

Intermediate Code & Local Optimizations

CS143
Lecture 14

<https://web.stanford.edu/class/cs143/>

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Lecture Outline

- Intermediate code
- Local optimizations
- Next time: global optimizations

Code Generation Summary

- We have discussed
 - Runtime organization
 - Simple stack machine code generation
 - Improvements to stack machine code generation
- Our compiler maps AST to assembly language
 - And does not perform optimizations

Optimization

- Optimization is our last compiler phase
- Most complexity in modern compilers is in the optimizer
 - Also by far the largest phase
- First, we need to discuss intermediate representations

Why Intermediate Representations?

- When should we perform optimizations?
 - On AST
 - Pro: Machine independent
 - Con: Too high level
 - On assembly language
 - Pro: Exposes optimization opportunities
 - Con: Machine dependent
 - Con: Must reimplement optimizations when retargetting
 - On an intermediate representation (language)
 - Pro: Machine independent
 - Pro: Exposes optimization opportunities

Intermediate Representations (IR)

- Intermediate representation = high-level assembly
 - Uses register names, but has an unlimited number
 - Uses control structures like assembly language
 - Uses opcodes but some are higher level
 - E.g., `push` translates to several assembly instructions
 - Most opcodes correspond directly to assembly opcodes

Definition: Three-Address Intermediate Code

- Each instruction is of the form

$$x := y \text{ op } z$$
$$x := \text{op } y$$

- y and z are registers or constants
 - Common form of intermediate code
- The expression $x + y * z$ is translated

$$t_1 := y * z$$
$$t_2 := x + t_1$$

- Each subexpression has a “name”

Generating Intermediate Code

- Similar to assembly code generation
- But use any number of IR registers to hold intermediate results

Generating Intermediate Code (Cont.)

Intermediate Code Notes

- You should be able to use intermediate code
 - At the level discussed in lecture
- You are not expected to know how to generate intermediate code
 - Because we won't discuss it
 - But really just a variation on code generation . . .

An Intermediate Representation

$P \rightarrow S P \mid \epsilon$

$S \rightarrow id := id \ op \ id$

| $id := op \ id$

| $id := id$

| $push \ id$

| $id := pop$

| $if \ id \ relop \ id \ goto \ L$

| $L:$

| $jump \ L$

- id's are register names
- Constants can replace id's
- Typical operators: +, -, *

Definition: Basic Blocks

- A basic block is a maximal sequence of instructions with:
 - no labels (except at the first instruction), and
 - no jumps (except in the last instruction)
- Idea:
 - Cannot jump into a basic block (except at beginning)
 - Cannot jump out of a basic block (except at end)
 - A basic block is a single-entry, single-exit, straight-line code segment

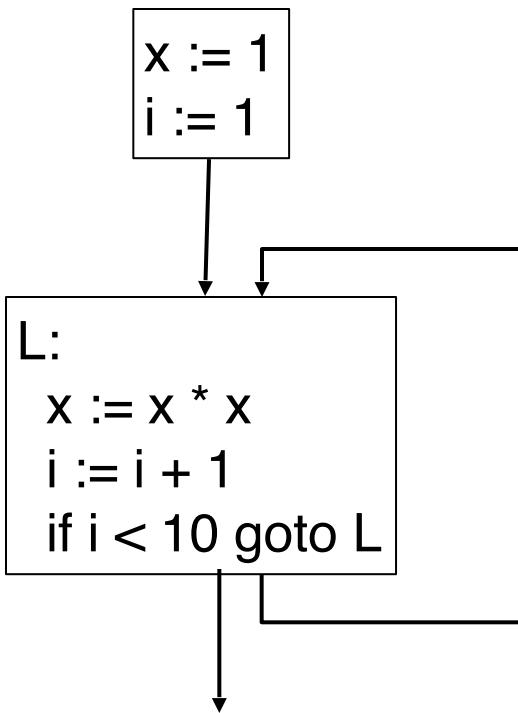
Basic Block Example

- Consider the basic block
 1. L:
 2. $t := 2 * x$
 3. $w := t + x$
 4. if $w > 0$ goto L'
- (3) executes only after (2)
 - We can change (3) to $w := 3 * x$
 - Can we eliminate (2) as well?

