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Preface

This is an example of “frontmatter”, which comes before the main text of the book.

Chapter 1

(1981.)

, 4 1981. X

1.1

$A, u \in U, f \in F.$

$$Au = f, \quad u \in U, \quad f \in F \tag{1.1}$$

$u, f \in A. f(u), \dots$

$-\dots - , \dots , \dots , \dots , \dots$

. “ \dots , \dots .” [@@, - 1967]. [\(1.1\)](#), \dots , \dots .
 \dots [@@ - 1965]. \dots -, \dots . (\dots) -, [@@ - 1958].
 .

1.2

1.2.1

$$Au \equiv \int_a^b K(x-t)u(t) dt = f(x), \quad c \leq x \leq d, \quad (1.2)$$

-, . $A - K(t)$, .
:

@@Eddington-1913 [@@, - 1959]. $t - , x - , s = x - t - , u(t), f(x)$
— , $b = -a = \infty$,
$$K(s) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{s^2}{2\sigma^2}} -$$

[@@-1959]

$t - , x - , s = x - t - , u(t), f(t) - . u(t) = N(v), \quad n(r) \quad r :$

$$n(r) = \left| \frac{\partial v}{\partial r} \right| N(v).$$

$b = -a = \infty, K(s) - . f(x) - .$

() **[@@van deHulst-1941, - 1970]**

- :

$$Au \equiv \int_0^{2\pi i} \int_{-\pi/2}^{\pi/2} K(\alpha' - \alpha, \delta' - \delta) \cos \delta I(\alpha, \delta) d\delta d\alpha = I_*(\alpha', \delta') \quad (1.3)$$

$I-\,,I_*-\,,K-\,,\alpha-\,,\delta-\,.$

1.2.2 I

[@@, -1959]

$t=r-\,,x=m-\,,u(t)=D(r)-\,,f(x)=A(m)-\quad m, K(x,t)=r^2\varphi(m+5-5\lg r-a(r),\varphi(M)-\,,a(r)-\quad.$
 $\qquad\qquad\qquad:$

$$Au\equiv\int\limits_a^bK(x,t)u(t)\,dt=f(x),\quad c\leq x\leq d,\tag{1.4}$$

$a=0, b=d=-c=\infty.$

$$p(m)A(m)=\int\limits_a^bD(r)\varphi(m+5-5\lg r-a(t))r\,dr,\tag{1.5}$$

$p(m)-\quad m.$

[@@ -1954]

$XOY\quad,\,x\quad,\quad,\,x,y-\quad,\,XOY.$
 $x',y'-\quad.\quad u(x,y)\quad f(x',y')$

$$\int\limits_0^{\infty}\int\limits_{-\infty}^{\infty}K(x'-x,y,y')u(x,y)\,dx\,dy=2\pi y'^2f(x',y'),\quad -\infty< x'<\infty,\quad 0\leq y',$$

$$\mathbf{K}(\mathbf{x},\mathbf{y},\mathbf{z})=\left[1-\left(\frac{2yz}{x^2+y^2+z^2}\right)^2\right]^{-1/2}.\tag{1.6}$$

1.2.3

[@@,, - 1978]

— , . i - , $l_i(\Delta)$, Δ — . I_i — $d\sigma$, φ_i — , i - , . ξ ρ I II . S

$$\iint_{S(\Delta)} I_2(\rho) \varphi_1(\xi) d\sigma = 1 - l_1(\Delta), \quad \iint_{S(\Delta)} I_1(\rho) \varphi_2(\xi) d\sigma = 1 - l_2(\Delta). \quad (1.7)$$

,

$$2\pi \sum_{i=1}^2 \int_0^{r_i} I_i(\rho) \rho d\rho = 1, \quad (1.8)$$

 r_i — .

I , (), II — , “” ():

$$I_2(\rho) = I_2^\circ \left(1 - \kappa + \kappa \sqrt{1 - \frac{\rho^2}{r_2^2}} \right), \quad 0 \leq \kappa \leq 1 - - - , \quad (1.9)$$

$$\varphi_2(\rho) = \begin{cases} 1, & 0 \leq \rho \leq r_2, \\ 0, & r_2 < \rho. \end{cases} \quad (1.10)$$

Chapter 2

1982 , 03.11.1982 . ()

2.1

ń , , ż [@@, – 1967].

$$Au = f, \quad f \in F, \quad u \in U \quad (2.1)$$

$f \in F, u \in U, A: F \rightarrow U$.
 $u, f \in A^{-1}f(u), \dots f \in g. \text{ 1.1 } U, \dots - , \dots$
 $\dots, \dots, \dots, \dots$
 $\text{1.1}, \dots$

$$u = A^1 f, \quad (2.2)$$

$(,), \dots u, \dots - u, \dots, \dots$
 $\dots (,), \dots$
 $\dots \text{1.1} \dots, \dots, \dots () , \dots, \dots, \dots$
 $\dots ()$
 $\dots (), \dots$
 $() . \dots () . - , \dots (, -), \dots$
 $\dots, \dots, \dots, \dots, \dots \square.$

: (experimentum – ,) , .

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2.2

, ,
(), . , , .. [@@1979].

