}{\partial W}$$

2. If g > t for some threshold t:

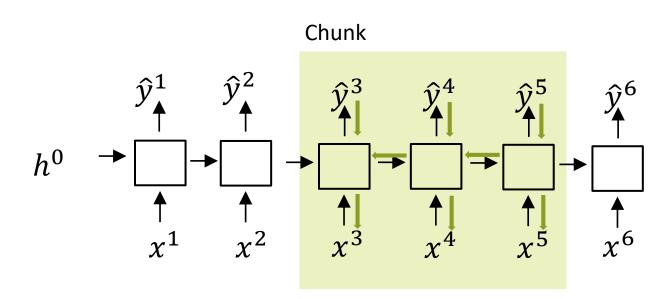
$$g = \frac{t}{\|g\|} g$$

Threshold t is selected given the dynamic of loss function over iterations

Problems of classic RNN

Solution:

- Gradient clipping to scale big gradients
- Truncated backpropagation through time



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Problems of classic RNN

Gradients vanishing is a more

serious problem

Many values < 1

Product << 1

Bias parameters to capture long-term dependencies

Hard to detect!

Tricks:

Activation functions

Use ReLU

Parameter initialization

- Initialize weights to identity matrix
- Initialize biases to zero

Another big problem of classic RNN

Problem: Neural networks forget fast, and it is hard to learn long-term dependencies

Solution: Gated architectures

More complex recurrent units with gates to control what information is passed through

- GRU (Gated Recurrent Unit)
- LSTM (Long-Short Term Memory)

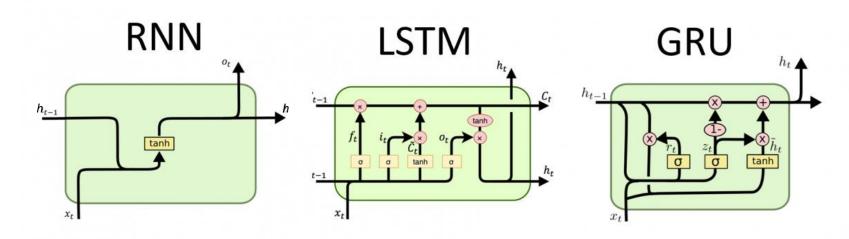
Selection of RNN architecture



Better RNN units: LSTM and GRU

LSTM: long short term memory [1]

GRU: Gated recurrent unit [2]



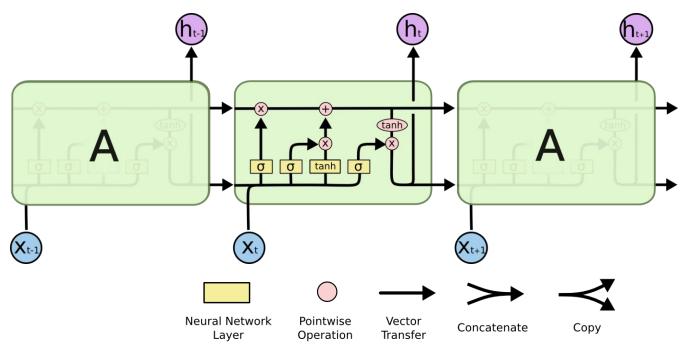
- 1. Schmidhuber, J., & Hochreiter, S. (1997). Long short-term memory. *Neural Comput*, *9*(8), 1735-1780.
- 2. Cho, K., Van Merriënboer et al. (2014). Learning phrase representations using RNN encoder-decoder for statistical machine translation. *arXiv* preprint arXiv:1406.1078.

Details on how LSTM works

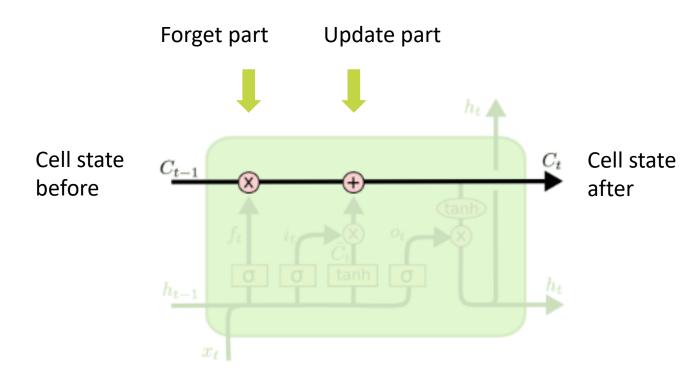
Remembering information for long periods of time is practically the default behavior of LSTM