Definition: Control-Flow Graphs (CFG)

- A control-flow graph is a directed graph with
 - Basic blocks as nodes
 - An edge from block A to block B if the execution can pass from the last instruction in A to the first instruction in B
 - E.g., the last instruction in A is jump L_B
 - E.g., execution can fall-through from block A to block B

Example of Control-Flow Graphs



- The body of a method (or procedure) can be represented as a control-flow graph
- There is one initial node
- All “return” nodes are terminal

Optimization Overview

- Optimization seeks to improve a program's resource utilization
 - Execution time (most often)
 - Code size
 - Network messages sent, etc.
- Optimization should not alter what the program computes
 - The answer must still be the same

A Classification of Optimizations

- For languages like C and Cool there are three granularities of optimizations
 1. Local optimizations
 - Apply to a basic block in isolation
 2. Global optimizations
 - Apply to a control-flow graph (method body) in isolation
 3. Inter-procedural optimizations
 - Apply across method boundaries
- Most compilers do (1), many do (2), few do (3)

Cost of Optimizations

- In practice, a conscious decision is made not to implement the fanciest optimization known
- Why?
 - Some optimizations are hard to implement
 - Some optimizations are costly in compilation time
 - Some optimizations have low benefit
 - Many fancy optimizations are all three!
- Goal: Maximum benefit for minimum cost

Local Optimizations

- The simplest form of optimizations
- No need to analyze the whole procedure body
 - Just the basic block in question
- Example: algebraic simplification

Algebraic Simplification

- Some statements can be deleted

$x := x + 0$

$x := x * 1$

- Some statements can be simplified

$x := x * 0 \Rightarrow x := 0$

$y := y ** 2 \Rightarrow y := y * y$

$x := x * 8 \Rightarrow x := x << 3$

$x := x * 15 \Rightarrow t := x << 4; x := t - x$

(on some machines $<<$ is faster than $*$; but not on all!)

Constant Folding

- Operations on constants can be computed at compile time
 - If there is a statement $x := y \text{ op } z$
 - And y and z are constants
 - Then $y \text{ op } z$ can be computed at compile time
- Example: $x := 2 + 2 \Rightarrow x := 4$
- Example: $\text{if } 2 < 0 \text{ jump L}$ can be deleted
- When might constant folding be dangerous?

Flow of Control Optimizations

- Eliminate unreachable basic blocks:
 - Code that is unreachable from the initial block
 - E.g., basic blocks that are not the target of any jump or “fall through” from a conditional
- Why would such basic blocks occur?
- Removing unreachable code makes the program smaller
 - And sometimes also faster
 - Due to memory cache effects (increased spatial locality)

Definition: Static Single Assignment (SSA) Form

- Some optimizations are simplified if each register occurs only once on the left-hand side of an assignment
- Rewrite intermediate code in single assignment form

$$x := z + y \qquad \qquad b := z + y$$
$$a := x \qquad \Rightarrow \qquad a := b$$
$$x := 2 * x \qquad \qquad x := 2 * b$$

(*b* is a fresh register)

- More complicated in general, due to loops

Common Subexpression Elimination

- If
 - Basic block is in single assignment form
 - A definition $x :=$ is the first use of x in a block
- Then
 - When two assignments have the same rhs, they compute the same value
- Example:

$x := y + z$

...

$w := y + z$

\Rightarrow

$x := y + z$

...