2.2.1

$z(x, u), \quad u_i. \quad x_1, \dots, x_n, \quad v_1, \dots, v_n \quad z, \quad w_1, \dots, w_n, \quad n > m, \quad : \quad u,$

$$S(u) = \sum i1nw_i[v_iz(x_i, u)]^2 \quad (2.3)$$

.

$$J^1(u)J(u)y(u) = f \quad (2.4)$$

$f \quad y(u) \quad \sqrt{w_i}v_i, \sqrt{w_i}z(x_i, u), \quad J(u) \quad \frac{\partial y_k(u)}{\partial u_i} \quad i- \quad k- . \quad (@@3) \quad (@@1).$

, $z(x, u), \quad v \quad w_i.$

$z(x, u) \quad u () \quad (@@3) \quad (\quad -). \quad , \quad .$

$$C_u = f$$

$C \quad nm \quad , \quad . \quad nm \quad U \quad nm \quad V,$

$$C = UDV^T$$

$D \quad nm ; \quad d_{ii} \quad C.$

$$D_y = g,$$

$$y = V^T u \quad g = U^T f, \quad u = Vy.$$

FORTRAN 4 [@@, , - 1980]

[@@.. , .. , .. , 22.10.1980, S. Aarseth, E.L.Turner, J.R. Yott].
[@@.. -1980,.. ..].

.

I (−):

$$\int\limits_a^b K(x,t)u(t) \, dt = f(x), \quad c \leq x \leq d \tag{2.5}$$

1.:

- ;
- ;
- ;
- ;
- ;
- .

¹ - .

2.2.2

$$\frac{du}{dt} = g(u, t), u(t_o) = u_o \quad (2.6)$$

$u, g -$.

•

• a) $(, ,) [@@. - 1966, . . . , . . - .]$ b) $[@@.. , . . , . . , . .]$.

•

• $[@@, . . . , .]$.

• $[@@ - 1979]$. , , , , , . ,
 , .. . - $\dot{n}z$, $[@@ - 1981]$.
 - . , , . , , , . , , .
 . - - .
 . , , .

N

, $(@@S) \ 3N \quad g = \Phi, u = (r_1, \dots, r_n)$. . $- r_i$:

$$\Phi(r_i) = +G \sum_{i+j=1}^N \frac{m_j}{\sqrt{(r_i - r_j)^2 + \varepsilon^2}}, \quad (2.7)$$

$G - , m_j - , \varepsilon) -$ softening parameter .
 :

$$\Delta\Phi = -4\pi GV, \quad (2.8)$$

$V - , \Delta - . -$.

[@@..,..] () [@@R.W. Hockney, F. Hohl, R. Wielen, M. Lecan, S.J. Aarseth, J.R. Yott, P. Bierman, P. Bouvier].

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- N . . -, (, - -). -, -, , .
- -, (, ,).
- [.., .]. ().

(). , , [@@..,..,..,..,..].

, ñž [@@..,..,..,..,.. ..].

2.3

, - . , - .

$$n = 2b^{m1}(b1)(P_L + P_U + 1) + 1,$$
$$b \text{ --- } (), m \text{ --- } (), P_U \text{ --- }, P_L \text{ --- } .$$

(2.9)

$$\left| \frac{\bar{t} - t}{\bar{t}} \right| [S\bar{t}] \leq \left[\frac{1}{2\alpha_1} b^{1-m} \right] \leq \frac{1}{2} b^{1-m},$$
$$b = 16, m = 14, P_U = 63, P_L = 64 \Rightarrow n \approx 1.7 * 10^{19}$$

(2.10)

$$S\bar{t} \leq \frac{2^{-53} \approx 1.11 * 10^{-16}}{m = 14} < \frac{2^{-21} \approx 4.8 * 10^{-7}}{m = 6}$$

, (S
2 :

1. $0.22 + 0.033 + 0.0044 = 0.25$,
 $0.0044 + 0.033 + 0.22 = 0.26$
2. $0.90 * (0.90 + 0.14) = 0.90 * 1.0 = 0.90$,
 $(0.90 * 0.90) + (0.90 * 0.14) = 0.81 + 0.13 = 0.94$
— ().

ń - - , , ž
—[@@, . 36].

ń , . - , , ; , . , , : , . , , , , ž
—[@@. , .243].

, .

2.4

1. Aarseth J.S., Lecar M. Computer Simulation of Stellar Systems. – Ann.Rev.Astron. Astrophys vol. 13, p.1-21, 1975.
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9. ., .,, ., 1980
10. . . (). . ., ., 1979.
11. .., ..,, ., 1978.

2.5

1.

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Chapter 3

15 04.02.1986

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 . . Fixsterne 20 . 1718 (, , -). , [@@, 1954] ,
 , , Φ , t (). . — . .. , .
 . , R, Q, Z , , $z = 0$, . , . — , .

0

0.1

, , I - , .
 .

3.1

[@@, 1968, .72] , — , : $\dot{n} - \dot{z}$
 — . Bertil Lindblad (1895-1965) [@@, 1977].
 1927 — , 1948 — 1952 ..
 1926 . , (), , .

1-2-3-4 ()

5

$$\omega = V/R \quad R.$$
$$P \quad \mathfrak{I}_{m0} \quad (R, 0) \quad EP :$$
$$:$$
$$(-) \quad , \quad .$$

.

$$\mathfrak{I} < 2\Phi, .. E > 0,$$
$$(\quad \Phi = 0,$$
$$\mathfrak{I} 2\Phi, .. E0,$$
$$. \quad I.$$

3.2 -

$$(2). \quad . \quad (R, Z) \quad ($$

., 1977

.. . . ., 32, 5, 332-368, 1953

., 1962, 39-132

.. . . ., 1958

.. . . ., 1954

., 1968

., 1948