LSTM was proposed by J. Schmidhuber group in 1991

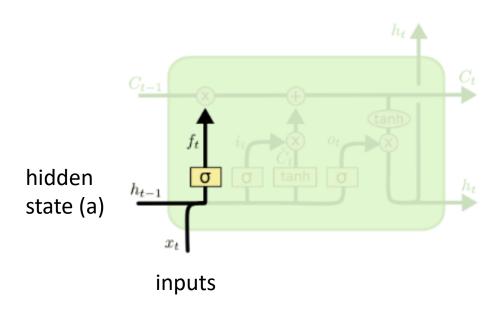


Long term memory part – Cell state



Forget part

Identify how much should we forget: sigmoid returns value between 0 and 1

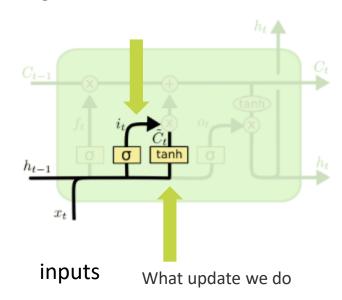


$$f_t = \sigma\left(W_f \cdot [h_{t-1}, x_t] + b_f\right)$$

hidden

state (a)

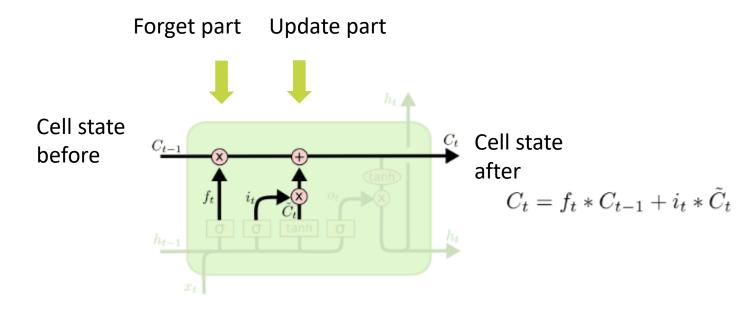
Identify how much should we update: sigmoid returns value between 0 and 1



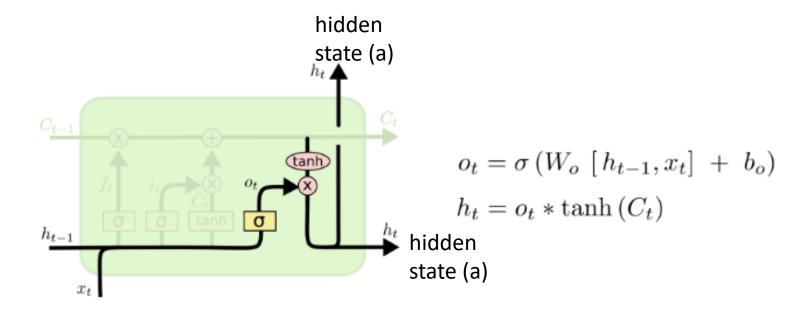
$$i_t = \sigma \left(W_i \cdot [h_{t-1}, x_t] + b_i \right)$$

$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

Long term memory part – Cell state

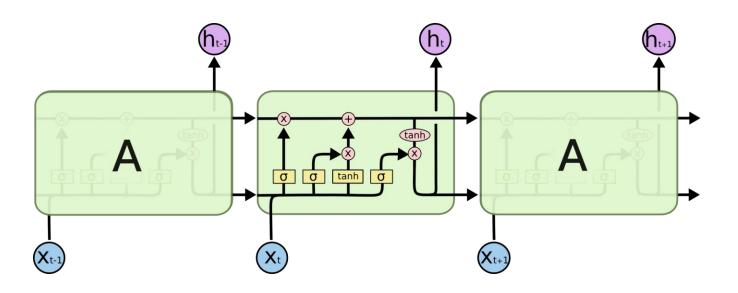


Update everything else

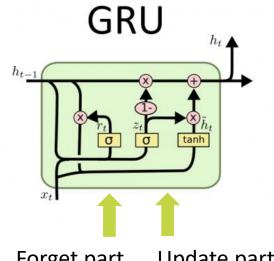


Details on how LSTM works

- There are cell and hidden (activation) states
- LSTM block forgets and updates cell state during processing at one block