$w := x$

(the values of x , y , and z do not change in the ... code)

Copy Propagation

- If $w := x$ appears in a block, replace subsequent uses of w with uses of x
 - Assumes single assignment form
- Example:
$$\begin{array}{ll} b := z + y & b := z + y \\ a := b & \Rightarrow a := b \\ x := 2 * a & x := 2 * b \end{array}$$
- Only useful for enabling other optimizations
 - Constant folding
 - Dead code elimination

Copy Propagation and Constant Folding

- Example:

a := 5

x := 2 * a \Rightarrow

y := x + 6

t := x * y

a := 5

x := 10

y := 16

t := 160

Copy Propagation and Dead Code Elimination

If

$w := \text{rhs}$ appears in a basic block

w does not appear anywhere else in the program

Then

the statement $w := \text{rhs}$ is dead and can be eliminated

– Dead = does not contribute to the program's result

Example: (a is not used anywhere else)

$$\begin{array}{lll} b := z + y & b := z + y & b := z + y \\ a := b & \Rightarrow & a := b \\ x := 2 * a & & x := 2 * b \end{array}$$

Applying Local Optimizations

- Each local optimization does little by itself
- Typically optimizations interact
 - Performing one optimization enables another
- Optimizing compilers repeat optimizations until no improvement is possible
 - The optimizer can also be stopped at any point to limit compilation time

An Example

- Initial code:

```
a := x ** 2  
b := 3  
c := x  
d := c * c  
e := b * 2  
f := a + d  
g := e * f
```

An Example

- Algebraic optimization:

a := x ** 2

b := 3

c := x

d := c * c

e := b * 2

f := a + d

g := e * f

An Example

- Algebraic optimization:

a := x * x

b := 3

c := x

d := c * c

e := b << 1

f := a + d

g := e * f

An Example

- Copy propagation:

```
a := x * x  
b := 3  
c := x  
d := c * c  
e := b << 1  
f := a + d  
g := e * f
```

An Example

- Copy propagation:

```
a := x * x  
b := 3  
c := x  
d := x * x  
e := 3 << 1  
f := a + d  
g := e * f
```

An Example

- Constant folding:

```
a := x * x  
b := 3  
c := x  
d := x * x  
e := 3 << 1  
f := a + d  
g := e * f
```

An Example

- Constant folding:

a := x * x

b := 3

c := x

d := x * x

e := 6

f := a + d

g := e * f

An Example

- Common subexpression elimination:

a := x * x

b := 3

c := x

d := x * x

e := 6

f := a + d

g := e * f

An Example

- Common subexpression elimination:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + d

g := e * f

An Example

- Copy propagation:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + a

g := 6 * f

An Example

- Dead code elimination:

a := x * x

b := 3

c := x

d := a

e := 6

f := a + a

g := 6 * f

An Example

- Dead code elimination:

a := x * x

f := a + a
g := 6 * f

- This is the final form

Peephole Optimizations on Assembly Code

- These optimizations work on intermediate code
 - Target independent
 - But they can be applied on assembly language also
- Peephole optimization is effective for improving assembly code
 - The “peephole” is a short sequence of (usually contiguous) instructions
 - The optimizer replaces the sequence with another equivalent one (but faster)

Peephole Optimizations (Cont.)

- Write peephole optimizations as replacement rules
 $i_1, \dots, i_n \rightarrow j_1, \dots, j_m$
where the rhs is the improved version of the lhs
- Example:
 - move \$a \$b, move \$b \$a \rightarrow move \$a \$b
 - Works if move \$b \$a is not the target of a jump
- Another example
addiu \$a \$a i, addiu \$a \$a j \rightarrow addiu \$a \$a i+j

Peephole Optimizations (Cont.)

- Many (but not all) of the basic block optimizations can be cast as peephole optimizations
 - Example: `addiu $a $b 0` → `move $a $b`
 - Example: `move $a $a` →
 - These two together eliminate `addiu $a $a 0`
- As for local optimizations, peephole optimizations must be applied repeatedly for maximum effect

Local Optimizations: Notes

- Intermediate code is helpful for many optimizations
- Many simple optimizations can still be applied on assembly language
- “Program optimization” is somewhat misnamed
 - Code produced by “optimizers” is not optimal in any reasonable sense
 - “Program improvement” is a more appropriate term
- Next time: global optimizations