$$\mathbf{r}^{t} = \sigma(W_{xr}\mathbf{x}^{t} + W_{hr}\mathbf{h}^{t-1} + b_{r})$$
$$\mathbf{z}^{t} = \sigma(W_{xz}\mathbf{x}^{t} + W_{hz}\mathbf{h}^{t-1} + b_{z})$$



Update part Forget part

$$\widetilde{\mathbf{h}}^{t} = \tanh(W_{xh}\mathbf{x}^{t} + W_{hr}(\mathbf{r}^{t} \odot \mathbf{h}^{t-1}) + b_{h})$$

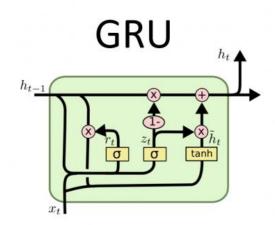
$$\mathbf{h}^{t} = \mathbf{z}^{t} \odot \mathbf{h}^{t-1} + (1 - \mathbf{z}^{t}) \odot \widetilde{\mathbf{h}}^{t}$$

Cho, Kyunghyun et al. 2014. Learning Phrase Representations using RNN Encoder-Decoder for Statistical Machine Translation.

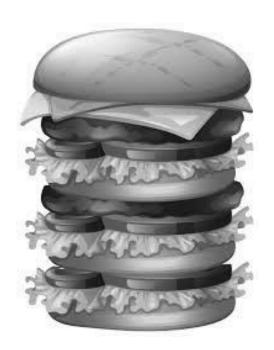
GRU – Gated Recurrent Unit

- Update gate what to pay attention to
- Reset gate what to forget

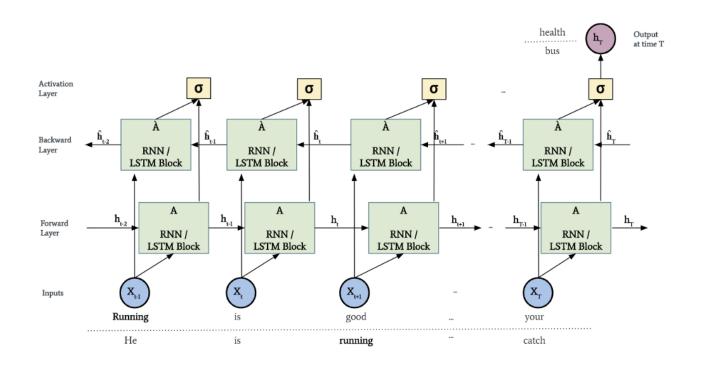
- Slightly worse than LSTM for NLP but not in all problems
- Simpler and cheaper than LSTM



Multilayer architectures



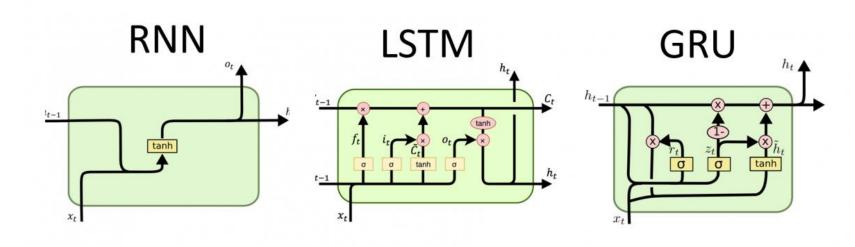
Other architectures: bidirectional LSTM



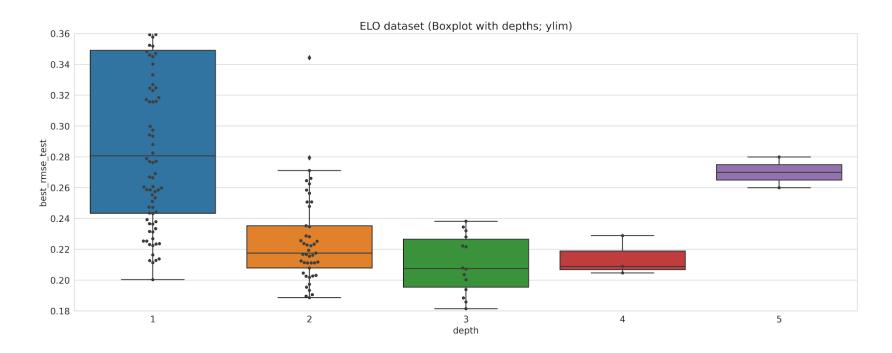
Other architectures: bidirectional LSTM

Bidirectional LSTM are useful when we benefit from the future data or can use it:

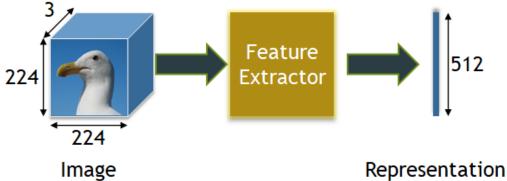
- Handwriting Recognition
- Speech Recognition
- Protein Structure Prediction (Bioinformatics)



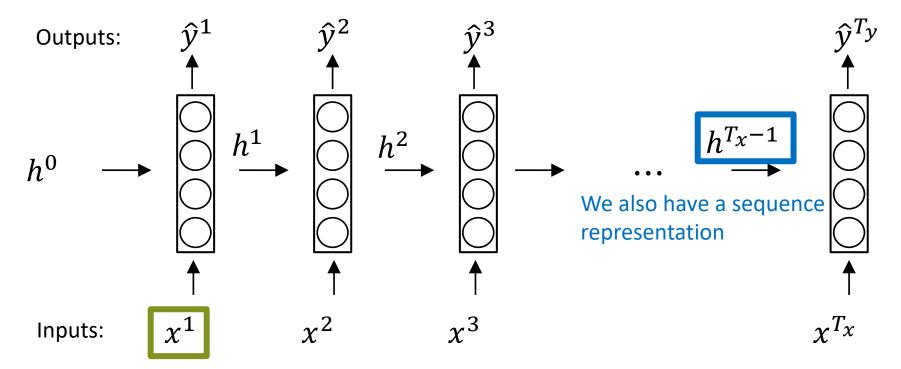
Multiple layers RNN performance



Representation
learning is the core
feature of Neural
Networks



Representation learning is still here for Recurrent Neural Networks



Most of the time we also learn representations of objects in an end2end manner with backpropagation

Attention mechanism

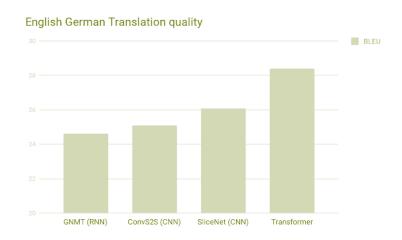
ech

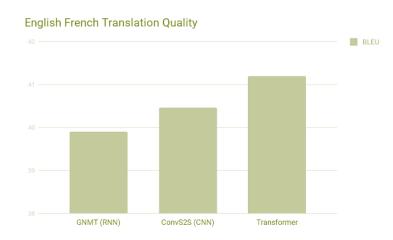
New state of the art: attention is all we need

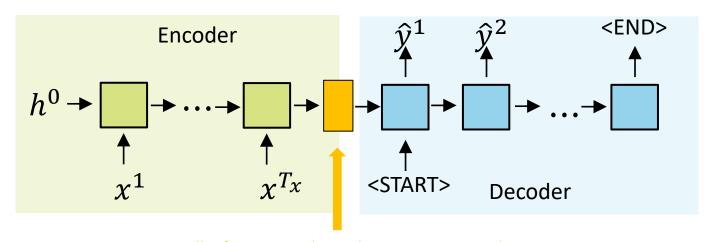


Higher BLEU scores are better

attention







All information about the sequence is in this vector

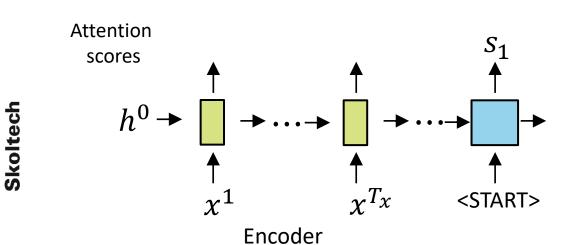
Attention

- Solution to the bottleneck problem
- Direction connection between parts of input and output sequence

Sequence 2 sequence with attention

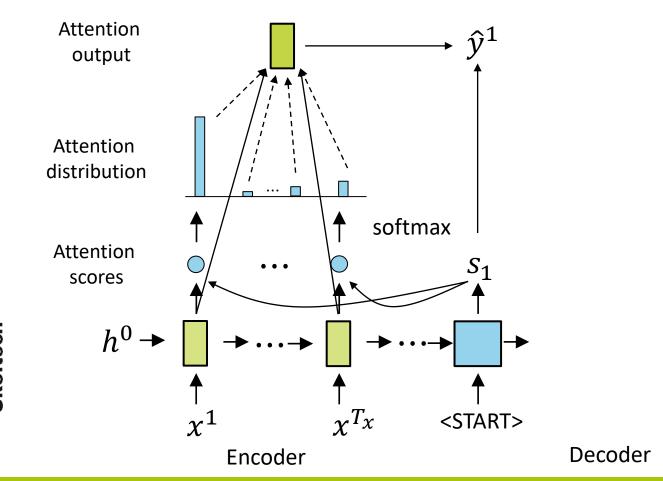
Attention output

Attention distribution

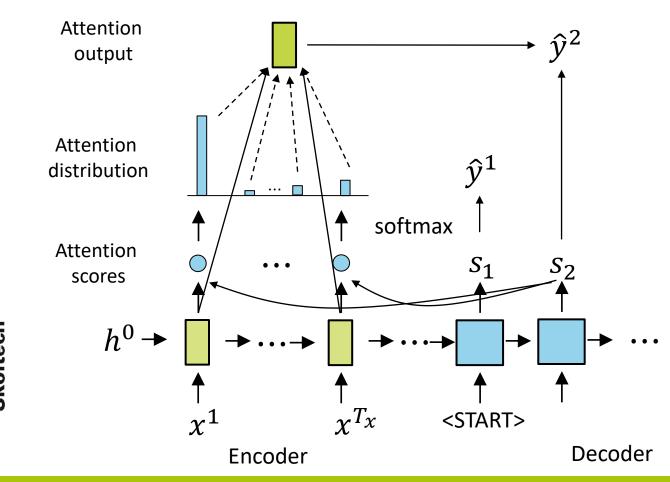


Decoder

Sequence 2 sequence with attention



Sequence 2 sequence with attention



Attention: formulas

- First RNN produces encoder hidden states $m{h}_1$, ..., $m{h}_{T_x} \in \mathbb{R}^h$
- Decoder hidden state $\mathbf{s}_t \in \mathbb{R}^h$ at time step t
- Attention scores for step t:

$$oldsymbol{e^t} = [oldsymbol{s_t^T} oldsymbol{h}_1, \dots, oldsymbol{s_t^T} oldsymbol{h}_{T_x}] \in \mathbb{R}^{T_x}$$

 Softmax to get attention distribution: all values are positive, sum of all values is 1:

$$\boldsymbol{\alpha^t} = \operatorname{softmax}(\boldsymbol{e^t}) \in \mathbb{R}^{T_x}$$

Attention output a_t is a weighted sum of hidden states:

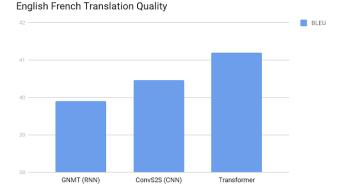
$$oldsymbol{a}_t = \sum_{i=1}^{T_{\mathcal{X}}} lpha_i^t oldsymbol{h}_i \in \mathbb{R}^h$$

We concatenate the attention output a_t with the decoder hidden state \boldsymbol{s}_t and proceed to the non-attention part of our seq2seq model

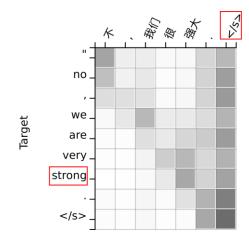
$$[\boldsymbol{a}_t, \boldsymbol{s}_t] \in \mathbb{R}^{2h}$$

Attention is just great

- Significantly improves performance of NMT
- Solves the bottleneck problem
 - All encoder tokens are connected to all decoder tokens
- No more vanishing gradients
 - All to All connection
- Provides some interpretability
 - see alignment figure
- Similar to RNN seq2seq, but greater!



BLEU scores (higher is better) of single models on the standard WMT newstest2014 English to French translation benchmark.



Attention is a general deep learning idea

We can use attention in many architectures and many tasks

- Other NLP problems
- Sequential data processing
- Graph Neural Networks

Key value interpretation:

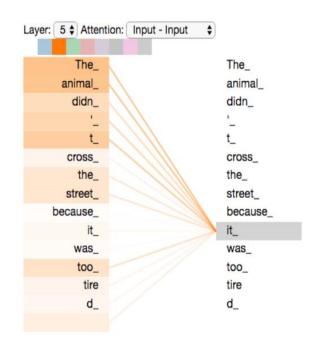
 S_i - query to a database Hidden state of the decoder

 k_i - keys in the database Hidden state of the encoder

 h_i - values in the database Hidden state of the encoder

- Calculate correspondence $e(s_i, k_i)$
- Calculate weights on the base of correspondence values
- Extract information as weighted sum of values $\sum_{i=1}^{n} \alpha_i \boldsymbol{h}_i$

Interpretability of attention



Remove a token i^* with max attention...

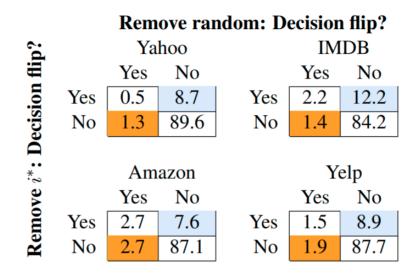


Figure source: https://jalammar.github.io/illustrated-transformer/, https://github.com/jessevig/bertviz Serrano, Sofia, and Noah A. Smith. "Is attention interpretable?." arXiv preprint arXiv:1906.03731 (2019). ACL 2019.

Does a better recurrent block exist?

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Towards a better recurrent block

- LSTM architecture is ad-hoc and has a substantial number of components whose purpose is not immediately apparent
- Like the LSTM, it is hard to tell, at a glance, which part of the GRU is essential for its functioning.
- Let's compare 10 000 different architectures on 3 problems with 1 000 of them pass the initial filtering stage: genetic algorithm
- Each architecture has been evaluated on about 220 hyperparameter settings.
- 230 000 hyperparameter configurations in total!



Best found architectures MUTx are close to GRU

GRU:

$$r_{t} = \operatorname{sigm}(W_{xr}x_{t} + W_{hr}h_{t-1} + b_{r})$$

$$z_{t} = \operatorname{sigm}(W_{xz}x_{t} + W_{hz}h_{t-1} + b_{z})$$

$$\tilde{h}_{t} = \operatorname{tanh}(W_{xh}x_{t} + W_{hh}(r_{t} \odot h_{t-1}) + b_{h})$$

$$h_{t} = z_{t} \odot h_{t-1} + (1 - z_{t}) \odot \tilde{h}_{t}$$

Arch.	N	N-dropout	P
Tanh	3.612	3.267	6.809
LSTM	3.492	3.403	6.866
LSTM-f	3.732	3.420	6.813
LSTM-i	3.426	3.252	6.856
LSTM-o	3.406	3.253	6.870
LSTM-b	3.419	3.345	6.820
GRU	3.410	3.427	6.876
MUT1	3.254	3.376	6.792
MUT2	3.372	3.429	6.852
MUT3	3.337	3.505	6.840

Table 2. Negative Log Likelihood on the music datasets. N stands for Nottingham, N-dropout stands for Nottingham with nonzero dropout, and P stands for Piano-Midi.

MUT1:

$$\begin{aligned} z &= \operatorname{sigm}(W_{\mathsf{xz}}x_t + b_{\mathsf{z}}) \\ r &= \operatorname{sigm}(W_{\mathsf{xr}}x_t + W_{\mathsf{hr}}h_t + b_{\mathsf{r}}) \\ h_{t+1} &= \operatorname{tanh}(W_{\mathsf{hh}}(r \odot h_t) + \operatorname{tanh}(x_t) + b_{\mathsf{h}}) \odot z \\ &+ h_t \odot (1-z) \end{aligned}$$

MUT2:

$$z = \operatorname{sigm}(W_{xz}x_t + W_{hz}h_t + b_z)$$

$$r = \operatorname{sigm}(x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

MUT3:

$$z = \operatorname{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z)$$

$$r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

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Towards a better recurrent block

- LSTM architecture is ad-hoc and has a substantial number of components whose purpose is not immediately apparent
- Like the LSTM, it is hard to tell, at a glance, which part of the GRU is essential for its functioning.
- Let's compare 8 LSTM variants and hope for the best by search over the space of hyperparameters with 5400 runs in total
- No significant improvement over the common LSTM
- Some advices on hyperparameters selection



Neural architecture search for a better Recurrent block

- Linear: $f(x_1,...,x_n) = W_1x_1 + ... + W_nx_n + b$,
- Blending (element wise): $f(z, x, y) = z \odot x + (1 z) \odot y$,
- Element wise product and sum,
- Activations: Tanh, Sigmoid, and LeakyReLU.

- Number of nodes < 25
- Number of hidden states < 4
- Number of linear input vectors < 4

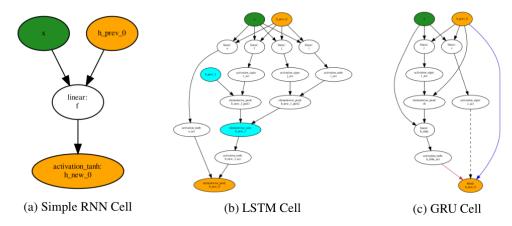
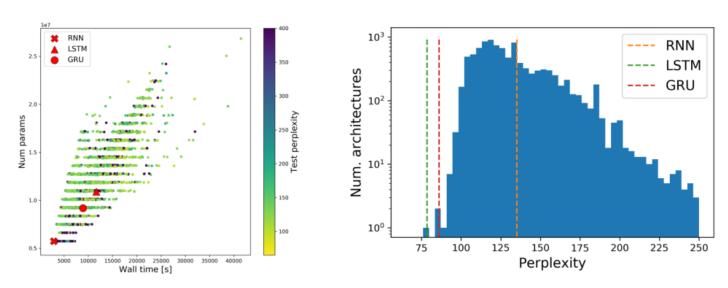


Figure 2: Examples of conventional RNN cells. Colors of nodes highlight the corresponding previous and new hidden states, green color also highlights the input vector. Black dashed, blue and red edges indicate blending arguments z, x and y respectively.

Neural architecture search for a better Recurrent block



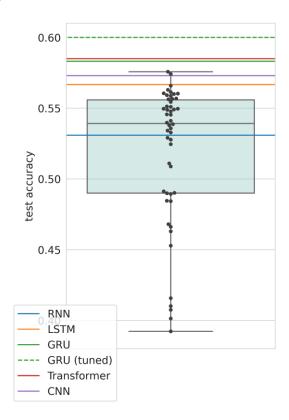
(a) Joint distribution of metrics.

(b) Best test perplexity distribution.

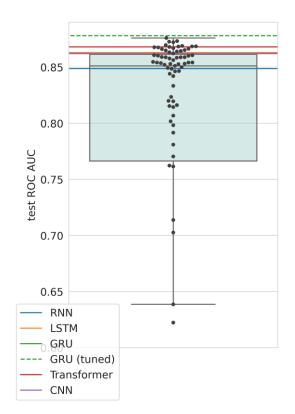
Figure 4: Architectures metrics on PTB.

Best architecture for Transactions data

Age prediction



Gender prediction



Architecture performance transferability

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0.81

0.82

0.83

0.84

Gender test ROC AUC

0.85

0.86

0.87

0.88

